Worksheet: Limits of functions of 2 or 3 variables

1. Compute the limit:
$$\lim_{(x,y)\to(2,3)} \frac{1}{y} - \frac{4}{x} =$$

2. Compute the limit:
$$\lim_{(x,y)\to(0,0)} \frac{x^2 - xy}{\sqrt{x} + \sqrt{y}} =$$

3. Where is the function $f(x,y) = \frac{1}{y(x-1)}$ continuous? Find the largest region.

4. Where is the function $g(x,y,z)=\frac{1}{x^2+z^2-1}$ continuous? Find the largest region.

5. If $f(x,y) = x^2 - 3y$, find the limit: $\lim_{h \to 0} \frac{f(1+h,y) - f(1,y)}{h} =$