<< ML with Python — Take-home Midterm Project >>

Knight's Tour Problem by "Dynamic" WARNSDORFF Algorithm

On-line Report Turn-in Due: 2019/04/25 9:00am

[期中報告注意事項]:

- 1. 請將期中報告電子檔以 **ipynb** 副檔名格式上傳至 LMS 教學網,檔案名稱如下:
 MLwP midterm 第OO組.ipynb (例如:MLwP midterm 第一組.ipynb)
- 2. 期中報告電子檔內,須註明報告標題以及各組成員們的科系、年級、學號和姓名。
- 3. 期中報告的問題、演算法、內容、輸出格式等等定義於第4&5頁中!
- 4. 期中報告缺交和遲交者,不能補交,並以零分計算!

[建議]:無論是否能完成所有問題需求,請務必於期限內,上傳期中報告電子檔!

<前言>

從圖論 (Graph Theory) 角度而言, Knight's Tour (騎士旅程問題) 是一個 Hamiltonian Path/Circle Problems (漢彌爾頓路徑 或 漢彌爾頓循環 的問題)。通常,以 Depth-first Search algorithm (深度優先搜尋演算法) 來求解在 8x8 西洋棋盤上的騎士旅程問題;求解過程中,當路徑搜尋遇到 dead-end 的問題時,會採用 backtracking (回溯) 方式解決該問題。從程式設計的角度,這將會利用"遞迴" (Recursion) 演算法來協助實作 backtracking。

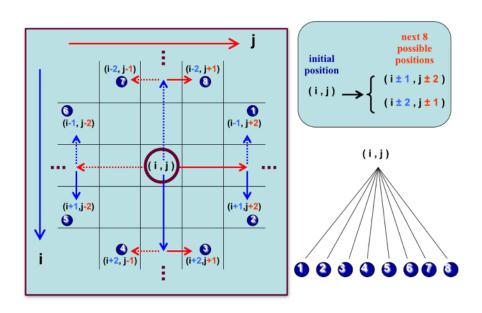
一般而言,上述的搜尋計算效能不高,因此,Warnsdorff (1823) 提出一套"規則"(亦即 演算法),有助於提升搜尋 Hamiltonian Path 的效能。雖然如此,問題是:"靜態" Warnsdorff rules 仍然無法避免搜尋時可能遇到 dead-end,必須"回溯"(backtracking) 搜尋。

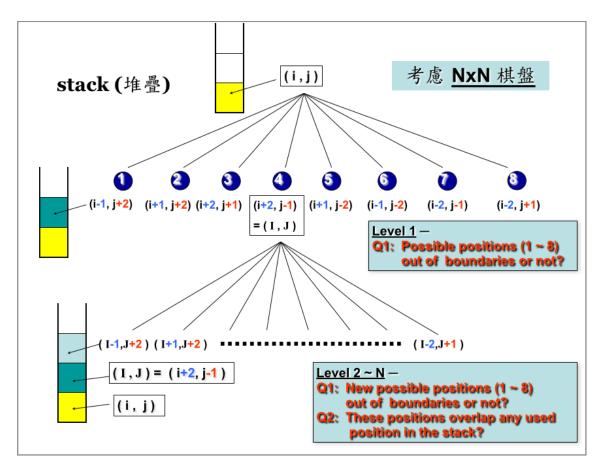
本期中專案旨在利用"動態 (dynamic)" Warnsdorff 演算法,藉由動態更新各棋盤格點的 degree 值,來協助避開搜尋時遇到 dead-end 的問題,在無需回溯的情況下,快速求解騎士旅程問題。

[有關騎士旅程問題 - 簡述]

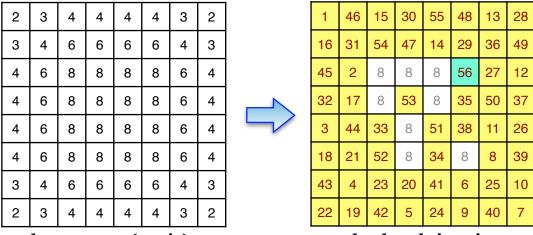
今有 8x8 的西洋棋棋盤,若將騎士的第一步放於棋盤中的任一位置,請利用"動態"的 Warnsdorff 演算法撰寫一程式,找出騎士在 64 步內,依據:「每個方格只能走一次,不得重複!」方式,將棋盤全部方格走完。

· Depth-first Search (DFS) Algorithm with Backtracking





· Warnsdorff Rules



degree map (static)

dead-end situation

(without backtracking)

Hamiltonian Path

(without backtracking)

K	3	4	4	3	4	3	2	1	26	15	24	29	36	13	32
3	4	K.	6	6	6	4	3	16	23	28	35	14	31	40	37
34	5	8	8	7	8	6	4	27	2	25	30	61	38	33	12
4	5	8	77	8	8	6	4	 22	17	62	45	34	41	50	39
4	6	8	8	8	8	6	4	3	46	2	60	49	64	11	42
4	6	8	8	8	8	6	4	18	57	48	63	44	53	8	51
3	4	6	6	6	6	4	3	47	4	55	20	59	6	43	10
2	3	4	4	4	4	3	2	56	19	58	5	54	9	52	7

degree map (dynamic)

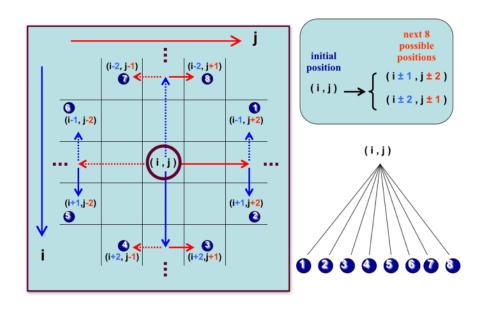
REFERENCE

- 1. "Knight's Tour", Wikipedia. https://en.wikipedia.org/wiki/Knight%27s_tour
- 2. D. Squirrel and P. Cull, "A Warnsdorff-Rule Algorithm for Knight's Tours on Square Chessboards", PDF, 1996. http://math.oregonstate.edu/~math_reu/proceedings/REU_Proceedings/Proceedings1996/1996Squirrel.pdf
- 3. "KNIGHT'S TOUR USING WARNSDORFF ALGORITHM (PYTHON RECIPE)", http://code.activestate.com/recipes/578382-knights-tour-using-warnsdorff-algorithm/

[Problem 1]: An Algorithm for an 8x8 Chessboard Solution

STEP 1: Creating a degree map for an 8x8 chessboard.

STEP 2: Creating the 8 possible moves.



STEP 3: Initiating the **start position** of Knight.

[Note]: It could be chosen at *any* start position for the Knight.

	STEP 4 :	Looping	for fi	nding th	e Hamil	ltonian	Path	for :	Knight's	Tour.
--	-----------------	---------	--------	----------	---------	---------	------	-------	----------	-------

- (1) Checking if the moves within the board boundaries or not.
- (2) Finding the next position for Knight's movement.
- (3) Updating the degree map and the new move.

STEP 5: **Print out** the Hamiltonian Path for Knight's Tour; *something like the following*:

1	26	15	24	29	36	13	32
16	23	28	35	14	31	40	37
27	2	25	30	61	38	33	12
22	17	62	45	34	41	50	39
3	46	21	60	49	64	11	42
18	57	48	63	44	53	8	51
47	4	55	20	59	6	43	10
56	19	58	5	54	9	52	7

[Problem 2] : An Algorithm for an NxN Chessboard Solution ($8 \le N \le 30$)

— Following the **STEPs** in [**Problem 1**] to solve the Knight's Tour problem for an *arbitrary NxN* chessboard, where $8 \le N \le 30$.

-____

Good luck!!