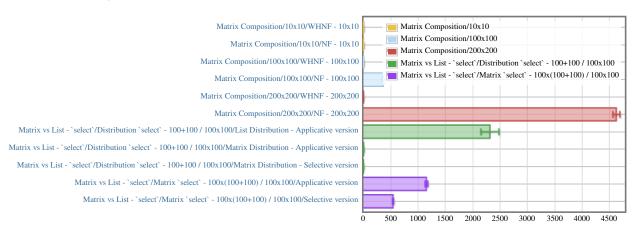
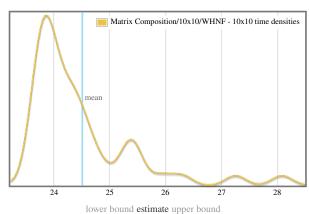
### criterion performance measurements

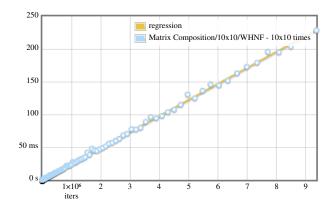
#### overview

want to understand this report?



### Matrix Composition/10x10/WHNF - 10x10





 OLS regression
 24.3 ns
 24.5 ns
 24.7 ns

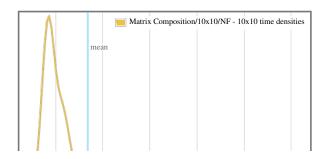
 R² goodness-of-fit
 0.999
 0.999
 1.000

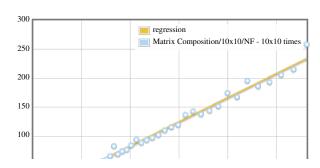
 Mean execution time
 24.3 ns
 24.5 ns
 24.9 ns

 Standard deviation
 700 ps
 965 ps
 1.42 ns

Outlying measurements have severe (62.3%) effect on estimated standard deviation.

### Matrix Composition/10x10/NF - 10x10





lower bound estimate upper bound

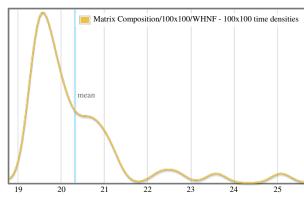
 OLS regression
  $202 \mu s$   $208 \mu s$   $215 \mu s$ 
 $R^2$  goodness-of-fit
 0.993 0.995 0.998 

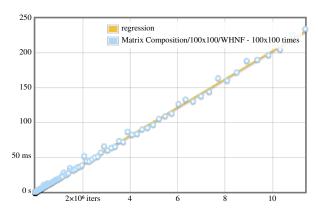
 Mean execution time
  $204 \mu s$   $207 \mu s$   $212 \mu s$  

 Standard deviation
  $9.39 \mu s$   $12.7 \mu s$   $16.9 \mu s$ 

Outlying measurements have severe (59.3%) effect on estimated standard deviation.

### Matrix Composition/100x100/WHNF - 100x100

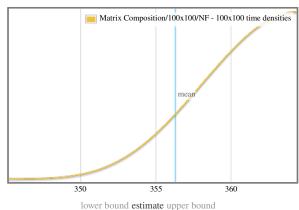


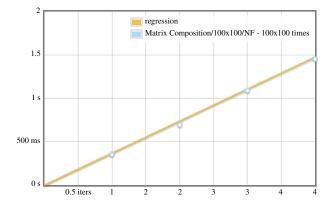


lower bound estimate upper bound

Outlying measurements have severe (78.4%) effect on estimated standard deviation.

### Matrix Composition/100x100/NF - 100x100





 OLS regression
 341 ms
 369 ms
 394 ms

 R² goodness-of-fit
 0.999
 0.999
 1.000

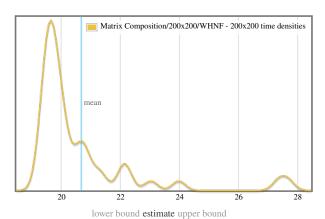
 Mean execution time
 350 ms
 356 ms
 363 ms

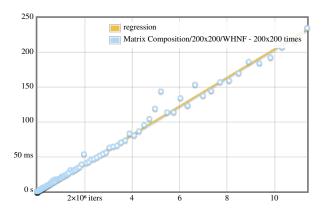
 Standard deviation
 3.52 ms
 7.81 ms
 9.19 ms

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Outlying measurements have moderate (18.8%) effect on estimated standard deviation.

### Matrix Composition/200x200/WHNF - 200x200





 OLS regression
 20.1 ns
 20.5 ns
 21.0 ns

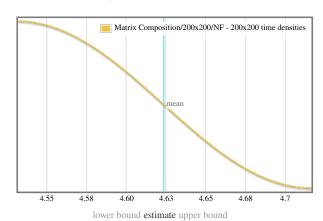
 R² goodness-of-fit
 0.988
 0.994
 0.999

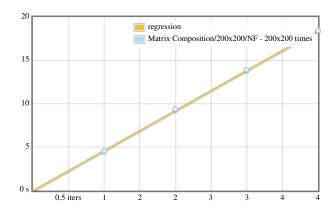
 Mean execution time
 20.2 ns
 20.7 ns
 21.4 ns

 Standard deviation
 1.12 ns
 1.86 ns
 2.89 ns

Outlying measurements have severe (89.8%) effect on estimated standard deviation.

### Matrix Composition/200x200/NF - 200x200

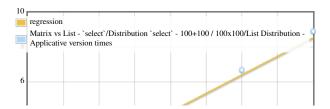




Outlying measurements have moderate (18.7%) effect on estimated standard deviation.

# Matrix vs List - `select`/Distribution `select` - 100+100 / 100x100/List Distribution - Applicative version

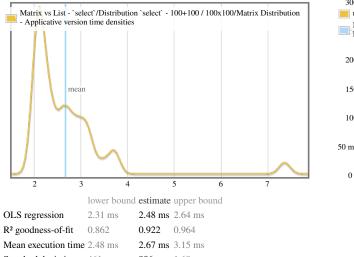


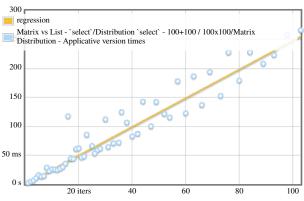


lower bound estimate upper bound 1.88 s 2.14 s 2.26 s OLS regression R2 goodness-of-fit 0.996 0.998 1.000 Mean execution time 2.22 s 2.31 s 2.48 s Standard deviation 166 ms 196 ms

Outlying measurements have moderate (20.2%) effect on estimated standard deviation.

### Matrix vs List - `select`/Distribution `select` - 100+100 / 100x100/Matrix Distribution - Applicative version

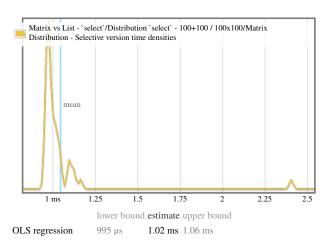


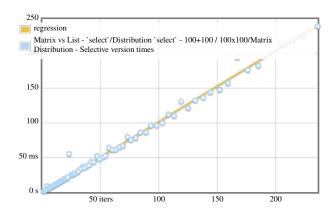


Standard deviation 461 µs 906 μs 1.69 ms

Outlying measurements have severe (96.0%) effect on estimated standard deviation.

### Matrix vs List - `select`/Distribution `select` - 100+100 / 100x100/Matrix Distribution - Selective version





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lower bound estimate upper bound

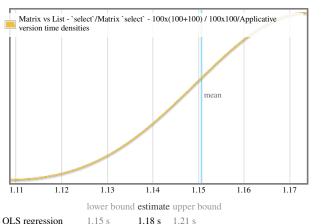
 R² goodness-of-fit
 0.981
 0.991
 0.998

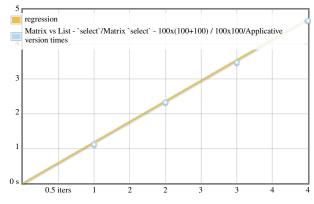
 Mean execution time
 1.01 ms
 1.05 ms
 1.19 ms

 Standard deviation
 49.4 μs
 217 μs
 493 μs

Outlying measurements have severe (92.4%) effect on estimated standard deviation.

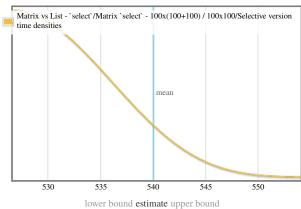
# Matrix vs List - `select`/Matrix `select` - 100x(100+100) / 100x100/Applicative version

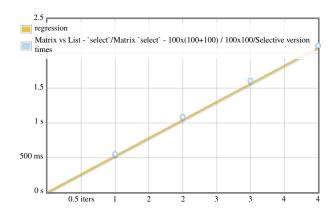




Outlying measurements have moderate (18.8%) effect on estimated standard deviation.

# Matrix vs List - `select`/Matrix `select` - 100x(100+100) / 100x100/Selective version





Outlying measurements have moderate (18.7%) effect on estimated standard deviation.

### understanding this report

In this report, each function benchmarked by criterion is assigned a section of its own. The charts in each section are active; if you hover your mouse over data points and annotations, you will see more details.

- The chart on the left is a kernel density estimate (also known as a KDE) of time measurements. This graphs the probability of any given time measurement occurring. A spike indicates that a measurement of a particular time occurred; its height indicates how often that measurement was repeated.
- The chart on the right is the raw data from which the kernel density estimate is built. The x axis indicates the number of loop iterations, while the y axis shows measured execution time for the given number of loop iterations. The line behind the values is the linear regression prediction of execution time for a given number of iterations. Ideally, all measurements will be on (or very near) this line.

Under the charts is a small table. The first two rows are the results of a linear regression run on the measurements displayed in the right-hand chart.

- OLS regression indicates the time estimated for a single loop iteration using an ordinary least-squares regression model. This number is more accurate than the mean estimate below it, as it more effectively eliminates measurement overhead and other constant factors.
- R<sup>2</sup> goodness-of-fit is a measure of how accurately the linear regression model fits the observed measurements. If the measurements are not too noisy, R<sup>2</sup> should lie between 0.99 and 1, indicating an excellent fit. If the number is below 0.99, something is confounding the accuracy of the linear model.
- Mean execution time and standard deviation are statistics calculated from execution time divided by number of iterations.

We use a statistical technique called the bootstrap to provide confidence intervals on our estimates. The bootstrap-derived upper and lower bounds on estimates let you see how accurate we believe those estimates to be. (Hover the mouse over the table headers to see the confidence levels.)

A noisy benchmarking environment can cause some or many measurements to fall far from the mean. These outlying measurements can have a significant inflationary effect on the estimate of the standard deviation. We calculate and display an estimate of the extent to which the standard deviation has been inflated by outliers.

### colophon

This report was created using the <u>criterion</u> benchmark execution and performance analysis tool.

Criterion is developed and maintained by Bryan O'Sullivan.

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