

# Overview of the functionalities of the package lavaSearch2

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April 11, 2023

Load **lavaSearch2** in the R session:

```
library(lavaSearch2)
```

## 1 Inference

### 1.1 Introductory example

You may have noticed that for simple linear regression, the p-values of the Wald tests from `lm`:

```
## simulate data
mSim <- lvm(Y[1:1]~0.3*X1+0.2*X2)
set.seed(10)
df.data <- sim(mSim, 2e1)

## fit linear model
summary(lm(Y~X1+X2, data = df.data))$coef
```

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	0.7967775	0.2506767	3.1785069	0.005495832
X1	0.1550938	0.2205080	0.7033477	0.491360483
X2	0.4581556	0.2196785	2.0855736	0.052401103

differ from those obtained with the corresponding latent variable model estimated by maximum likelihood:

```
## fit latent variable model
m <- lvm(Y~X1+X2)
e <- estimate(m, data = df.data)

## extract Wald tests
summary(e)$coef
```

	Estimate	Std. Error	Z-value	P-value
Y~X1	0.1550938	0.2032984	0.7628877	0.4455303456
Y~X2	0.4581556	0.2025335	2.2621221	0.0236898575
Y~~Y	0.5557910	0.1757566	3.1622777	NA
Y	0.7967775	0.2311125	3.4475747	0.0005656439

For instance, the p-value for the effect of X2 is 0.024 in the latent variable model and 0.052 in the linear regression. The discrepancy is due to 2 corrections that **lm** applies in order to improve the control of the type 1 error of the Wald tests:

- use of a Student *t*-distribution instead of a Gaussian distribution (informally using a t-value instead of z-value).
- use of an unbiased estimator of the residuals variance instead of the ML-estimator. **lavaSearch2** attempts to generalize these

corrections to models with correlated and heteroschedastic measurements. In the case of a simple linear regression, Wald tests obtained with **lavaSearch2** match almost exactly those of **lm**:

```
summary2(e)$coef
```

	estimate	se	statistic	df	p.value
Y	0.7967775	0.2506766	3.1785073	17.00	0.005495827
Y~X1	0.1550938	0.2205080	0.7033478	17.00	0.491360428
Y~X2	0.4581556	0.2196784	2.0855738	17.00	0.052401076
Y~~Y	0.6538716	0.2242761	NA	4.25	NA

## 1.2 How it works in a nutshell

When using **lava**, the p.values that are obtained from the summary (Wald tests) rely on a Gaussian approximation and maximum likelihood estimation. While being asymptotically valid, they usually do not provide a very accurate control of the type 1 error rate in small samples. Simulations have shown that the type 1 error rate tends to be too large, i.e. the p.values are have a downward bias. **lavaSearch2** provides two improvements:

- using a Student's *t*-distribution instead of a Gaussian distribution to account for the uncertainty on the variance of the coefficients. The degrees of freedom are estimated using Satterwaite approximation, i.e. identifying the chi-squared distribution that best fit the observed moments of the variance of the coefficients.
- (partially) correcting for the first order bias in the ML estimates of the variance parameters. This correction also affects the standard error of the estimates.

## 1.3 Single univariate Wald test

We will illustrate the functionalities using a simulated dataset:

```
## simulate data
mSim <- lvm(Y1~eta,Y2~eta,Y3~0.4+0.4*eta,Y4~0.6+0.6*eta,eta~0.5*X1+0.7*X2)
latent(mSim) <- ~eta
set.seed(12)
df.data <- sim(mSim, n = 3e1, latent = FALSE)

## display
head(df.data)
```

	Y1	Y2	Y3	Y4	X1	X2
1	-1.7606233	0.1264910	0.66442611	0.2579355	0.2523400	-1.5431527
2	3.0459417	2.4631929	0.00283511	2.1714802	0.6423143	-1.3206009
3	-2.1443162	-0.3318033	0.82253070	0.3008415	-0.3469361	-0.6758215
4	-2.5050328	-1.3878987	-0.10474850	-1.7814956	-0.5152632	-0.3670054
5	-2.5307249	0.3012422	1.22046986	-1.0195188	0.3981689	-0.5138722
6	-0.9521366	0.1669496	-0.21422548	1.5954456	0.9535572	-0.9592540

We first fit the latent variable model using, as usual, the `estimate` function:

```
m <- lvm(c(Y1,Y2,Y3,Y4)~eta, eta~X1+X2)
e <- estimate(m, data = df.data)
```

We can extract the Wald tests based on the traditional approach using `summary`:

```
summary(e)$coef[c("Y2","Y3","Y2~eta","Y3~eta","eta~X1","eta~X2"), ]
```

	Estimate	Std. Error	Z-value	P-value
Y2	0.2335412	0.2448593	0.9537775	0.3401962906
Y3	0.5114275	0.1785886	2.8637186	0.0041869974
Y2~eta	0.9192847	0.2621248	3.5070497	0.0004531045
Y3~eta	0.2626930	0.1558978	1.6850339	0.0919820326
eta~X1	0.5150072	0.2513393	2.0490515	0.0404570768
eta~X2	0.6212222	0.2118930	2.9317729	0.0033703310

As explain at the begining of this section, **lavaSearch2** implements two corrections that can be directly applied by calling the `summary2` method:

```
summary2(e)$coef[c("Y2","Y3","Y2~eta","Y3~eta","eta~X1","eta~X2"), ]
```

	estimate	se	statistic	df	p.value
Y2	0.2335412	0.2518218	0.9274067	12.332567	0.371510180
Y3	0.5114275	0.1828716	2.7966475	24.693254	0.009851893
Y2~eta	0.9192847	0.2653220	3.4647887	3.518708	0.031533355
Y3~eta	0.2626930	0.1562776	1.6809386	5.953880	0.144155715
eta~X1	0.5150072	0.2642257	1.9491180	20.047646	0.065412240
eta~X2	0.6212222	0.2221293	2.7966698	27.739008	0.009272041

To use the Satterthwaite correction alone, set the argument `ssc` to `FALSE`:

```
summary2(e, ssc = FALSE)$coef[c("Y2","Y3","Y2~eta","Y3~eta","eta~X1","eta~X2"), ]
```

	estimate	se	statistic	df	p.value
Y2	0.2335412	0.2448593	0.9537775	12.911877	0.357711941
Y3	0.5114275	0.1785886	2.8637186	25.780552	0.008210968
Y2~eta	0.9192847	0.2621248	3.5070497	3.674640	0.028396459
Y3~eta	0.2626930	0.1558978	1.6850339	6.222912	0.141185621
eta~X1	0.5150072	0.2513393	2.0490515	21.571210	0.052814794
eta~X2	0.6212222	0.2118930	2.9317729	30.370334	0.006351686

When using the Satterthwaite correction alone, the standard error are left unchanged compared to the original lava output. The only change is how the p-values are computed, i.e. based on the quantiles of a Student's  $t$ -distribution instead of a Gaussian distribution.

To only use the bias correction, set the argument `df` to `FALSE`:

```
summary2(e, df = FALSE)$coef[c("Y2", "Y3", "Y2~eta", "Y3~eta", "eta~X1", "eta~X2"), ]
```

	estimate	se	statistic	df	p.value
Y2	0.2335412	0.2518218	0.9274067	Inf	0.3537154044
Y3	0.5114275	0.1828716	2.7966475	Inf	0.0051635832
Y2~eta	0.9192847	0.2653220	3.4647887	Inf	0.0005306482
Y3~eta	0.2626930	0.1562776	1.6809386	Inf	0.0927748494
eta~X1	0.5150072	0.2642257	1.9491180	Inf	0.0512813393
eta~X2	0.6212222	0.2221293	2.7966698	Inf	0.0051632271

## 1.4 Saving computation time with `estimate2`

For each call to `summary2` the small sample size correction(s) will be recalculated. However the calculation of the sample correction(s) can be time consuming.

```
system.time(
  res <- summary2(e, ssc = FALSE)
)
```

```
user system elapsed
0.128  0.000  0.129
```

In such a case one can pre-compute the main terms of the correction (e.g. the derivative of the variance-covariance matrix) once for all using the `estimate2` method:

```
e2 <- estimate2(e)
```

`estimate2` automatically store the pre-computed terms in the `sCorrect` slot of the object. It also adds the class `lvmfit2` to the object:

```
class(e2)
```

```
[1] "lvmfit2" "lvmfit"
```

Calling the `summary` methods is now much faster:

```
system.time(
  summary(e2)
)
```

```
user system elapsed
0.027  0.000  0.026
```

## 1.5 Single multivariate Wald test

The function `compare` from the `lava` package can be used to perform multivariate Wald tests, i.e. to test simultaneously several linear combinations of the coefficients. We can test the linear hypothesis by specifying in `compare` the parameters we would like to test:

```
resTest0 <- lava::compare(e, par = c("Y2", "Y2~eta", "eta~X1"))
resTest0
```

- Wald test -

Null Hypothesis:

[Y2] = 0

[Y2~eta] = 0

[eta~X1] = 0

data:

chisq = 21.332, df = 3, p-value = 8.981e-05

sample estimates:

	Estimate	Std.Err	2.5%	97.5%
[Y2]	0.2335412	0.2448593	-0.2463741	0.7134566
[Y2~eta]	0.9192847	0.2621248	0.4055295	1.4330399
[eta~X1]	0.5150072	0.2513393	0.0223912	1.0076231

`compare` uses a chi-squared distribution to compute the p-values. Similarly to the Gaussian approximation, while being valid asymptotically this procedure may not provide a very accurate control of the type 1 error rate in small samples. Fortunately, the correction proposed for the univariate Wald statistic can be adapted to the multivariate Wald statistic. This is achieved by `compare2`:

```
resTest1 <- compare2(e, linfct = c("Y2", "Y2~eta", "eta~X1"))
resTest1
```

- Wald test -

Null Hypothesis:

[Y2] = 0

[Y2~eta] = 0

[eta~X1] = 0

data:

F-statistic = 6.7118, df1 = 3, df2 = 11.11, p-value = 0.007577

sample estimates:

	Estimate	Std.Err	df	2.5%	97.5%
[Y2]	0.2335412	0.2518218	12.332567	-0.31349486	0.7805774
[Y2~eta]	0.9192847	0.2653220	3.518708	0.14114161	1.6974278
[eta~X1]	0.5150072	0.2642257	20.047646	-0.03607414	1.0660884

The same result could have been obtained by first defining a contrast matrix to encode (by rows) which linear combination of coefficients should be tested, e.g.:

```
resC <- createContrast(e, linfct = c("Y2=0", "Y2~eta=0", "eta~X1=0"))
resC$contrast
```

```

      Y2 Y3 Y4 eta Y2~eta Y3~eta Y4~eta eta~X1 eta~X2 Y1~~Y1 Y2~~Y2 Y3~~Y3 Y4~~Y4
[Y2] = 0      1  0  0  0      0      0      0      0      0      0      0      0
[Y2~eta] = 0  0  0  0  0      1      0      0      0      0      0      0      0
[eta~X1] = 0  0  0  0  0      0      0      0      1      0      0      0      0
      eta~~eta
[Y2] = 0      0
[Y2~eta] = 0    0
[eta~X1] = 0    0
```

and passing it to the argument `linfct`:

```
resTest2 <- compare2(e2, linfct = resC$contrast)
identical(resTest1, resTest2)
```

```
[1] TRUE
```

Now a F-distribution is used to compute the p-values. As before one can set the argument `ssc` to `FALSE` to use the Satterthwaite approximation alone:

```
resTest3 <- compare2(e, ssc = FALSE, linfct = resC$contrast)
resTest3
```

```
- Wald test -
```

```
Null Hypothesis:
```

```
[Y2] = 0
```

```
[Y2~eta] = 0
```

```
[eta~X1] = 0
```

```
data:
```

```
F-statistic = 7.1107, df1 = 3, df2 = 11.13, p-value = 0.006182
```

```
sample estimates:
```

```

      Estimate Std.Err      df      2.5%      97.5%
[Y2]      0.2335412 0.2448593 12.91188 -0.295812256 0.7628948
[Y2~eta] 0.9192847 0.2621248  3.67464  0.165378080 1.6731913
[eta~X1] 0.5150072 0.2513393 21.57121 -0.006840023 1.0368543
```

In this case the F-statistic of `compare2` is the same as the chi-squared statistic of `compare` divided by the rank of the contrast matrix:

```
resTest0$statistic/qr(resC$contrast)$rank
```

```
chisq
```

```
7.110689
```

## 1.6 Robust Wald tests

When one does not want to assume normality distributed residuals, robust standard error can be used instead of the model based standard errors. They can be obtained by setting the argument `robust` to `TRUE` when computing univariate Wald tests:

```
summary2(e, robust = TRUE)$coef[c("Y2", "Y3", "Y2~eta", "Y3~eta", "eta~X1", "eta~X2"), ]
```

	estimate	robust	SE	statistic	df	p.value
Y2	0.2335412	0.2353245	0.9924222	12.332567	0.340064859	
Y3	0.5114275	0.1897160	2.6957534	24.693254	0.012453535	
Y2~eta	0.9192847	0.1791240	5.1321143	3.518708	0.009583913	
Y3~eta	0.2626930	0.1365520	1.9237580	5.953880	0.103104593	
eta~X1	0.5150072	0.2167580	2.3759546	20.047646	0.027583693	
eta~X2	0.6212222	0.2036501	3.0504385	27.739008	0.004986632	

By default the degrees of freedom of the modeled based variance is used. Degrees of freedom can be computed via a Satterthwaite approximation using `lava.options(df.robust=2)`. However it is not recommended as the resulting degrees of freedom showed a strange behavior. Multivariate Wald test can be obtained in a similar way using the `compare2` method:

```
compare2(e2, linfct = c("Y2", "Y2~eta", "eta~X1"), robust = TRUE)
```

- Wald test -

Null Hypothesis:

[Y2] = 0

[Y2~eta] = 0

[eta~X1] = 0

data:

F-statistic = 12.526, df1 = 3, df2 = 8.41, p-value = 0.001832

sample estimates:

	Estimate	robust	SE	df	2.5%	97.5%
[Y2]	0.2335412	0.2353245	12.332567	-0.27765746	0.7447400	
[Y2~eta]	0.9192847	0.1791240	3.518708	0.39394539	1.4446240	
[eta~X1]	0.5150072	0.2167580	20.047646	0.06292679	0.9670875	

It may be surprising that the (corrected) robust standard errors are (in this example) smaller than the (corrected) model-based one. This is also the case for the uncorrected one:

```
rbind(robust = diag(crossprod(iid(e))),
      model = diag(vcov(e)))
```

	Y2	Y3	Y4	eta	Y2~eta	Y3~eta	Y4~eta
robust	0.04777252	0.03325435	0.03886706	0.06011727	0.08590732	0.02179453	0.02981895
model	0.05995606	0.03189389	0.04644303	0.06132384	0.06870941	0.02430412	0.03715633

	eta~X1	eta~X2	Y1~~Y1	Y2~~Y2	Y3~~Y3	Y4~~Y4	eta~~eta
robust	0.05166005	0.05709393	0.2795272	0.1078948	0.03769614	0.06923165	0.3198022
model	0.06317144	0.04489865	0.1754744	0.1600112	0.05112998	0.10152642	0.2320190

This may be explained by the fact the robust standard error tends to be liberal in small samples (e.g. see Kauermann 2001, A Note on the Efficiency of Sandwich Covariance Matrix Estimation ).

## 1.7 Assessing the type 1 error of the testing procedure

The function `calibrateType1` can be used to assess the type 1 error of a Wald statistic on a specific example. This however assumes that the estimated model is correctly specified. Let's make an example. For this we simulate some data:

```
set.seed(10)
m.generative <- lvm(Y ~ X1 + X2 + Gene)
categorical(m.generative, labels = c("ss", "ll")) <- ~Gene
d <- lava::sim(m.generative, n = 50, latent = FALSE)
```

Let's now imagine that we want to analyze the relationship between Y and Gene using the following dataset:

```
head(d)
```

	Y	X1	X2	Gene
1	-1.14369572	-0.4006375	-0.7618043	ss
2	-0.09943370	-0.3345566	0.4193754	ss
3	-0.04331996	1.3679540	-1.0399434	ll
4	2.25017335	2.1377671	0.7115740	ss
5	0.16715138	0.5058193	-0.6332130	ss
6	1.73931135	0.7863424	0.5631747	ss

For this we fit define a LVM:

```
myModel <- lvm(Y ~ X1 + X2 + Gene)
```

and estimate the coefficients of the model using `estimate`:

```
e <- estimate(myModel, data = d)
e
```

	Estimate	Std. Error	Z-value	P-value
<b>Regressions:</b>				
Y~X1	1.02349	0.12017	8.51728	<1e-12
Y~X2	0.91519	0.12380	7.39244	<1e-12
Y~Gene11	0.48035	0.23991	2.00224	0.04526
<b>Intercepts:</b>				
Y	-0.11221	0.15773	-0.71141	0.4768
<b>Residual Variances:</b>				
Y	0.67073	0.13415	5.00000	

We can now use `calibrateType1` to perform a simulation study. We just need to define the null hypotheses (i.e. which coefficients should be set to 0 when generating the data) and the number of simulations:



```
mySimulation <- calibrateType1(e,
                              param = "Y~Genell",
                              n.rep = 50,
                              trace = FALSE, seed = 10)
```

To save time we only make 50 simulations but much more are necessary to really assess the type 1 error rate. Then we can use the `summary` method to display the results:

```
summary(mySimulation)
```

Estimated type 1 error rate [95% confidence interval]

sample size: 50 | number of simulations: 50

	link	statistic	correction	type1error	CI
[Y~Genell] == 0	Wald	Gaus	0.12	[0.05492 ; 0.24242]	
		Satt	0.10	[0.04224 ; 0.21869]	
		SSC	0.08	[0.03035 ; 0.19456]	
		SSC + Satt	0.08	[0.03035 ; 0.19456]	

Corrections: Gaus = Gaussian approximation

SSC = small sample correction

Satt = Satterthwaite approximation

## 2 Adjustment for multiple comparisons

### 2.1 Univariate Wald test, single model

When performing multiple testing, adjustment for multiple comparisons is necessary in order to control the type 1 error rate, i.e. to provide interpretable p.values. The **multcomp** package enables to do such adjustment when all tests comes from the same **lvmfit** object:

```
## simulate data
mSim <- lvm(Y ~ 0.25 * X1 + 0.3 * X2 + 0.35 * X3 + 0.4 * X4 + 0.45 * X5 + 0.5 * X6)
set.seed(10)
df.data <- sim(mSim, n = 4e1)

## fit lvm
e.lvm <- estimate(lvm(Y ~ X1 + X2 + X3 + X4 + X5 + X6), data = df.data)
name.coef <- names(coef(e.lvm))
n.coef <- length(name.coef)

## Create contrast matrix
resC <- createContrast(e.lvm, linfct = paste0("Y~X",1:6), rowname.rhs = FALSE)
resC$contrast
```

	Y	Y~X1	Y~X2	Y~X3	Y~X4	Y~X5	Y~X6	Y~~Y
[Y~X1]	0	1	0	0	0	0	0	0
[Y~X2]	0	0	1	0	0	0	0	0
[Y~X3]	0	0	0	1	0	0	0	0
[Y~X4]	0	0	0	0	1	0	0	0
[Y~X5]	0	0	0	0	0	1	0	0
[Y~X6]	0	0	0	0	0	0	1	0

```
e.glht <- multcomp::glht(e.lvm, linfct = resC$contrast, rhs = resC$null)
summary(e.glht)
```

#### Simultaneous Tests for General Linear Hypotheses

Fit: estimate.lvm(x = lvm(Y ~ X1 + X2 + X3 + X4 + X5 + X6), data = df.data)

Linear Hypotheses:

	Estimate	Std. Error	z value	Pr(> z )
[Y~X1] == 0	0.3270	0.1589	2.058	0.20725
[Y~X2] == 0	0.4025	0.1596	2.523	0.06611 .
[Y~X3] == 0	0.5072	0.1383	3.669	0.00144 **
[Y~X4] == 0	0.3161	0.1662	1.902	0.28582
[Y~X5] == 0	0.3875	0.1498	2.586	0.05554 .
[Y~X6] == 0	0.3758	0.1314	2.859	0.02482 *

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
(Adjusted p values reported -- single-step method)

Note that this correction relies on the Gaussian approximation. To use small sample corrections implemented in **lavaSearch2**, just call `glht2` instead of `glht`:

```
e.glht2 <- glht2(e.lvm, linfct = resC$contrast, rhs = resC$null)
summary(e.glht2)
```

## Simultaneous Tests for General Linear Hypotheses

### Multiple Comparisons of Means (two sided tests)

```
Fit: estimate.lvm(x = lvm(Y ~ X1 + X2 + X3 + X4 + X5 + X6), data = df.data)
Standard errors: Model-based
```

#### Linear Hypotheses:

	estimate	se	df	lower	upper	statistic	p.value
[Y~X1] == 0	0.327006	0.174976	33.000000	-0.158914	0.812926	1.8689	0.32895
[Y~X2] == 0	0.402533	0.175670	33.000000	-0.085313	0.890380	2.2914	0.14817
[Y~X3] == 0	0.507242	0.152209	33.000000	0.084548	0.929937	3.3325	0.01232 *
[Y~X4] == 0	0.316099	0.182995	33.000000	-0.192089	0.824288	1.7274	0.41283
[Y~X5] == 0	0.387459	0.164970	33.000000	-0.070673	0.845590	2.3487	0.13153
[Y~X6] == 0	0.375763	0.144712	33.000000	-0.026113	0.777639	2.5966	0.07617 .

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(CIs/p-values adjusted for multiple comparisons -- single step max-test)

Error when computing the adjusted p-value by numerical integration: 0.00012125

The single step method is the appropriate correction when one wants to report the most significant p-value relative to a set of hypotheses. If the second most significant p-value is also to be reported then the method "free" is more efficient:

```
summary(e.glht2, test = multcomp::adjusted("free"))
```

## Simultaneous Tests for General Linear Hypotheses

### Multiple Comparisons of Means (two sided tests)

```
Fit: estimate.lvm(x = lvm(Y ~ X1 + X2 + X3 + X4 + X5 + X6), data = df.data)
Standard errors: Model-based
```

#### Linear Hypotheses:

	estimate	se	df	statistic	p.value
[Y~X1] == 0	0.32701	0.17498	33.00000	1.8689	0.12911
[Y~X2] == 0	0.40253	0.17567	33.00000	2.2914	0.09129 .
[Y~X3] == 0	0.50724	0.15221	33.00000	3.3325	0.01242 *
[Y~X4] == 0	0.31610	0.18299	33.00000	1.7274	0.12911
[Y~X5] == 0	0.38746	0.16497	33.00000	2.3487	0.09129 .

```
[Y~X6] == 0 0.37576 0.14471 33.00000 2.5966 0.06451 .
```

```
---
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
(CIs/p-values adjusted for multiple comparisons -- step down max-test)
```

See the book: "Multiple Comparisons Using R" by Frank Bretz, Torsten Hothorn, and Peter Westfall (2011, CRC Press) for details about the theory underlying the **multcomp** package.

## 2.2 Univariate Wald test, multiple models

Pipper et al. in "A Versatile Method for Confirmatory Evaluation of the Effects of a Covariate in Multiple Models" (2012, Journal of the Royal Statistical Society, Series C) developed a method to assess the effect of an exposure on several outcomes when a different model is fitted for each outcome. This method has been implemented in the **mmm** function from the **multcomp** package for glm and Cox models. **lavaSearch2** extends it to lvm.

Let's consider an example where we wish to assess the treatment effect on three outcomes X, Y, and Z. We have at hand three measurements relative to outcome Z for each individual:

```
mSim <- lvm(X ~ Age + 0.5*Treatment,
            Y ~ Gender + 0.25*Treatment,
            c(Z1,Z2,Z3) ~ eta, eta ~ 0.75*treatment,
            Age[40:5]~1)
latent(mSim) <- ~eta
categorical(mSim, labels = c("placebo","SSRI")) <- ~Treatment
categorical(mSim, labels = c("male","female")) <- ~Gender

n <- 5e1
set.seed(10)
df.data <- sim(mSim, n = n, latent = FALSE)
head(df.data)
```

	X	Age	Treatment	Y	Gender	Z1	Z2	Z3
1	39.12289	39.10415	placebo	0.6088958	female	1.8714112	2.2960633	-0.09326935
2	39.56766	39.25191	SSRI	1.0001325	female	0.9709943	0.6296226	1.31035910
3	41.68751	43.05884	placebo	2.1551047	female	-1.1634011	-0.3332927	-1.30769267
4	44.68102	44.78019	SSRI	0.3852728	female	-1.0305476	0.6678775	0.99780139
5	41.42559	41.13105	placebo	-0.8666783	male	-1.6342816	-0.8285492	1.20450488
6	42.64811	41.75832	SSRI	-1.0710170	female	-1.2198019	-1.9602130	-1.85472132
	treatment							
1	1.1639675							
2	-1.5233846							
3	-2.5183351							
4	-0.7075292							
5	-0.2874329							
6	-0.4353083							

We fit a model specific to each outcome:

```
lvmX <- estimate(lvm(X ~ Age + Treatment), data = df.data)
lvmY <- estimate(lvm(Y ~ Gender + Treatment), data = df.data)
lvmZ <- estimate(lvm(c(Z1,Z2,Z3) ~ 1*eta, eta ~ -1 + Treatment),
                 data = df.data)
```

and combine them into a list of lvmfit objects:

```
mmm.lvm <- multcomp::mmm(X = lvmX, Y = lvmY, Z = lvmZ)
```

We can then call `glht2` to apply the small sample corrections, generate a contrast matrix containing tests for all coefficient related to the treatment, and collect the results:

```
lvm.glht2 <- glht2(mmm.lvm, linfct = "TreatmentSSRI")
summary(lvm.glht2)
```

### Simultaneous Tests for General Linear Hypotheses

Multiple Comparisons of Means (two sided tests)

Linear Hypotheses:

	estimate	se	df	lower	upper	statistic
X: [TreatmentSSRI] == 0	0.466150	0.253280	47.000000	-0.154910	1.087209	1.8405
Y: [TreatmentSSRI] == 0	-0.542096	0.261321	47.000000	-1.182874	0.098682	-2.0744
Z: [TreatmentSSRI] == 0	-0.619822	0.440397	47.000000	-1.699707	0.460063	-1.4074

p.value

X: [TreatmentSSRI] == 0	0.1863
Y: [TreatmentSSRI] == 0	0.1165
Z: [TreatmentSSRI] == 0	0.3912

(CIs/p-values adjusted for multiple comparisons -- single step max-test)  
 Error when computing the adjusted p-value by numerical integration: 0.00025692

This can be compared to the unadjusted p.values:

```
summary(lvm.glht2, test = multcomp::adjusted("none"))
```

### Simultaneous Tests for General Linear Hypotheses

Multiple Comparisons of Means (two sided tests)

Linear Hypotheses:

	estimate	se	df	lower	upper	statistic
X: [TreatmentSSRI] == 0	0.466150	0.253280	47.000000	-0.043383	0.975682	1.8405
Y: [TreatmentSSRI] == 0	-0.542096	0.261321	47.000000	-1.067807	-0.016385	-2.0744
Z: [TreatmentSSRI] == 0	-0.619822	0.440397	47.000000	-1.505787	0.266143	-1.4074

p.value

X: [TreatmentSSRI] == 0	0.07202 .
Y: [TreatmentSSRI] == 0	0.04354 *

```
Z: [TreatmentSSRI] == 0 0.16588
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
(CIs/p-values not adjusted for multiple comparisons)
```

## 3 Model diagnostic

### 3.1 Detection of local dependencies

The `modelsearch` function of **lava** is a diagnostic tool for latent variable models. It enables to search for local dependencies (i.e. model misspecification) and add them to the model. Obviously it is a data-driven procedure and its usefulness can be discussed, especially in small samples:

- the procedure is instable, i.e. is likely to lead to two different models when applied on two different dataset sampled from the same generative model.
- it is hard to define a meaningful significance threshold since p-values should be adjusted for multiple comparisons and sequential testing. However traditional methods like Bonferroni-Holm tend to over corrected and therefore reduce the power of the procedure since they assume that the test are independent.

The function `modelsearch2` in **lavaSearch2** partially solves the second issue by adjusting the p-values for multiple testing. Let's see an example:

```
## simulate data
mSim <- lvm(c(y1,y2,y3)~u, u~x1+x2)
latent(mSim) <- ~u
covariance(mSim) <- y2~y3
transform(mSim, Id~u) <- function(x){1:NROW(x)}
set.seed(10)
df.data <- lava::sim(mSim, n = 125, latent = FALSE)
head(df.data)
```

	y1	y2	y3	x1	x2	Id
1	5.5071523	4.883752014	6.2928016	0.8694750	2.3991549	1
2	-0.6398644	0.025832617	0.5088030	-0.6800096	-0.0898721	2
3	-2.5835495	-2.616715027	-2.8982645	0.1732145	-0.8216484	3
4	-2.5312637	-2.518185427	-2.9015033	-0.1594380	-0.2869618	4
5	1.6346220	-0.001877577	0.3705181	0.7934994	0.1312789	5
6	0.4939972	1.759884014	1.5010499	1.6943505	-1.0620840	6

```
## fit model
m <- lvm(c(y1,y2,y3)~u, u~x1)
latent(m) <- ~u
addvar(m) <- ~x2
e.lvm <- estimate(m, data = df.data)
```

`modelsearch2` can be used to sequentially apply the `modelsearch` function with a given correction for the p.values:

```
resScore <- modelsearch2(e.lvm, alpha = 0.1, trace = FALSE)
displayScore <- summary(resScore)
```

Sequential search for local dependence using the score statistic

The variable selection procedure retained 2 variables:

	link	statistic	p.value	adjusted.p.value	dp.Info	selected	nTests
1	u~x2	36.436487	1.577228e-09	5.008615e-08	1	TRUE	10
2	y2~~y3	6.912567	8.559203e-03	6.056378e-02	1	TRUE	9
3	y3~x1	3.136429	7.656125e-02	2.814343e-01	1	FALSE	8

Confidence level: 0.9 (two sided, adjustment: fastmax)

This indeed matches the highest score statistic found by modelsearch:

```
resScore0 <- modelsearch(e.lvm, silent = TRUE)
c(statistic = sqrt(max(resScore0$test[, "Test Statistic"])),
  p.value = min(resScore0$test[, "P-value"]))
```

	statistic	p.value
	6.036264e+00	1.577228e-09

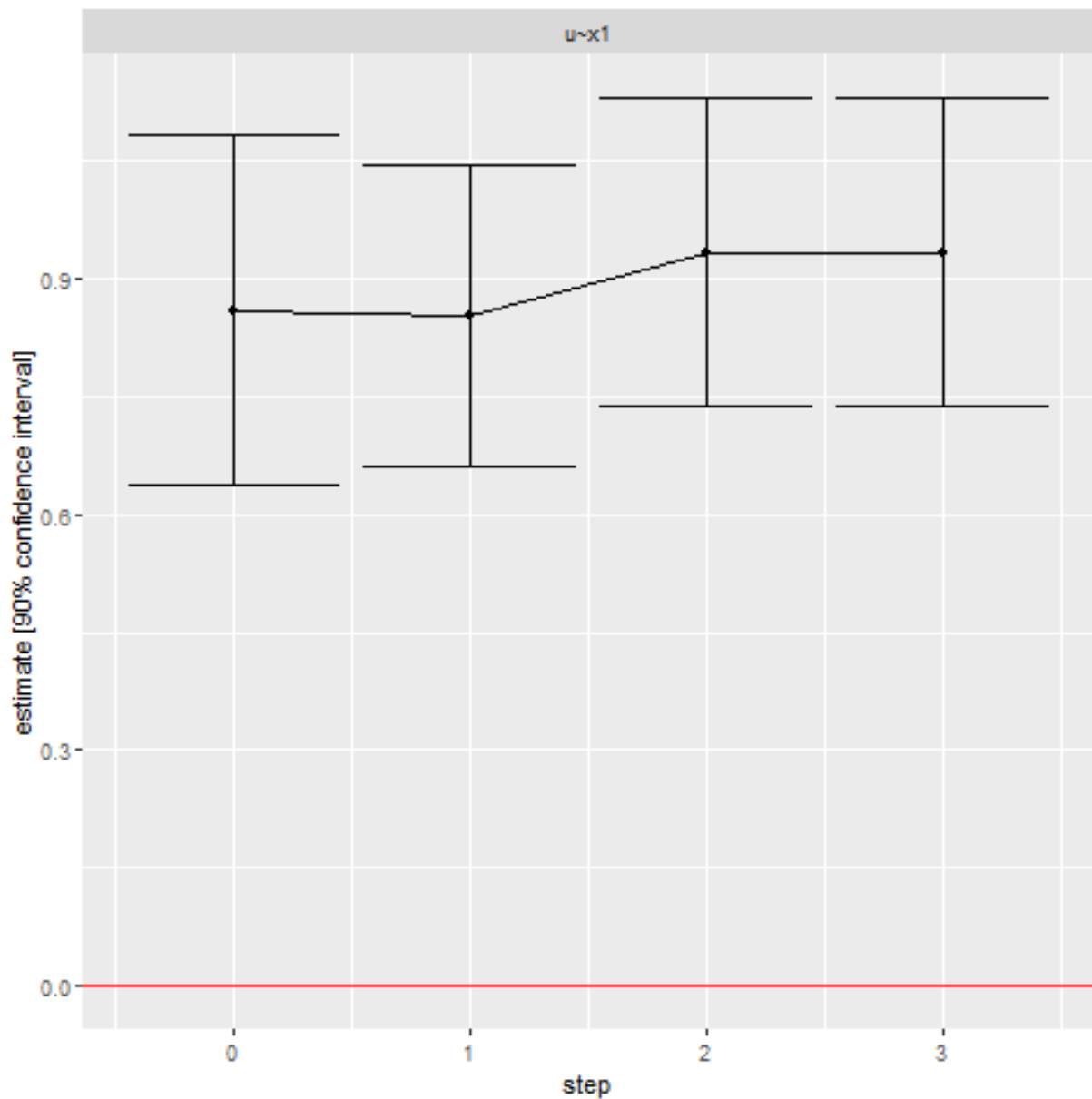
We can compare the adjustment using the max distribution to bonferroni:

```
data.frame(link = displayScore$table[, "link"],
           none = displayScore$table[, "p.value"],
           bonferroni = displayScore$table[, "p.value"] * displayScore$table[1, "nTests"],
           max = displayScore$table[, "adjusted.p.value"])
```

	link	none	bonferroni	max
1	u~x2	1.577228e-09	1.577228e-08	5.008615e-08
2	y2~~y3	8.559203e-03	8.559203e-02	6.056378e-02
3	y3~x1	7.656125e-02	7.656125e-01	2.814343e-01

In theory, the correction based on the max statistic should give a p value that is smaller or equal than the p value adjusted using Bonferroni. However for very small p-values, the max-correction can be numerically inaccurate and result in p-values that are slightly larger. The evolution of the estimation of a given coefficient across the sequential search can be displayed using autoplot:





In many cases, all links are not plausible so the user should indicate which links should be investigated by `modelsearch2`. This can be done via the argument `link`:

```
resRed <- modelsearch2(e.lvm, link = c("y1~~y2", "y1~~y3", "y2~~y3"), trace = FALSE)
print(resRed)
```

Sequential search for local dependence using the score statistic

The variable selection procedure did not retain any variable

	link	statistic	p.value	adjusted.p.value	dp.Info	selected	nTests
1	y1~~y3	3.076875	0.07941299	0.1818963	1	FALSE	3

Confidence level: 0.95 (two sided, adjustment: fastmax)

The function `findNewLink` can help the user to identify the set of relevant links:

```
findNewLink(e.lvm$model, type = "covariance")$link
```

```
[1] "y1~~y2" "y1~~y3" "y2~~y3"
```

## 3.2 Checking that the names of the variables in the model match those of the data

When estimating latent variable models using **lava**, it sometimes happens that the model does not converge:

```
## simulate data
set.seed(10)
df.data <- sim(lvm(Y~X1+X2), 1e2)

## fit model
mWrong <- lvm(Y ~ X + X2)
eWrong <- estimate(mWrong, data = df.data)
```

Warning messages:

```
1: In estimate.lvm(mWrong, data = df.data) :
  Lack of convergence. Increase number of iteration or change starting values.
2: In sqrt(diag(asVar())) : NaNs produced
```

This can have several reasons:

- the model is not identifiable.
- the optimization routine did not managed to find a local optimum. This may happen for complex latent variable model where the objective function is not convex or locally convex.
- the user has made a mistake when defining the model or has not given the appropriate dataset.

The `checkData` function enables to check the last point. It compares the observed variables defined in the model and the one given by the dataset. In case of mismatch it returns a message:

```
checkData(mWrong, df.data)
```

Missing variable in data: X

In presence of latent variables, the user needs to explicitly define them in the model, otherwise `checkData` will identify them as an issue:

```
## simulate data
set.seed(10)
mSim <- lvm(c(Y1,Y2,Y3)~eta)
latent(mSim) <- ~eta
df.data <- sim(mSim, n = 1e2, latent = FALSE)

## fit model
m <- lvm(c(Y1,Y2,Y3)~eta)
checkData(m, data = df.data)
```

Missing variable in data: eta

```
latent(m) <- ~eta  
checkData(m, data = df.data)
```

No issue detected

## 4 Information about the R session used for this document

```
sessionInfo()
```

```
R version 4.2.0 (2022-04-22)
```

```
Platform: x86_64-pc-linux-gnu (64-bit)
```

```
Running under: Ubuntu 20.04.4 LTS
```

```
Matrix products: default
```

```
BLAS: /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.9.0
```

```
LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.9.0
```

```
locale:
```

```
[1] LC_CTYPE=en_US.UTF-8      LC_NUMERIC=C              LC_TIME=en_US.UTF-8
[4] LC_COLLATE=en_US.UTF-8    LC_MONETARY=en_US.UTF-8   LC_MESSAGES=en_US.UTF-8
[7] LC_PAPER=en_US.UTF-8      LC_NAME=C                 LC_ADDRESS=C
[10] LC_TELEPHONE=C           LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C
```

```
attached base packages:
```

```
[1] stats      graphics  grDevices  utils      datasets  methods    base
```

```
other attached packages:
```

```
[1] lavaSearch2_2.0.1 lava_1.7.2      ggplot2_3.4.0    butils.base_1.2
[5] Rcpp_1.0.9        devtools_2.4.3  usethis_2.1.5    data.table_1.14.2
```

```
loaded via a namespace (and not attached):
```

```
[1] pkgload_1.2.4          splines_4.2.0          foreach_1.5.2
[4] brio_1.1.3             assertthat_0.2.1       butils_1.4.7
[7] remotes_2.4.2          sessioninfo_1.2.2      globals_0.16.1
[10] numDeriv_2016.8-1.1    pillar_1.8.1           lattice_0.20-45
[13] glue_1.6.2             digest_0.6.31          colorspace_2.0-3
[16] sandwich_3.0-2         Matrix_1.4-1           plyr_1.8.7
[19] pkgconfig_2.0.3        listenv_0.8.0          purrr_1.0.0
[22] mvtnorm_1.1-3          scales_1.2.1           processx_3.5.3
[25] tibble_3.1.8           generics_0.1.3         ellipsis_0.3.2
[28] TH.data_1.1-1          cachem_1.0.6           withr_2.5.0
[31] cli_3.5.0             survival_3.5-0         magrittr_2.0.3
[34] crayon_1.5.2           memoise_2.0.1          ps_1.7.0
[37] fs_1.5.2              future_1.28.0          fansi_1.0.3
[40] parallelly_1.32.1      doParallel_1.0.17      nlme_3.1-157
[43] MASS_7.3-57           xml2_1.3.3             RcppArmadillo_0.11.2.0.0
[46] pkgbuild_1.3.1         progressr_0.11.0       tools_4.2.0
[49] prettyunits_1.1.1      lifecycle_1.0.3        multcomp_1.4-20
[52] stringr_1.5.0          munsell_0.5.0          callr_3.7.0
[55] compiler_4.2.0         rlang_1.0.6            grid_4.2.0
[58] iterators_1.0.14       boot_1.3-28            testthat_3.1.4
[61] gtable_0.3.1          codetools_0.2-18       abind_1.4-5
```

[64] DBI_1.1.3	roxygen2_7.2.1	reshape2_1.4.4
[67] R6_2.5.1	zoo_1.8-11	knitr_1.39
[70] dplyr_1.0.10	fastmap_1.1.0	future.apply_1.9.1
[73] utf8_1.2.2	rprojroot_2.0.3	desc_1.4.1
[76] stringi_1.7.8	parallel_4.2.0	vctrs_0.5.1
[79] tidyselect_1.2.0	xfun_0.31	