

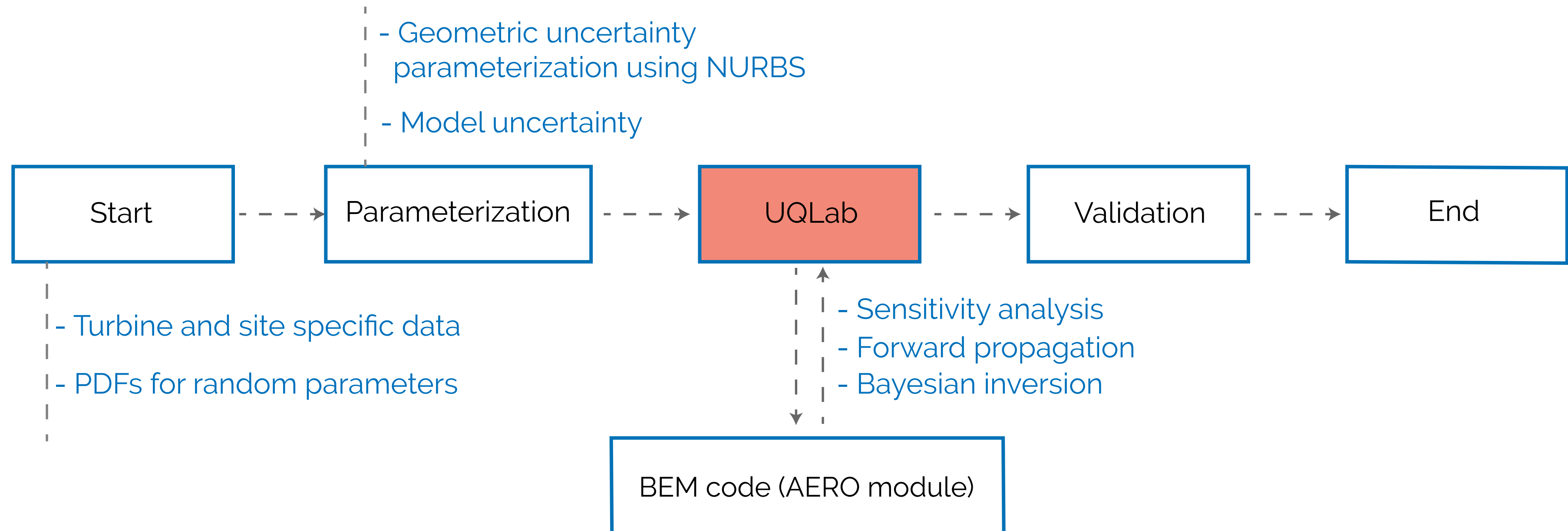
WindTrue: Sensitivity analysis applied to DANAERO wind turbine

Prashant Kumar
Benjamin Sanderse

The CWI logo consists of a red parallelogram with the white text "CWI" inside.

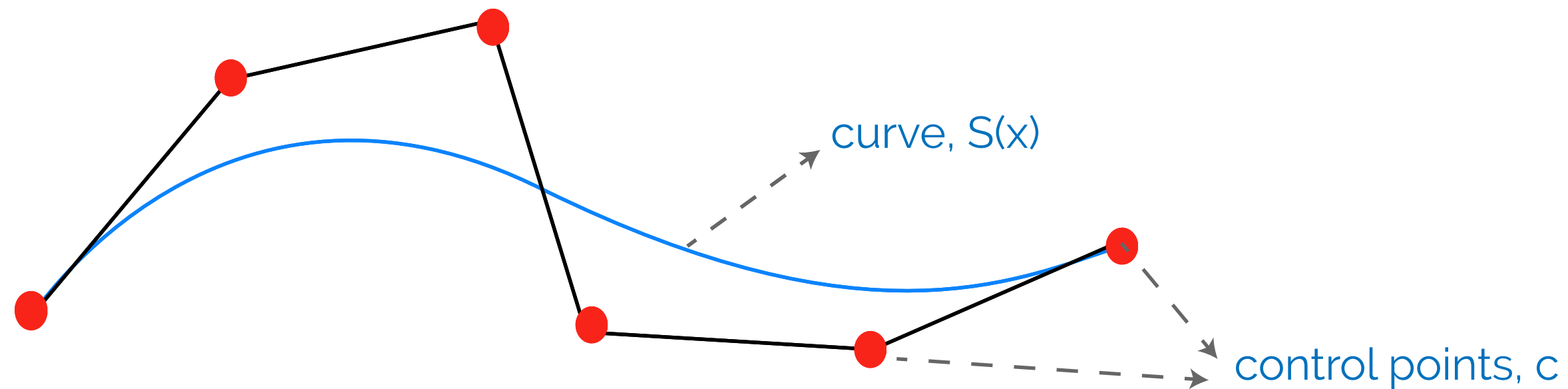
CWI

Workflow



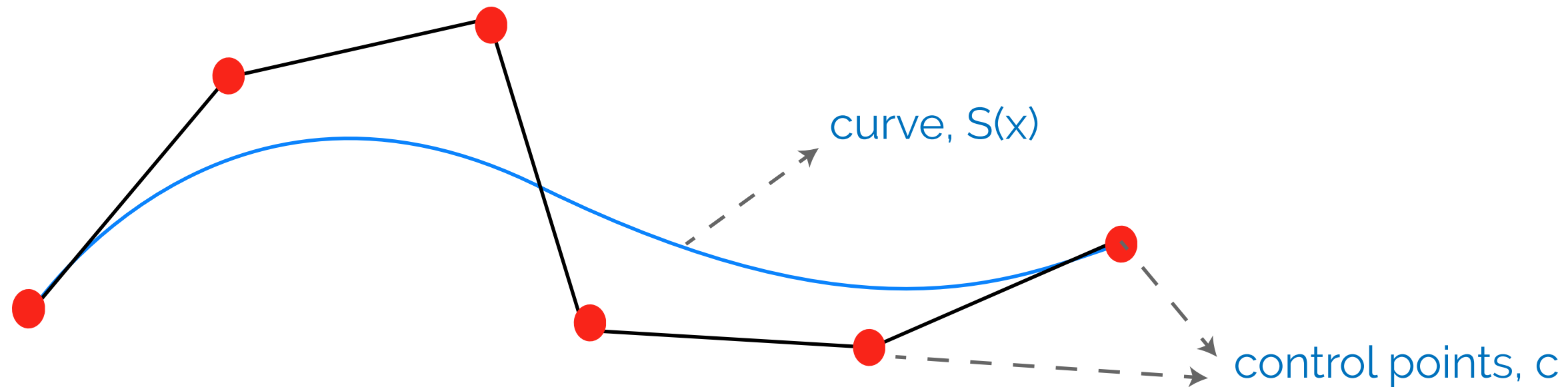
NURBS based parametrization

Non-Uniform Rational Basis Spline (NURBS)



$$S(x) = \sum_{i=0}^{N-1} c_i B_{i,p}(x)$$

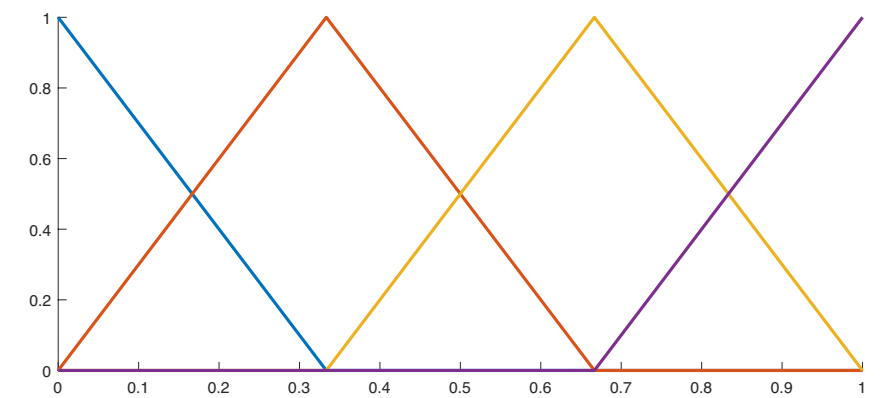
Non-Uniform Rational Basis Spline (NURBS)



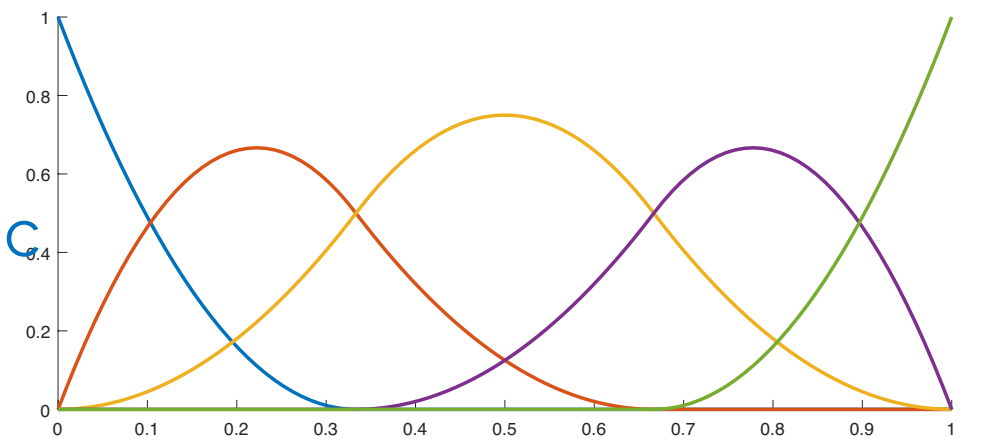
$$S(x) = \sum_{i=0}^{N-1} c_i B_{i,p}(x)$$

Basis functions, $B_{i,p}(x)$

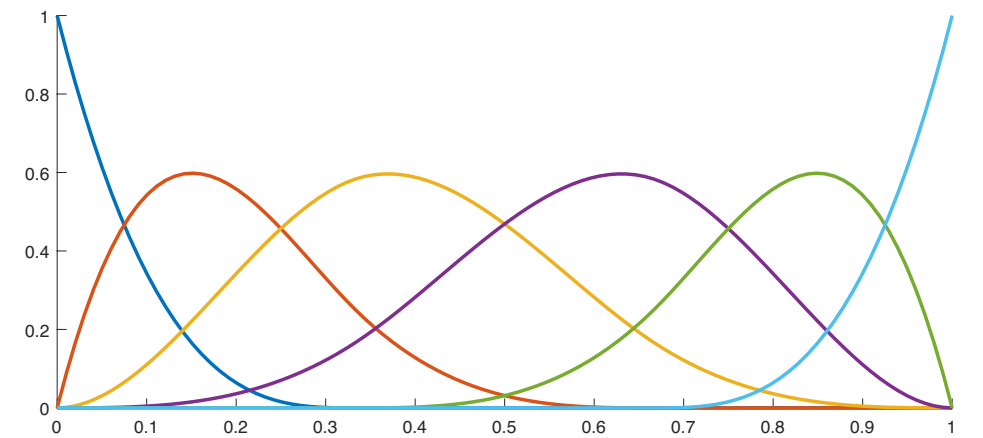
linear



quadratic



cubic



x

Why NURBS?

- > Represent complex shapes with very few points
- > Flexibility to design a large variety of shapes
- > Easy to obtain high-order polynomials

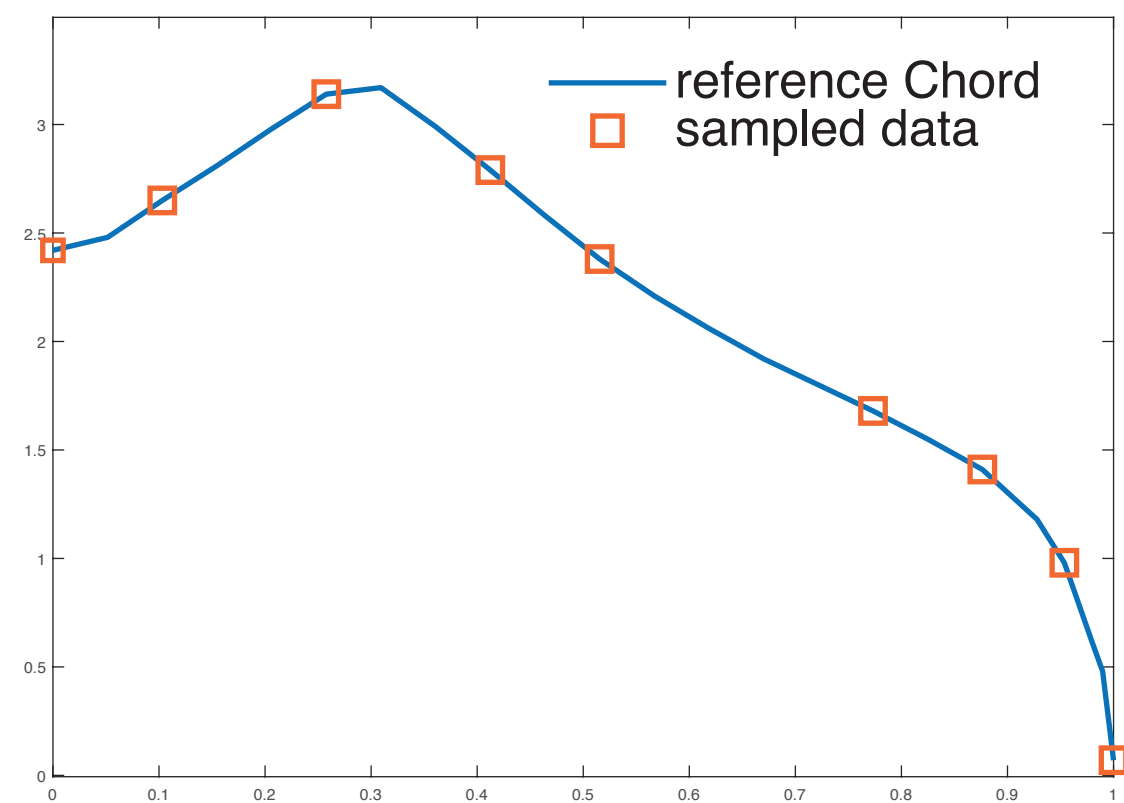
Parameterization using NURBS

Goal: Obtain perturbed chord/twist from a given reference curves

Parameterization using NURBS

Goal: Obtain perturbed chord/twist from a given reference curves

Step 1: Sample locations from the reference curve



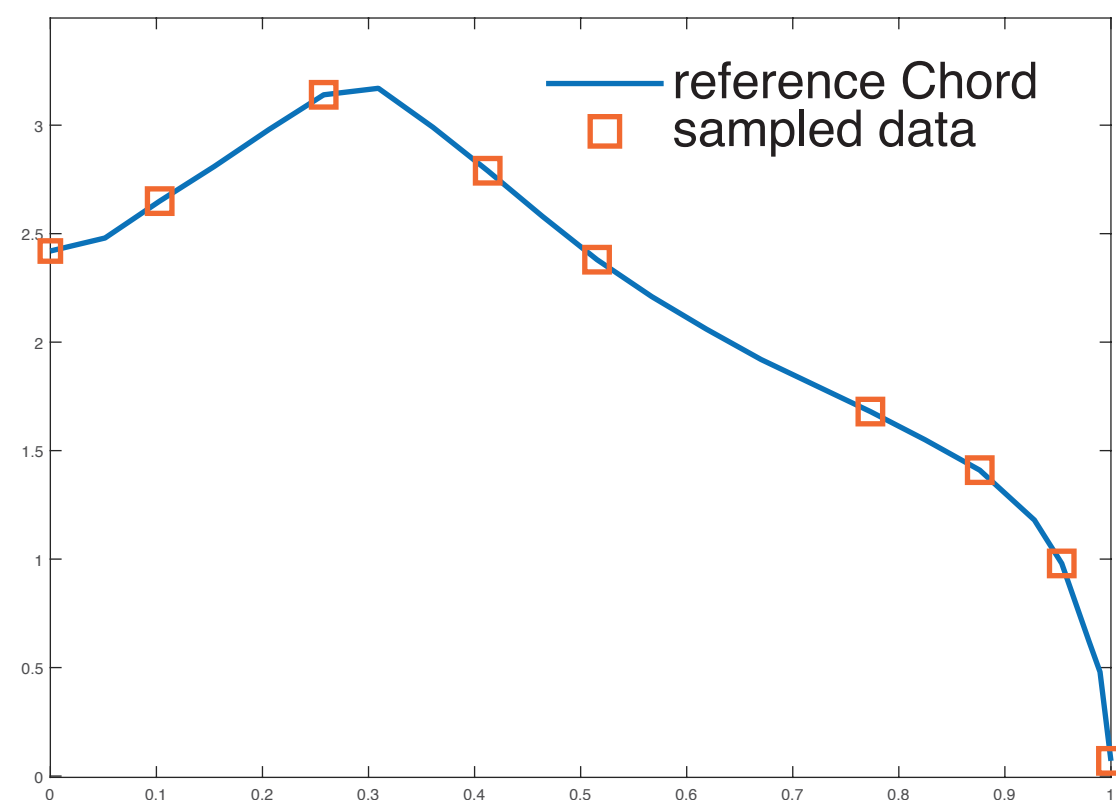
Parameterization using NURBS

Goal: Obtain perturbed chord/twist from a given reference curves

Step 1: Sample locations from the reference curve

Step 2: Compute control points at sampled location via inversion

$$\begin{array}{ccc} S(x) = \sum_{i=0}^{N-1} c_i B_{i,p}(x) & \implies & \mathbf{B}\mathbf{c} = \mathbf{S} \\ \downarrow & & \downarrow \\ \text{known} & & \text{known} \end{array}$$

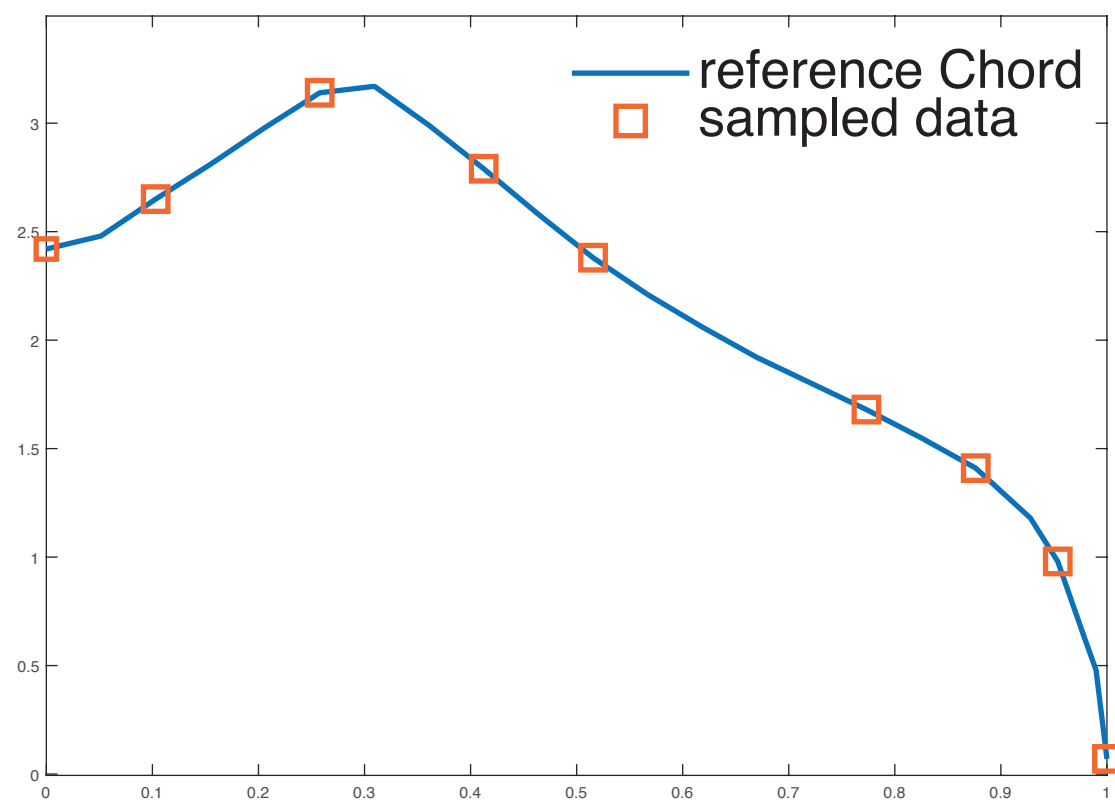


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Parameterization using NURBS

Goal: Obtain perturbed chord/twist from a given reference curves

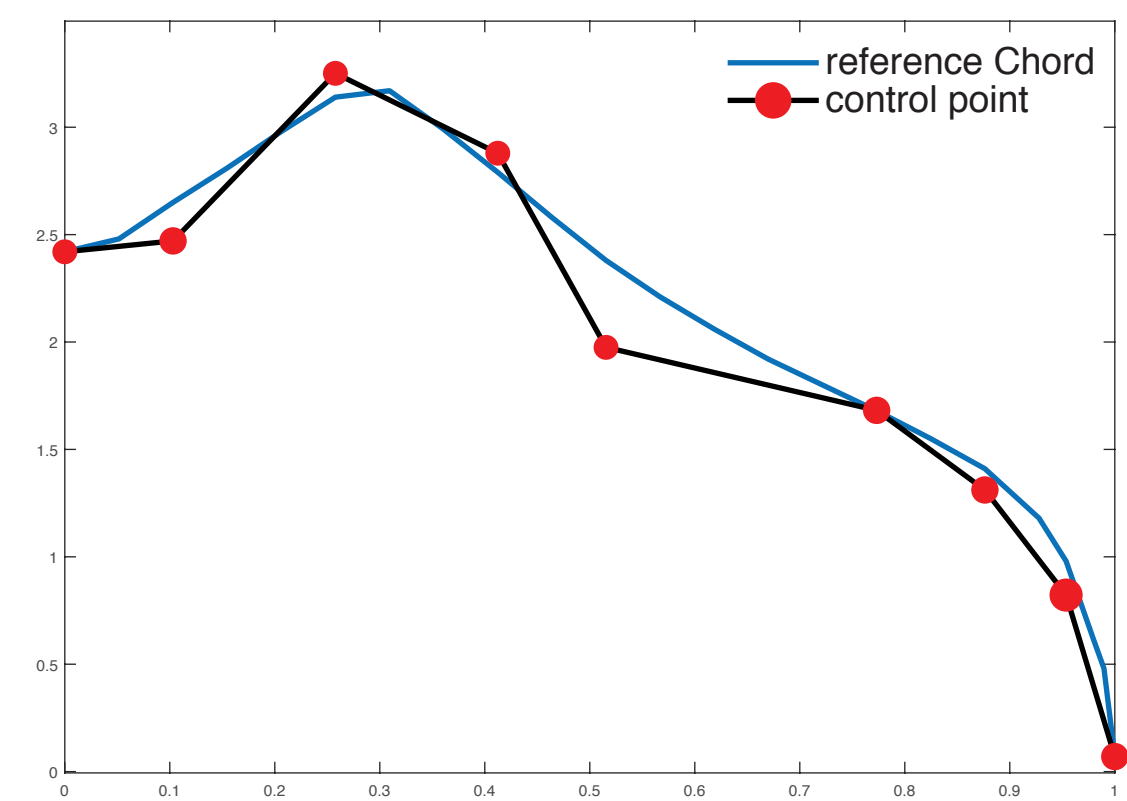
Step 1: Sample locations from the reference curve



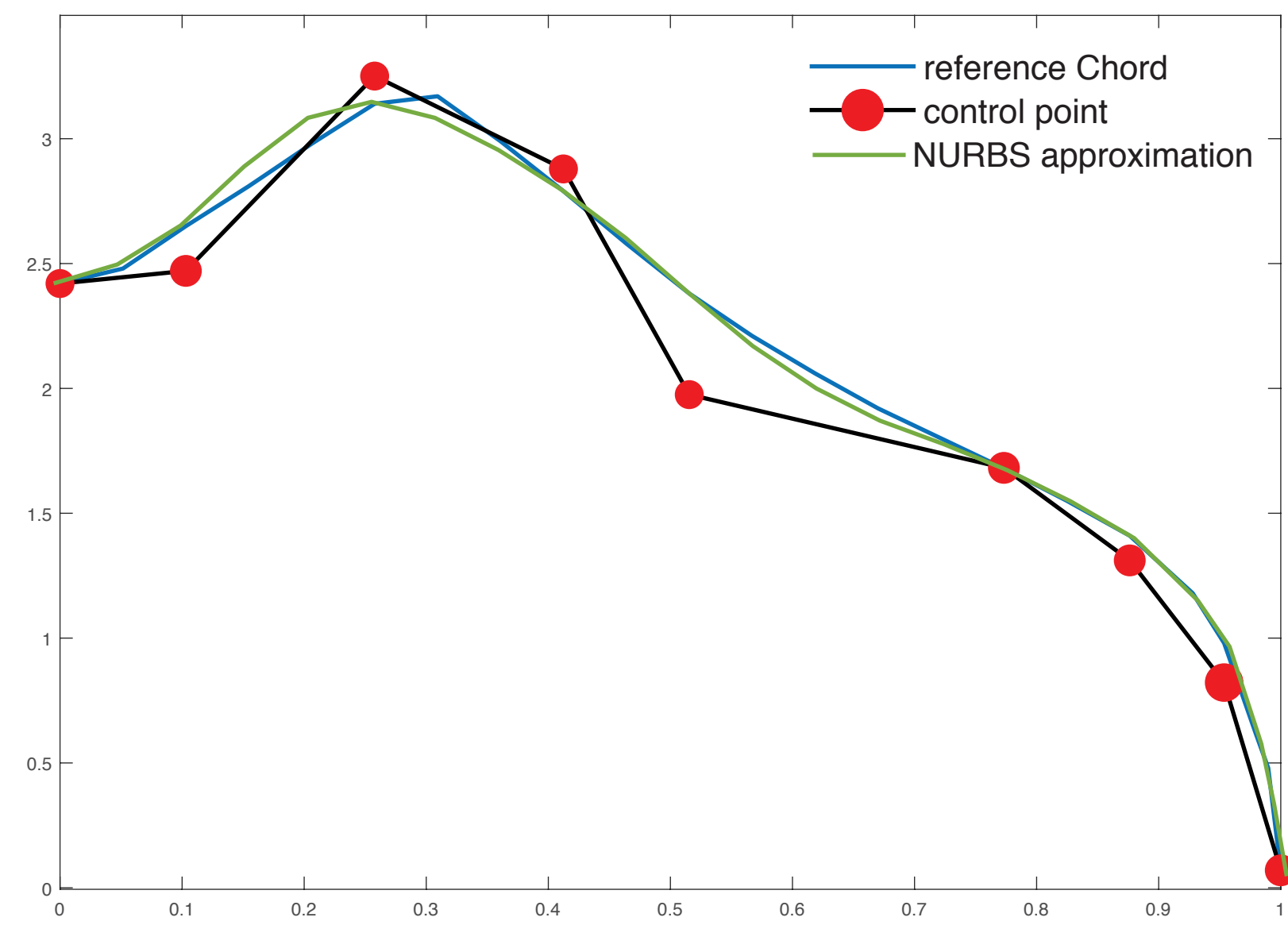
Step 2: Compute control points at sampled location via inversion

$$S(x) = \sum_{i=0}^{N-1} c_i B_{i,p}(x) \implies \mathbf{B}\mathbf{c} = \mathbf{S}$$

known known

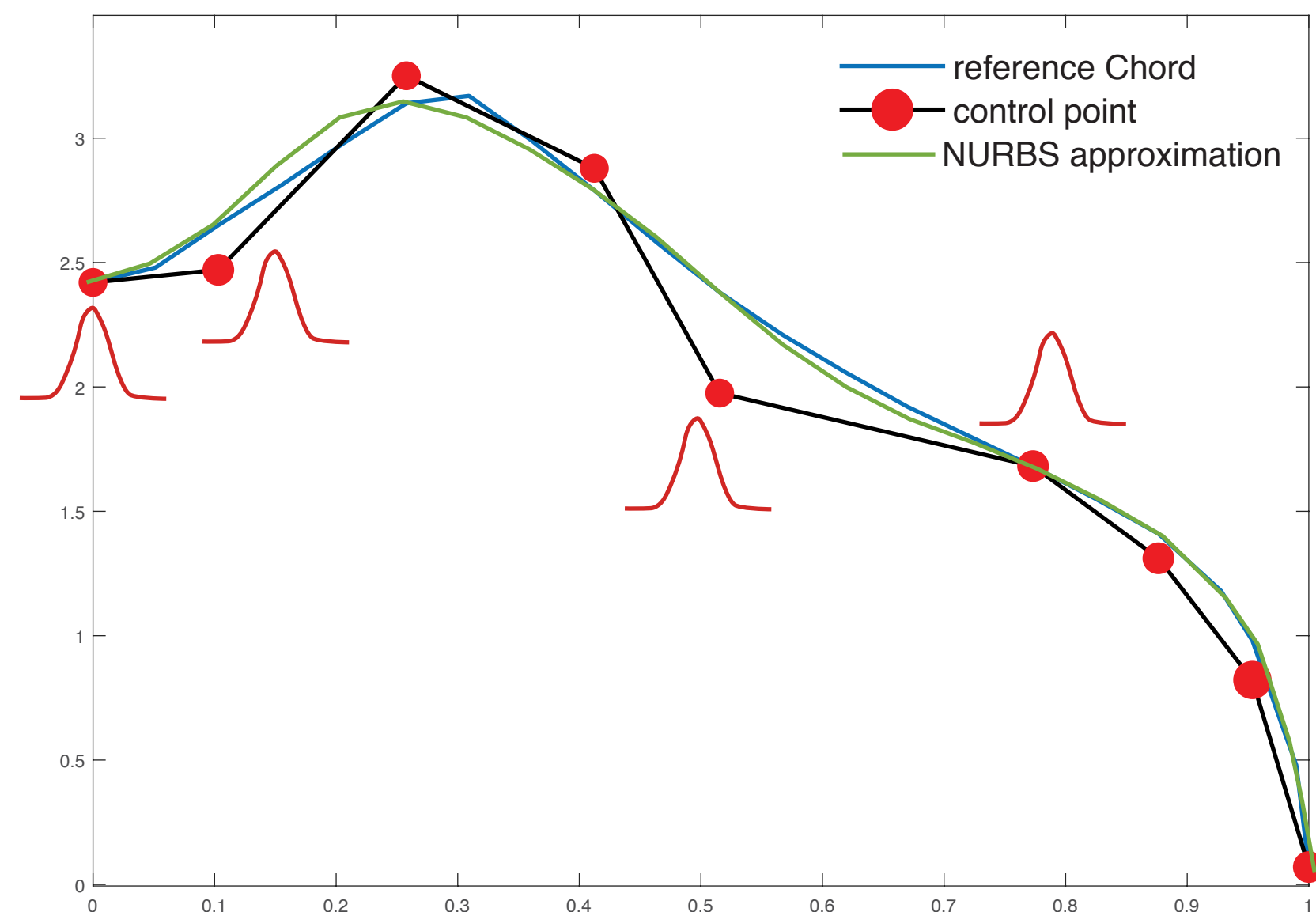


Parameterization using NURBS



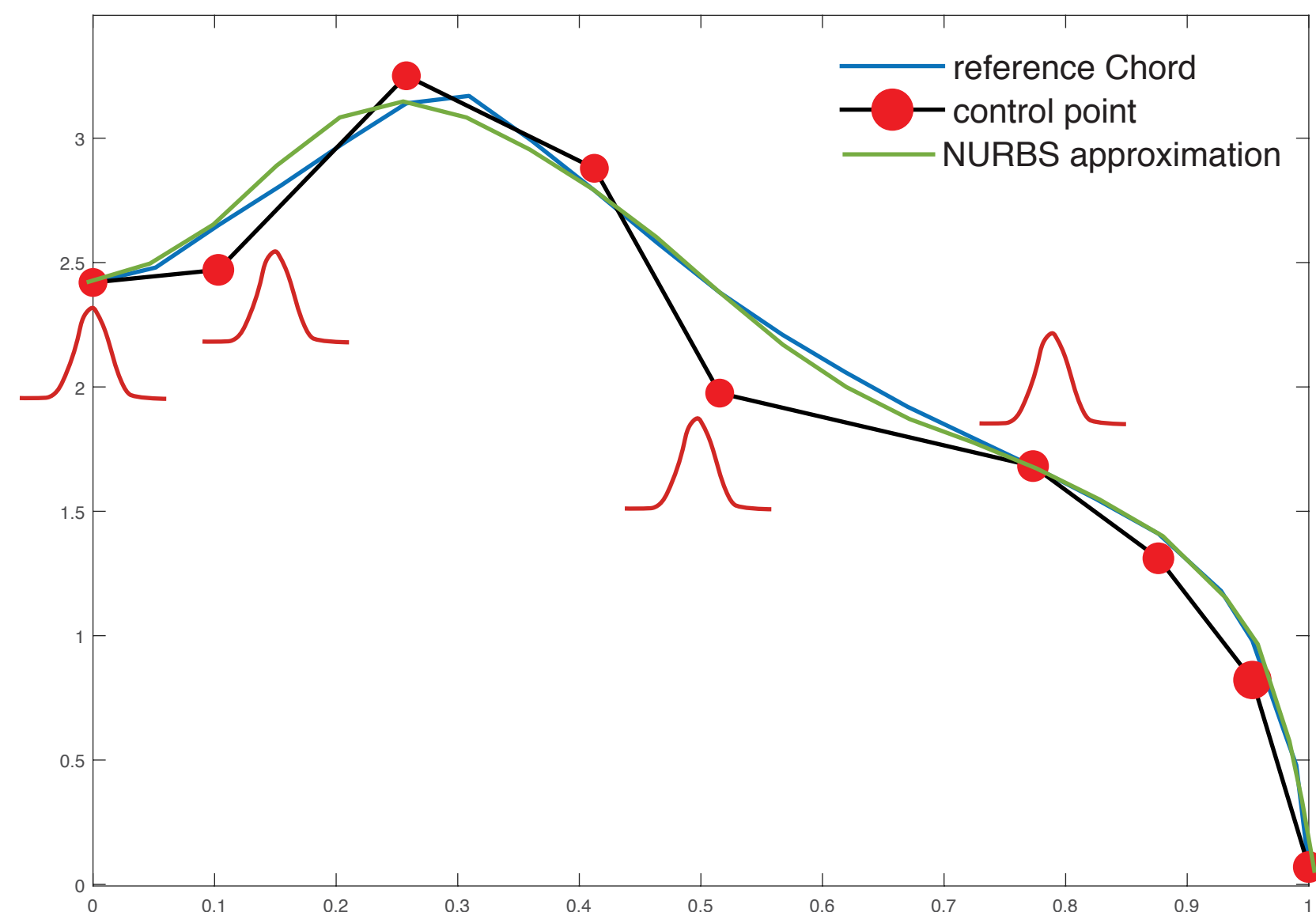
Parameterization using NURBS

Step 3: Perturb control point values using some PDF

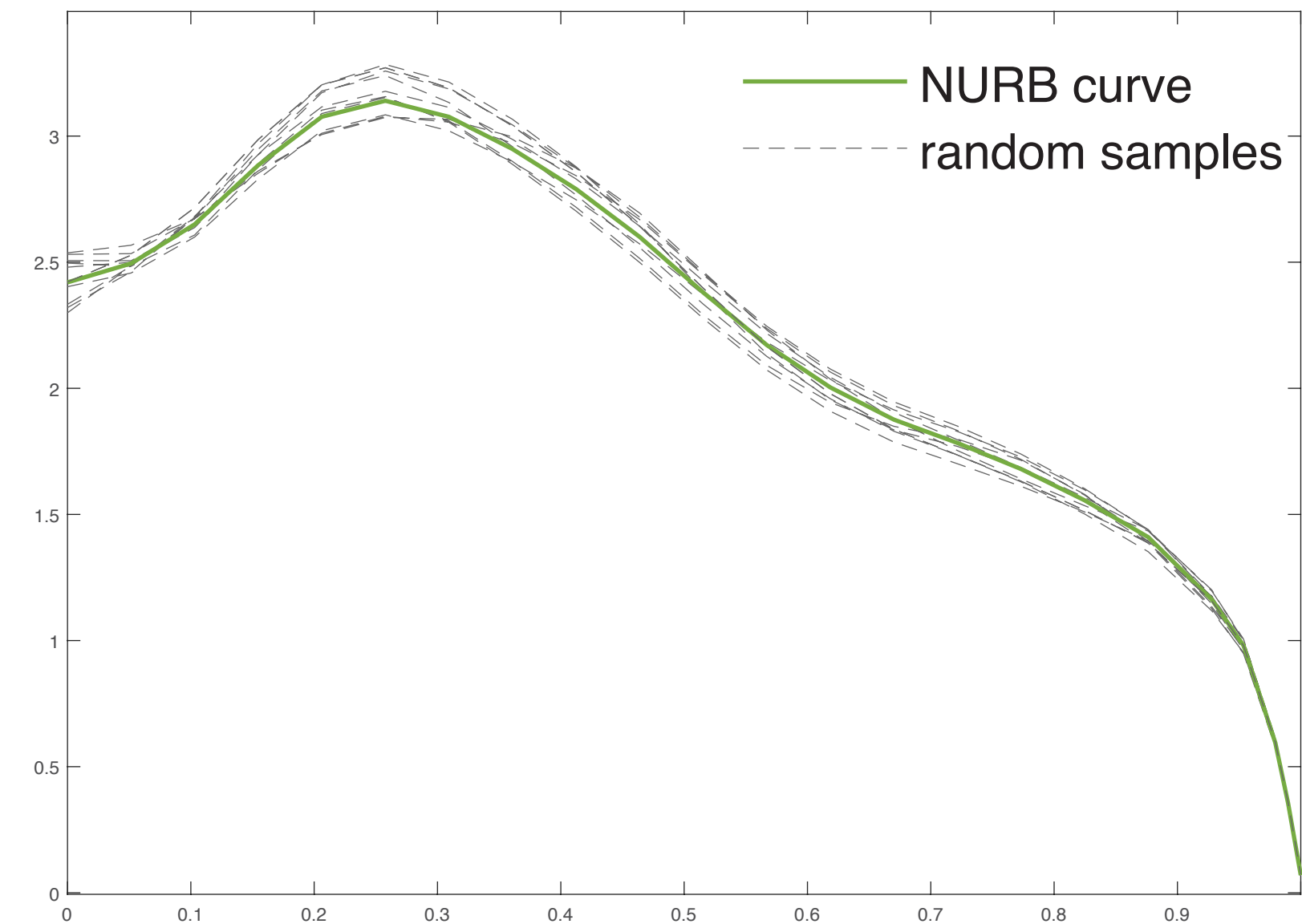


Parameterization using NURBS

Step 3: Perturb control point values using some PDF



Step 4: Sample perturbed curves



Global sensitivity analysis

Global sensitivity analysis

- > Goal is to rank the uncertain parameters in the order of importance
- > Global approaches cover the uncertainty spaces more exhaustively
- > Better able to capture uncertainty in the model output

Sobol sensitivity indices

Main idea: Decompose the variance of model output in terms of contribution from individual input parameters and their combinations.

$$V(y) = \sum_i V_i + \sum_{i,j} V_{i,j} + \text{higher order terms}$$

First order indices

$$S_1 = \frac{V_1}{V}, S_2 = \frac{V_2}{V}, \dots$$

Second order indices

$$S_{1,2} = \frac{V_{1,2}}{V}, S_{1,3} = \frac{V_{1,3}}{V}, \dots$$

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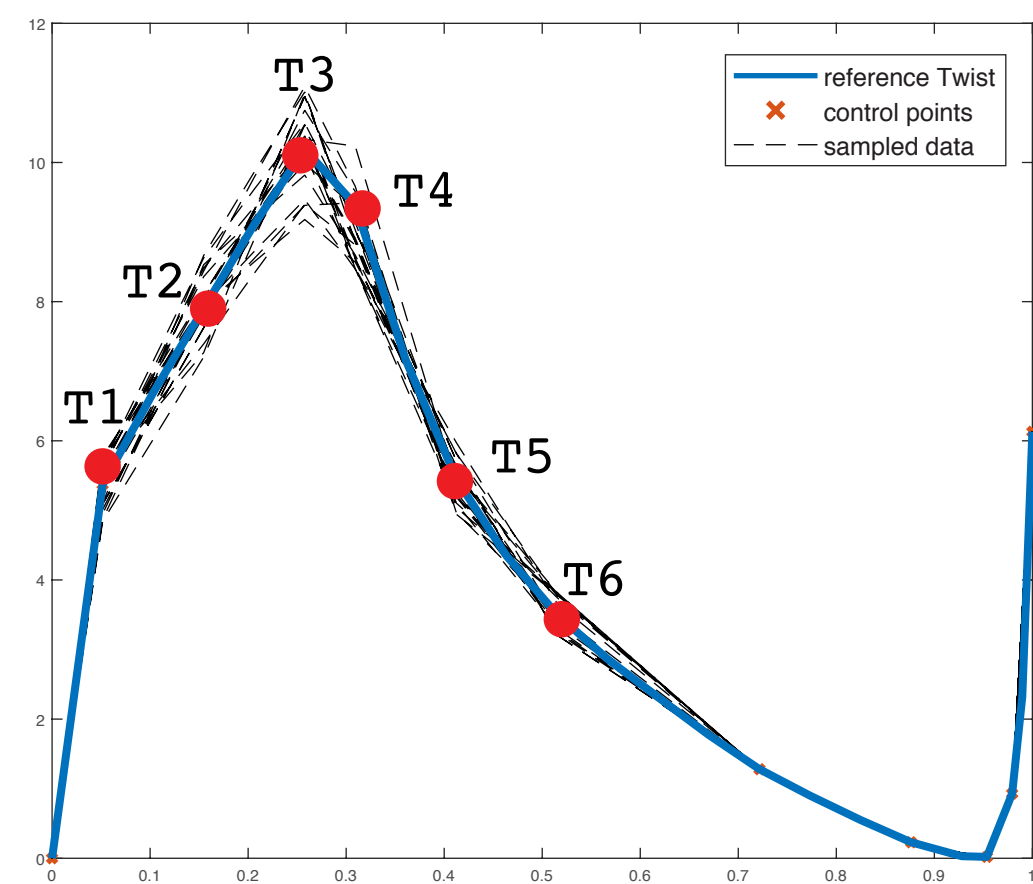
Second order indices

$$S_{1,2} = \frac{V_{1,2}}{V}, S_{1,3} = \frac{V_{1,3}}{V}, \dots$$

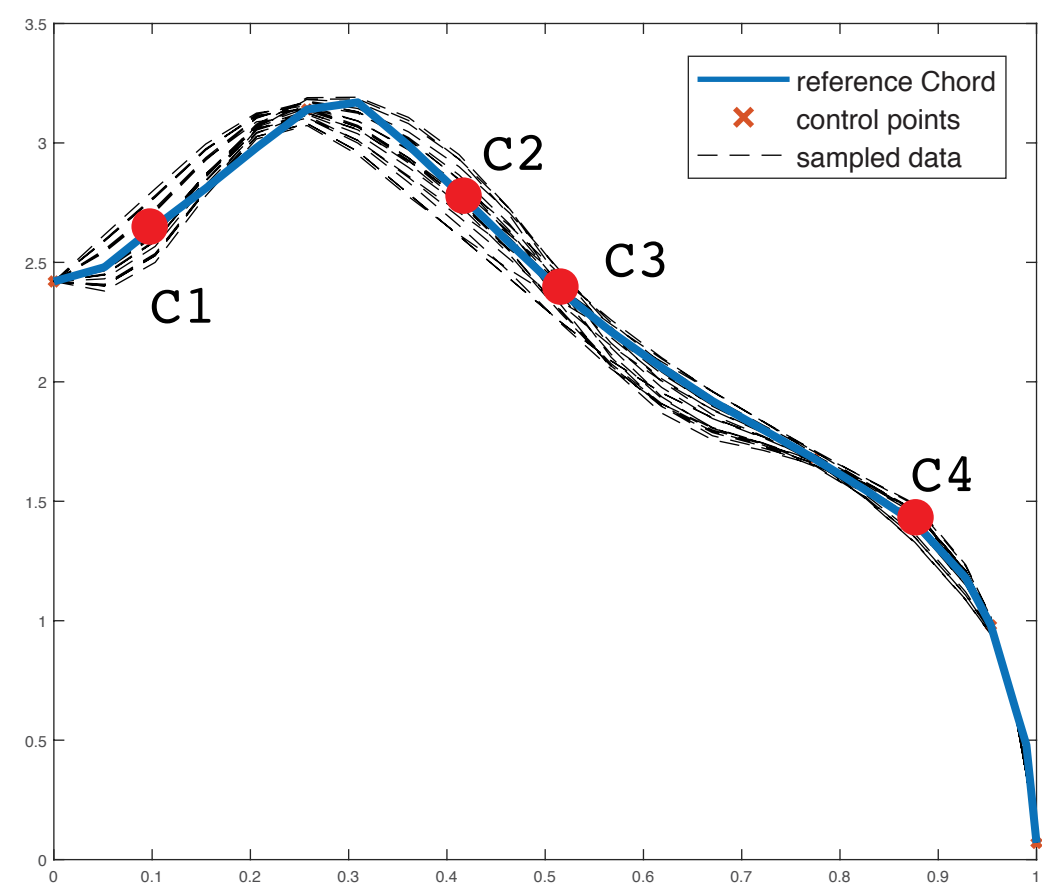
We use **adaptive Polynomial Choas Expansion** (Least angle regression) to compute variances

Sensitivity analysis results

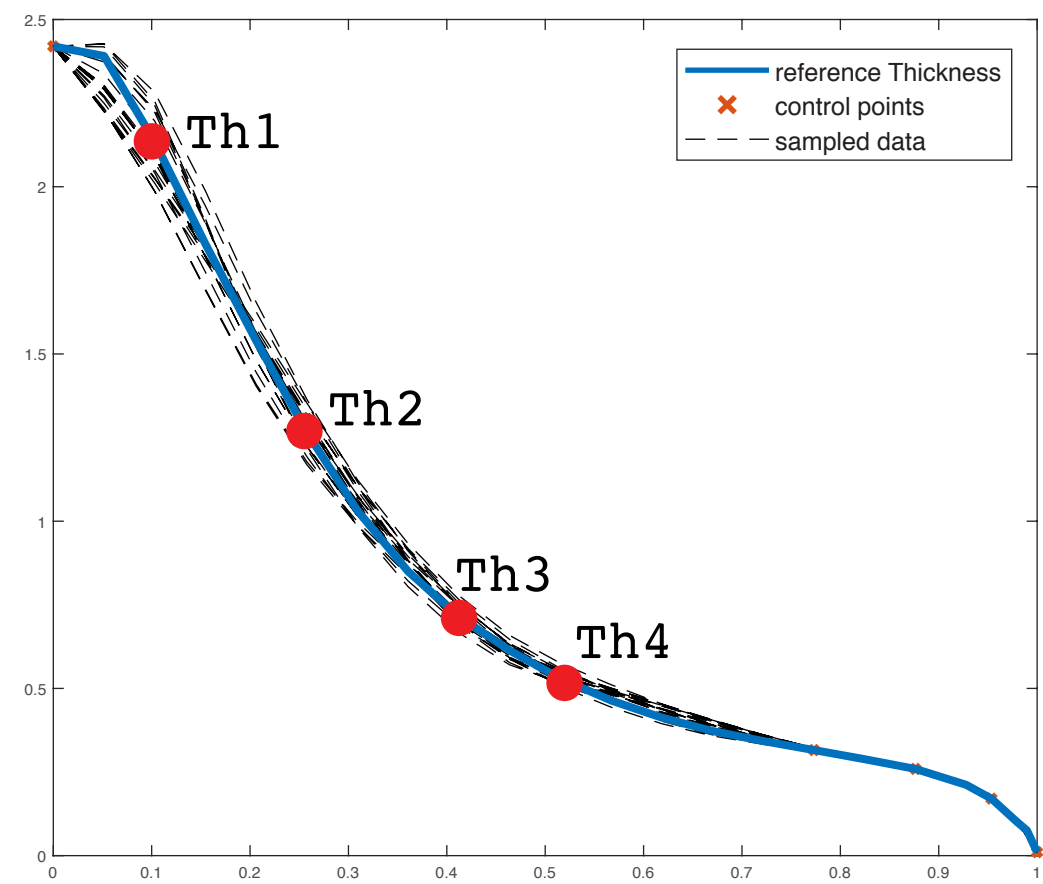
Geometric Uncertainty



Twist



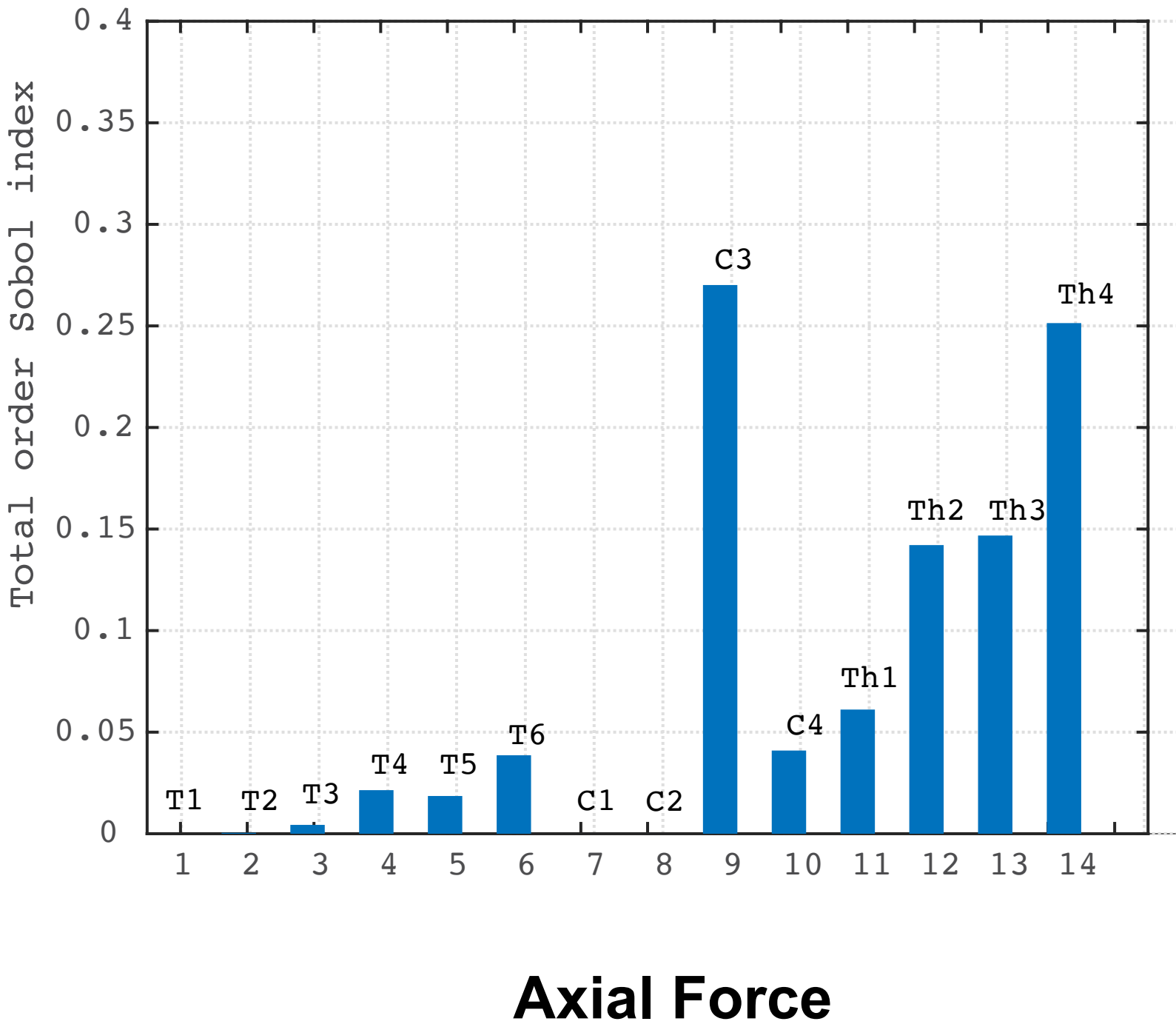
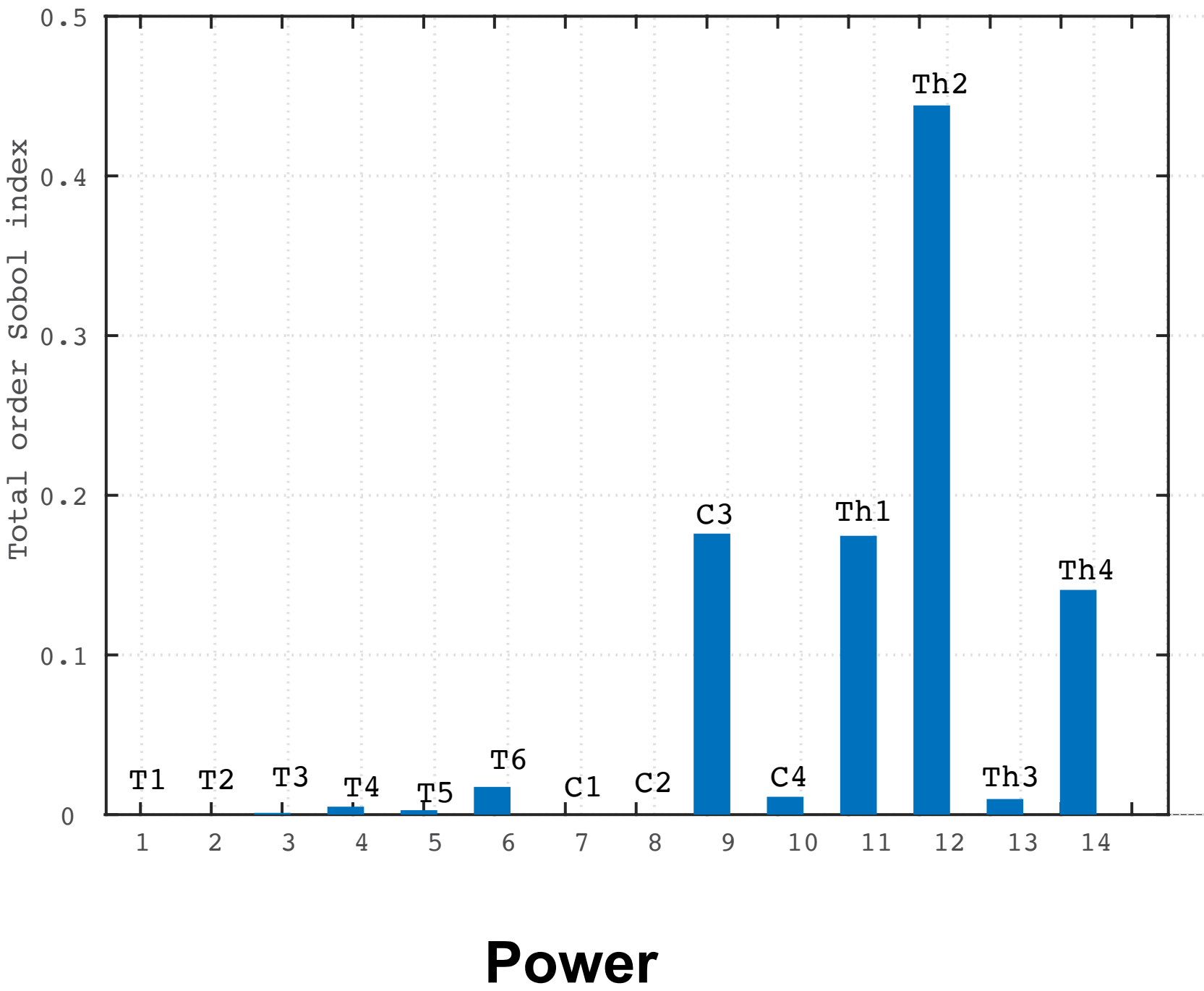
Chord



Thickness

10% (uniformly distributed) uncertainty in chosen control point

Sobol indices



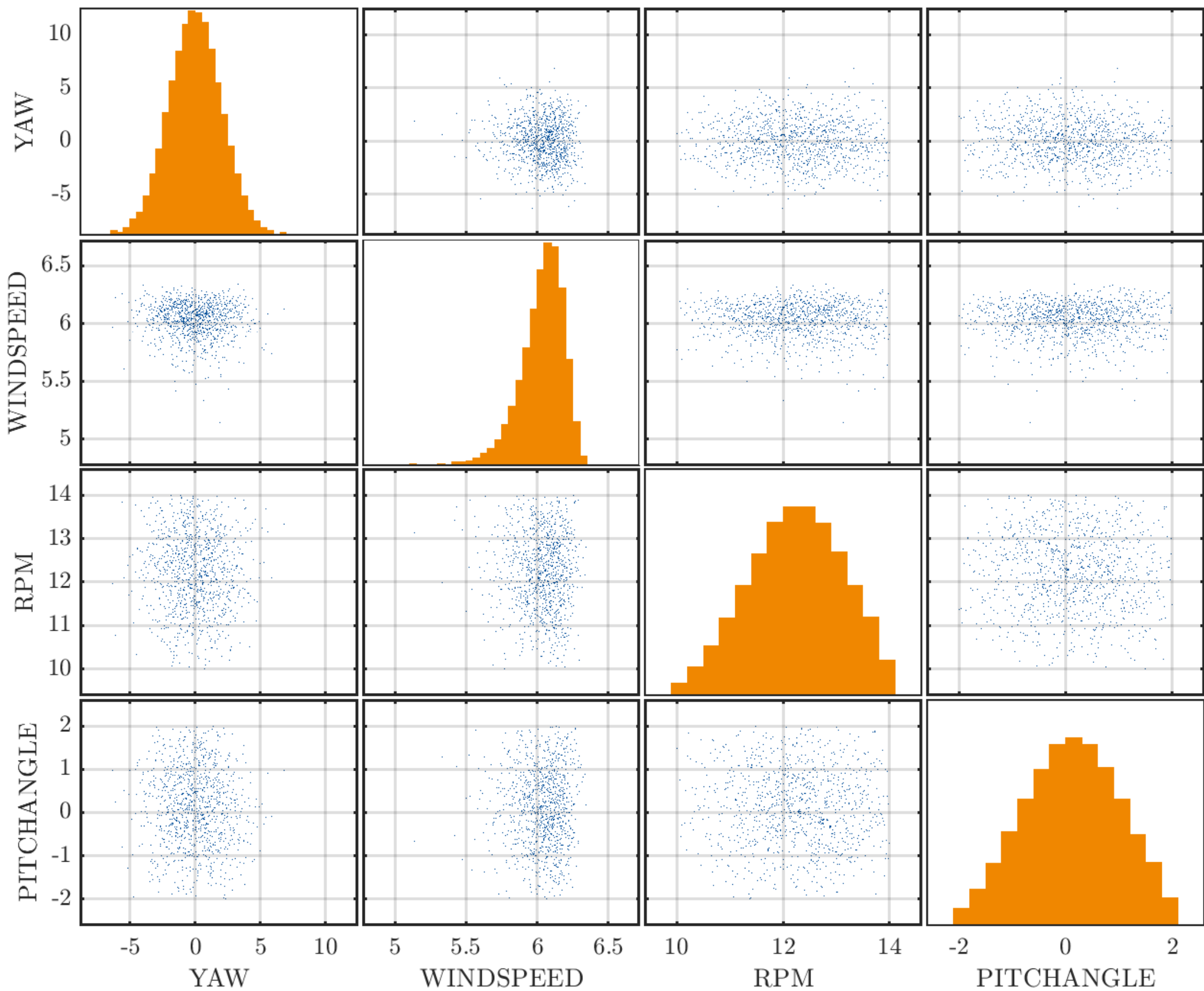
Operation Uncertainty

Yaw
Truncated Gaussian [mean = 0, std = 2, LB = -10, UB = 10]

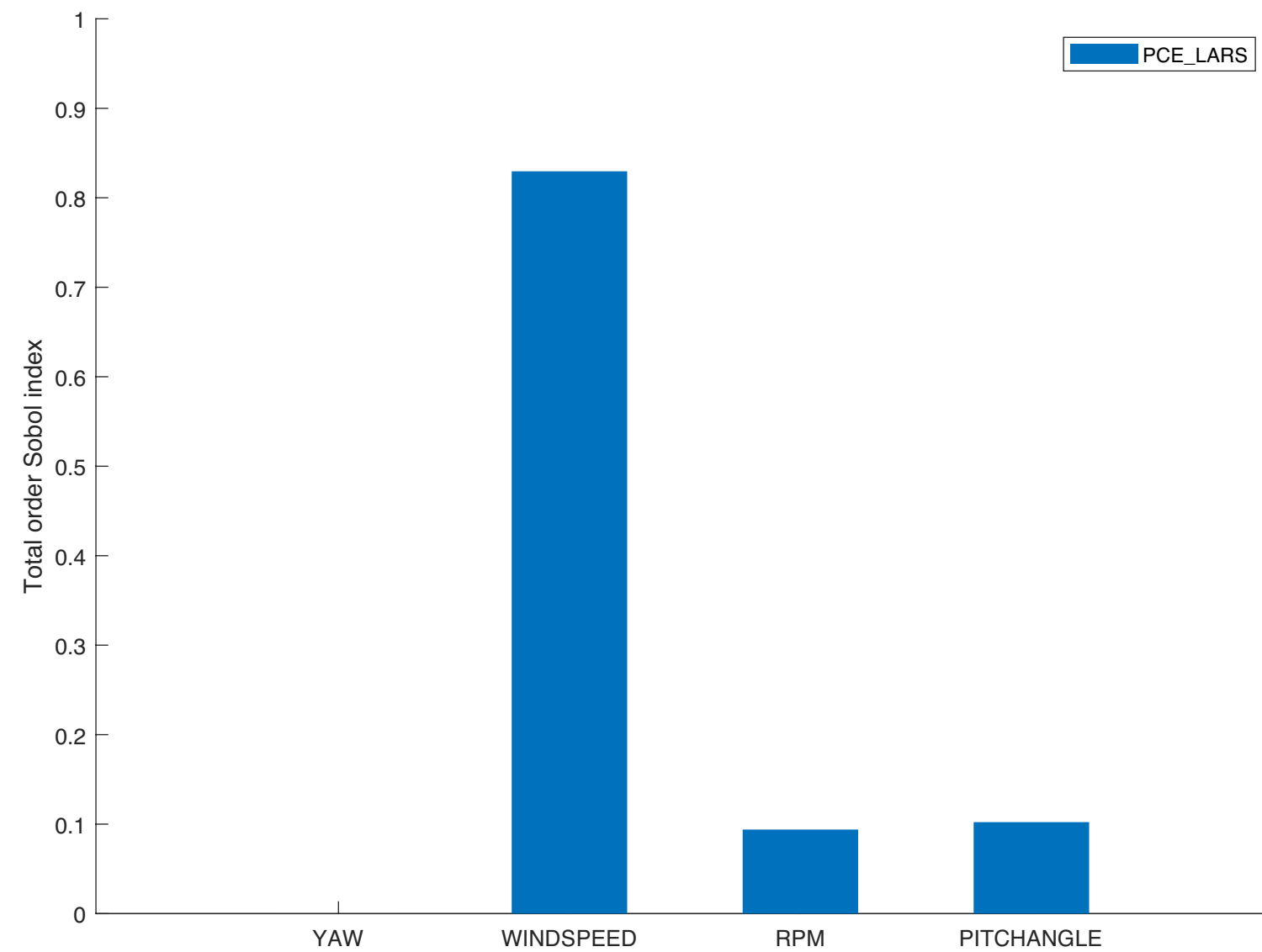
WindSpeed
Weibull distribution [Scale = 6.1, Shape = 50]

RPM
Truncated Gaussian [mean = 12.3, std = 1, LB = 10, UB = 14]

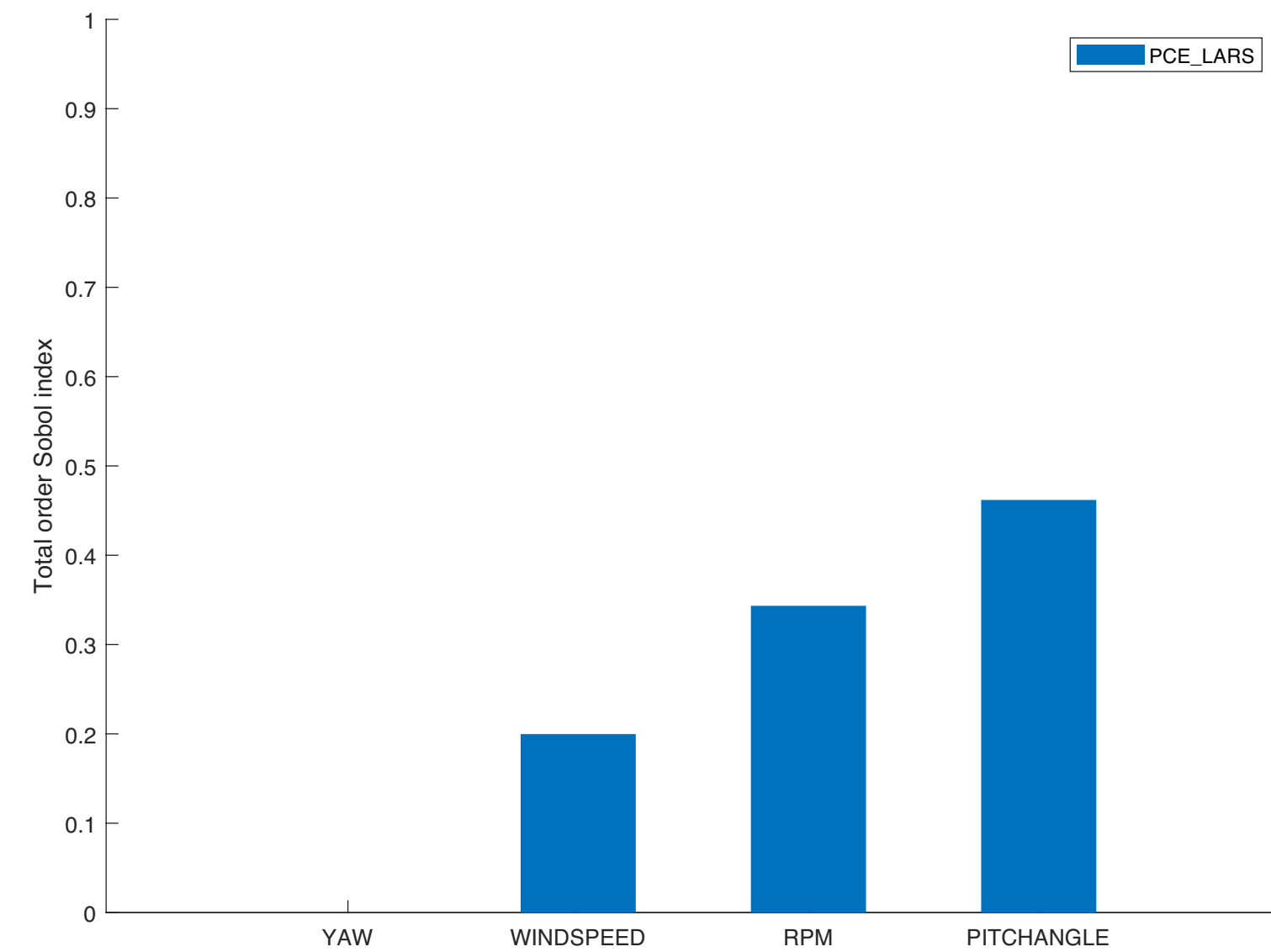
PitchAngle
Truncated Gaussian [mean = 0.15, std = 1, LB = -2, UB = 2]



Sobol indices



Power



Axial Force

-> Yaw angle is least sensitive parameter

Next Steps:

- > Determine realistic amount of perturbations for uncertain parameters
- > Parametrization for other random inputs, model-form uncertainty
- > Include other BEM codes in the workflow and perform comparisons