Overview of the functionalities of the package lavaSearch2

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Load lavaSearch2 in the R session:

1 Inference

1.1 Introductory example

You may have noticed that for simple linear regression, the p-values of the Wald tests from 1m:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.7967775 0.2506767 3.1785069 0.005495832
X1 0.1550938 0.2205080 0.7033477 0.491360483
X2 0.4581556 0.2196785 2.0855736 0.052401103
```

differ from those obtained with lava:

```
Estimate Std. Error Z-value P-value
Y~X1 0.1550938 0.2032984 0.7628877 0.4455303456
Y~X2 0.4581556 0.2025335 2.2621221 0.0236898575
Y~~Y 0.5557910 0.1757566 3.1622777 NA
Y 0.7967775 0.2311125 3.4475747 0.0005656439
```

For instance, the p-value for the effect of X2 is 0.024 according to lava and 0.052 according to lm. The discrepancy is due to 2 corrections that lm applies in order to improve the control of the type 1 error of the Wald tests:

- use of a student distribution instead of a normal distribution (informally t-value instead of z-value).
- use of a bias-corrected estimator of the residuals variance instead of the ML-estimator.

lavaSearch2 attempts to generalize these corrections to models with correlated and heteroschedastic measurements. In the case of a simple linear regression, Wald tests obtained with lavaSearch2 closely approximate the results of lm:

```
Estimate Std. Error t-value P-value df
Y~X1 0.1550938 0.2205078 0.7033483 0.49136012 17.00
Y~X2 0.4581556 0.2196783 2.0855754 0.05240092 17.00
Y~~Y 0.6538707 0.2242758 2.9154759 NA 4.25
Y 0.7967775 0.2506765 3.1785096 0.00549580 17.00
```

1.2 How it works in a nutshell

When using **lava**, the p.values that are obtained from the summary (Wald tests) rely on a Gaussian approximation. While being asymptotically valid, this approximation may not provide a very accurate control of the type 1 error rate in small samples. Simulations have shown that the type 1 error rate tends to be too large, i.e. the p.values are have a downward bias. gg **lavaSearch2** improves the Gaussian approximation in two way:

- using a Student's t distribution instead of a normal distribution to account for the uncertainty on the variance of the coefficients. The degrees of freedom are estimated using Satterwaite approximation, i.e. identifying the chi-squared distribution that best fit the observed moments of the variance of the coefficients.
- correct for the first order bias in the residual variance due to ML estimation. This bias also affects the standard error of the estimates and the control of the type 1 error. The correction does not change the estimates (i.e. the column "Estimate" in the summary remain unchanged), but it changes the corresponding standard error and degree of freedoms (i.e. columns "Std. Error" and "df" in the summary are modified).

1.3 Single univariate Wald test

We will illustrate the functionalities using a simulated dataset:

```
Y1
                                                                   X2
                     Y2
                                  Y3
                                             Y4
                                                        X1
1 -1.7606233
              0.1264910
                         0.66442611
                                      0.2579355
                                                 0.2523400 -1.5431527
  3.0459417
              2.4631929
                         0.00283511
                                      2.1714802
                                                 0.6423143 -1.3206009
3 -2.1443162 -0.3318033
                         0.82253070
                                     0.3008415 -0.3469361 -0.6758215
4 -2.5050328 -1.3878987 -0.10474850 -1.7814956 -0.5152632 -0.3670054
5 -2.5307249
              0.3012422
                         1.22046986 -1.0195188
                                                 0.3981689 -0.5138722
6 -0.9521366
              0.1669496 -0.21422548 1.5954456
                                                 0.9535572 -0.9592540
```

We first fit the latent variable model using, as usual, the estimate function: We can extract the Wald tests based on a normal approximation using summary:

```
Estimate Std. Error
                              Z-value
                                            P-value
                  0.2448593 0.9537775 0.3401962906
Y2
       0.2335412
                  0.1785886 2.8637186 0.0041869974
Y3
       0.5114275
                  0.2621248 3.5070497 0.0004531045
Y2~eta 0.9192847
Y3~eta 0.2626930
                  0.1558978 1.6850339 0.0919820326
eta~X1 0.5150072
                  0.2513393 2.0490515 0.0404570768
eta~X2 0.6212222 0.2118930 2.9317729 0.0033703310
```

As explain at the begining of this section, lavaSearch2 implements two corrections that can be directly applied by calling the summary2 method:

```
Estimate Std. Error t-value P-value df
Y2 0.2335412 0.2518218 0.9274067 0.371516094 12.328385
Y3 0.5114275 0.1828716 2.7966475 0.009848769 24.707696
Y2~eta 0.9192847 0.2653220 3.4647887 0.031585600 3.515034
Y3~eta 0.2626930 0.1562776 1.6809386 0.143826633 5.993407
```

```
eta~X1 0.5150072 0.2642257 1.9491180 0.065414617 20.044312 eta~X2 0.6212222 0.2221293 2.7966698 0.009275494 27.718363
```

To use the Satterthwaite correction alone, set the argument bias.correct to FALSE:

```
Estimate Std. Error
                         t-value
                                    P-value
                                                df
Y2
               0.2448593 0.9537775 0.357711941 12.911877
Y3
      0.5114275
               0.1785886 2.8637186 0.008210968 25.780552
Y2~eta 0.9192847
               0.2621248 3.5070497 0.028396459
                                           3.674640
Y3~eta 0.2626930
               0.1558978 1.6850339 0.141185621
               0.2513393 2.0490515 0.052814794 21.571210
eta~X1 0.5150072
```

When using the Satterthwaite correction alone, the standard error are left unchanged compared to the original lava output. The only change is how the p-values are computed, i.e. based on the quantiles of a Student's t distribution instead of a Gaussian distribution.

1.4 Saving computation time with sCorrect

For each call to summary2 the small sample size correction(s) will be recalculated. However the calculation of the sample correction(s) can be time consuming.

```
user system elapsed 0.24 0.00 0.24
```

In such a case one can pre-compute the main terms of the correction (e.g. the derivative of the variance-covariance matrix) once for all using the sCorrect method (sCorrect stands for Satterthwaite correction). When calling sCorrect, the right hand side indicates whether the bias correction should be used (equivalent to bias.correct argument described previously): sCorrect automatically store the pre-computed terms in the sCorrect slot of the object. It also adds the class lvmfit2 to the object:

```
[1] "lvmfit2" "lvmfit"
```

Then p-values computed using the small sample correction can be obtained calling the summary method, as usual:

```
Estimate Std. Error
                                    P-value
                          t-value
                                                 df
Y2
      Y3
      0.5114275
               0.1828716 2.7966475 0.009848769 24.707696
               0.2653220 3.4647887 0.031585600
Y2~eta 0.9192847
                                            3.515034
Y3~eta 0.2626930
               0.1562776 1.6809386 0.143826633
eta~X1 0.5150072
               0.2642257 1.9491180 0.065414617 20.044312
eta~X2 0.6212222 0.2221293 2.7966698 0.009275494 27.718363
```

The summary 2 methods take approximately the same time as the usual summary method:

```
user system elapsed 0.10 0.00 0.09 user system elapsed 0.08 0.00 0.08
```

1.5 Single multivariate Wald test

The function compare can be use to perform multivariate Wald tests, i.e. to test simultaneously several linear combinations of the coefficients. compare uses a contrast matrix to encode in lines which linear combination of coefficients should be tested. For instance if we want to simultaneously test whether all the mean coefficients are 0, we can create a contrast matrix using createContrast:

\$contrast

```
Y2 Y3 Y4 eta Y2~eta Y3~eta Y4~eta eta~X1 eta~X2 Y1~~Y1 Y2~~Y2 Y3~~Y3 Y4~~Y4
[Y2] = 0
                1
                   0
                      0
                           0
                                   0
                                           0
                                                   0
                                                           0
                                                                   0
                                                                           0
                                                                                   0
                                                                                           0
                                                                                                   0
[Y2^{eta}] = 0
                0
                   0
                      0
                           0
                                   1
                                           0
                                                   0
                                                           0
                                                                   0
                                                                           0
                                                                                   0
                                                                                           0
                                                                                                   0
[eta^X1] = 0
                                   0
                                           0
                                                   0
                                                           1
                                                                           0
                                                                                   0
                                                                                           0
                   0
                                                                   0
                                                                                                   0
              eta~~eta
[Y2] = 0
                       0
[Y2^eta] = 0
                       0
[eta^X1] = 0
                       0
$null
    [Y2] = 0 [Y2^eta] = 0 [eta^X1] = 0
            0
                           0
$Q
[1] 3
```

We can then test the linear hypothesis by specifying in compare the left hand side of the hypothesis (argument contrast) and the right hand side (argument null):

```
- Wald test -
        Null Hypothesis:
        [Y2] = 0
        [Y2^{eta}] = 0
        [eta^X1] = 0
data:
chisq = 21.332, df = 3, p-value = 8.981e-05
sample estimates:
          Estimate
                     Std.Err
                                    2.5%
                                              97.5%
         0.2335412 0.2448593 -0.2463741 0.7134566
[Y2]
[Y2~eta] 0.9192847 0.2621248
                              0.4055295 1.4330399
[eta~X1] 0.5150072 0.2513393 0.0223912 1.0076231
```

compare uses a chi-squared distribution to compute the p-values. Similarly to the Gaussian approximation, while being valid asymptotically this procedure may not provide a very accurate control of the type 1 error rate in small samples. Fortunately, the correction proposed for the univariate Wald statistic can be adapted to the multivariate Wald statistic. This is achieved by compare2:

```
- Wald test -
```

[Y2~eta] = 0 0.9192847 0.2653220 3.515034 0.1407653 1.6978041

[eta~X1] = 0 0.5150072 0.2642257 20.044312 -0.0360800 1.0660943

0.2335412 0.2518218 12.328385 -0.3135148 0.7805973

[1] TRUE

Null Hypothesis:

Now a F distribution is used to compute the p-values. As before on can set the argument bias.correct to FALSE to use the Satterthwaite approximation alone:

The same result could have been obtained using the par argument to define the linear hypothesis:

```
- Wald test -
        Null Hypothesis:
        [Y2] = 0
        [Y2^eta] = 0
        [eta^X1] = 0
data:
F-statistic = 7.1107, df1 = 3, df2 = 11.13, p-value = 0.006182
sample estimates:
                         Std.Err
                                        df
                                                   2.5%
              Estimate
                                                            97.5%
             0.2335412 0.2448593 12.91188 -0.295812256 0.7628948
[Y2~eta] = 0 0.9192847 0.2621248 3.67464 0.165378080 1.6731913
[eta~X1] = 0 0.5150072 0.2513393 21.57121 -0.006840023 1.0368543
```

In this case the F-statistic of compare 2 is the same as the chi-squared statistic of compare divided by the rank of the contrast matrix:

```
chisq
7.110689
```

1.6 Robust Wald tests

When one does not want to assume normality distributed residuals, robust standard error can be used instead of the model based standard errors. They can be obtain by setting the argument robust to TRUE when computing univariate Wald tests:

```
Estimate robust SE t-value P-value df V2 0.2355412 0.2353245 0.9924222 0.340071187 12.328385
```

```
Y3 0.5114275 0.1897160 2.6957535 0.012449993 24.707696

Y2~eta 0.9192847 0.1791240 5.1321150 0.009609880 3.515034

Y3~eta 0.2626930 0.1365520 1.9237585 0.102782655 5.993407

eta~X1 0.5150072 0.2167580 2.3759546 0.027585480 20.044312

eta~X2 0.6212222 0.2036501 3.0504389 0.004989038 27.718363
```

or multivariate Wald test:

```
- Wald test -

Null Hypothesis:

[Y2] = 0

[Y2~eta] = 0

[eta~X1] = 0
```

data:

```
F-statistic = 12.526, df1 = 3, df2 = 11.1, p-value = 0.0006959 sample estimates:
```

```
Estimate robust SE df 2.5% 97.5% [Y2] = 0 0.2335412 0.2353245 12.328385 -0.27767612 0.7447586 [Y2~eta] = 0 0.9192847 0.1791240 3.515034 0.39369139 1.4448780 [eta~X1] = 0 0.5150072 0.2167580 20.044312 0.06292197 0.9670923
```

Only the standard error is affected by the argument robust, the degrees of freedom are the one of the model-based standard errors. It may be surprising that the (corrected) robust standard errors are (in this example) smaller than the (corrected) model-based one. This is also the case for the uncorrected one:

```
Y2
                           Y3
                                      Y4
                                                         Y2~eta
                                                                    Y3~eta
                                                                               Y4~eta
                                                eta
robust 0.04777252 0.03325435 0.03886706 0.06011727 0.08590732 0.02179453 0.02981895
model
       0.05995606\ 0.03189389\ 0.04644303\ 0.06132384\ 0.06870941\ 0.02430412\ 0.03715633
                                 Y1~~Y1
                                           Y2~~Y2
                                                       Y3~~Y3
                                                                  Y4~~Y4 eta~~eta
           eta~X1
                      eta~X2
robust 0.05166005 0.05709393 0.2795272 0.1078948 0.03769614 0.06923165 0.3198022
       0.06317144 0.04489865 0.1754744 0.1600112 0.05112998 0.10152642 0.2320190
```

This may be explained by the fact the robust standard error tends to be liberal in small samples (e.g. see Kauermann 2001, A Note on the Efficiency of Sandwich Covariance Matrix Estimation).

1.7 Assessing the type 1 error of the testing procedure

The function calibrateType1 can be used to assess the type 1 error of a Wald statistic on a specific example. This however assumes that the estimated model is correctly specified. Let's make an example. For this we simulate some data: Let's now imagine that we want to analyze the relationship between Y and Gene using the following dataset:

```
Y X1 X2 Gene
1 -1.14369572 -0.4006375 -0.7618043 ss
2 -0.09943370 -0.3345566 0.4193754 ss
3 -0.04331996 1.3679540 -1.0399434 11
```

```
4 2.25017335 2.1377671 0.7115740 ss
5 0.16715138 0.5058193 -0.6332130 ss
6 1.73931135 0.7863424 0.5631747 ss
```

For this we fit define a LVM: and estimate the coefficients of the model using estimate:

```
Estimate Std. Error Z-value P-value
Regressions:
   Y~X1
                     1.02349
                                0.12017 8.51728
                                                    <1e-12
   Y~X2
                     0.91519
                                0.12380
                                         7.39244
                                                    <1e-12
   Y~Genell
                     0.48035
                                0.23991
                                         2.00224
                                                   0.04526
Intercepts:
                    -0.11221
                                0.15773 -0.71141
                                                    0.4768
Residual Variances:
                     0.67073
                                0.13415 5.00000
```

We can now use calibrateType1 to perform a simulation study. We just need to define the null hypotheses (i.e. which coefficients should be set to 0 when generating the data) and the number of simulations: To save time we only make 50 simulations but much more are necessary to really assess the type 1 error rate. Then we can use the summary method to display the results:

```
Estimated type 1 error rate [95% confidence interval]

> sample size: 50 | number of simulations: 50

link statistic correction type1error CI

Y~Genell Wald Gaus 0.12 [0.05492; 0.24242]

Satt 0.10 [0.04224; 0.21869]

SSC 0.10 [0.04224; 0.21869]

SSC + Satt 0.08 [0.03035; 0.19456]
```

2 Adjustment for multiple comparisons

2.1 Univariate Wald test, single model

When performing multiple testing, adjustment for multiple comparisons is necessary in order to control the type 1 error rate, i.e. to provide interpretable p.values. The **multcomp** package enables to do such adjustment when all tests comes from the same lvmfit object:

```
Y Y~X1 Y~X2 Y~X3 Y~X4 Y~X5 Y~X6 Y~~Y
                       0
Y~X1 0
                 0
                            0
                                  0
Y~X2 0
                       0
                            0
           0
                 1
                                        0
                                             0
Y~X3 0
           0
                 0
                            0
                                  0
                                        0
                       1
                                             0
Y~X4 0
                       0
                                  0
           0
                 0
                            1
                                        0
                                             0
                       0
Y~X5 0
           0
                 0
                            0
                                        0
                                             0
                                  0
Y~X6 0
           0
                 0
                       0
                            0
                                        1
                                             0
```

Simultaneous Tests for General Linear Hypotheses

```
Fit: estimate.lvm(x = lvm(Y \sim X1 + X2 + X3 + X4 + X5 + X6), data = df.data)
```

Linear Hypotheses:

```
Estimate Std. Error z value Pr(>|z|)
                      0.1589
                               2.058 0.20725
Y^{X1} == 0
           0.3270
Y^{X2} == 0
           0.4025
                      0.1596
                               2.523 0.06611 .
Y~X3 == 0
                               3.669 0.00144 **
           0.5072
                      0.1383
Y^{X4} == 0
                      0.1662
                               1.902 0.28582
           0.3161
Y~X5 == 0
           0.3875
                      0.1498
                               2.586 0.05554 .
Y^{X}6 == 0
            0.3758
                               2.859 0.02482 *
                      0.1314
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
(Adjusted p values reported -- single-step method)
```

Note that this correction relies on the Gaussian approximation. To use small sample corrections implemented in lavaSearch2, just call glht2 instead of glht:

Simultaneous Tests for General Linear Hypotheses

```
Fit: estimate.lvm(x = lvm(Y \sim X1 + X2 + X3 + X4 + X5 + X6), data = df.data)
```

Linear Hypotheses:

```
Estimate Std. Error t value Pr(>|t|)
Y^{X1} == 0
            0.3270
                       0.1750
                                1.869
                                         0.3290
Y^{X2} == 0
            0.4025
                       0.1757
                                 2.291
                                         0.1482
Y^{X} = 0
            0.5072
                       0.1522
                                3.333
                                         0.0123 *
Y^{X}4 == 0
            0.3161
                       0.1830
                                1.727
                                         0.4128
Y~X5 == 0
            0.3875
                       0.1650
                                2.349
                                         0.1315
Y^{X}6 == 0
            0.3758
                       0.1447
                                2.597
                                         0.0762 .
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
(Adjusted p values reported -- single-step method)
```

The single step method is the appropriate correction when one wants to report the most significant p-value relative to a set of hypotheses. If the second most significant p-value is also to be reported then the method "free" is more appropriate:

Simultaneous Tests for General Linear Hypotheses

```
Fit: estimate.lvm(x = lvm(Y \sim X1 + X2 + X3 + X4 + X5 + X6), data = df.data)
Linear Hypotheses:
          Estimate Std. Error t value Pr(>|t|)
Y^{X1} == 0
            0.3270
                        0.1750
                                  1.869
                                           0.1291
Y^{X2} == 0
            0.4025
                        0.1757
                                  2.291
                                           0.0913 .
Y~X3 == 0
            0.5072
                        0.1522
                                  3.333
                                           0.0123 *
Y^{X4} == 0
            0.3161
                        0.1830
                                  1.727
                                           0.1291
Y^{X5} == 0
            0.3875
                        0.1650
                                  2.349
                                           0.0913 .
Y^{X}6 == 0
            0.3758
                        0.1447
                                  2.597
                                           0.0645 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Adjusted p values reported -- free method)
```

Indeed, here there is no relations between the hypotheses. See the book: "Multiple Comparisons Using R" by Frank Bretz, Torsten Hothorn, and Peter Westfall (2011, CRC Press) for details about the theory underlying the **multcomp** package.

2.2 Univariate Wald test, multiple models

Pipper et al. in "A Versatile Method for Confirmatory Evaluation of the Effects of a Covariate in Multiple Models" (2012, Journal of the Royal Statistical Society, Series C) developed a method to assess the effect of an exposure on several outcomes when a different model is fitted for each outcome. This method has been implemented in the mmm function from the multcomp package for glm and Cox models. lavaSearch2 extends it to lvm.

Let's consider an example where we wish to assess the treatment effect on three outcomes X, Y, and Z. We have at hand three measurements relative to outcome Z for each individual:

```
X
                                        Y Gender
                                                                     Z2
                Age Treatment
                                                         Z1
                                                                                 Z3
1 39.12289 39.10415
                                                  1.8714112
                      placebo
                                0.6088958 female
                                                             2.2960633 -0.09326935
2 39.56766 39.25191
                                1.0001325 female 0.9709943
                                                             0.6296226
                         SSRI
3 41.68751 43.05884
                      placebo
                                2.1551047 female -1.1634011 -0.3332927 -1.30769267
4 44.68102 44.78019
                         SSRI
                                0.3852728 female -1.0305476
                                                             0.6678775
                                                                        0.99780139
5 41.42559 41.13105
                      placebo -0.8666783
                                            male -1.6342816 -0.8285492
                                                                        1.20450488
6 42.64811 41.75832
                         SSRI -1.0710170 female -1.2198019 -1.9602130 -1.85472132
   treatment
  1.1639675
1
2 -1.5233846
3 -2.5183351
4 -0.7075292
5 -0.2874329
6 -0.4353083
```

We fit a model specific to each outcome: and combine them into a list of lvmfit objects: We can then generate a contrast matrix to test each coefficient related to the treatment:

		Х:	(Intercept)	X: A	lge 1	X: 7	Γ reatm	ent	SSRI	Х:	si	gma:	2 Y:	: Y			
X :	TreatmentSSRI		0		0				1			(0	0			
Υ:	Y~TreatmentSSRI		0		0				0			(0	0			
Z:	eta~TreatmentSSRI		0		0				0			(0	0			
		Υ:	Y~Genderfema	le Y	7: Y	~Tre	eatmer	tSS	RI Y	: Y	~~Y	Z :	Z1	Z :	Z2	Z :	Z3
X :	TreatmentSSRI			0					0		0		0		0		0
Υ:	Y~TreatmentSSRI			0					1		0		0		0		0
Z:	eta~TreatmentSSRI			0					0		0		0		0		0
		Z:	eta~Treatmen	tSSR	RI Z	: Z	1~~Z1	Z:	Z2~~	Z2 Z	Z: 2	Z3~	~Z3	Z:	eta	a~~	eta
X :	TreatmentSSRI				0		0			0			0				0
Υ:	Y~TreatmentSSRI				0		0			0			0				0
Z:	eta~TreatmentSSRI				1		0			0			0				0

Simultaneous Tests for General Linear Hypotheses

Linear Hypotheses:

This can be compared to the unadjusted p.values:

Simultaneous Tests for General Linear Hypotheses

Linear Hypotheses:

```
Estimate Std. Error t value Pr(>|t|)

X: TreatmentSSRI == 0     0.4661     0.2533     1.840     0.0720 .

Y: Y~TreatmentSSRI == 0     -0.5421     0.2613     -2.074     0.0435 *

Z: eta~TreatmentSSRI == 0     -0.6198     0.4404     -1.407     0.1659

---

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Univariate p values reported)
```

3 Model diagnostic

3.1 Detection of local dependencies

The modelsearch function of lava is a diagnostic tool for latent variable models. It enables to search for local dependencies (i.e. model misspecification) and add them to the model. Obviously it is a data-driven procedure and its usefulness can be discussed, especially in small samples:

- the procedure is instable, i.e. is likely to lead to two different models when applied on two different dataset sampled from the same generative model.
- it is hard to define a meaningful significance threshold since p-values should be adjusted for multiple comparisons and sequential testing. However traditional methods like Bonferonni-Holm tend to over corrected and therefore reduce the power of the procedure since they assume that the test are independent.

The function modelsearch2 in lavaSearch2 partially solves the second issue by adjusting the p-values for multiple testing.

Let's see an example:

```
x2 Id
                                 уЗ
                                            x1
         у1
                      у2
            4.883752014
  5.5071523
                         6.2928016
                                    0.8694750
                                                2.3991549
             0.025832617
                         0.5088030 -0.6800096 -0.0898721
2 -0.6398644
3 -2.5835495 -2.616715027 -2.8982645 0.1732145 -0.8216484
 -2.5312637 -2.518185427 -2.9015033 -0.1594380 -0.2869618
  1.6346220 -0.001877577 0.3705181
                                    0.7934994
  0.4939972 1.759884014
                         1.5010499 1.6943505 -1.0620840
```

modelsearch2 can be used to sequentially apply the modelsearch function with a given correction for the p.values:

Sequential search for local dependence using the score statistic The variable selection procedure retained 2 variables:

```
link statistic
                        p.value adjusted.p.value dp.Info selected nTests
    u~x2 6.036264 1.577228e-09
                                     5.008615e-08
                                                        1
                                                              TRUE
                                                                        10
2 y2~~y3 2.629176 8.559198e-03
                                     6.055947e-02
                                                        1
                                                              TRUE
                                                                         9
  y3~x1 1.770997 7.656118e-02
                                     2.814424e-01
                                                        1
                                                             FALSE
                                                                         8
Confidence level: 0.9 (two sided, adjustement: fastmax)
```

This indeed matches the highest score statistic found by modelsearch:

```
statistic p.value
6.036264e+00 1.577228e-09
```

We can compare the adjustment using the max distribution to bonferroni:

```
link none bonferroni max

1 u~x2 1.577228e-09 1.577228e-08 5.008615e-08

2 y2~~y3 8.559198e-03 8.559198e-02 6.055947e-02

3 y3~x1 7.656118e-02 7.656118e-01 2.814424e-01
```

3.2 Checking that the names of the variables in the model match those of the data

When estimating latent variable models using **lava**, it sometimes happens that the model does not converge:

Warning messages:

```
1: In estimate.lvm(mWrong, data = df.data) :
   Lack of convergence. Increase number of iteration or change starting values.
2: In sqrt(diag(asVar)) : NaNs produced
```

This can have several reasons:

- the model is not identifiable.
- the optimization routine did not managed to find a local optimum. This may happen for complex latent variable model where the objective function is not convex or locally convex.
- the user has made a mistake when defining the model or has not given the appropriate dataset.

The checkData function enables to check the last point. It compares the observed variables defined in the model and the one given by the dataset. In case of mismatch it returns a message:

```
Missing variable in data: X
```

In presence of latent variables, the user needs to explicitly define them in the model, otherwise checkData will identify them as an issue:

Missing variable in data: eta

No issue detected

4 Information about the R session used for this document

R version 3.5.1 (2018-07-02)

Platform: x86_64-w64-mingw32/x64 (64-bit)

Running under: Windows 7 x64 (build 7601) Service Pack 1

Matrix products: default

locale:

- [1] LC_COLLATE=Danish_Denmark.1252 LC_CTYPE=Danish_Denmark.1252
- [3] LC_MONETARY=Danish_Denmark.1252 LC_NUMERIC=C
- [5] LC_TIME=Danish_Denmark.1252

attached base packages:

[1] stats graphics grDevices utils datasets methods base

other attached packages:

[1] lavaSearch2_1.4 ggplot2_3.0.0 lava_1.6.3

loaded via a namespace (and not attached):

[1]	Rcpp_0.12.19	pillar_1.3.0	compiler_3.5.1	plyr_1.8.4
[5]	bindr_0.1.1	tools_3.5.1	tibble_1.4.2	gtable_0.2.0
[9]	lattice_0.20-35	pkgconfig_2.0.2	rlang_0.2.2	Matrix_1.2-14
[13]	parallel_3.5.1	mvtnorm_1.0-8	bindrcpp_0.2.2	withr_2.1.2
[17]	dplyr_0.7.6	stringr_1.3.1	grid_3.5.1	tidyselect_0.2.4
[21]	glue_1.3.0	R6_2.2.2	survival_2.42-6	multcomp_1.4-8
[25]	TH.data_1.0-9	purrr_0.2.5	reshape2_1.4.3	magrittr_1.5
[29]	scales_1.0.0	codetools_0.2-15	MASS_7.3-50	splines_3.5.1
[33]	assertthat_0.2.0	colorspace_1.3-2	numDeriv_2016.8-1	sandwich_2.5-0
[37]	stringi_1.2.4	lazyeval_0.2.1	munsell_0.5.0	crayon_1.3.4
[41]	zoo_1.8-4			