The Verb From Probabilities to Internal Categories

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Steedman and Bozsahin (2017). Projecting from the Lexicon, submitted Bozsahin (2017). Verbs, Heads, Word Orders and Types. in Word Order in Turkish, Springer, Ozsoy (ed.).



Verb

- Thematic structure
- Argument structure
- Word order
- Tense
- Aspect
- Mood

They have a lot to do with how we report ACTIONs and EVENTs.

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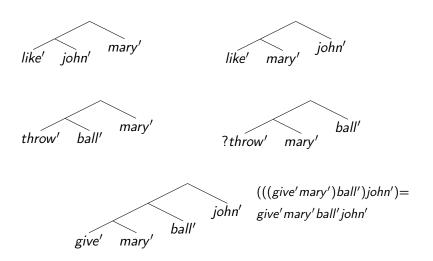
A brief history of Linguistics

- Thematic structure from argument structure
- Argument structure from thematic structure
- How do we get syntactic forms, logical forms and phonological forms ON THE FLY?
- These "interfaces" must be quite trivial

Language of Thought

- There seems to be a universal conceptual space (things, actions, events)
- That space seems to be asymmetric
- All human languages are probably homomorphic in that space
- Since languages differ in surface structure, surface structure cannot be homomorphic to that space
- That brings us to WORD ORDER
- How do we capture BOTH aspects if parsing is a reflex? (Garrett)

Asymmetry and structure



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The Verb

- (1) a. The window broke. init'(broken'w')
 - b. The stone broke the window. $\lambda z.cause'(init'(broken'w'))st'z$
 - c. The man broke the window with a stone. cause'(init'(broken'w'))st'man'

init'state': an inchoative event culminating in state state'

What are these primes and LFs? Hypotheses about LOT.

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Surface structure

(2) a. persuades :=
$$(S \setminus NP_{3s})/VP_{to-inf}/NP$$
 English

b. promises :=
$$(S \setminus NP_{3s})/VP_{\text{to-inf}}/NP$$

c. expects :=
$$(S \setminus NP_{3s})/VP_{\text{to-inf}}/NP$$

d. broke :=
$$(S \setminus NP)/PP/NP$$

e. broke :=
$$(S \setminus NP)/NP$$

f. broke :=
$$S \setminus NP$$

g. gwelodd (
$$saw.3s$$
) := $(S/NP)/NP_{3s}$

Welsh

h. iniutusan (order) :=
$$(S_{\rm DV}/VP)/NP_{\rm ANG,AGR}/NP_{\rm NG}$$
 Tagalog

_ ...

i. savundum (
$$defended.1s$$
) := $S \setminus S'_{acc}$

Turkish

j. viu (
$$saw.3s$$
) := $(S \setminus NP_{3s})/NP$

Portuguese

<ロ > < 個 > < 量 > < 重 > のQ ♡

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Categories: surface and argument structure

- (3) a. The window broke. broke := $S \setminus NP : \lambda x.init'(broken'x)$
 - b. The stone broke the window. broke := $(S \setminus NP)/NP : \lambda x \lambda y \lambda z.cause'(init'(broken'x))yz$
 - c. The man broke the window with a stone. $(S \setminus NP)/PP/NP : \lambda x \lambda y \lambda z. cause'(init'(broken'x))yz$

We get thematic structure as an inference over predicate-argument structure

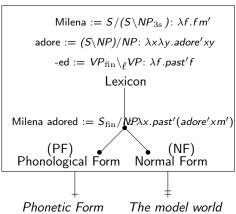


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Question

If surface structure is not homomorphic to universal conceptual structure, how do children learn the word order of their language?

Linguistic architecture



- combinatory projection to constituents of *string* := *syn:sen*
- serialization of feature geometry from *string* and *syn*
- normalization from syn and sem

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Conjecture

- Syntax is a HIDDEN variable for the child.
- She has to infer a CATEGORY from form-meaning pairs only.
- These pairs are subject to universal combinatorics. (PARSING)
- These inferences set up a MENTAL GRAMMAR.
- Such grammars are necessarily PROBABILISTIC.
- Change the nature of categories, and we might end up with PLANS and SCRIPTS.

Now with full categories

- (4) a. persuades := $(S \setminus NP_{3s})/VP_{\text{to-inf}}/NP: \lambda x \lambda p \lambda y. persuade'(px)xy$
 - b. promises := $(S \setminus NP_{3s})/VP_{\text{to-inf}}/NP$: $\lambda x \lambda p \lambda y . promise'(py) x y$
 - c. expects := $(S \setminus NP_{3s})/VP_{\text{to-inf}}/NP$: $\lambda x \lambda p \lambda y. expect'(px)y$
 - d. broke := $(S\NP)/PP/NP$: $\lambda x \lambda y \lambda z.cause'(init'broken'x)yz$
 - e. broke := $(S \setminus NP)/NP$: $\lambda x \lambda y \lambda z$.cause'(init' broken' x)yz
 - f. broke := $S \setminus NP$: $\lambda x.init'(broken'x)$
 - g. gwelodd (saw.3s) := $(S/NP)/NP_{3s}$: $\lambda x \lambda y.saw'yx$
 - h. iniutusan (order) := $(S_{\rm DV}/VP)/NP_{\rm ANG,AGR}/NP_{\rm NG}$: $\lambda x \lambda y \lambda p. order'(py)yx$
 - i. savundum (defended.1s) := $S_{\rm pd} \backslash S'_{\rm acc}$: $\lambda p. defend' pi' \wedge topic' i'$
 - j. viu (saw.3s) := $(S \setminus NP_{3s})/NP_{rex}$: $\lambda x \lambda y.saw' xy$

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Categorial Word order: not a metrical concept

(5) a. $(S \setminus NP)/NP$: $\lambda x \lambda y . verb' xy$	(SVO)
b. $(S/NP)\NP: \lambda x \lambda y.verb'yx$	(SVO')
c. $(S/NP)\NP: \lambda x \lambda y.verb'xy$	(OVS)
d. $(S \setminus NP)/NP$: $\lambda x \lambda y . verb' y x$	(OVS')
e. $(S\NP)\NP: \lambda x \lambda y.verb'xy$	(SOV)
f. $(S\NP)\NP: \lambda x \lambda y.verb'yx$	(OSV)
g. $(S/NP)/NP$: $\lambda x \lambda y$.verb'xy	(VOS)
h. $(S/NP)/NP$: $\lambda x \lambda y . verb' y x$	(VSO)

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Categorial Word order: not a metrical concept

(6) a. $(S \setminus NP)/NP$: $\lambda x \lambda y . verb' xy$	(SVO)	English
b. $(S/NP)\NP: \lambda x \lambda y.verb'yx$	(SVO')	Huastec
c. $(S/NP)\NP: \lambda x \lambda y. verb' xy$	(OVS)	Hixkaryana
d. $(S \setminus NP)/NP$: $\lambda x \lambda y . verb' y x$	(OVS')	Päri
e. $(S \setminus NP) \setminus NP$: $\lambda x \lambda y . verb' x y$	(SOV)	Turkish
f. $(S\NP)\NP: \lambda x \lambda y.verb'yx$	(OSV)	Dyirbal
g. $(S/NP)/NP$: $\lambda x \lambda y$.verb'xy	(VOS)	Tagalog
h. $(S/NP)/NP$: $\lambda x \lambda y$.verb' yx	(VSO)	Welsh

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A Micro Word-order Thought Experiment

- Syntax is a HIDDEN variable for the child.
- She has to infer a CATEGORY from form-meaning pairs only.
- These pairs are subject to universal combinatorics. (PARSING)
- These inferences set up a MENTAL GRAMMAR.
- Such grammars are necessarily PROBABILISTIC.
- All word orders are available to the child IN THE BEGINNING.

My Lab in Cyberspace: CCGlab

http://tinyurl.com/CCGlab-tool

Probabilistic CCG

L: Logical Form

S: Sentence

- D: Derivation
- Hidden variable problem: θ are weights of lexical assumptions

$$\arg\max_{L} P(L \mid S; \bar{\theta}) = \arg\max_{L} \sum_{D} P(L, D \mid S; \bar{\theta})$$
 (1)

- Ds are inferred, not observed.
- Relating probabilities and weights (hence categories):

$$P(L, D \mid S; \bar{\theta}) = \frac{e^{\bar{f}(L, D, S) \cdot \bar{\theta}}}{\sum_{L} \sum_{D} e^{\bar{f}(L, D, S) \cdot \bar{\theta}}}$$
(2)

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The Verb

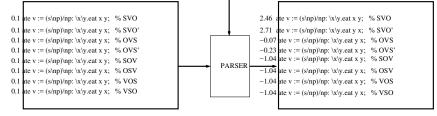
Parameter estimation: weight update

- Assume a mental grammar.
- Assume some data to be true (training set)
- What is assumed is form-meaning correspondence, not syntactic knowledge.
- Parse-to-learn to re-estimate the parameters

Learning workflow

TRAINING SET

threw the dog mommy: throw (def dog) mommy; the dog ate the biscuit : eat (def biscuit) (def dog); the eat ate the biscuit : eat (def biscuit) (def cat); mommy ate the biscuit : eat (def biscuit) mommy; he biscuit ate mommy: eat (def biscuit) mommy; % not favor OVS mommy threw the ball : throw (def ball) mommy; mommy threw the dog : throw (def dog) mommy:



GRAMMAR updated GRAMMAR

Log-likelihood of training data S_i, L_i

Log-linear model of structure prediction

$$O(\bar{\theta}) = \sum_{i=1}^{n} \log P(L_i \mid S_i; \bar{\theta}) = \sum_{i=1}^{n} \log (\sum_{D} P(L_i, D \mid S_i; \bar{\theta}))$$
(3)

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Derivative: How well each parameter serves training

$$\frac{\partial O}{\partial \theta_j} = E_{f_j(L_i, D, S_i) P(D|S_i, L_i; \bar{\theta})} - E_{f_j(L, D, S_i) P(L, D|S_i; \bar{\theta})}$$
(4)

Which is

$$\frac{\partial O}{\partial \theta_j} = \sum_{i=1}^n \sum_D f_j(L_i, D, S_i) P(D \mid S_i, L_i; \bar{\theta}) - \sum_{i=1}^n \sum_L \sum_D f_j(L, D, S_i) P(L, D \mid S_i; \bar{\theta})$$
(5)

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Then we apply Stochastic Gradient to re-estimate

Initialize $\bar{\theta}$ to some value.

for
$$k = 0 \cdots N - 1$$

for $i = 1 \cdots n$
 $\bar{\theta} = \bar{\theta} + \frac{\alpha_0}{1 + c(i + kn)} \frac{\partial \log P(L_i | S_i; \bar{\theta})}{\partial \bar{\theta}}$



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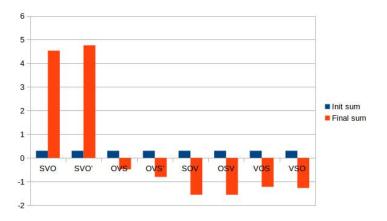
Micro-world

- All possibilities for all verbs are entered in initial mental grammar.
- Give a set of utterances whose meanings are assumed to be known.
- Train the categories on probabilities coming from the parses.
- Some will increase, some decrease, some stay the same.
- How big is the difference from initial grammar?

The training set

```
the dog ate the biscuit : eat (def biscuit) (def dog);
the cat ate the biscuit : eat (def biscuit) (def cat);
mommy ate the biscuit : eat (def biscuit) mommy;
the biscuit ate mommy: eat (def biscuit) mommy;
mommy threw the ball : throw (def ball) mommy;
mommy threw the dog : throw (def dog) mommy;
threw the dog mommy: throw (def dog) mommy;
the dog saw mommy : see mommy (def dog) ;
mommy saw the dog : see (def dog) mommy;
the dog walked: walk (def dog);
the cat slept : sleep (def cat);
the cat walked : walk (def cat);
the dog : def dog;
the cat: def cat:
mommy: mommy;
```

Verb categories update: 3 verbs total \times 8 categories

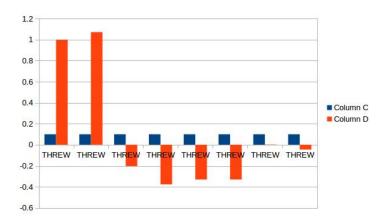


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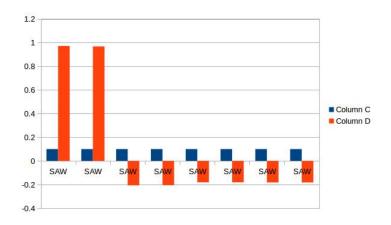
Ate parameters



Threw parameters



Saw parameters



Conclusion

- These conditions are quite realistic for the child.
- A computationally efficient grammatical theory can attack the hidden-variable problem in syntax
- to fast convergence without brain switches,
- to meet the timeframe of language acquisition and the size of grammars children learn.

Ta!