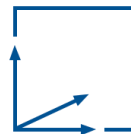


Module IN 2018

Introduction to Augmented Reality

Prof. Gudrun Klinker



Markerless Optical Tracking and Feature Detection
SS 2018

Literature

- *Parallel Tracking and Mapping for Small AR Workspaces*, G. Klein and D. Murray, ISMAR 2007.
- *Parallel Tracking and Mapping on a Camera Phone*, G. Klein and D. Murray, ISMAR 2009.
- *MonoSLAM: Real-Time Single Camera SLAM*, A.J. Davison, I. Reid, N. Molton and O. Stasse, IEEE Trans. PAMI 2007 29(6): 1052-1067 (2007).

Agenda

- 1. Motivation
- 2. Introduction to „Simultaneous Localization-And-Mapping“ (SLAM)
- 3. PTAM: System Overview
- 4. Feature Map
- 5. Tracking
- 6. Mapping
- 7. Results

1. Motivation

Typical situation in Augmented Reality

- Mobile user
 - Local (inside-out) tracker (here: camera in user's hand or on HMD)
 - Fast, erratic motions (esp. rotations)
- Unprepared environment:
 - No markers
 - No 3D scene description (3D model)
 - No external (outside-in) observing system
- ~~Even worse:~~
 - ~~– Moving (changing) objects~~
 - ~~– Changing illumination~~
 - ~~– Very large area~~
- Need for „Extensible Tracking“

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2. SLAM

Similar situation in robotics (mobile vehicle with camera)

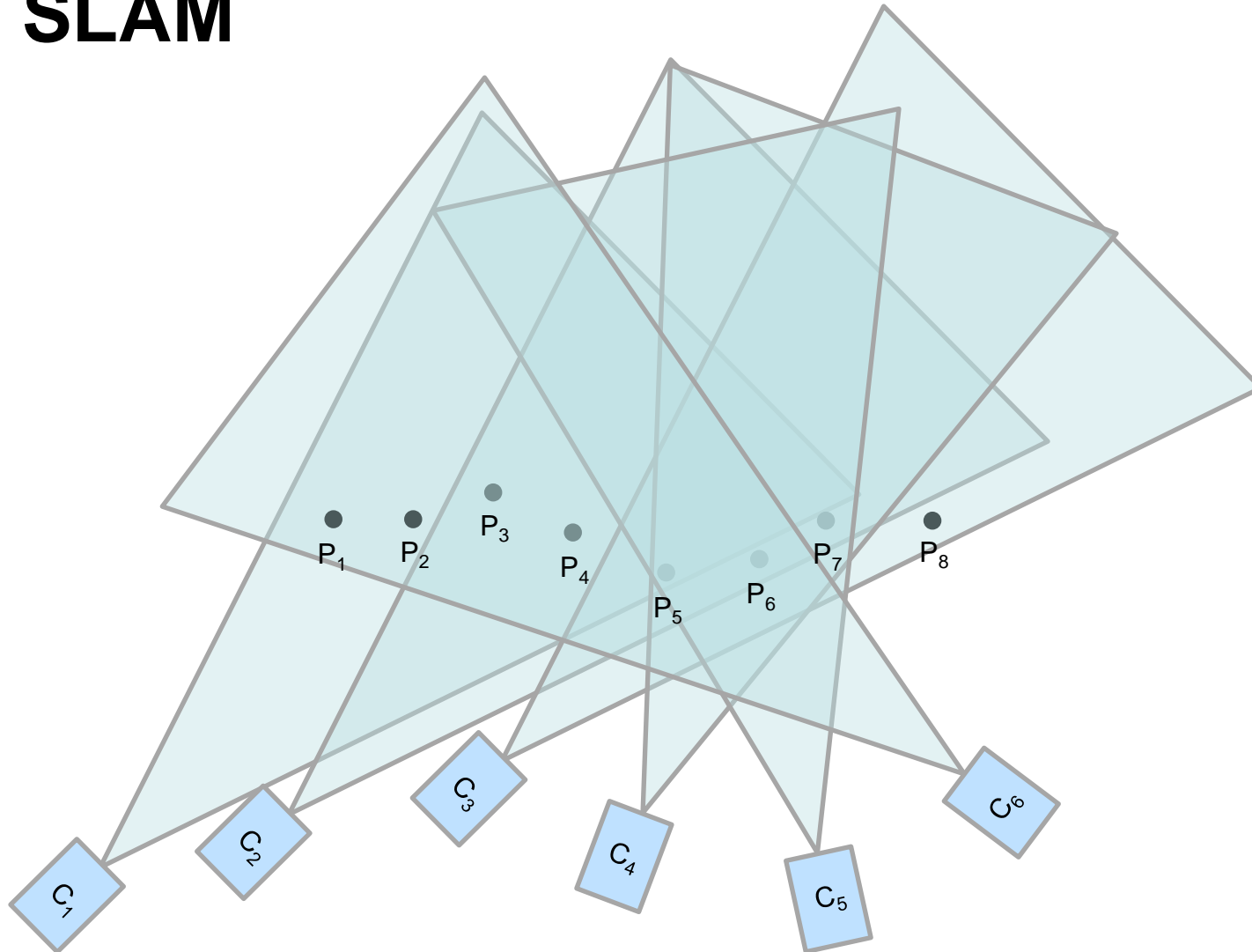
- **SLAM** algorithm (Simultaneous Localization And Map-Building) with a single camera: [Davison 1998]
<http://www.doc.ic.ac.uk/~ajd/publications.html>

2. SLAM

General idea

- Two separate issues
 - Localization
 - By some sensors
 - By a camera – if a scene model (map) is available
 - Map-building: 3D scene reconstruction
 - By generalized stereo
 - By a single, moving camera – if motion is known
- If only a single camera is used and no external scene description is available, both problems need to be solved simultaneously (chicken-and-egg problem).

2. SLAM



2. SLAM

$$\begin{bmatrix} X_{ij}/Z_{ij} \\ Y_{ij}/Z_{ij} \\ 1 \\ 1/Z_{ij} \end{bmatrix} \approx \begin{bmatrix} X_{ij} \\ Y_{ij} \\ Z_{ij} \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & s & c_x & 0 \\ 0 & f_y & c_y & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x_i \\ y_i \\ z_i \\ 1 \end{bmatrix}$$

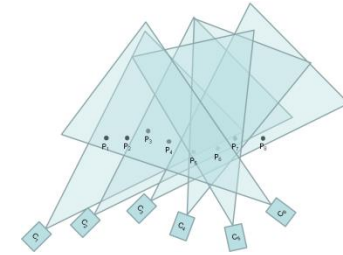


Image formation equation: $\vec{P}_{ij} = K_j [R_j | t_j] \vec{p}_i$

Unknowns

- Position (x_i, y_i, z_i) of every point \vec{p}_i , with $i \in \{0..M-1\}$
- Camera pose $C_j = [R_j | t_j]$ with $j \in \{0..N-1\}$
 $= f(tx_j, ty_j, tz_j, rx_j, ry_j, rz_j)$
 (assume: intrinsic parameters K_j to be known)

→ 3M

→ 6N

→ 3M + 6N

Givens (for points that are seen in all images)

- Image position $\vec{P}_{ij} = (X_{ij}, Y_{ij})$ of Point \vec{p}_i in camera image C_j

→ 2MN

Required points and images for an over-determined system of equations

$$2MN \geq 3M + 6N$$

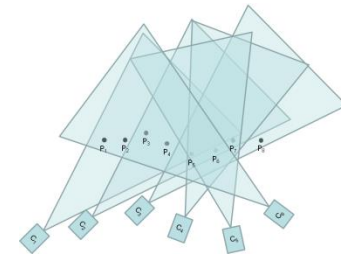
$$N \geq \frac{3M}{2M - 6}$$

Also known as „Structure from Motion“ problem

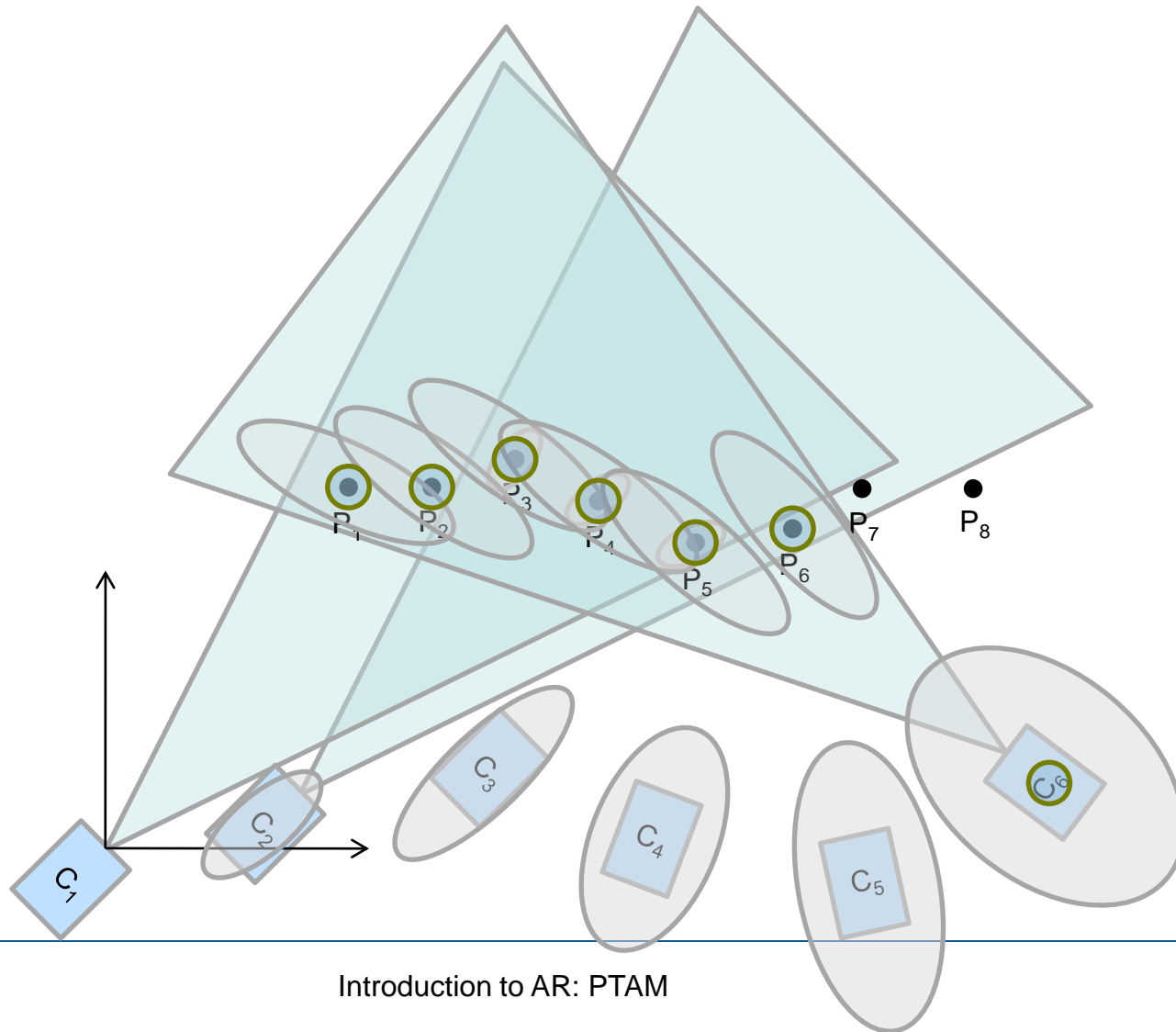
M points	N images
4	6
5	4
6	3
7	3

2. SLAM

- Offline solutions
 - Structure from motion (computer vision)
 - Bundle adjustment (photogrammetry)
- Online solution: SLAM
 - Incremental map-building
 - Maintenance of a „system state“ that changes over time (Kalman)
 - Explicit models of measurement uncertainty and process noise (both for camera and object poses)



2. SLAM



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3. PTAM: System Overview

Parallel Tracking and Mapping

Georg Klein and David Murray (Oxford University).

<http://www.robots.ox.ac.uk/~gk/>

- Paper: *Parallel Tracking and Mapping for Small AR Workspaces*, G. Klein and D. Murray, ISMAR 2007.
- Free source code.
- Winner of first ISMAR Tracking Contest 2008
<http://ismar08.org/wiki/doku.php?id=program-competition>
(Using Robert Castle's multiple map approach).
- Paper: *Parallel Tracking and Mapping on a Camera Phone*, G. Klein and D. Murray, ISMAR 2009.
<http://www.youtube.com/watch?v=pBI5HwitBX4>

3. PTAM: System Overview

Requirements for AR-related tracking and 3D reconstruction

- Fast
- Accurate
- Robust

Tracking a hand-held camera is more difficult than tracking a robot because

- Robots often have odometry
- Robots can be arbitrarily slow

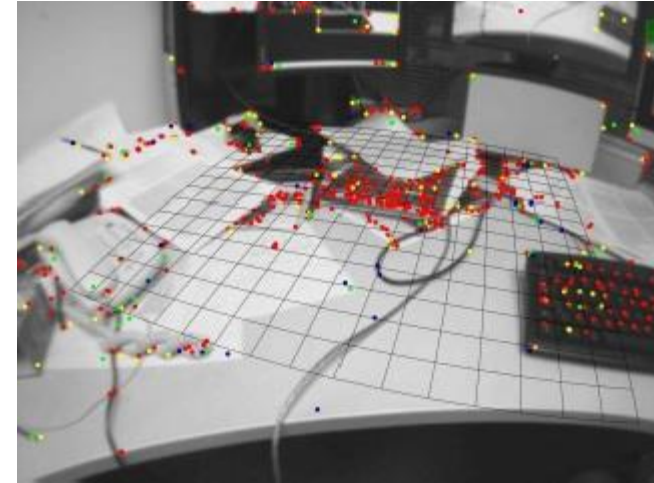
Problems with SLAM

- Potential data association errors (wrong matches) due to high speeds
 - Not robust enough because tracking is tied to map-building (too slow for tracking, too fast for high-quality map-building)
- Does not exploit dual-core facilities
- Sparse map of high-quality features vs. dense map of low-quality features (key frames)

3. PTAM: System Overview

Assumptions

- Mostly static scene
(Not many moving or deformable objects)
- Small
(User spends most time in the same space)



Main concepts

- Tracking and Mapping separated (two parallel threads)
- Mapping based on keyframes (processed using offline techniques: bundle adjustment)
- Map densely initialized from a stereo pair (5-point algorithm)
- New points initialized via epipolar search
- Thousands of points

Agenda

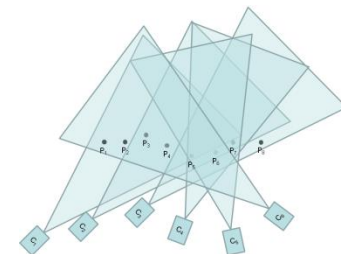
1. Motivation
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4. Feature Map

- 4.1 Knowledge Representation
- 4.2 Image Pyramids
- 4.3 Keyframes

4.1 Feature Representation

- M point features $p_{jw} = (x_{jw}, y_{jw}, z_{jw}, 1)$ (in some world coordinate system W)
 - Assume: locally planar surface patch with normal n_{jw}
 - Associated with 8x8 pixel patch in some keyframe at some level
- N keyframes (specially selected images of the moving camera)
 - Associated local coordinate system K_i
 - 4-level image pyramid
- Typical feature map contains:
 - M=2000..6000 points
 - N=40..120 keyframes



4. Feature Map

4.1 Knowledge Representation

→ 4.2 Image Pyramids

4.3 Keyframes

4.2 Image Pyramids

- Pyramid of recursively smoothed and reduced representations of the original image
 - Requires less than twice the amount of space
 - Fast to compute
 - Increases robustness
 - Maintains accuracy
- Exponentially reduced image sizes at increasing levels l:

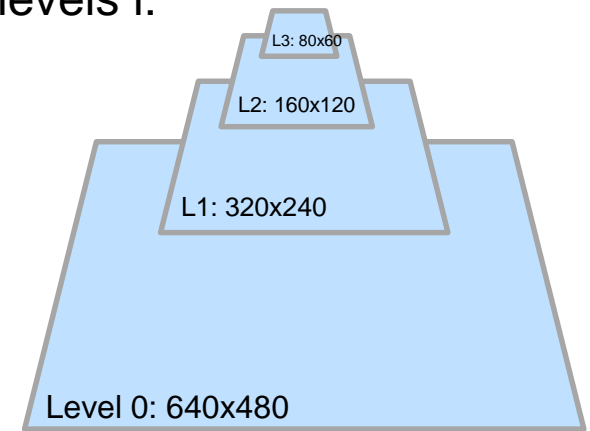
$$w_l = \frac{w}{2^l} \quad h_l = \frac{h}{2^l}$$

Level 0: 640 x 480 pixels

Level 1: 320 x 240 pixels

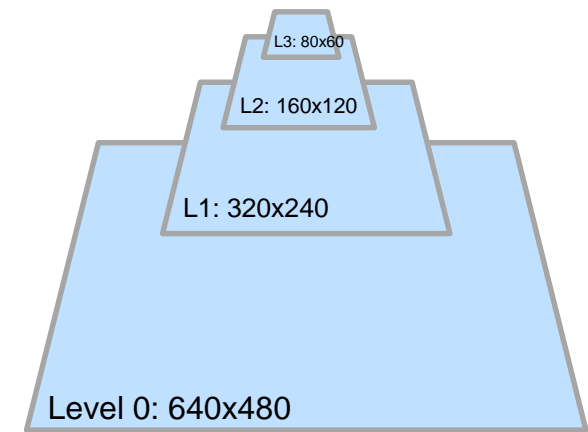
Level 2: 160 x 120 pixels

Level 3 : 80 x 60 pixels

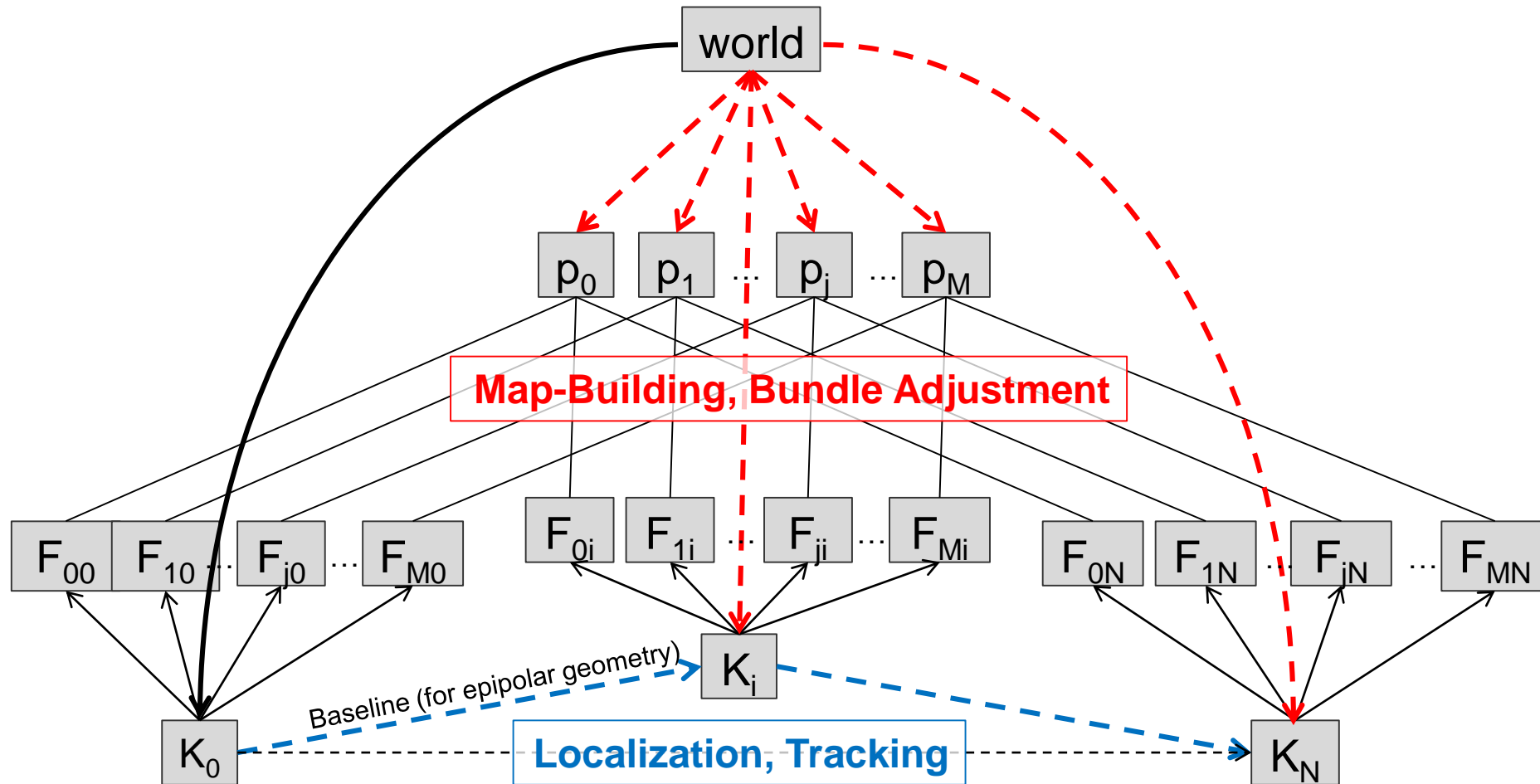


4.2 Image Pyramids

- 8x8 patches on all levels, representing areas of increasing sizes at level 0
 - 8x8 patch at level 3: 64x64 pixels at level 0
 - 8x8 patch at level 2: 32x32 pixels at level 0
 - 8x8 patch at level 1: 16x16 pixels at level 0
 - 8x8 patch at level 0: 8x 8 pixels at level 0
- Patch at coarse level = approximate description of large image area
 - Overview: only dominant image content (LF)
 - For fast wide-area search (correlation) (Redetection after fast camera movements)
- Patch a fine-grained level = precise description of small image area
 - Detail: very specific image data (HF)
 - For high-precision local-area search



4.2 SRG (Spatial Relationship Graph)



4. Feature Map

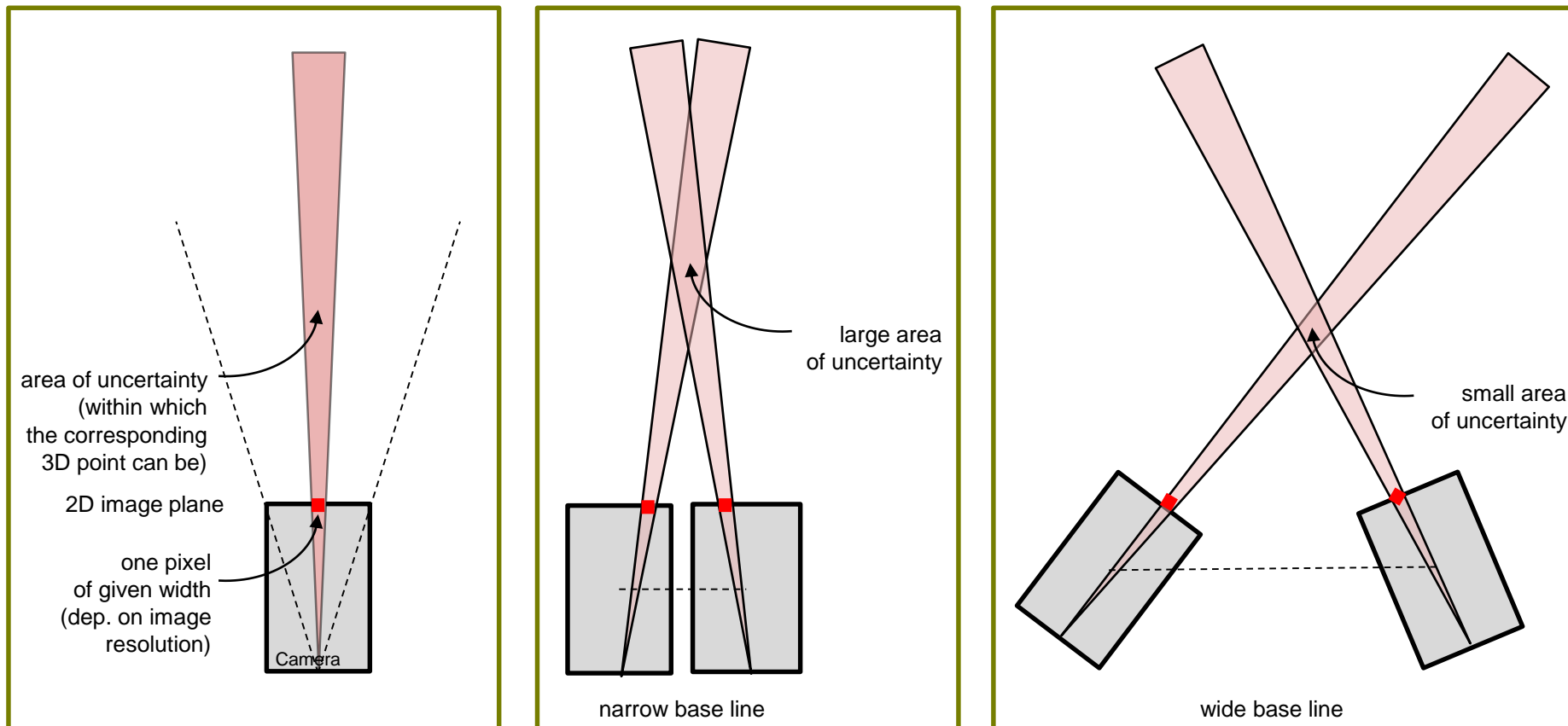
4.1 Knowledge Representation

4.2 Image Pyramids

→ 4.3 Keyframes

4.3 Keyframes

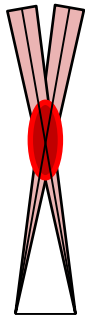
Wide baseline (distance) between cameras (views) important



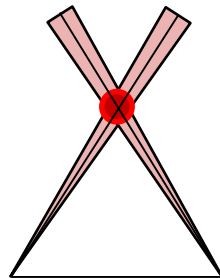
4.3 Keyframes

Wide baseline (distance) between cameras (views) important

- The wider the baseline the better the depth estimation



narrow base line



wide base line

- Skip images from nearly the same viewpoint
 - Poor accuracy
 - Waste of space
 - Waste of time

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6. Mapping
7. Results

5. Tracking

- 5.1 Overview
- 5.2 Image Acquisition
- 5.3 Camera Pose and Projection
- 5.4 Patch Search
- 5.5 Pose Update
- 5.6 Two-Stage Coarse-to-Fine Tracking
- 5.7 Tracking Quality and Failure Recovery

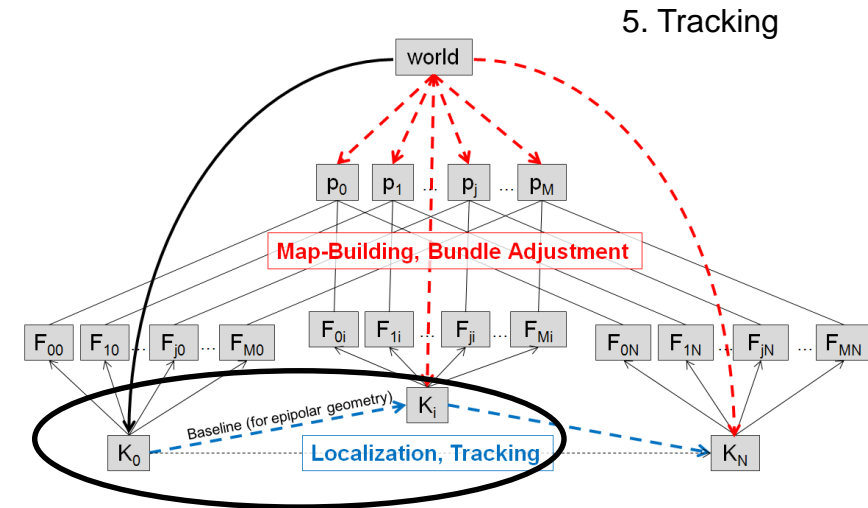
5.1 Overview

Assumptions

- Given: a set of 3D points, P_j , with associated 2D image features F_j in various keyframes of images $\{0..i-1\}$ and across various levels l

Key steps of the algorithm

1. Acquire new frame I_i from a hand-held camera, generate a prior pose estimate K_i^-
2. Project map points into the image, according to K_i^-
3. Search for a small number (50) of the coarsest-scale features
4. Update camera pose from coarse matches
5. Reproject larger number (1000) of points into the image, search for their refined location
6. Compute final pose estimate K_i



5.2 Image Acquisition

- Frame grabbing
- Convert to black & white
- Generate image pyramid
- Determine interesting points (corners) on each pyramid level
- Compute prior estimate of camera pose K_i^-
 - Decaying velocity model
(Lacking new measurements, the estimated camera slows down)

5.3 Camera Pose and Projection

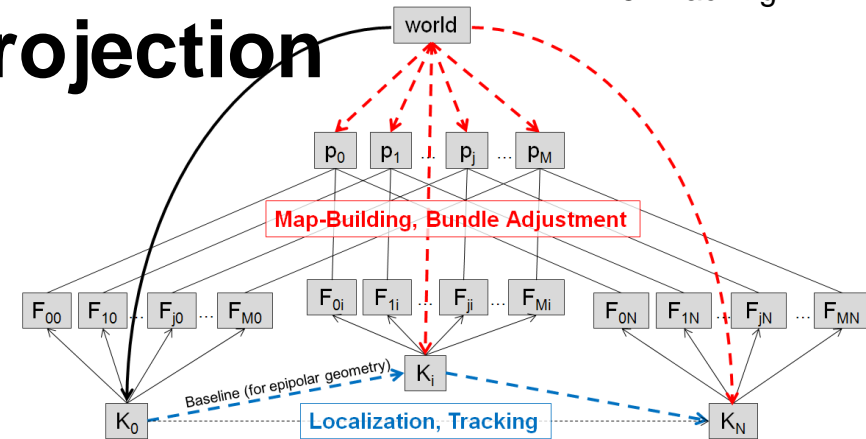
- Transfer 3D points p_j from world coordinate system to estimated camera coordinate system K_i using transformation matrix E_{cw}^-

$$\mathbf{p}_{jc} = E_{cw}^- \mathbf{p}_{jw}$$

- Project points from 3D camera frame into image using given intrinsic parameters, focal length (f_u, f_v), principal point (u_0, v_0), and radial distortion r' :

$$\begin{pmatrix} u_j \\ v_j \end{pmatrix} = CamProj(\mathbf{p}_{jc})$$

$$CamProj(\mathbf{p}_{jc}) = \begin{pmatrix} u_0 \\ v_0 \end{pmatrix} + \begin{bmatrix} f_u & 0 \\ 0 & f_v \end{bmatrix} \frac{r'}{r} \begin{pmatrix} x_{jc} / z_{jc} \\ y_{jc} / z_{jc} \end{pmatrix}$$



5.4 Patch Search

- Fixed-range image search around the predicted image location (circular region with fixed radius) of a point \mathbf{p}_j
 - Warp the 8x8 image patch according to the orientation of its normal \mathbf{n}_j and the current viewpoint orientation (affine warp)
 - Determine appropriate pyramid level for search from the projected patch size
 - Generate an 8x8 search template from the source level, using the warp and bilinear interpolation
 - Subtract the average intensity to discount illumination changes
 - Calculate matching quality at all interesting points (corners) in the search area (quality criterion: SSD)
 - If best score is below threshold, a match has been found
- For high pyramid levels, refine matching position to sub-pixel precision (iterative error minimization) (computationally expensive)

5.5 Pose Update

- For each of S successful observations (found patches)
 - Patch location at $(u, v)^T$ with measurement noise $\sigma^2 = 2^2$
- Iterative minimization of a robust objective function of the reprojection error vector \mathbf{e}_j for a motion matrix \mathbf{M}

$$\mathbf{e}_j = \begin{pmatrix} u_j \\ v_j \end{pmatrix} - \text{CamProj}(\mathbf{M}\mathbf{p}_{jc})$$

5.6 Two-Stage Coarse-to-Fine Tracking

Two consecutive phases of patch searching and pose update

- Phase 1:
 - Initial coarse search (50 map points) at highest pyramid level
 - Over a large search radius
 - With subpixel refinement
 - Pose update
- Phase 2:
 - Re-projection of up to 1000 of the remaining potentially visible image patches
 - Small search region
 - Refinements only for patches at highest pyramid level
 - Final frame pose from both coarse and fine image measurements

5.7 Tracking Quality, Failure Recovery

- Estimation of tracking quality as the fraction of successful feature observations
- If quality is below threshold, tracking continues, but no new keyframes are taken (in order not to degrade the 3D scene model)
- If quality is below a second threshold for more than a few frames, tracking is considered lost.
→ Tracking recovery is initiated.

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7. Results

6. Mapping

- 6.1 Overview
- 6.2 Stereo Initialization
- 6.3 Keyframe Insertion
- 6.4 Bundle Adjustment
- 6.5 Data Association Refinement
- 6.6 General Remarks

6.1 Overview

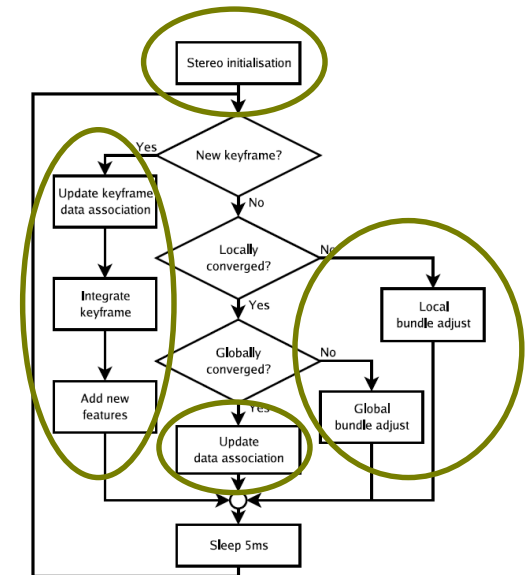
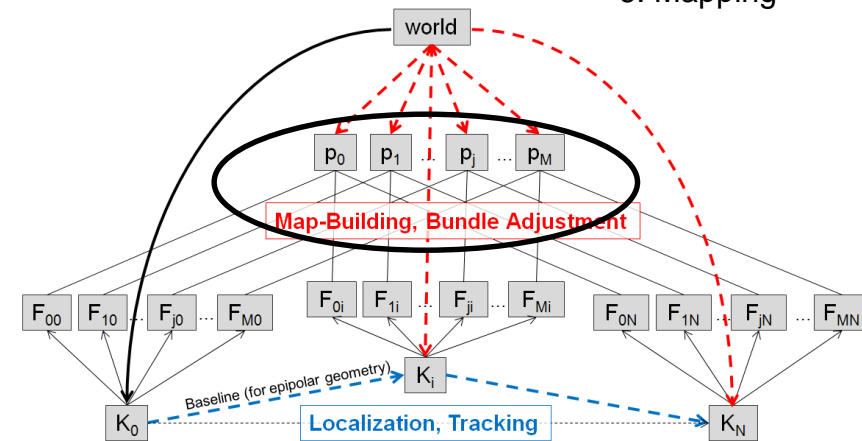
Assumptions

- Given: A set of previous keyframes $K_0 \dots K_{i-1}$ with 2D image features F_j in various levels l , associated 3D points, P_j .

Key aspects of the algorithm:

1. Stereo Initialization
2. Keyframe insertion (and epipolar search)
3. Bundle adjustment
4. Data association refinement

6. Mapping

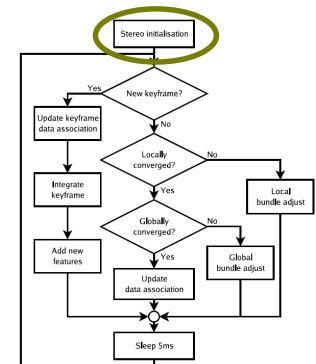


6.2 Stereo Initialization

At startup

- User-initiated initialization with two images (key frames)
 - User positions the camera above the work space and presses a key
 - First image (keyframe) is captured
 - 1000 image patches (interesting points) are automatically selected in the lowest pyramid level
 - User moves the camera by some amount (e.g., 10 cm) and presses a key
 - Second image (keyframe) is captured
 - During the camera motion, the features were already tracked
 - Second keyframe has patches related to first keyframe
- Relative pose estimation and 3D reconstruction using stereo computer vision
- Refinement through bundle adjustment
- Scaled to metric units by assuming that the camera moved by approx. 10 cm.

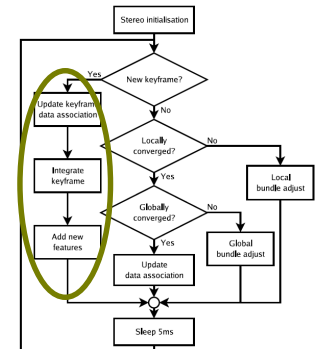
6. Mapping



6. Mapping

6.3 Keyframe Insertion

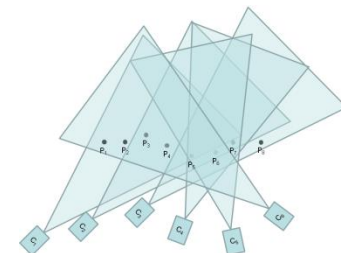
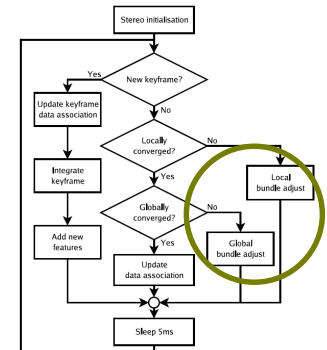
- New keyframes are added whenever:
 - Tracking quality is good
 - At least 20 frames since last keyframe have passed
 - New keyframe has a minimum distance to all previous keyframes (minimum distance threshold depends on mean depth of observed features)
- Existing feature points that may have been ignored by the tracking system are updated
- Interesting (salient) new features are computed in each pyramid level, filtered and added to the feature map.
- The depth of the new features is determined by mapping them to the closest already existing keyframe.



6.4 Bundle Adjustment

- Global bundle adjustment is very time-consuming; its time demand is dominated by the number of keyframes (currently not feasible in real-time for more than 50 keyframes).
- Local bundle adjustment:
 - Adjust only a small set X of keyframes (the current plus the four closest neighbors)
 - The current set of map points Z consists of all those points that have been detected in any of those five keyframes.
 - Extend the set of keyframes to the set Y of all frames in which the map points of Z have been seen (yet, the pose of these additional keyframes is not part of the adjustment process).

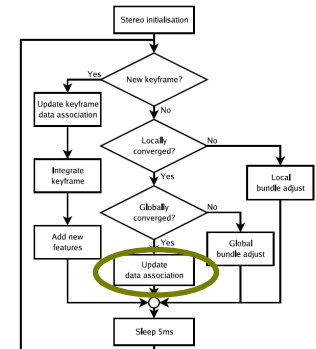
6. Mapping



6.5 Data Association Refinement

- „Luxury routine“: executed when there is spare time (on the non-tracking thread)
- Make new measurements in old keyframes:
Measure newly created map features from new frames also in older frames
 - Measure newly created map features in older keyframes
 - Re-measure outlier measurements
- Issues addressed
 - Problems with repetitive features (patterns)

6. Mapping



6.6 General Remarks

Some aspects of the current implementation could be improved

- Simple set of heuristics to remove outliers from the map
- Patches are initialized with a normal vector parallel to the viewing axis
- Two-stage approach can lead to increased tracking jitter

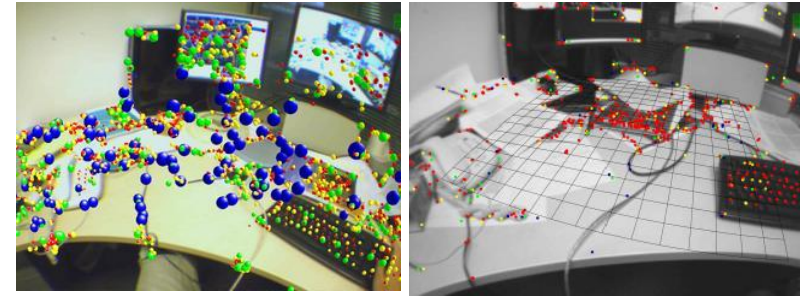
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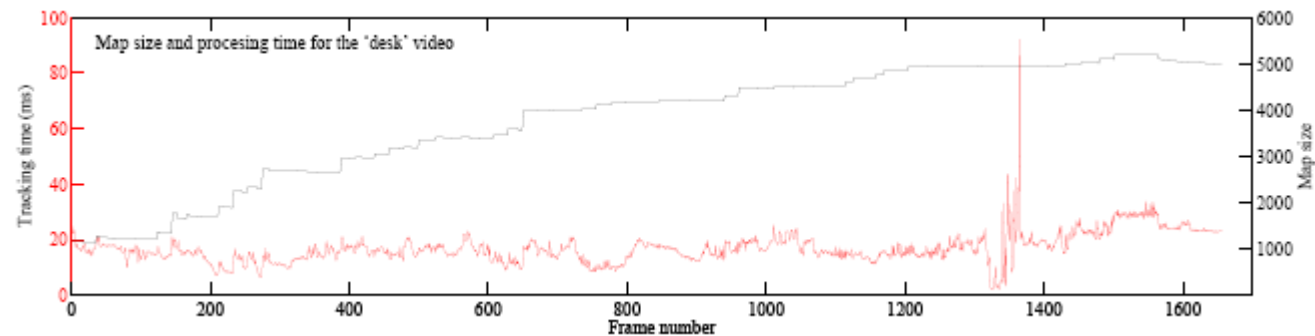
Video of live demonstration

- Cluttered desk with immediate surroundings
- Over 1656 frames (55.2 seconds), 57 keyframes, 4997 point features
- Distribution across pyramid levels: L0: 51%, L1: 33%, L2: 9%, L3: 7%

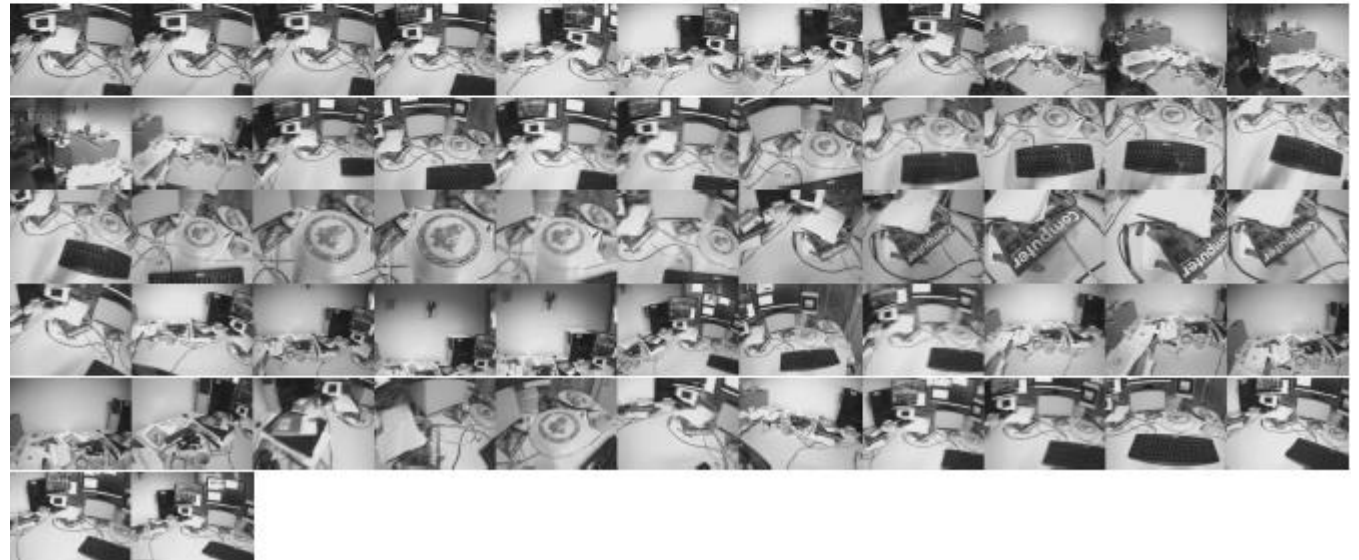
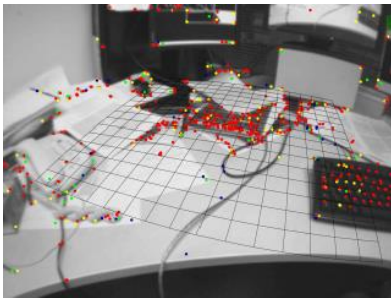
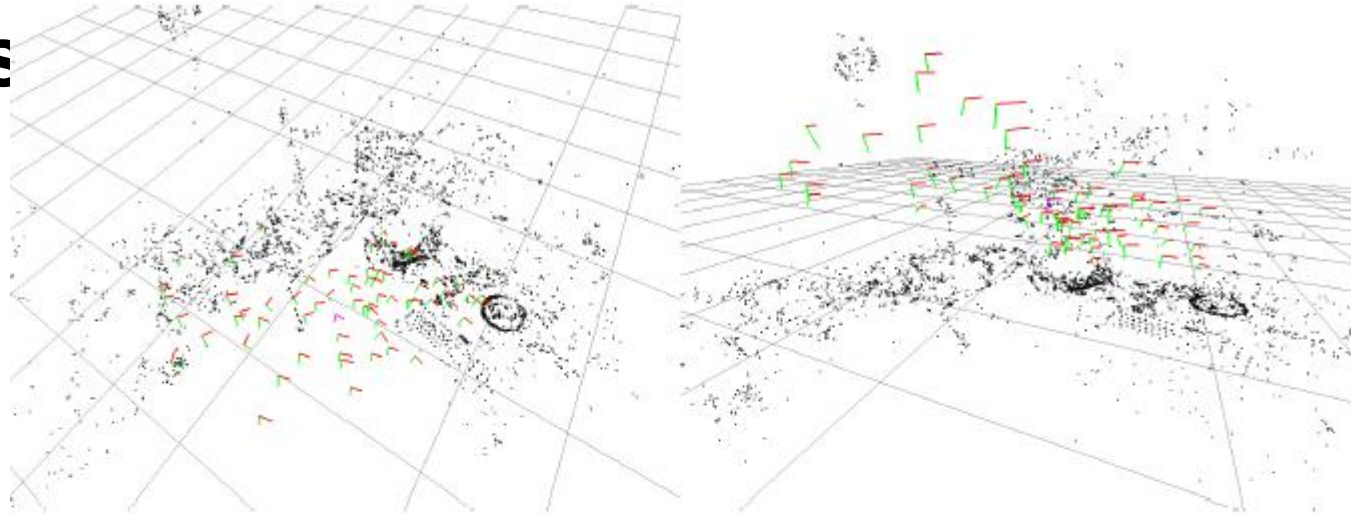


Demos:

- Scale change
- Lens simulation: camera as input device, camera-centered lens to scorch the environment
- Ewok rampage: camera used to aim Darth Vader's laser pistol. Movement is controlled with the keyboard.



7. Results



7. Results

More demos:

- PTAM at ISMAR 2007 in Nara, Japan
- Tracking Contest 2008
- PTAM on iPhone, ISMAR 2009
<http://www.youtube.com/watch?v=pBI5HwitBX4>



Thank you!

