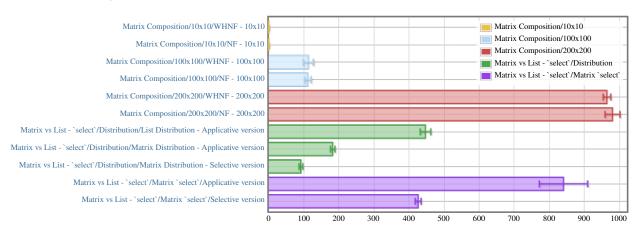
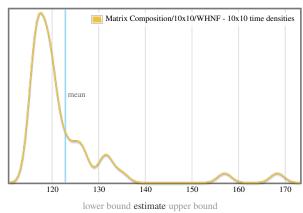
criterion performance measurements

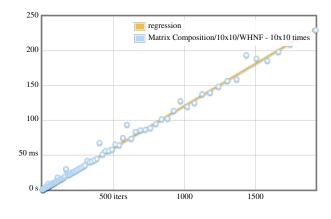
overview

want to understand this report?



Matrix Composition/10x10/WHNF - 10x10





 OLS regression
 119 μ s
 121 μ s
 124 μ s

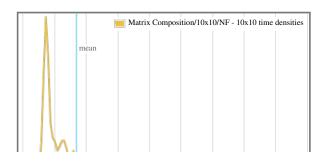
 R² goodness-of-fit
 0.991
 0.995
 0.998

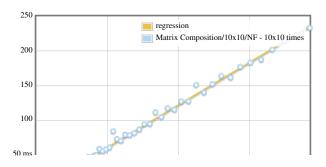
 Mean execution time
 120 μ s
 123 μ s
 128 μ s

 Standard deviation
 5.12 μ s
 10.3 μ s
 19.0 μ s

Outlying measurements have severe (75.0%) effect on estimated standard deviation.

Matrix Composition/10x10/NF - 10x10





lower bound estimate upper bound

 OLS regression
 $121 \,\mu s$ $122 \,\mu s$ $124 \,\mu s$

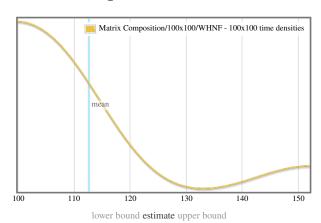
 R² goodness-of-fit
 0.995 0.997 0.999

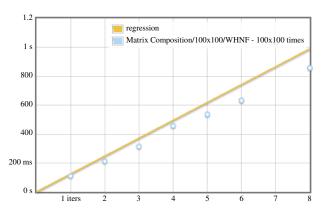
 Mean execution time
 $122 \,\mu s$ $123 \,\mu s$ $126 \,\mu s$

 Standard deviation
 $4.88 \,\mu s$ $7.50 \,\mu s$ $12.3 \,\mu s$

Outlying measurements have severe (61.4%) effect on estimated standard deviation.

Matrix Composition/100x100/WHNF - 100x100





 OLS regression
 104 ms
 124 ms
 165 ms

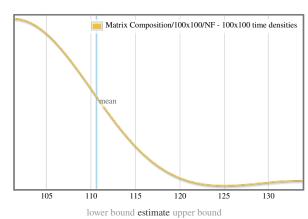
 R² goodness-of-fit
 0.815
 0.915
 1.000

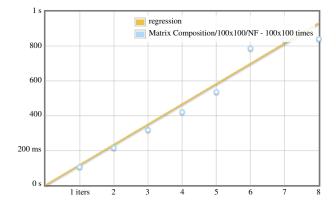
 Mean execution time
 107 ms
 113 ms
 128 ms

Mean execution time 107 ms 113 ms 128 ms Standard deviation 2.79 ms 14.5 ms 22.8 ms

Outlying measurements have moderate (35.8%) effect on estimated standard deviation.

Matrix Composition/100x100/NF - 100x100

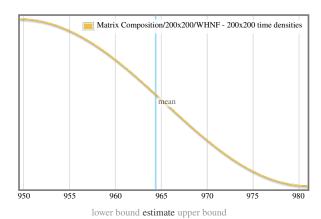


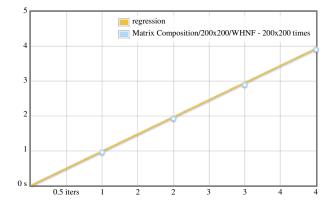


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Outlying measurements have moderate (23.4%) effect on estimated standard deviation.

Matrix Composition/200x200/WHNF - 200x200





 OLS regression
 971 ms
 986 ms
 1.02 s

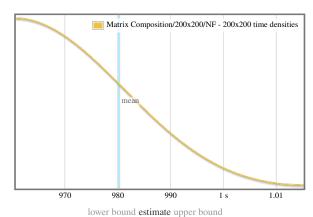
 R² goodness-of-fit
 1.000
 1.000
 1.000

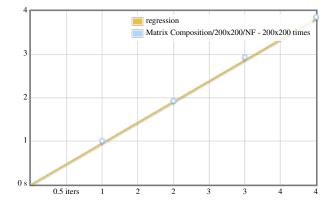
 Mean execution time
 955 ms
 964 ms
 974 ms

Standard deviation 4.80 ms 10.8 ms 15.1 ms

Outlying measurements have moderate (18.7%) effect on estimated standard deviation.

Matrix Composition/200x200/NF - 200x200





 OLS regression
 921 ms
 956 ms
 1.01 s

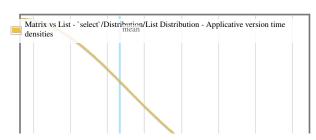
 R² goodness-of-fit
 1.000
 1.000
 1.000

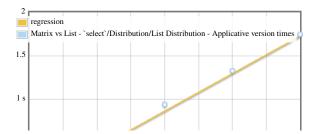
 Mean execution time
 965 ms
 980 ms
 999 ms

 Standard deviation
 235 μs
 21.3 ms
 26.2 ms

Outlying measurements have moderate (18.8%) effect on estimated standard deviation.

Matrix vs List - `select`/Distribution/List Distribution - Applicative version

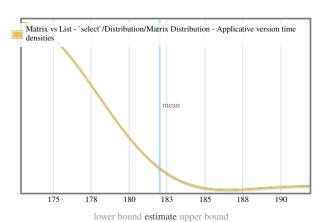


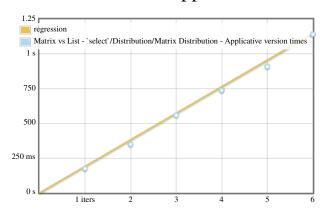


 $\begin{array}{ccccc} & lower bound \ estimate \ upper bound \\ OLS \ regression & 390 \ ms & 431 \ ms & 499 \ ms \\ R^2 \ goodness-of-fit & 0.992 & 0.997 & 1.000 \\ Mean \ execution \ time \ 438 \ ms & 447 \ ms & 462 \ ms \\ Standard \ deviation & 1.36 \ ms & 15.0 \ ms & 18.7 \ ms \\ \end{array}$

Outlying measurements have moderate (18.8%) effect on estimated standard deviation.

Matrix vs List - `select`/Distribution/Matrix Distribution - Applicative version





 OLS regression
 175 ms
 191 ms
 198 ms

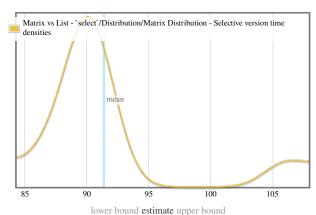
 R² goodness-of-fit
 0.995
 0.998
 1.000

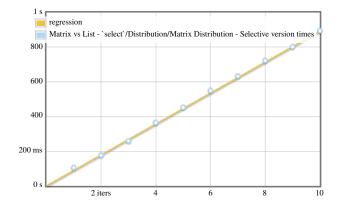
 Mean execution time
 177 ms
 182 ms
 186 ms

 Standard deviation
 4.25 ms
 6.30 ms
 8.49 ms

Outlying measurements have moderate (13.9%) effect on estimated standard deviation.

Matrix vs List - `select`/Distribution/Matrix Distribution - Selective version





 OLS regression
 87.5 ms
 89.1 ms
 91.4 ms

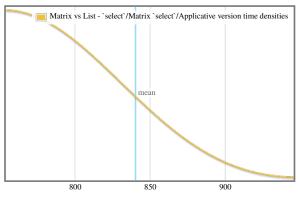
 R² goodness-of-fit
 0.998
 0.999
 1.000

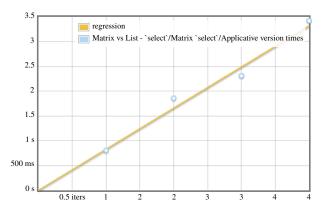
 Mean execution time
 89.3 ms
 91.4 ms
 96.8 ms

 Standard deviation
 1.43 ms
 5.34 ms
 9.30 ms

Outlying measurements have moderate (18.2%) effect on estimated standard deviation.

Matrix vs List - `select`/Matrix `select`/Applicative version





lower bound estimate upper bound

 OLS regression
 450 ms
 829 ms
 1.11 s

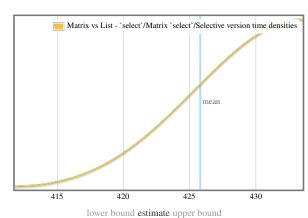
 R² goodness-of-fit
 0.918
 0.977
 1.000

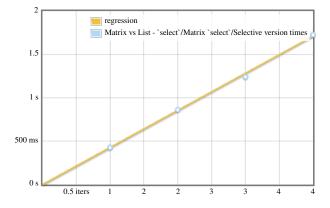
 Mean execution time
 779 ms
 840 ms
 892 ms

 Standard deviation
 27.7 ms
 69.0 ms
 92.3 ms

Outlying measurements have moderate (21.4%) effect on estimated standard deviation.

Matrix vs List - `select`/Matrix `select`/Selective version





OLS regression 377 ms 428 ms 428 ms 28 ms 28 goodness-of-fit 0.992 0.998 1.000 Mean execution time 414 ms 28 426 ms 430 ms Standard deviation 159 μ s 8.50 ms 10.5 ms

Outlying measurements have moderate (18.8%) effect on estimated standard deviation.

understanding this report

In this report, each function benchmarked by criterion is assigned a section of its own. The charts in each section are active; if you hover your mouse over data points and annotations, you will see more details.

- The chart on the left is a kernel density estimate (also known as a KDE) of time measurements. This graphs the probability of any given time measurement occurring. A spike indicates that a measurement of a particular time occurred; its height indicates how often that measurement was repeated.
- The chart on the right is the raw data from which the kernel density estimate is built. The x axis indicates the number of loop iterations, while the y axis shows measured execution time for the given number of loop iterations. The line behind the values is the linear regression prediction of execution time for a given number of iterations. Ideally, all measurements will be on (or very near) this line.

Under the charts is a small table. The first two rows are the results of a linear regression run on the measurements displayed in the right-hand chart.

- OLS regression indicates the time estimated for a single loop iteration using an ordinary least-squares regression model. This number is more accurate than the mean estimate below it, as it more effectively eliminates measurement overhead and other constant factors.
- R² goodness-of-fit is a measure of how accurately the linear regression model fits the observed measurements. If the measurements are not too noisy, R² should lie between 0.99 and 1, indicating an excellent fit. If the number is below 0.99, something is confounding the accuracy of the linear model.
- Mean execution time and standard deviation are statistics calculated from execution time divided by number of iterations.

We use a statistical technique called the bootstrap to provide confidence intervals on our estimates. The bootstrap-derived upper and lower bounds on estimates let you see how accurate we believe those estimates to be. (Hover the mouse over the table headers to see the confidence levels.)

A noisy benchmarking environment can cause some or many measurements to fall far from the mean. These outlying measurements can have a significant inflationary effect on the estimate of the standard deviation. We calculate and display an estimate of the extent to which the standard deviation has been inflated by outliers.

6 of 7

colophon

This report was created using the <u>criterion</u> benchmark execution and performance analysis tool.

Criterion is developed and maintained by Bryan O'Sullivan.

7 of 7