CSCI432 GW6

Brock Ellefson, Seth Severa

November 27, 2017

1 Diversify your group

We talked about this earlier, we will diversify for the next assignment.

2 Recall the Skyline problem. Give pseudocode for the sweepline algorithm

SkyLine sweep-line algorithm

Algorithm 1 Skyline

```
1: List buildings
 2: PriorityQueue events
 3: while currentBuilding \neq null do
       events.add(currentBuilding, currentBuilding.left)
       events.add(currentBuilding, currentBuilding.right)
       currentBuilding = currentBuilding.next
 6:
 7: end while
 8:
 9: List skyline
10: List currSkyline
11: double maxHeight = 0
   while events.peek() \neq null do
13:
       if event.peek().isLeft() then
14:
          currSkyline.add(event.peek())
          if maxheight
                          \neq checkMaxHeight(currSkyline) then sky-
   line.add(event.pop().left, checkmaxHeight(currSkyline))
          end if
16:
17:
       else
          currSkyline.remove(event.peek())
18:
          if maxheight \neq checkMaxHeight(currSkyline) then sky-
   line.add(event.pop().right, checkmaxHeight(currSkyline))
          end if
20:
       end if
21:
22: end while
23: return skyline
```

The loop invariant of this algorithm is that as the sweepline goes from left to right we always use the height of the current tallest building.

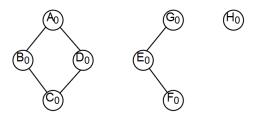
3 For the sweepline algorithm that computes whether there exist two line segments that intersect, explain how a line segment is added to or removed from T (the data structure that keeps track of the lines that intersect the sweep line).

T is a red-black tree, we sweep through the graph from left to right, stopping at endpoints to check for intersections and add or remove line segments to T. Every time we stop at an endpoint, we check the order of T, if the order of T is different than the order of T from the previous enpoint we stopped at, then there was an intersection. After this check, if the endpoint of the line segment the sweepline is on is the leftmost endpoint of the line, then we add that line segment to the red-black tree. If the endpoint of the line segment the sweepline is on is the rightmost endpoint of the line, then we remove that line segment from the red-black tree.

4 Union and Path Compression

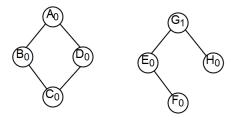
This iteration has 3 components all with rank 0 $\,$

Iteration I.



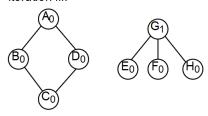
This iteration combines two components now giving g a rank of 1. We now only have 2 components

Iteration II.



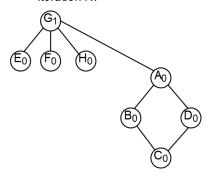
This iteration uses the second heuristic, path compression, along the find path. They now point directly to the root. We still have 2 components

Iteration III.



This iteration adds the two components together, since the g component has a higher rank than the a component, a will be added to g, however the rank will not be increased. There is now only one component

Iteration IV.



This iteration uses the second heuristic, path compression, along the find path. They now point directly to the root. We still have 1 component

