

# CSCI338 HW3

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## 1 Context-Free Grammars

**1.1**  $\{ a^n b^m \mid n \neq 2m \}$

$S \rightarrow aaSb \mid A \mid B$

$A \rightarrow aA \mid a$

$B \rightarrow bB \mid b$

**1.2**  $\{ a^i b^j c^k \mid i, j, k \geq 0 \text{ } j = k \text{ or } j = i \}$

$S \rightarrow S_1 \mid S_2$

$S_1 \rightarrow abS_1 \mid A \mid \epsilon$

$A \rightarrow cA \mid c \mid \epsilon$

$S_2 \rightarrow aS_2 \mid B \mid \epsilon$

$B \rightarrow Bbc \mid bc \mid \epsilon$

**1.3**  $\{ a^n b^m \mid n = 3m \}$

$S \rightarrow aaaSb \mid \epsilon$

**1.4**  $\{ a^n b^m \mid n \leq m + 3 \}$

$S \rightarrow aSb \mid A$

$A \rightarrow a \mid aa \mid aaa \mid B$

$B \rightarrow bB \mid \epsilon$

## 2 Ambiguous Grammer

Can I construct an identical string using two different paths?

Lets construct the string aab

$S \rightarrow aaB \rightarrow b \rightarrow aab$

$S \rightarrow AB:$

$A \rightarrow aA \rightarrow aa$

$B \rightarrow b$

$\rightarrow aab$

This language is ambiguous

## 3 CFG to PDA

## 4 Pumping Lemma

### 4.1

This language accepts some amount ( $\geq 0$ ) of 0's followed by atleast 1, but no more than 2 #, following by some amount ( $\geq 0$ ) of 0's

### 4.2

If G is a context free then there is a number P (Pumping length) such that  $S \in$  and  $|S| \geq P$  then S can be decomposed into  $S = UVXYZ$  S.T.:

1.  $uv^i xy^i z$
2.  $|vy| > 0$
3.  $|vxy| \leq P$