

LIQUID LEVEL SYSTEM

$$q_o(h) = Ch^{\frac{1}{2}}$$

$$q(h) - q_o(t) = A \frac{dh}{dt}$$

$$q(h) - Ch^{\frac{1}{2}} = A \frac{dh}{dt}$$

nonlinear difference equation

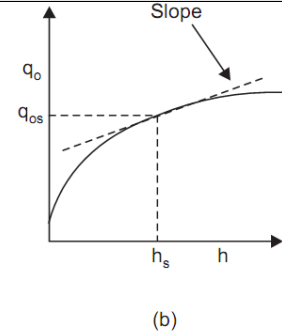
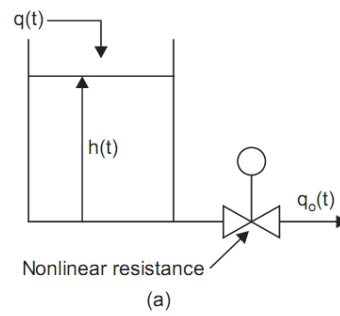


Fig A.5 Liquid-level system with non-linear resistance

$$f(x(t)) = f(a) + \left(\frac{\frac{dx(t)}{dt} \Big|_{t=a}}{1!} \right) (x - a)$$

$$q_o(h) = q_o(h_s) + \left(\frac{\frac{d[q_o(h)]}{dt} \Big|_{h=h_s}}{1!} \right) (h - h_s)$$

$$q_o(h) = q_o(h_s) + \frac{d \left[Ch^{\frac{1}{2}} \right]}{dt} \Big|_{h=h_s} (h - h_s) = q_o(h_s) + \left(\frac{1}{2} \frac{C}{\sqrt{h_s}} \right) (h - h_s)$$

$$q_o(h) = q_o(h_s) + \left(\frac{1}{2} \frac{C}{\sqrt{h_s}} \right) (h - h_s)$$

$$q(h) - \left[q_o(h_s) + \left(\frac{1}{2} \frac{C}{\sqrt{h_s}} \right) (h - h_s) \right] = A \frac{dh}{dt}$$

BLOCK DIAGRAM MODELS

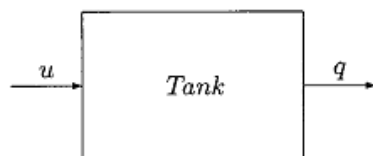


Figure 3.1: Block diagram for the tank in Section 2.3.

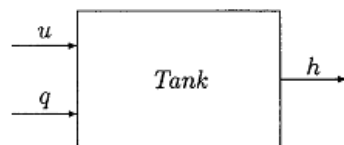


Figure 3.2: Block diagram describing how the level in the tank depends on the inflow and the outflow.

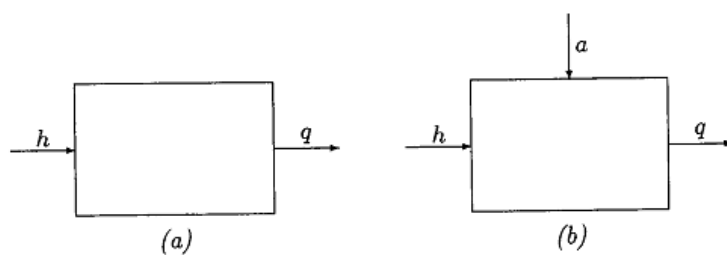


Figure 3.3: (a) Outflow as a function of the level, and (b) as a function of the level and the outflow area.

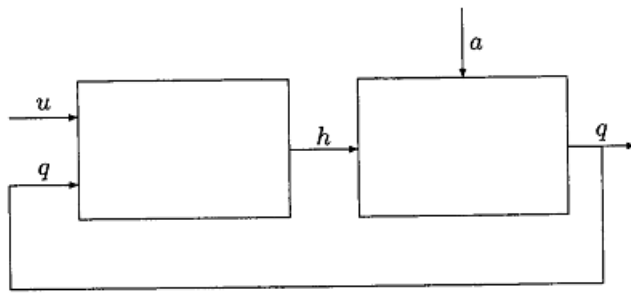


Figure 3.4: Block diagram for the tank system.