

CSbIA Exam Prep 4

We will start at Berkeley Time!

Summer 2021
Midterm
Q2a

Write a function `order_order` which takes a non-empty list of 2-argument functions `operators` and returns a new 2-argument function. When called, this returned function should print the result of applying the first function in `operators` to the two parameters passed in. It should then return another function that applies the second function in `operators` to the parameters, and so on. When the returned function has called the last function in the `operators` list, it should cycle back to the beginning of the list and use the first function again on the next call.

See the doctest for an example.

```
def order_order(operators):
    """
    >>> from operator import add, mul, sub
    >>> ops = [add, mul, sub]
    >>> order = order_order(ops)
    >>> order = order(1, 2) # applies add and returns mul
    3
    >>> order = order(1, 2) # applies mul and returns sub
    2
    >>> order = order(1, 2) # applies sub and cycles back to return add
    -1
    >>> order = order(1, 2) # cycles back to applying add
    3
    >>> order = order(1, 2)
    2
    >>> order = order(1, 2)
    -1
    """
```

```
def apply(x, y):
    print(operators[0](x, y))
    # (a)
    return order_order(operators[1:]+[operators[0]])(x, y)
    # (b)
    return apply(x, y)
    # (c)
```

`operators[1:] + [operators[0]]`
[mul, sub] add

`operators[0](x)(y)`
add(x, y)

`operators[0](x, y)`
`order_order(operators[1:]+[operators[0]])(x, y)`
apply

Summer
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Q2b

A skip list is defined as a sublist of a list such that each element in the sublist is non adjacent in the original list. For original list [5, 6, 8, 2], the lists [5, 8], [5, 2], [6, 2], [5], [6], [8], [2], [] are all skip lists of the original list. The empty list is always a skip list of any list.

Given a list `int_lst` of unique integers, return a list of all unique skip lists of `int_lst` where **each skip list contains integers in strictly increasing order**. The order in which the skip lists are returned does not matter.

```
def list_skipper(int_lst):
    """
    0 1 2 3
    >>> list_skipper([5, 8, 2])
    [[5, 8], [5], [6], [8], [2], []]
    >>> list_skipper([1, 2, 3, 4, 5])
    [[1, 3, 5], [1, 3], [1, 4], [1, 5], [1], [2, 4], [2, 5], [2], [3, 5], [3], [4], [5], []]
    >>> list_skipper([])
    [[]]
    """
    if len(int_lst) == 0:
        return [[]]
    # (a)
    with_first = list_skipper(int_lst[2:])
    # (b)
    without_first = list_skipper(int_lst[1:])
    # (c)
    with_first = [int_lst[0]] + [x for x in with_first if x != []]
    # (d)
    return with_first + without_first
    # (e)
```

Fall 2018 Midterm 2 Q4a

Definition. A *plus expression* for a non-negative integer n is made by inserting $+$ symbols in between digits of n , such that there are **never more than two consecutive digits** in the resulting expression. For example, one plus expression for 2018 is $20+1+8$, and its value is 29. Assume that a two-digit number starting with 0 evaluates to its one's digit. For example, another plus expression for 2018 is $2+01+8$, and its value is 11.

(a) (3 pt) Implement `plus`, which takes a non-negative integer n . It returns the largest value of any plus expression for n .

```
def plus(n):  
    """Return the largest sum that results from inserting +'s into n.  
    >>> plus(123456)    # 12 + 34 + 56 = 102  
    102  
    >>> plus(1604)      # 1 + 60 + 4 = 65  
    65  
    >>> plus(160450)    # 1 + 60 + 4 + 50 = 115  
    115  
    """  
    if n:  
        return max(n%10 + plus(n//10), n%100 + plus(n//100))  
    return 0
```

Handwritten notes for Q4a:

- A red box highlights "largest sum" in the docstring.
- Examples of plus expressions:
 - $123456 \rightarrow 12 + 34 + 56 = 102$
 - $1604 \rightarrow 1 + 60 + 4 = 65$
 - $160450 \rightarrow 1 + 60 + 4 + 50 = 115$
- Handwritten diagrams showing the recursive breakdown of n :
 - $n \% 10$ and $n // 10$
 - For 16 : 6 (boxed) + 12345 (underlined)
 - For 56 : 56 (boxed) + 1234 (underlined)
- The recursive formula is highlighted in green: $\max(n \% 10 + \text{plus}(n // 10), n \% 100 + \text{plus}(n // 100))$.

Fall 2018 Midterm 2 Q4b

(b) (5 pt) Implement `plusses`, which takes non-negative integers n and cap . It returns the number of plus expressions for n that have a value less than cap .

```
def plusses(n, cap):  
    """Return the number of plus expressions for n with values below cap.  
    >>> plusses(123, 16) # 1+2+3=6 and 12+3=15, but 1+23=24 isn't below cap.  
    2  
    >>> plusses(2018, 38) # 2+0+1+8, 20+1+8, 2+0+18, and 2+01+8, but not 20+18.  
    4  
    >>> plusses(1, 2)  
    1  
    """  
    if n < 10 and n < cap:  
        return 1  
    elif cap < 0:  
        return 0  
    else:  
        return plusses(n//10, cap - n%10) + plusses(n//100, cap - n%100)
```

Handwritten notes for Q4b:

- Examples of plus expressions for 123 with $\text{cap}=16$:
 - $1 + 23$ (boxed)
 - $12 + 3$ (boxed)
- The recursive formula is highlighted in red: $\text{plusses}(n // 10, \text{cap} - n \% 10) + \text{plusses}(n // 100, \text{cap} - n \% 100)$.
- Handwritten conditions: $n < 10$ and $n < \text{cap}$, $\text{cap} < 0$.