

$$Y_1, \dots, Y_n \sim U(0, \theta)$$

$$S = \min(Y_1, \dots, Y_n)$$

$$T = \max(Y_1, \dots, Y_n)$$

$$F_S(s) = \Pr(S \leq s)$$

$$= \Pr(\min(Y_1, \dots, Y_n) \leq s)$$

$$= 1 - \Pr(\min(Y_1, \dots, Y_n) > s)$$

$$= 1 - \Pr(\text{all } Y_1, \dots, Y_n > s)$$

$$= 1 - (1 - F_{Y_i}(s))^n$$

$$F_T(t) = \Pr(T \leq t)$$

$$= \Pr(\max(Y_1, \dots, Y_n) \leq t) = \Pr(\text{all } Y_i \leq t)$$

$$= F_{Y_i}(t)^n$$