

Introduction to Functional Programming in *OCaml*

Roberto Di Cosmo, Yann Régis-Gianas, Ralf Treinen

Week 3 - Sequence 0: Tagged values



Overview of Week 3

1. Tagged values
2. Recursive types
3. Tree-like values
4. Case study: a story teller
5. Polymorphic algebraic datatypes
6. Advanced topics

Avoiding meaningless values

- ▶ In the database example, we had:

```
engine : database -> query -> status * database * contact
```

- ▶ The returned `database` and `contact` are meaningful only if the returned `status` is `true`. Otherwise, they must not be used.
- ▶ What if a type could capture this constraint?

Sum type: disjoint union of types

- ▶ We should change the type of engine into

```
engine : database -> query -> query_result
```

- ▶ Such that a value of type query_result can be **either**:

- ▶ an error, or
- ▶ a new database (in case an insertion or deletion query was successfully applied), or
- ▶ a contact and its index (in case a search query was successful).

- ▶ In *OCaml*, this is written as a **sum type**:

```
type query_result =  
  | Error  
  | NewDatabase of database  
  | FoundContact of contact * int
```

Sum type: disjoint union of types

```
type some_type_identifier =  
  | SomeTag of some_type * ... * some_type  
  | ...  
  | SomeTag of some_type * ... * some_type
```

- ▶ SomeTag is a tag identifier, start with an uppercase letter.
- ▶ Tag identifiers must be unique and distinct.
- ▶ **A tag characterizes one specific type** in this disjoint union of types.
- ▶ How to **construct** and **observe** values of this type?

Constructing tagged values

- ▶ Tags are also called **constructors**.
- ▶ A tag is used as a **marker to classify values** with respect to the different cases of the union.

`SomeTag (some_expression, ..., some_expression)`

- ▶ Parentheses can be omitted if there is only one argument and if that argument is a simple expression (like a variable or a literal for instance).

A sum type for queries I

```
type query =  
  | Insert of contact  
  | Delete of contact  
  | Search of string;;  
# type query =  
  Insert of contact  
  | Delete of contact  
  | Search of string
```

A sum type for queries II

```
let luke = { name = "luke"; phone_number = (1, 2, 3, 4) }  
let query1 = Insert luke;;  
# val luke : contact =  
  {name = "luke"; phone_number = (1, 2, 3, 4)}  
val query1 : query =  
  Insert {name = "luke"; phone_number = (1, 2, 3, 4)}  
let query2 = Search "luke";;  
# val query2 : query = Search "luke"  
let query3 = Delete luke;;  
# val query3 : query =  
  Delete {name = "luke"; phone_number = (1, 2, 3, 4)}
```


A special case: Tags with no argument are enumerations I

```
type color = Black | Gray | White;;  
# type color = Black | Gray | White  
let batman_s_color = Black;;  
# val batman_s_color : color = Black
```

Observing tagged values by case analysis

- ▶ Let **type** $t = A \mid B$ and x be an identifier of type t .
- ▶ x must have been constructed using A or B .
- ▶ Then, we know that x can be either an A **or** a B .
- ▶ If we want to write some computation that depends on x , we must provide some code for the case $x = A$ and some code for the case $x = B$.

Observing tagged values by case analysis

- ▶ When we observe a value of a sum type, **several cases are possible**.
- ▶ The programmer must provide an **expression for each possible case**.
- ▶ A **case** is described by a pattern of the form:
`SomeTag (some_pattern, ..., some_pattern)`
- ▶ A **branch** is composed of a pattern and an expression separated by an arrow.
`some_pattern -> some_expression`

Case analysis by pattern matching

- ▶ A **pattern matching** is a sequence of branches:

```
match some_expression with  
| some_pattern -> some_expression  
| some_pattern -> some_expression  
| ...  
| some_pattern -> some_expression
```

- ▶ There must be **at least one branch** in a pattern matching.
- ▶ To evaluate a pattern matching:
 1. we compute the value of `some_expression`;
 2. we try to **match** it with the pattern of the first branch ;
 3. if it does not, we try the next one until we find a match.

A pattern matching

```
let engine db query =  
  match query with  
  | Insert contact -> insert db contact  
  | Delete contact -> delete db contact  
  | Search name -> search db name;;
```

Functions defined by cases

- Many functions start with a case analysis over one argument:

```
let f x = match x with  
  | some_pattern -> some_expression  
  | ...  
  | some_pattern -> some_expression
```

- There is syntactic shortcut to define them:

```
let f = function  
  | some_pattern -> some_expression  
  | ...  
  | some_pattern -> some_expression
```

A function defined by cases

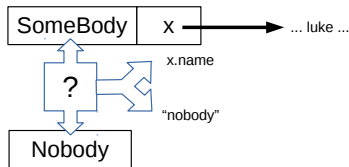
```
let engine db query = function  
  | Insert contact -> insert db contact  
  | Delete contact -> delete db contact  
  | Search name -> search db name;;
```

In the machine

Program

```
let p = Somebody luke  
let q = Nobody  
function  
| Somebody x → x.name  
| Nobody → "nobody"
```

Machine



- ▶ Each tag is represented by a (small) machine integer.
- ▶ A value of a sum type is either:
 - ▶ a tag if it is a constructor with no argument;
 - ▶ or a heap-allocated block starting with a tag.
- ▶ Pattern matching performs a dynamic test on this tag.

Pitfalls

- ▶ A pattern can be ill-typed.
- ▶ A case analysis can be non exhaustive.
- ▶ All these programming errors are caught by the type-checker!

Ill-typed patterns I

```
type data = None | Single of int | Pair of int * int;;  
# type data = None | Single of int | Pair of int * int  
let bad_arity (x : data) =  
  match x with  
  | None x -> x  
  | Single x -> x  
  | Pair (x, _) -> x;;  
# Characters 48-54:  
  | None x -> x  
  ~~~~~
```

Error: The **constructor** None expects 0 argument(s),
but is applied here **to** 1 argument(s)

Ill-typed patterns II

```
let bad_argument_type (x : data) =  
  match x with  
    | Single true -> false  
    | _ -> true;;
```

```
# Characters 63-67:  
    | Single true -> false  
      ^^^^
```

Error: This pattern matches **values of type** bool
but a pattern was expected which matches **values of type**
int

Non exhaustive case analysis I

```
type color = Black | Gray | White;;  
# type color = Black | Gray | White  
(* Black < Gray < White and forall x, not (x < x). *)  
let lighter c1 c2 =  
  match (c1, c2) with  
  | (Black, Black) -> false  
  | (White, White) -> false  
  | (Gray, Gray) -> false  
  | (Black, _) -> true  
  | (_, White) -> true  
  | (White, Gray) -> false  
  | (Gray, Black) -> false;;
```

Non exhaustive case analysis II

```
# Characters 76-291:
  ..match (c1, c2) with
    | (Black, Black) -> false
    | (White, White) -> false
    | (Gray, Gray) -> false
    | (Black, _) -> true
    | (_, White) -> true
    | (White, Gray) -> false
    | (Gray, Black) -> false..
```

Warning 8: this pattern-matching is **not** exhaustive.

Here is an example **of** a case that is **not** matched:

(White, Black)

```
val lighter : color -> color -> bool = <fun>
```