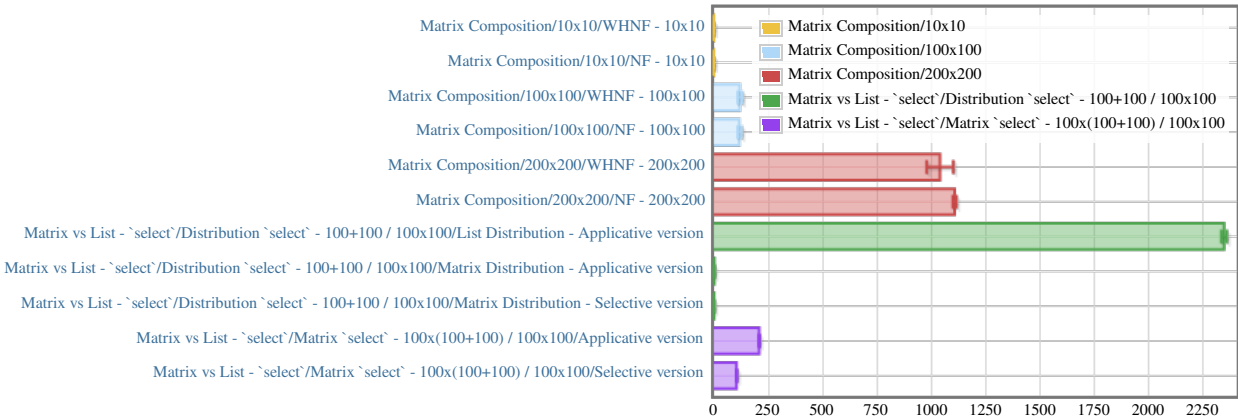


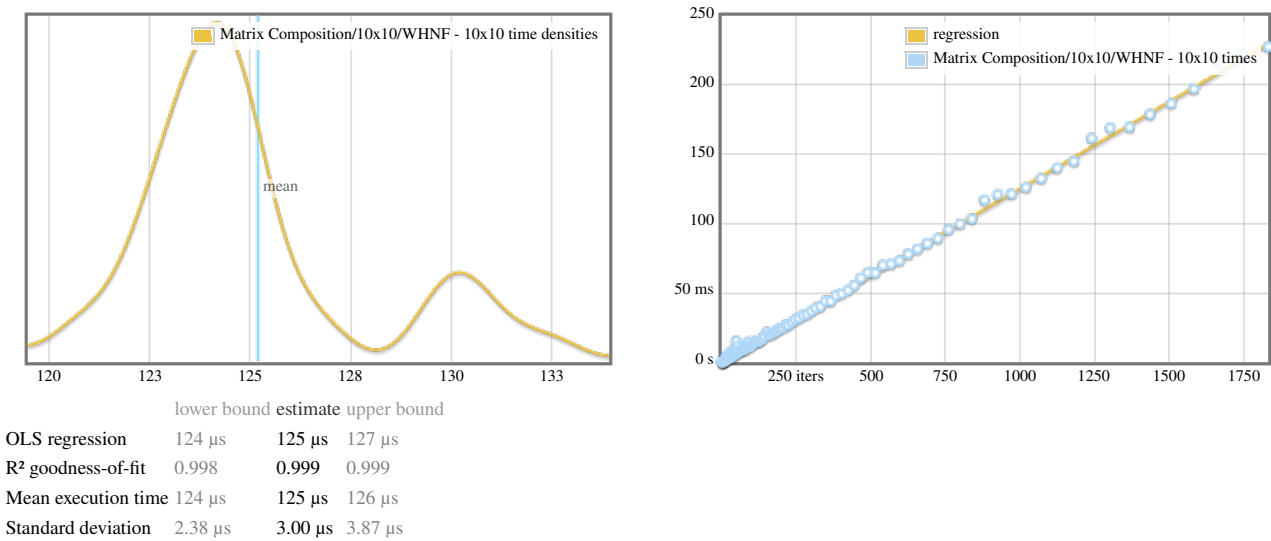
criterion performance measurements

overview

want to understand this report?

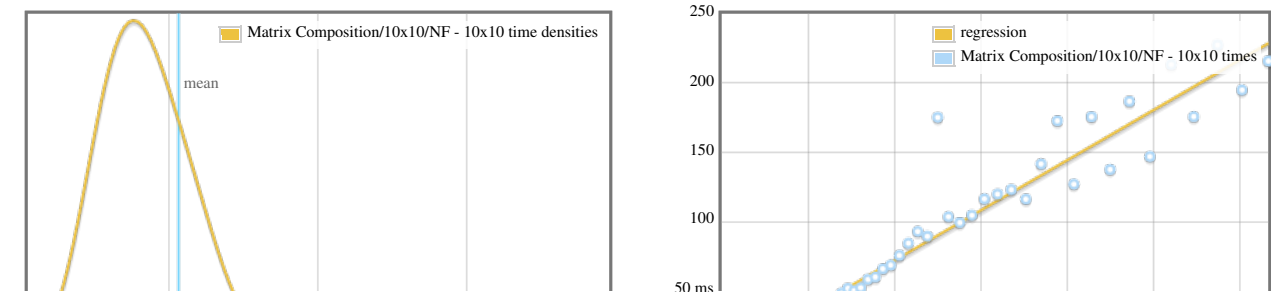


Matrix Composition/10x10/WHNF - 10x10



Outlying measurements have moderate (19.5%) effect on estimated standard deviation.

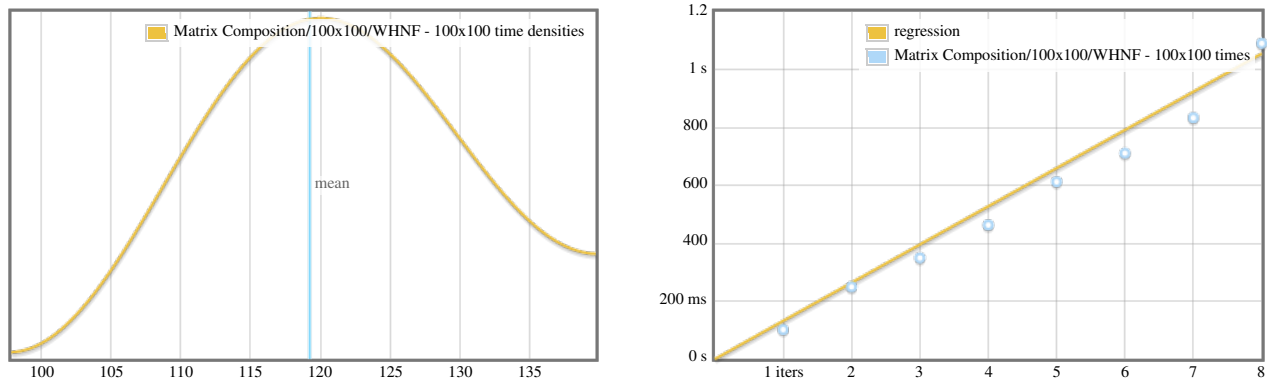
Matrix Composition/10x10/NF - 10x10



	lower bound	estimate	upper bound
OLS regression	135 $\mu$ s	144 $\mu$ s	156 $\mu$ s
R <sup>2</sup> goodness-of-fit	0.919	0.960	0.985
Mean execution time	145 $\mu$ s	153 $\mu$ s	167 $\mu$ s
Standard deviation	23.7 $\mu$ s	36.5 $\mu$ s	53.6 $\mu$ s

Outlying measurements have severe (96.1%) effect on estimated standard deviation.

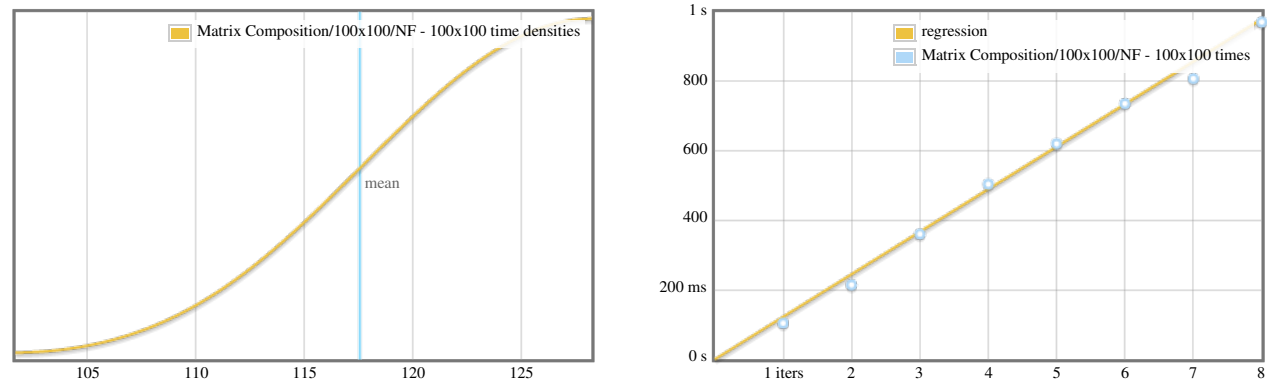
Matrix Composition/100x100/WHNF - 100x100



	lower bound	estimate	upper bound
OLS regression	117 ms	132 ms	149 ms
R <sup>2</sup> goodness-of-fit	0.970	0.985	0.999
Mean execution time	113 ms	119 ms	126 ms
Standard deviation	6.39 ms	9.78 ms	16.2 ms

Outlying measurements have moderate (23.2%) effect on estimated standard deviation.

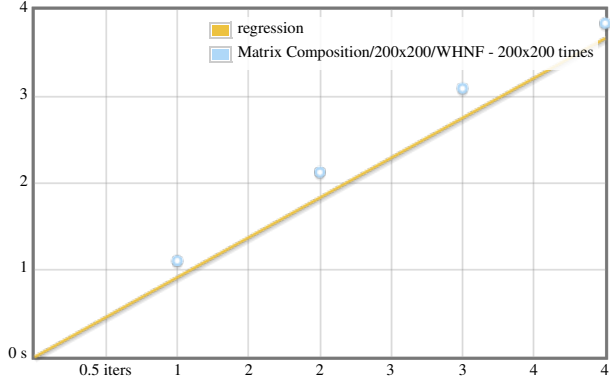
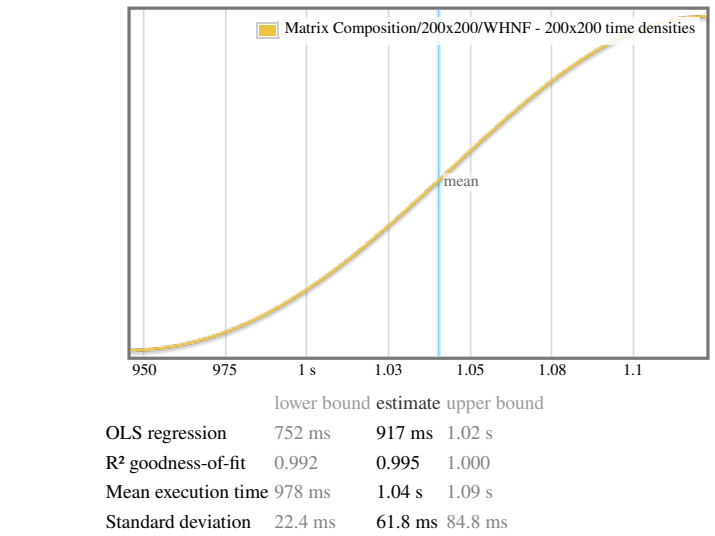
Matrix Composition/100x100/NF - 100x100



	lower bound	estimate	upper bound
OLS regression	111 ms	122 ms	131 ms
R <sup>2</sup> goodness-of-fit	0.987	0.995	0.999
Mean execution time	111 ms	118 ms	122 ms
Standard deviation	5.37 ms	8.15 ms	11.1 ms

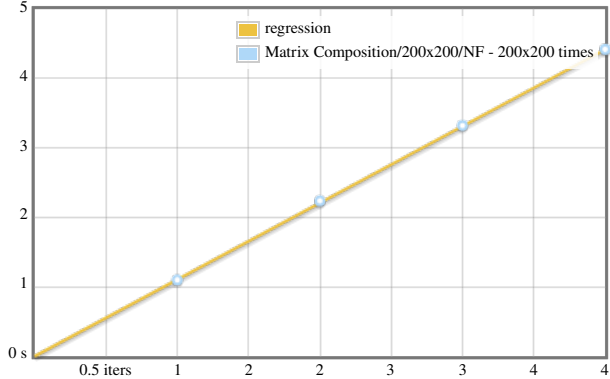
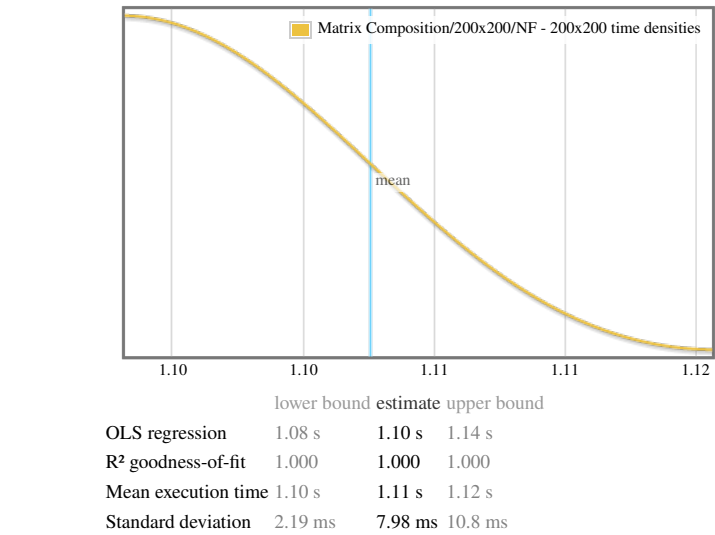
Outlying measurements have moderate (22.5%) effect on estimated standard deviation.

Matrix Composition/200x200/WHNF - 200x200



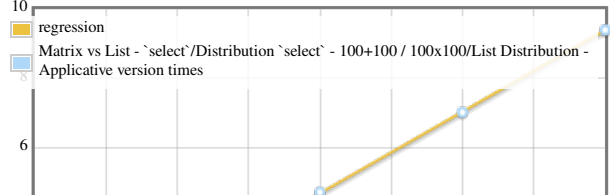
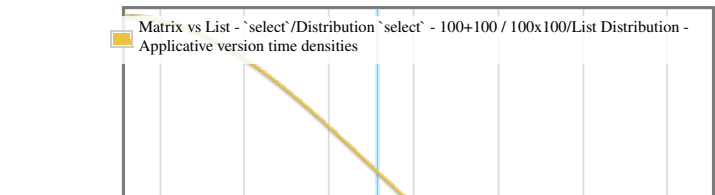
Outlying measurements have moderate (18.7%) effect on estimated standard deviation.

Matrix Composition/200x200/NF - 200x200



Outlying measurements have moderate (18.8%) effect on estimated standard deviation.

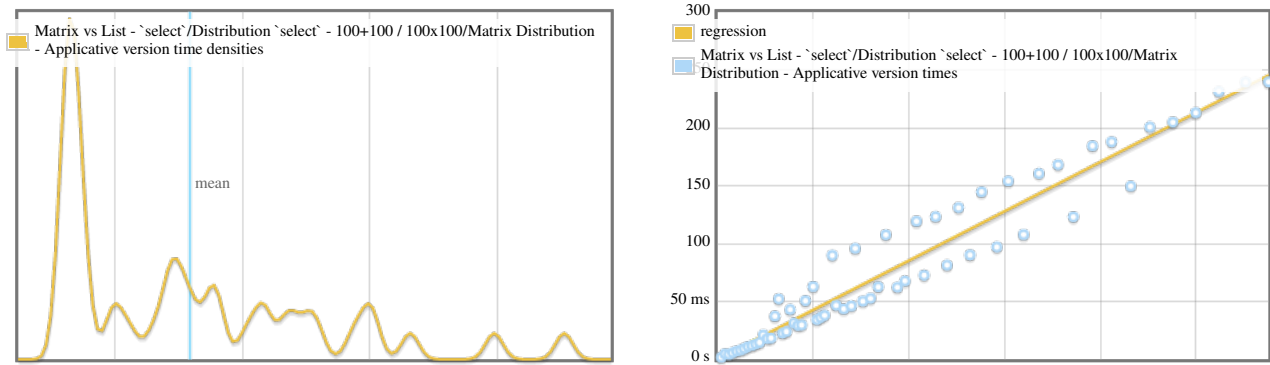
Matrix vs List - `select`/Distribution `select` - 100+100 / 100x100/List Distribution - Applicative version



	lower bound	estimate	upper bound
OLS regression	2.30 s	2.35 s	2.37 s
R <sup>2</sup> goodness-of-fit	1.000	1.000	1.000
Mean execution time	2.34 s	2.35 s	2.36 s
Standard deviation	3.62 ms	12.4 ms	16.7 ms

Outlying measurements have moderate (18.7%) effect on estimated standard deviation.

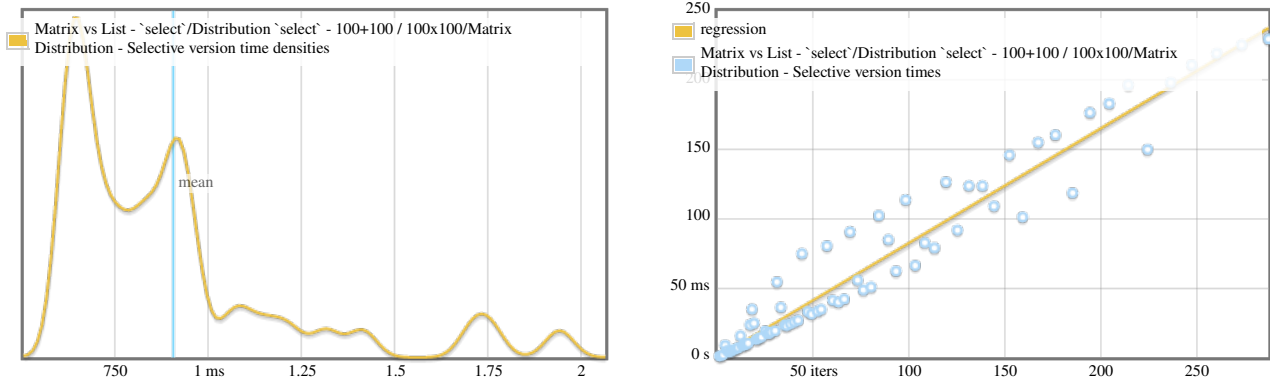
Matrix vs List - `select`/Distribution `select` - 100+100 / 100x100/Matrix  
 Distribution - Applicative version



	lower bound	estimate	upper bound
OLS regression	1.61 ms	1.70 ms	1.79 ms
R <sup>2</sup> goodness-of-fit	0.899	0.939	0.965
Mean execution time	1.64 ms	1.79 ms	1.97 ms
Standard deviation	394 $\mu$ s	502 $\mu$ s	659 $\mu$ s

Outlying measurements have severe (94.7%) effect on estimated standard deviation.

Matrix vs List - `select`/Distribution `select` - 100+100 / 100x100/Matrix  
 Distribution - Selective version

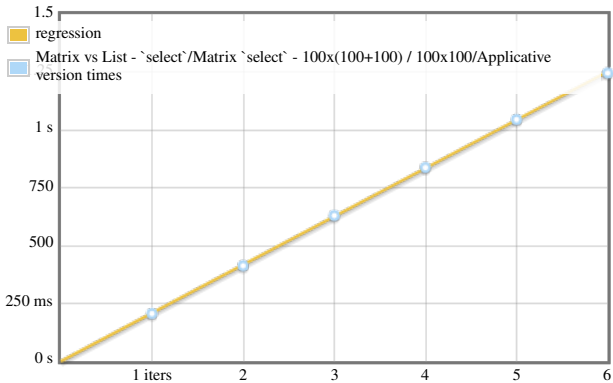
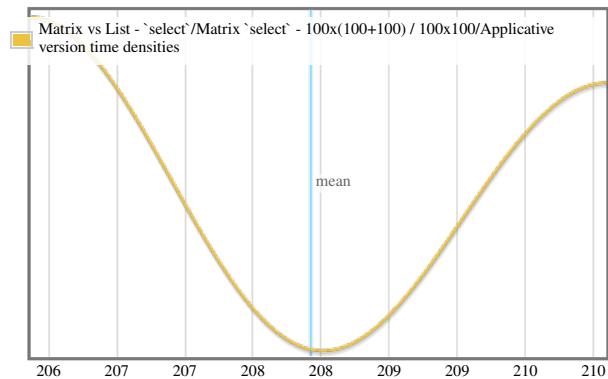


	lower bound	estimate	upper bound
OLS regression	781 $\mu$ s	828 $\mu$ s	872 $\mu$ s

	lower bound	estimate	upper bound
R <sup>2</sup> goodness-of-fit	0.911	0.947	0.968
Mean execution time	825 μs	904 μs	1.01 ms
Standard deviation	234 μs	318 μs	427 μs

Outlying measurements have severe (98.5%) effect on estimated standard deviation.

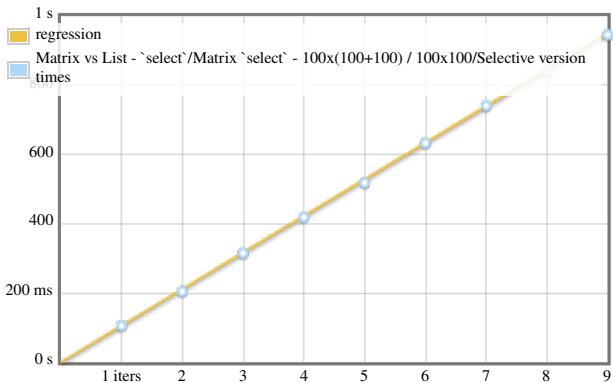
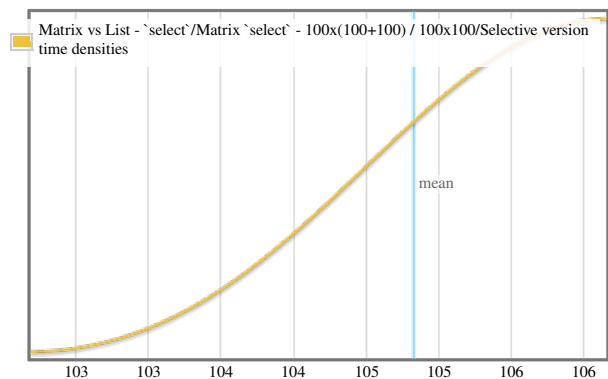
Matrix vs List - `select`/Matrix `select` - 100x(100+100) / 100x100/Applicative version



	lower bound	estimate	upper bound
OLS regression	205 ms	208 ms	212 ms
R <sup>2</sup> goodness-of-fit	1.000	1.000	1.000
Mean execution time	207 ms	208 ms	209 ms
Standard deviation	1.12 ms	1.51 ms	1.83 ms

Outlying measurements have moderate (13.9%) effect on estimated standard deviation.

Matrix vs List - `select`/Matrix `select` - 100x(100+100) / 100x100/Selective version



	lower bound	estimate	upper bound
OLS regression	105 ms	106 ms	107 ms
R <sup>2</sup> goodness-of-fit	1.000	1.000	1.000
Mean execution time	104 ms	105 ms	105 ms
Standard deviation	586 μs	1.08 ms	1.56 ms

Outlying measurements have slight (9.9%) effect on estimated standard deviation.

## understanding this report

In this report, each function benchmarked by criterion is assigned a section of its own. The charts in each section are active; if you hover your mouse over data points and annotations, you will see more details.

- The chart on the left is a [kernel density estimate](#) (also known as a KDE) of time measurements. This graphs the probability of any given time measurement occurring. A spike indicates that a measurement of a particular time occurred; its height indicates how often that measurement was repeated.
- The chart on the right is the raw data from which the kernel density estimate is built. The  $x$  axis indicates the number of loop iterations, while the  $y$  axis shows measured execution time for the given number of loop iterations. The line behind the values is the linear regression prediction of execution time for a given number of iterations. Ideally, all measurements will be on (or very near) this line.

Under the charts is a small table. The first two rows are the results of a linear regression run on the measurements displayed in the right-hand chart.

- *OLS regression* indicates the time estimated for a single loop iteration using an ordinary least-squares regression model. This number is more accurate than the *mean* estimate below it, as it more effectively eliminates measurement overhead and other constant factors.
- *R<sup>2</sup> goodness-of-fit* is a measure of how accurately the linear regression model fits the observed measurements. If the measurements are not too noisy,  $R^2$  should lie between 0.99 and 1, indicating an excellent fit. If the number is below 0.99, something is confounding the accuracy of the linear model.
- *Mean execution time* and *standard deviation* are statistics calculated from execution time divided by number of iterations.

We use a statistical technique called the [bootstrap](#) to provide confidence intervals on our estimates. The bootstrap-derived upper and lower bounds on estimates let you see how accurate we believe those estimates to be. (Hover the mouse over the table headers to see the confidence levels.)

A noisy benchmarking environment can cause some or many measurements to fall far from the mean. These outlying measurements can have a significant inflationary effect on the estimate of the standard deviation. We calculate and display an estimate of the extent to which the standard deviation has been inflated by outliers.

## colophon

This report was created using the criterion benchmark execution and performance analysis tool.

Criterion is developed and maintained by Bryan O'Sullivan.