# judgment day

```
library(reticulate)
library(data.table)
library(tidyverse)
## -- Attaching packages -----
                                                       ----- tidyverse 1.3.0 --
## v ggplot2 3.3.3
                      v purrr
                                  0.3.4
## v tibble 3.1.0 v dplyr
                                  1.0.5
## v tidyr 1.1.3 v stringr 1.4.0
## v readr 1.4.0 v forcats 0.5.1
## -- Conflicts -----
                                             ----- tidyverse_conflicts() --
## x dplyr::between() masks data.table::between()
## x dplyr::filter() masks stats::filter()
## x dplyr::first() masks data.table::first()
## x dplyr::lag() masks stats::lag()
## x dplyr::last() masks data.table::last()
## x purrr::transpose() masks data.table::transpose()
library(pROC)
## Type 'citation("pROC")' for a citation.
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
       cov, smooth, var
use_virtualenv("../venv/", required = TRUE)
source_python("util.py")
source_python("models.py")
```

# **Functions**

```
calculate_yhat_sklearn <- function(model, x) {
  return(model$predict_proba(x)[,2])
}

calculate_yhat_NN <- function(model, x) {
  return(model$predict(x))
}

calculate_TPR <- function(y, yhat) {
  P <- sum(y == 1)
  TP <- sum(((yhat > 0.5) == 1) & (y == 1))
  TPR <- TP / P</pre>
```

```
return(TPR)
}
calculate_FPR <- function(y, yhat) {</pre>
  N \leftarrow sum(y == 0)
  FP \leftarrow sum(((yhat > 0.5) == 1) & (y == 0))
 FPR <- FP / N
 return(FPR)
}
calculate_AUC <- function(y, yhat) {</pre>
  df <- data.frame(a=y, p=yhat)</pre>
  df <- df[order(df$a),]</pre>
  roc_obj <- roc(df$a, df$p)</pre>
  AUC <- auc(roc_obj)
  TPR10 <- coords(roc_obj, x=0.9, input="specificity")$sensitivity # Sensitivity is AKA the FPR
  return(c(AUC=AUC, TPR10=TPR10))
}
# This function assumes that the data variables are already defined in the environment.
# E.q. Black_x, AsianPI_y, etc.
calculate_results <- function(model, model_yhat_fn) {</pre>
  # (1) Prepare results matrix
  race_eth_all <- c('White', 'Black', 'AsianPI', 'AmeriIndian')</pre>
  results <- matrix(nrow = length(race_eth_all), ncol = 5)
  rownames(results) <- race_eth_all</pre>
  colnames(results) <- c('TPR', 'FPR', 'AUC', 'TPR10', 'Accuracy')</pre>
  # (2) Calculate TPR, AUC, and TPR10 for each race/ethnicity
  for (i in 1:length(race_eth_all)) {
    race_eth <- race_eth_all[i]</pre>
    x <- get(paste0(race_eth, '_x')) # get() gets a variable in the environment by name
    y <- get(paste0(race_eth, '_y'))</pre>
    yhat <- model_yhat_fn(model, x) # Note this depends on function arguments
    results[i, 1] <- calculate_TPR(y, yhat)</pre>
    results[i, 2] <- calculate_FPR(y, yhat)</pre>
    results[i, c(3, 4)] <- calculate_AUC(y, yhat)
    results[i, 5] \leftarrow mean((yhat > 0.5) == y)
  }
  return(data.frame(results))
```

#### Fairness evaluations

# Early Stillbirth

```
x <- fread('../data/final/stillbirth_test.csv')
outcome <- 'early stillbirth'
x$outcome <- as.numeric(x$outcome == outcome)</pre>
```

```
AmeriIndian_x <- x %>% filter(race_AmeriIndian == 1)

AmeriIndian_y <- AmeriIndian_x %outcome

AmeriIndian_x <- AmeriIndian_x %>% select(-outcome)

AsianPI_x <- x %>% filter(race_AsianPI == 1)

AsianPI_y <- AsianPI_x %outcome

AsianPI_x <- AsianPI_x %>% select(-outcome)

Black_x <- x %>% filter(race_Black == 1)

Black_y <- Black_x %outcome

Black_x <- Black_x %>% select(-outcome)

White_x <- x %>% filter(race_White == 1)

White_y <- White_x %outcome

White_x <- White_x %>% select(-outcome)
```

## Logistic Regression

```
lr_early <- load_pickle("../models/lr_early")</pre>
calculate_results(model = lr_early, model_yhat_fn = calculate_yhat_sklearn)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                     TPR
                                         AUC
                                                 TPR10 Accuracy
                               FPR.
## White
               0.6319825 0.2002173 0.7740625 0.4764513 0.7994961
## Black
               0.8699187 0.4967108 0.8124215 0.5249710 0.5047357
## AsianPI
               0.6153846 0.1380192 0.8053455 0.5219780 0.8615261
## AmeriIndian 0.5666667 0.2477958 0.6735228 0.3666667 0.7518387
```

## LightGBM

```
gb_early <- load_pickle("../models/gb_early")
calculate_results(model = gb_early, model_yhat_fn = calculate_yhat_sklearn)

## Setting levels: control = 0, case = 1

## Setting direction: controls < cases

## Setting direction: controls < cases

## Setting direction: controls < cases

## Setting levels: control = 0, case = 1

## Setting direction: controls < cases</pre>
```

#### ReLU Network

```
relu_early <- load_NN("../models/lrelu_early")</pre>
calculate_results(relu_early, calculate_yhat_NN)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                     TPR
                                FPR
                                                   TPR10 Accuracy
                                          AUC
## White
               0.4775465 0.06554349 0.7401706 0.5180723 0.9336763
## Black
               0.6643438 0.18627631 0.7865401 0.6097561 0.8131343
## AsianPI
               0.4780220 0.03400753 0.7664236 0.5769231 0.9650928
## AmeriIndian 0.4333333 0.04763785 0.6814822 0.5000000 0.9513396
```

#### SELU Network

```
selu_early <- load_NN("../models/selu_early")</pre>
calculate_results(selu_early, calculate_yhat_NN)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
                                FPR.
##
                                           AUC
                                                   TPR10 Accuracy
               0.6100767 0.08522958 0.8435614 0.6226725 0.9142501
## White
               0.8536585 0.28297052 0.8881560 0.7073171 0.7175685
## Black
## AsianPI
               0.6813187 0.04847925 0.8872953 0.7307692 0.9510226
## AmeriIndian 0.5666667 0.03329385 0.7920680 0.6000000 0.9659180
```

# Late Stillbirth

```
x <- fread('../data/final/stillbirth_test.csv')
outcome <- 'late stillbirth'
x$outcome <- as.numeric(x$outcome == outcome)

AmeriIndian_x <- x %>% filter(race_AmeriIndian == 1)
AmeriIndian_y <- AmeriIndian_x$outcome
AmeriIndian_x <- AmeriIndian_x %>% select(-outcome)

AsianPI_x <- x %>% filter(race_AsianPI == 1)
AsianPI_y <- AsianPI_x$outcome
AsianPI_x <- AsianPI_x %>% select(-outcome)

Black_x <- x %>% filter(race_Black == 1)
Black_y <- Black_x$outcome
Black_x <- black_x$outcome
Black_x <- black_x$outcome
White_x <- x %>% filter(race_White == 1)
White_y <- White_x$outcome
White_x <- White_x$outcome
White_x <- White_x %>% select(-outcome)
```

### Logistic Regression

```
lr_late <- load_pickle("../models/lr_late")</pre>
calculate_results(model = lr_late, model_yhat_fn = calculate_yhat_sklearn)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                     TPR.
                               FPR
                                         AUC
                                                  TPR10 Accuracy
## White
               0.6483376 0.2374591 0.7532278 0.4437340 0.7623739
## Black
               0.8432836 0.5149632 0.7725808 0.4440299 0.4859167
               0.5267176 0.1645129 0.7463088 0.4045802 0.8350773
## AmeriIndian 0.8292683 0.4420228 0.8016243 0.5609756 0.5587076
```

#### LightGBM

```
gb_late <- load_pickle("../models/gb_late")
calculate_results(model = gb_late, model_yhat_fn = calculate_yhat_sklearn)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases</pre>
```

```
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                     TPR
                                FPR
                                          AUC
                                                  TPR10 Accuracy
## White
               0.6413043 0.11387128 0.8367200 0.6259591 0.8857706
               0.7630597 0.27135383 0.8426006 0.6063433 0.7287307
## Black
## AsianPI
               0.6641221 0.05710634 0.8848103 0.7022901 0.9425237
## AmeriIndian 0.7073171 0.17633502 0.8677560 0.6341463 0.8233517
```

#### ReLU Network

```
relu_late <- load_NN("../models/lrelu_late")</pre>
calculate_results(relu_late, calculate_yhat_NN)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                      TPR
                                   FPR
                                              AUC
                                                      TPR10 Accuracy
## White
               0.05051151 0.0009627569 0.6649044 0.3804348 0.9976499
## Black
               0.31716418 0.0116490048 0.7086099 0.4645522 0.9867025
## AsianPI
               0.09923664 0.0080740049 0.7195041 0.4885496 0.9907414
## AmeriIndian 0.34146341 0.0191611246 0.7525820 0.5121951 0.9791174
```

## SELU Network

```
selu_late <- load_NN("../models/selu_late")
calculate_results(selu_late, calculate_yhat_NN)

## Setting levels: control = 0, case = 1

## Setting direction: controls < cases

## Setting levels: control = 0, case = 1

## Setting direction: controls < cases

## Setting levels: control = 0, case = 1

## Setting direction: controls < cases

## Setting direction: controls < cases

## Setting levels: control = 0, case = 1</pre>
```

```
## Setting direction: controls < cases

## TPR FPR AUC TPR10 Accuracy

## White 0.6585678 0.14210591 0.8320714 0.6131714 0.8576026

## Black 0.8190299 0.35812422 0.8416441 0.6082090 0.6423109

## AsianPI 0.6564885 0.06700613 0.8642600 0.6717557 0.9326270

## AmeriIndian 0.8292683 0.26173701 0.8766467 0.7073171 0.7385080
```

# Preterm Birth

```
x <- fread('../data/final/preterm_test.csv')
outcome <- 'preterm'
x$outcome <- as.numeric(x$outcome == outcome)

AmeriIndian_x <- x %>% filter(race_AmeriIndian == 1)
AmeriIndian_y <- AmeriIndian_x$outcome
AmeriIndian_x <- AmeriIndian_x %>% select(-outcome)

AsianPI_x <- x %>% filter(race_AsianPI == 1)
AsianPI_y <- AsianPI_x$outcome
AsianPI_x <- AsianPI_x %>% select(-outcome)

Black_x <- x %>% filter(race_Black == 1)
Black_y <- Black_x$outcome
Black_x <- Black_x %>% select(-outcome)

White_x <- x %>% filter(race_White == 1)
White_y <- White_x$outcome
White_x <- White_x %>% select(-outcome)
```

# Logistic Regression

```
lr_preterm <- load_pickle("../models/lr_preterm")</pre>
calculate_results(model = lr_preterm, model_yhat_fn = calculate_yhat_sklearn)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                     TPR.
                               FPR
                                          AUC
                                                  TPR10 Accuracy
## White
               0.3713707 0.1834861 0.6285827 0.2661478 0.7711041
## Black
               0.8916200 0.8203210 0.6197046 0.2465778 0.2900029
## AsianPI
               0.3102148 0.1314462 0.6308708 0.2689366 0.8140581
## AmeriIndian 0.5899497 0.4070898 0.6274294 0.2422111 0.5925188
```

```
LightGBM
gb_preterm <- load_pickle("../models/gb_preterm")</pre>
calculate_results(model = gb_preterm, model_yhat_fn = calculate_yhat_sklearn)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                               FPR
                                         AUC
                                                 TPR10 Accuracy
## White
               0.4273950 0.2193859 0.6418888 0.2705877 0.7445816
## Black
               0.8511784 0.7431200 0.6345674 0.2520533 0.3489737
               0.3724463 0.1732598 0.6425101 0.2801467 0.7823997
## AsianPI
## AmeriIndian 0.6055276 0.4139806 0.6382355 0.2462312 0.5885988
ReLU Network
relu_preterm <- load_NN("../models/lrelu_preterm")</pre>
calculate_results(relu_preterm, calculate_yhat_NN)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                     TPR.
                                FPR.
                                          AUC
                                                  TPR10 Accuracy
               0.2857222 0.11350406 0.6266735 0.2656780 0.8252099
## White
```

#### SELU Network

## Setting direction: controls < cases

## Black

## AsianPI

```
selu_preterm <- load_NN("../models/selu_preterm")
calculate_results(selu_preterm, calculate_yhat_NN)
## Setting levels: control = 0, case = 1</pre>
```

0.6912570 0.55304531 0.6190991 0.2456553 0.4848123

0.2588790 0.08965541 0.6303297 0.2728130 0.8467595

## AmeriIndian 0.3693467 0.18513131 0.6254665 0.2402010 0.7559631

```
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
##
                     TPR
                                FPR
                                          AUC
                                                  TPR10 Accuracy
## White
               0.3491525 0.15479196 0.6407108 0.2698968 0.7946045
               0.6738781 0.50254026 0.6330132 0.2505059 0.5247979
## Black
               0.2735464 0.09733821 0.6377759 0.2768989 0.8412582
## AsianPI
## AmeriIndian 0.4869347 0.28818620 0.6357260 0.2467337 0.6820809
```

# Notes

"Further research would also include inspecting the reproducibility of the results beyond the population of the United States with different ML models. The best machine learning models (SELU network, LGBM and averaged ensemble) were able to produce repeatable performance over two data sets. Using these machine learning models, especially for early stillbirth, could provide earlier identification of at-risk pregnancies with high accuracy and provide tools for better utilization of healthcare resources targeted to those needing it most."