

# Transformations of Space-time frames

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## INTRODUCTION

Transformations allow an observer to analyse different space frames. They contain four general types: translation, dilation, reflection and rotation. I propose there exists similar transformations between space-time frames. One of which has already been proposed by Einstein in "The theory of relativity" which observes translations between space-time frames.

Relativity at its mathematical foundation is describing translations between space-time frames. Perspectivity is describing dilation transformations between space-time frames. Symmetrivity describes reflection transformations between space-time frames. Imaginivity describes rotational transformations between space-time frames.

## RELATIVISTIC TRANSLATIONS OF SPACE-TIME

Einstein proposed that via Lorentz transformations from  $x, y, z, t$  to  $x', y', z', t'$  it is possible to observe two different space-time frames. The following equations describe the translations between two space-time frames,

$$x' = \frac{x - vt}{\sqrt{1 - \frac{v^2}{c^2}}}, \quad (1)$$

$$y' = y, \quad (2)$$

$$z' = z, \quad (3)$$

$$t' = \frac{t - \frac{xv}{c^2}}{\sqrt{1 - \frac{v^2}{c^2}}}, \quad (4)$$

When the velocity of light  $c$  becomes infinitely large, the Galilei transformations are obtained:

$$x' = x - vt, \quad (5)$$

$$y' = y, \quad (6)$$

$$z' = z, \quad (7)$$

$$t' = t, \quad (8)$$

## Special relativity

If a light signal is sent in positive x-direction we find

$$x = ct, \quad (9)$$

and so using Lorentz transformations we find that,

$$x' = \frac{(c - v)t}{\sqrt{1 - \frac{v^2}{c^2}}}, \quad (10)$$

$$t' = \frac{(1 - \frac{v}{c})t}{\sqrt{1 - \frac{v^2}{c^2}}}. \quad (11)$$

## PERSPECTIVE DILATION OF SPACE-TIME

X, Y and Z are the set of positions in the corresponding x,y and z dimensions. If we take a single (x,y,z,t) point and transform it at the speed of light in x-direction using perspective dilation of space-time, we obtain (X', Y', Z', t') where using interval notation,

$$X' = [x, x'], \text{ where } x' = \frac{x - vt}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (12)$$

$$Y' = [y, y'], \text{ where } y' = y \quad (13)$$

$$Z' = [z, z'], \text{ where } z' = z \quad (14)$$

$$t' = \frac{t - \frac{xv}{c^2}}{\sqrt{1 - \frac{v^2}{c^2}}}, \quad (15)$$

Now let's repeat this method but with sets X, Y and Z, where V is a set of velocities for all x in X and T is a set of points in time,

$$X'' = X \cup X', \text{ where } X' = \frac{X - Vt}{\sqrt{1 - \frac{V^2}{c^2}}} \quad (16)$$

$$Y'' = Y \cup Y', \text{ where } Y' = Y \quad (17)$$

$$Z'' = Z \cup Z', \text{ where } Z' = Z \quad (18)$$

$$T' = \frac{t - \frac{XV}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}}, \quad (19)$$

if all v in V are the same for all x then,

$$t' = \frac{t - \frac{XV}{c^2}}{\sqrt{1 - \frac{V^2}{c^2}}}, \quad (20)$$

We can repeat k times to obtain,

$$X^k = \cup_{i=1}^k X^i, \text{ where } X^{i+1} = \frac{X^i - V^i t}{\sqrt{1 - \frac{(V^i)^2}{c^2}}} \quad (21)$$

$$Y^k = \cup_{i=1}^k Y^i, \text{ where } Y^{i+1} = Y^i \quad (22)$$

$$Z^k = \cup_{i=1}^k Z^i, \text{ where } Z^{i+1} = Z^i \quad (23)$$

$$T^k = \frac{t - \frac{X^k V^k}{c^2}}{\sqrt{1 - \frac{(V^k)^2}{c^2}}}, \quad (24)$$

if all V in  $V^k$  are the same for all X then,

$$t = \frac{t - \frac{X^k V^k}{c^2}}{\sqrt{1 - \frac{(V^k)^2}{c^2}}}, \quad (25)$$

## Similar Perspectivity

If  $x'/x = y'/y = z'/z$ , then the dilation is uniform across all space-time and so everything remains the same in perspective of each other,

$$X' = Ax, \quad (26)$$

$$Y' = Ay, \quad (27)$$

$$Z' = Az, \quad (28)$$

$$t' = t, \quad (29)$$

## Quantum to classical to relativistic space-time frames

## SYMMETRIC REFLECTIONS OF SPACE-TIME

Supersymmetry, parallel universes in opposite time, parallel universes in opposite space

## IMAGINATIVE ROTATIONS OF SPACE-TIME

Imaginary numbers, waves, universes.

## TRANSFORMATION COMBINATIONS

### Relative perspective transformations

Perspective frames can be compared using relativity.

## CONCLUSION

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  - [3] A.P. Vanden Berg, D.A. Yuen, G. Beebe, M.D. Christiansen. *The dynamical impact of electronic thermal conductivity on deep mantle convection of exosolar planets.* (2010). Elsevier.