



# Introduction

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# AI and ML at Work



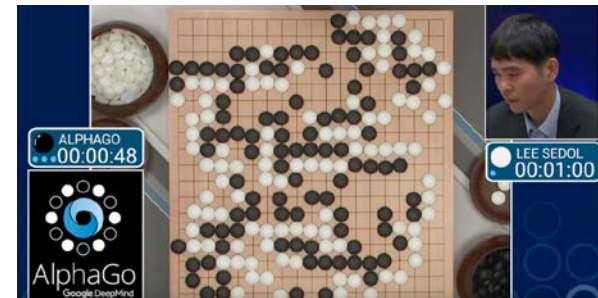
**Autonomous Cars and Navigation**



**“Alexa”, “Siri”, “Cortana” etc.**



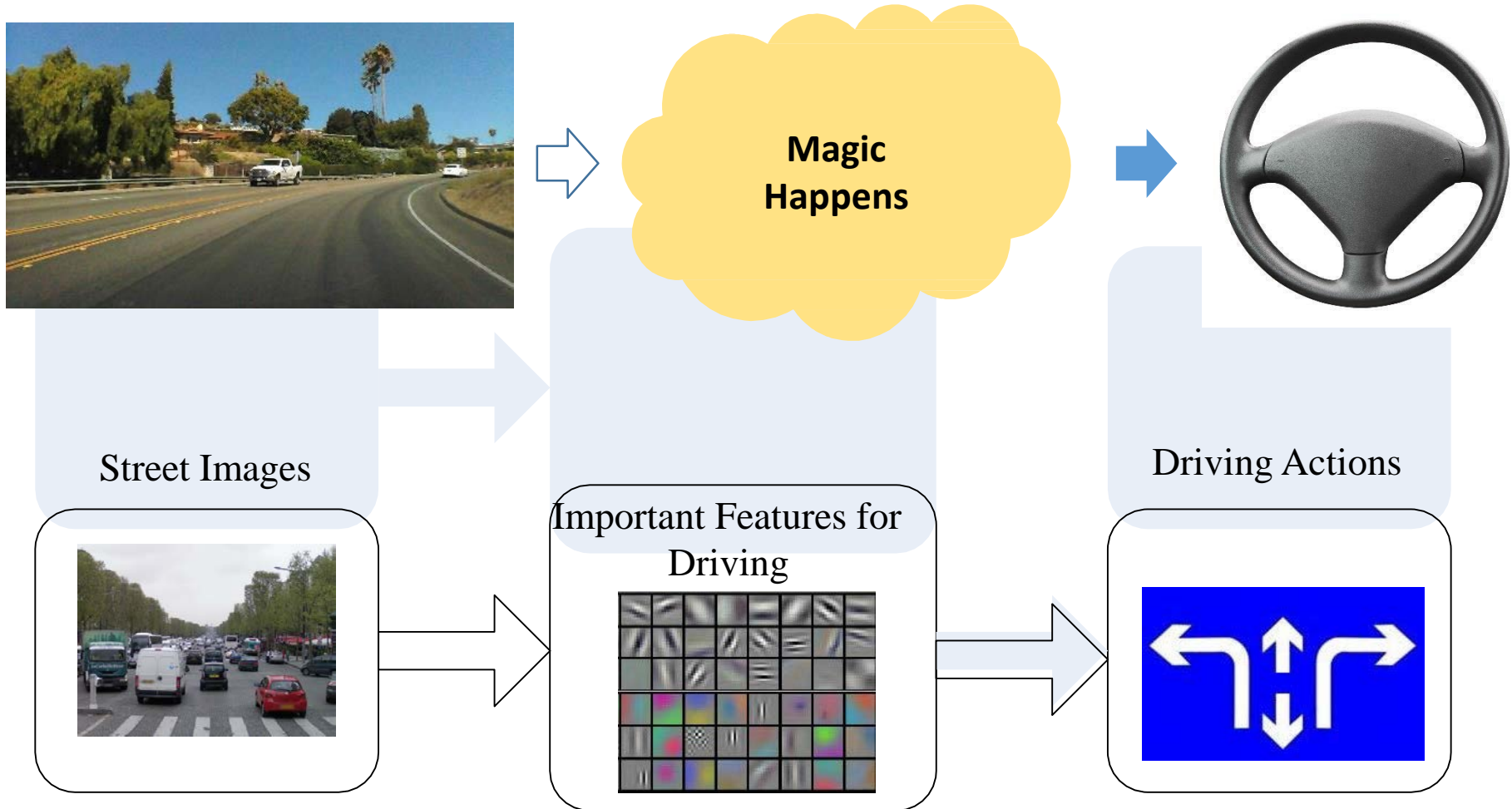
**Creativity: Generated Images**



**Playing Games better than Human**



# Modern AI: End 2 End Driving





# What is Modern AI and ML?

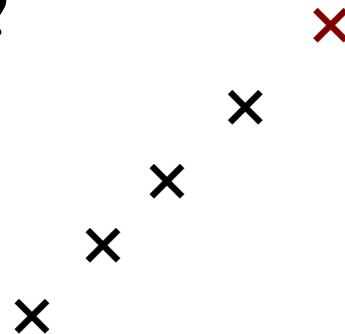


# A simple question

- 1, 3, 5, 7, 9, .... What is the next number?
  - Ans: 11. ; Odd numbers, Or  $2n+1$
- 1, 3, 9, 19, 33, ... What is the next number?
  - Ans: 51;  $2n^2+1$
- How do we solve such problems?
  - Find a pattern from the examples.
    - (function  $f(n) = 2n+1$ . Or model the data)
  - Use it to predict the next number (or solve the problem)
- How do we design a computational procedure?

# A simple question (cont.)

- We know: 1, 3, 9, 19, 33, ... What is the next number?
  - Ans: 51;  $2n^2+1$
- 0.99, 3.02, 9.00, 18.98, 33.01, ... What next?
- Consider a series of 2D points
  - (1,3), (2,6), (3,9), (4,12), ....
  - What is the next point?
  - (x,3x) Or
  - Function:
    - $Y = f(X) = 3 \cdot X$





# What makes it difficult?

- When numbers are “uncertain”
  - Noise in measurements
  - Missing values
- When numbers are not just “simple numbers”?
  - 2D points, 3D points
  - 100 Dimensional points
- When the function is complex or function nature is unknown
  - Simple linear functions are easy to guess.
  - Finding “best” parameters/coefficients can be hard.

# More Examples

- Given a set of numbers {7,26,17,11,25,32,5,8,92}, partition into two sets: (Unsupervised Learning)
  - Odd (7,17,11,25,5) and Even (26,32,8,92)
  - Why this? Why not single and two digit?
- Given a set of male people with and without anemia, their hemoglobin levels are: (Supervised Learning)
  - Positive cases: {8.5, 9.2, 7.4, 7.8}
  - Negative cases: {15.0, 14.9, 14.2, 13.8}
  - Does a patient with 7.7 have anemia?
  - Classification is simple: “anemia if  $f(x) < 10$ ”
  - Why 10? Why not 12?





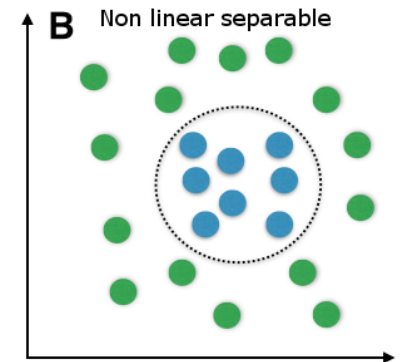
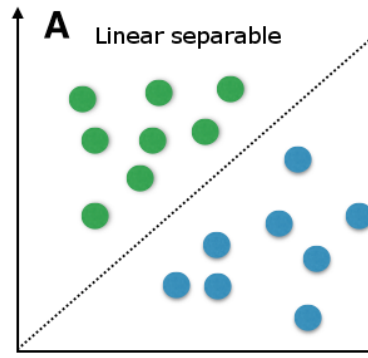
# Closer Look ..

- Who gives samples/examples?
  - The Data
  - Data + interpretations  $(\mathbf{X}, \mathbf{Y}) = (\text{sample}, \text{label})$
- Who gives functional form?
  - Most problems need complex functions
  - (“Linear” solutions are also good in many cases.)
- How to find the “optimal” parameters?
  - Optimization problem. Training. Computing
- How do we expect that it will work well in the future?



# “Classification”: A Popular Problem

- **Example:**
  - Given medical records, predict presence of Malaria
- **Data:** A set of Samples  $\{ X \}$  labeled by experts.
- **Performance:** Predict accurately on unseen data
- $\{0,1\}$  classification
  - “Yes” or “No”
  - Yes if  $f(X) > 0$
- **Multiclass classification**
- **Many more variants**





# Problem Space

- **Feature Extraction:** Find  $\mathbf{X}$  corresponding to an entity/item  $I$  (such as an image, web page, ECG etc.)
- **Classification:** Find a parameterized function  $f_w(\mathbf{X})$  which can make the right predictions  $\mathbf{Y}$ .
- **End to End:** Can we learn  $\mathbf{Y}$  directly from  $I$ .



# What is machine learning?

- A branch of **artificial intelligence**,
  - the design and development of algorithms
  - computers to capture and model behaviors
  - based on empirical data.
- Intelligence requires knowledge,
  - It is necessary for the computers to acquire knowledge.
  - Learn from external world; “teachers” etc. and solve problems.
- A very popular area now
  - Lots of data
  - Many recent success stories



# What is Machine Learning?

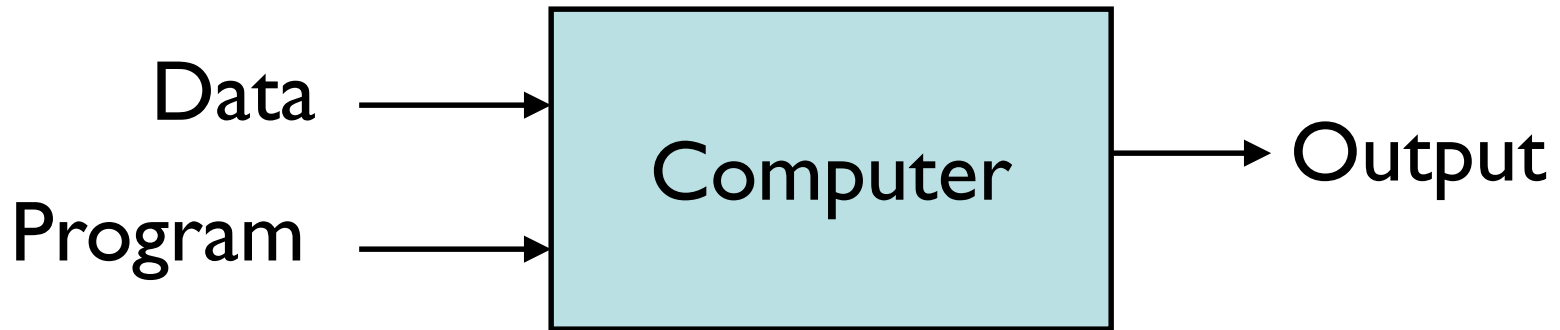
- [Arthur Samuel, 1959]
  - Field of study that gives computers
  - the ability to learn without being explicitly programmed
- [Kevin Murphy] algorithms that
  - automatically detect patterns in data
  - use the uncovered patterns to predict future data or other outcomes of interest
- [Tom Mitchell] algorithms that
  - improve their performance (P)
  - at some task (T)
  - with experience (E)



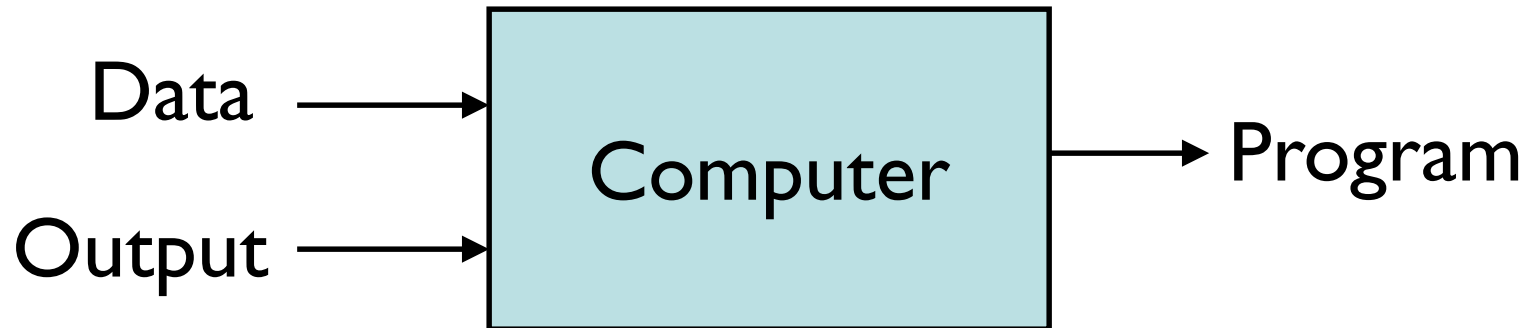
# What is Machine Learning?



## Traditional Programming

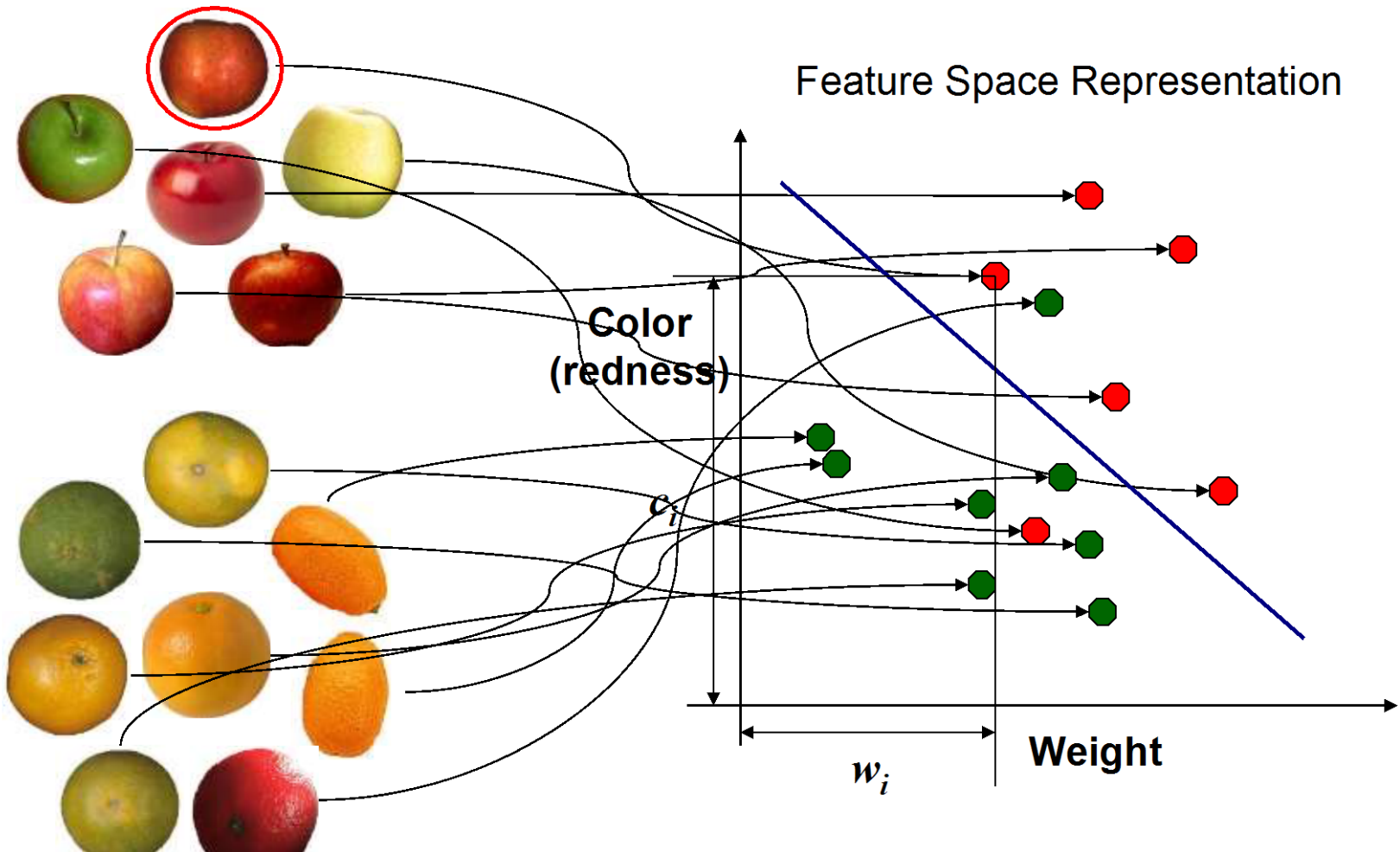


## Machine Learning





# Visualizing a Sample in 2D







# Sample/Point and Representation

A sample is easy to visualize in 2D

$$\mathbf{p} = (x, y) \text{ or } (x_1, x_2) \quad \mathbf{p} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

and sometime in 3D with some effort

$$\mathbf{p} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

And we often need much larger dimensionality in practice

$$\mathbf{p} = \begin{bmatrix} x_1 \\ x_2 \\ \cdot \\ x_{100} \end{bmatrix}$$

$$\mathbf{p} = \begin{bmatrix} x_1 \\ x_2 \\ \cdot \\ x_d \end{bmatrix}$$



# A bit more formal look



# The machine learning framework

- Apply a prediction function to a feature representation of the “sample” to get the desired output:

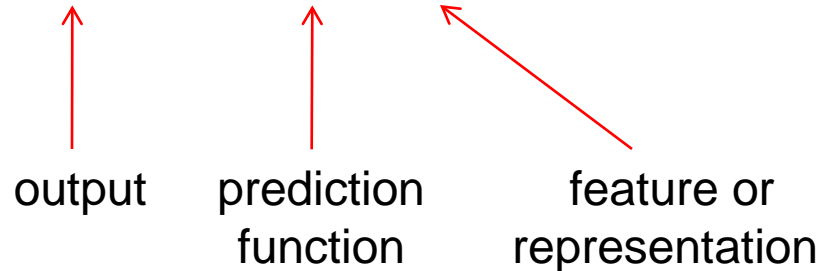
$$f(\text{apple image}) = \text{“apple”}$$

$$f(\text{tomato image}) = \text{“tomato”}$$

$$f(\text{cow image}) = \text{“cow”}$$

# The machine learning framework

$$y = f(\mathbf{x})$$

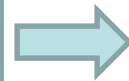


- **Training:** given a *training set* of labeled examples  $\{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_N, y_N)\}$ , estimate the prediction function  $f$  by minimizing the prediction error.
- **Testing:** apply  $f$  to a never before seen *test example*  $\mathbf{x}$  and output the predicted value  $y = f(\mathbf{x})$



## Training

Training Data



Features



Training  
Labels



Training



Learned  
model

## Testing



Test sample



Features

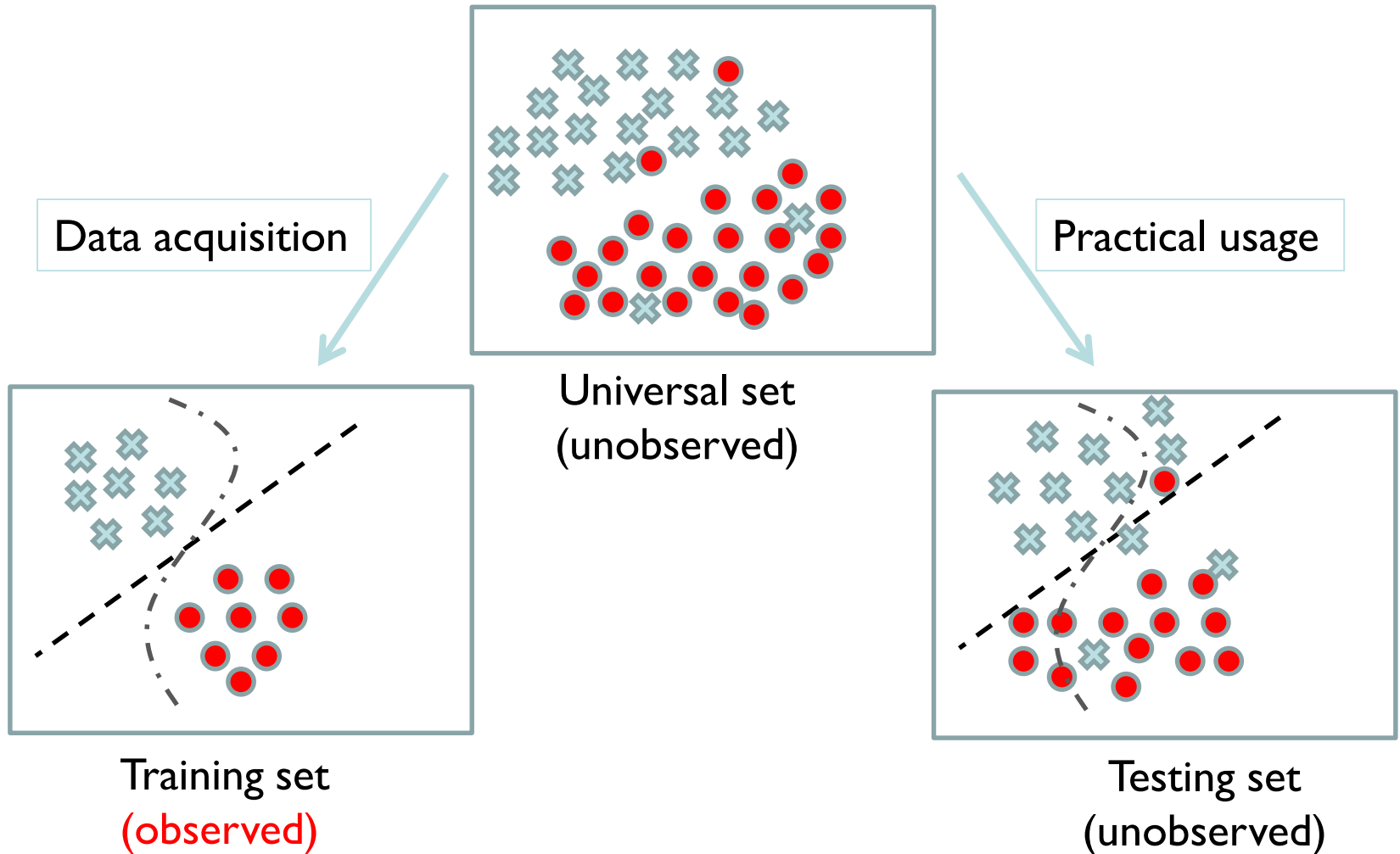


Learned  
model



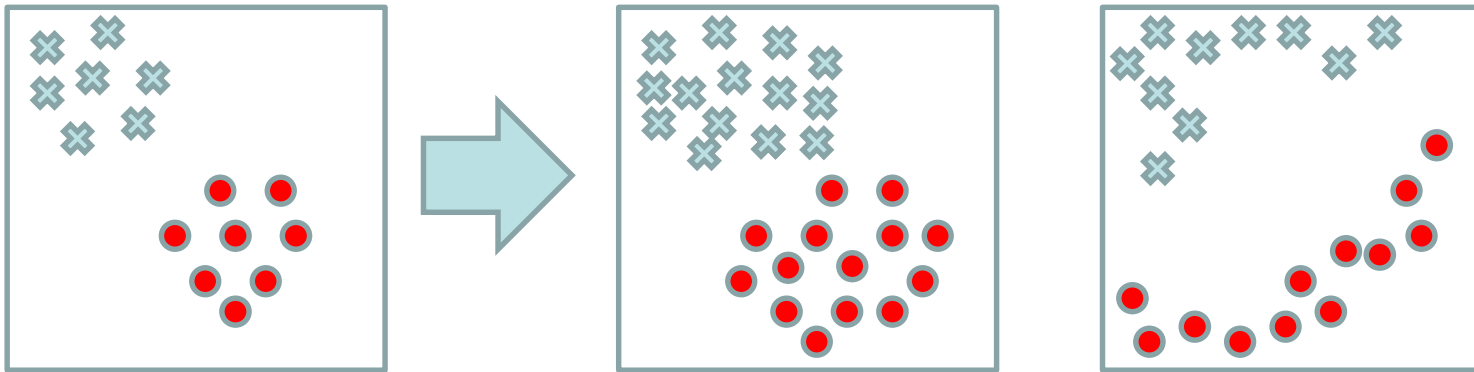
Prediction

# Training and testing



# Training and testing

- Training is the process of making the system able to learn.
- Assumptions:
  - Training set and testing set come from the same distribution
  - Need to make some assumptions or bias





# Two Prominent Learning Paradigms

- **Supervised learning** is the machine learning task of inferring a function from labeled training data.
- **Unsupervised:** Learn patterns from unlabeled data. Often look for a structure





# Nearest Neighbour Methods

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*``similar people show similar characters''*

# Nearest Neighbours

## Two types of neighbourhoods:

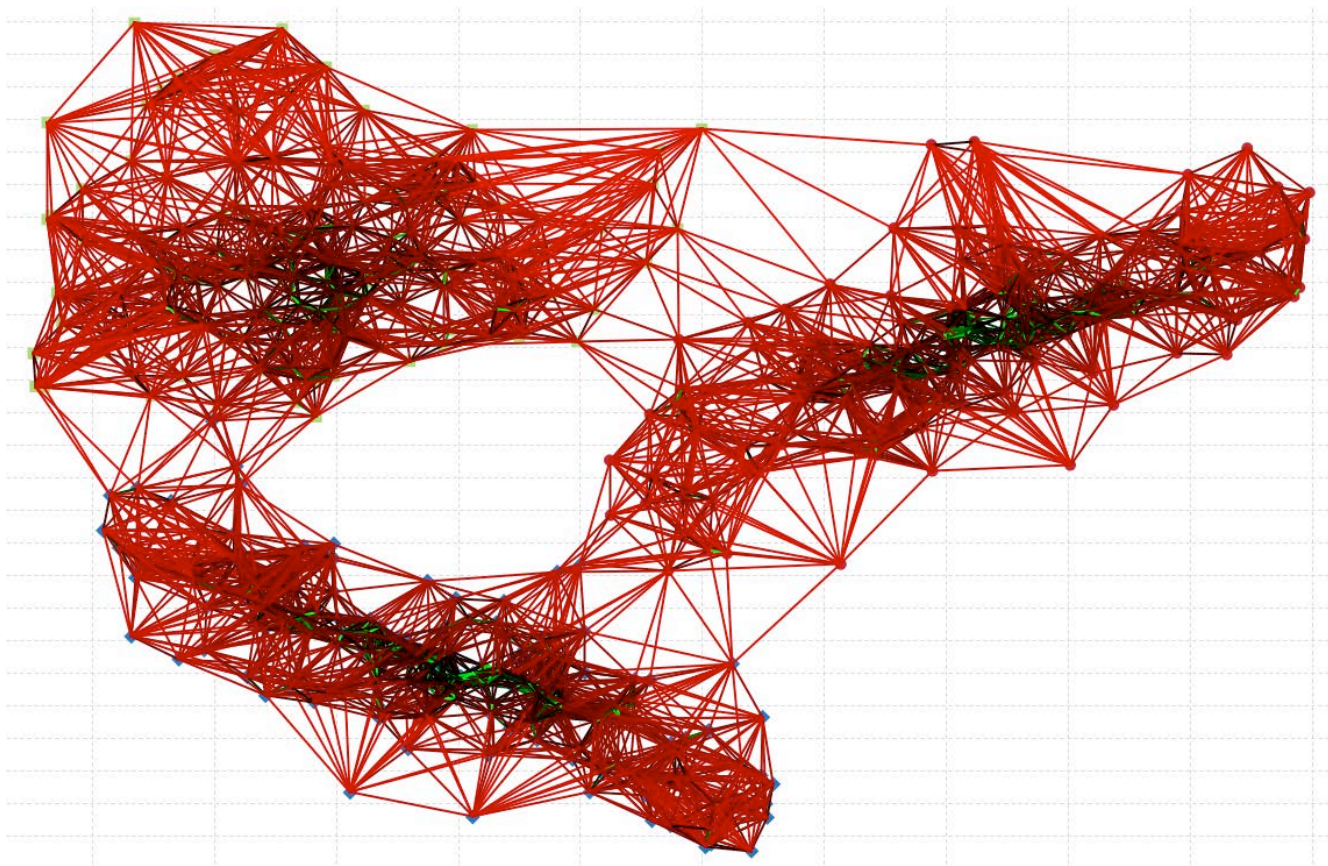
- **K Nearest Neighbours**
  - K samples that are closest to you.
- **Epsilon Neighbours**
  - Samples that have distances smaller than epsilon.

**Does  $x$  is in the K Nearest neighbourhood of  $y$  imply that  $y$  is in the K nearest neighbourhood of  $x$ ?**

**Does  $x$  is in the K Epsilon neighbourhood of  $y$  imply that  $y$  is in the Epsilon neighbourhood of  $x$ ?**

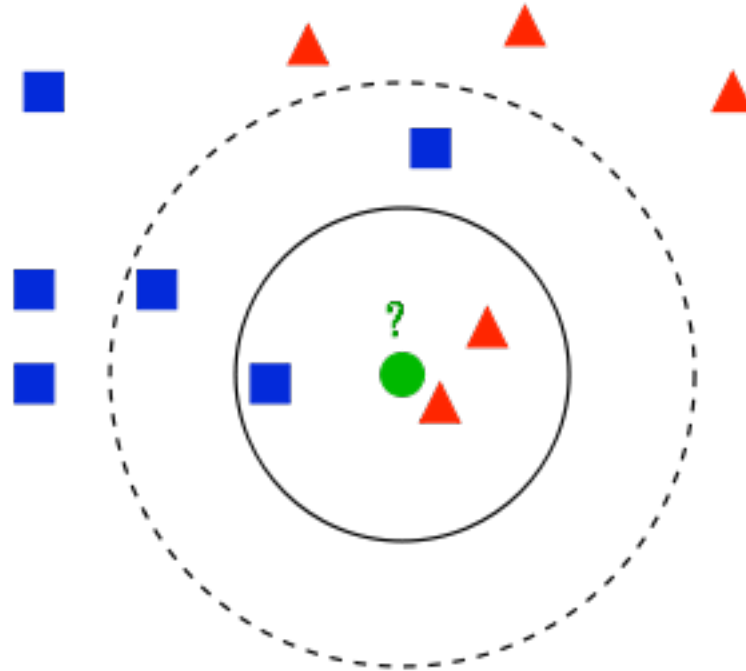


# Nearest Neighbour Graph[Remark\*]





# K Nearest Neighbours

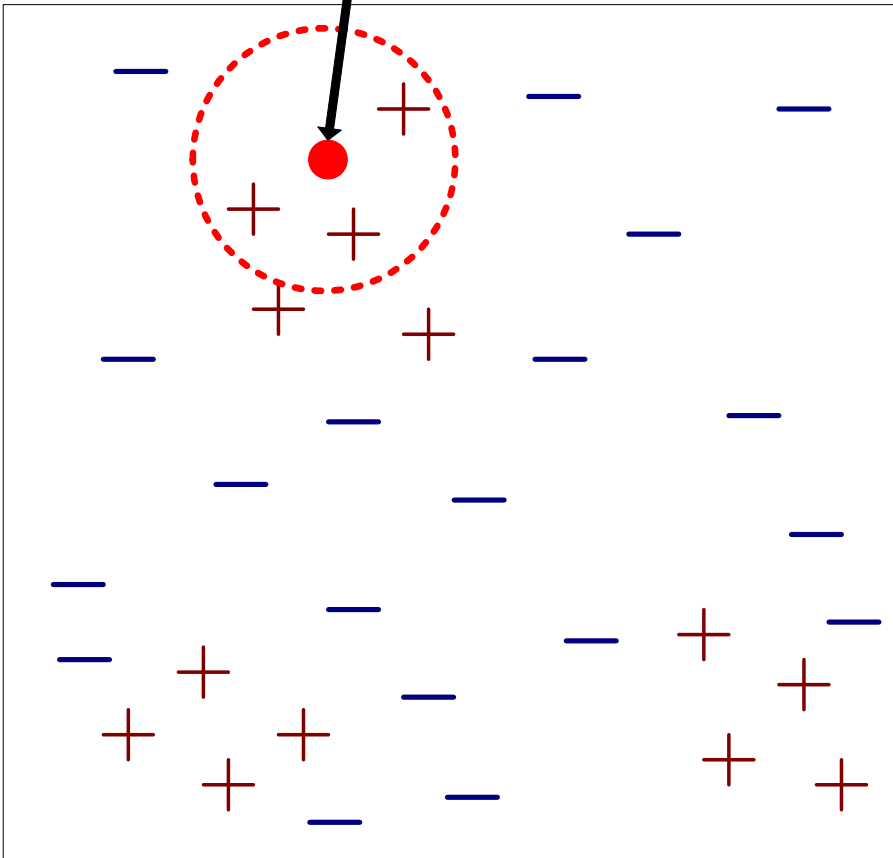


Classify the “test” sample as the majority label among the “K-Nearest Neighbours”



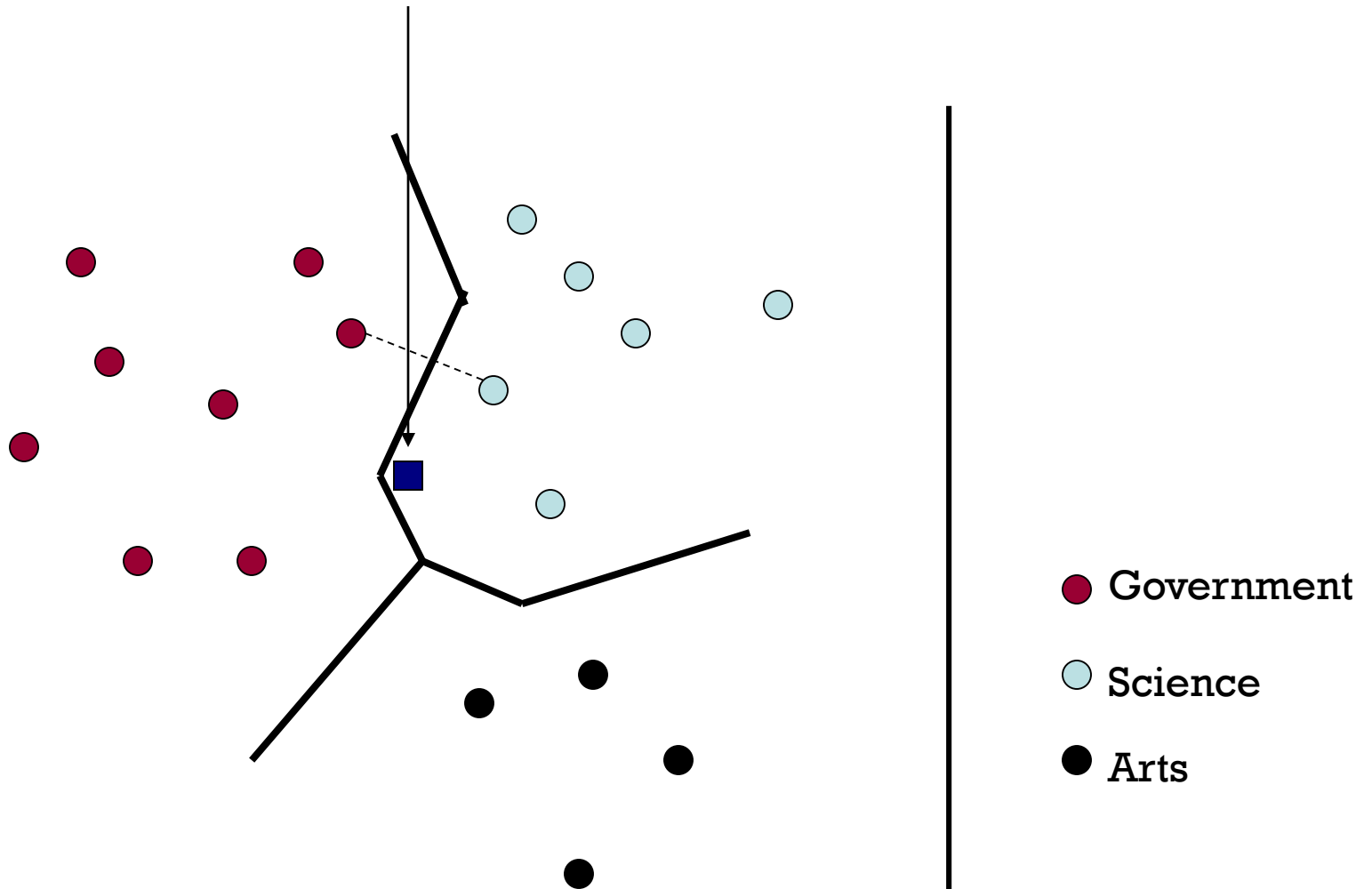
# Nearest-Neighbor Classifiers

Unknown record



- | Requires three things
  - The set of stored records
  - Distance Metric to compute distance between records
  - The value of  $k$ , the number of nearest neighbors to retrieve
  
- | To classify an unknown record:
  - Compute distance to other training records
  - Identify  $k$  nearest neighbors
  - Use class labels of nearest neighbors to determine the class label of unknown record (e.g., by taking majority vote)

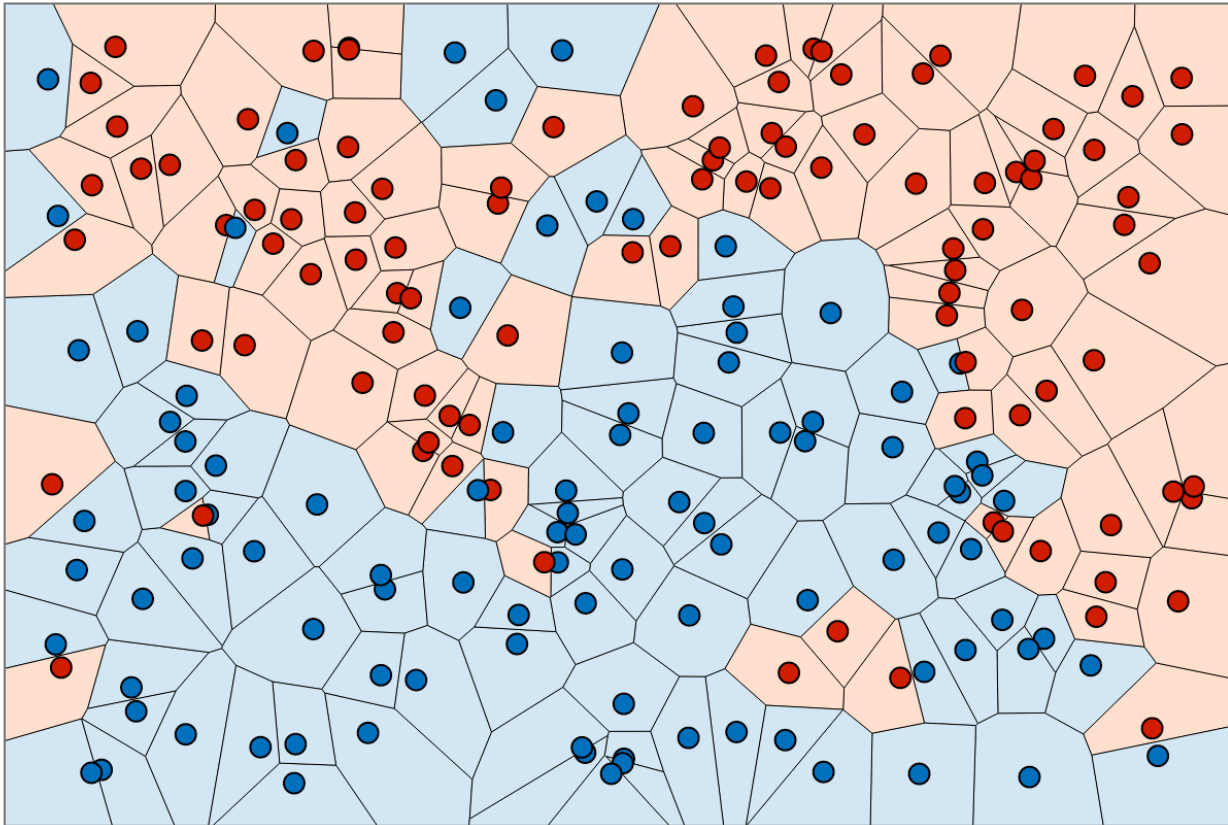
# Test Document = Science



Voronoi diagram



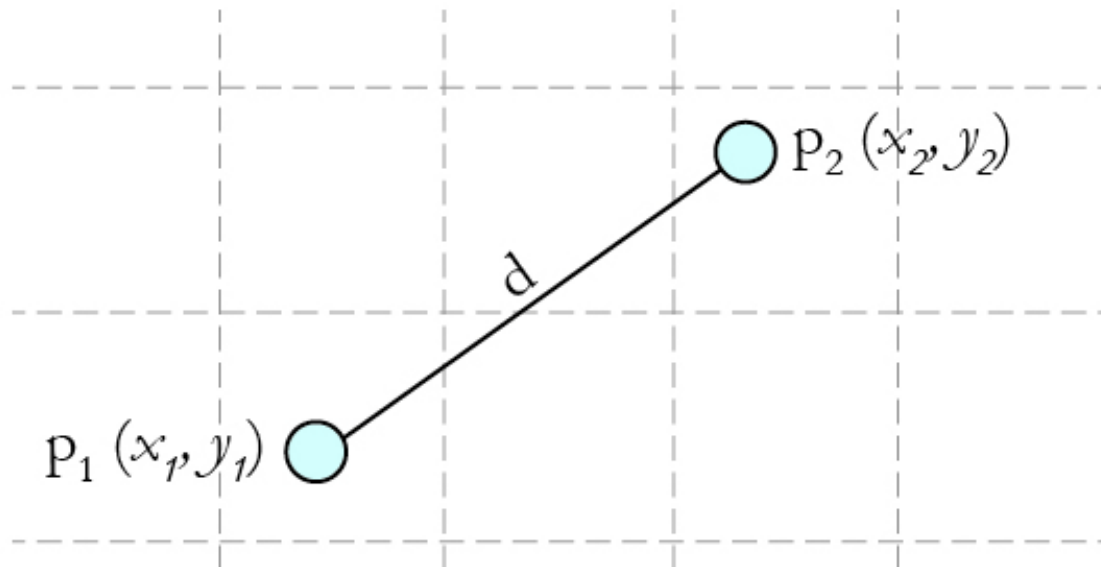
# Decision Boundary



Voronoi diagram



# Euclidean Distance



$$\text{Euclidean distance (d)} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d(\mathbf{p}, \mathbf{q}) = d(\mathbf{q}, \mathbf{p}) = \sqrt{(q_1 - p_1)^2 + (q_2 - p_2)^2 + \cdots + (q_n - p_n)^2}$$

$$= \sqrt{\sum_{i=1}^n (q_i - p_i)^2}.$$





# Parameters

- Distance measure
  - Not all distances are Euclidean.
  - Notion of similarity and distance.
- Value of K
  - Some “K”s are better than other.
  - Too small? Too large?
- Voting mechanism
  - Fusing results beyond a majority Vote.
  - Intuition: “far” imply less importance?
- Memory and Indexing (implimentation)



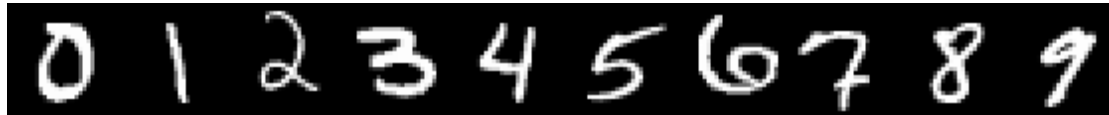
## Finding the “best” K?

- Determined experimentally
- Start with  $k=1$  and use a different “test set” to validate the error rate of the classifier
- Repeat with  $k=k+2$
- Choose the value of  $k$  for which the error rate is minimum
- Note:  $k$  is often odd number to avoid ties



Is this simple algorithm of any use?

# Example: Digit Recognition



- Yann LeCunn – MNIST Digit Recognition

- Handwritten digits
- 28x28 pixel images:  $d = 784$
- 60,000 training samples
- 10,000 test samples

- Nearest neighbour is competitive

	Test Error Rate (%)
Linear classifier (1-layer NN)	12.0
K-nearest-neighbors, Euclidean	5.0
K-nearest-neighbors, Euclidean, deskewed	2.4
K-NN, Tangent Distance, 16x16	1.1
K-NN, shape context matching	0.67
1000 RBF + linear classifier	3.6
SVM deg 4 polynomial	1.1
2-layer NN, 300 hidden units	4.7
2-layer NN, 300 HU, [deskewing]	1.6
LeNet-5, [distortions]	0.8
Boosted LeNet-4, [distortions]	0.7

# Problem of Retrieval

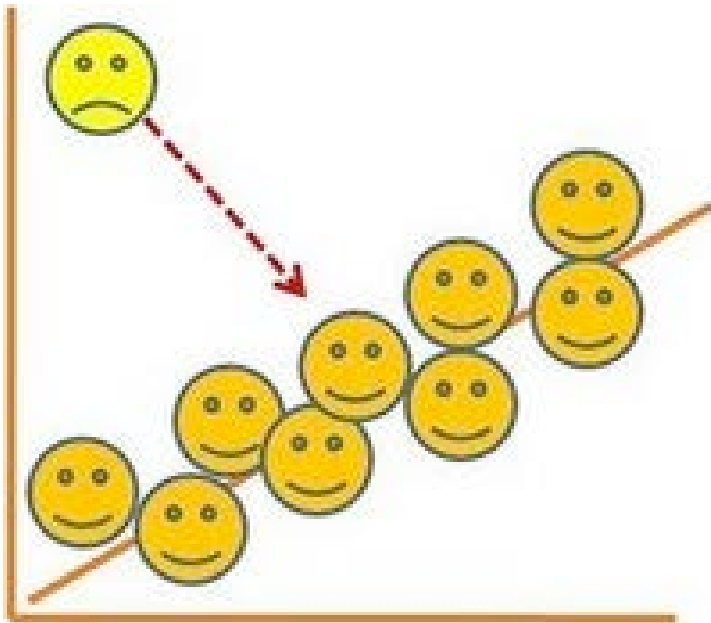
**Input: query  $q$ ; Outout: Ranked list**

**Given a Query “ $q$ ”, Sort and rank the database entries based of distance to the query  $d(q,x)$ .**





# Outlier



If a sample is not in the “K Neighbours” of at least  $T$  samples, it is an outlier.





# Advantages

- KNN is Simple
- KNNs are good if there are many many classes.
- Learn complex functions/decision boundaries (in fact piece-wise linear)
  - We will see linear methods soon, and also will see the need of nonlinearity
- No loss in information (everything is remembered). Fast to Train (no training?).





# Disadvantages

- High cost for classification/inference
  - Work “only” at the inference/test time
  - Carry examples (implication of memory)
- Uses all features/attributes:
  - Do not learn which features are important
  - Can be fooled easily with irrelevant features



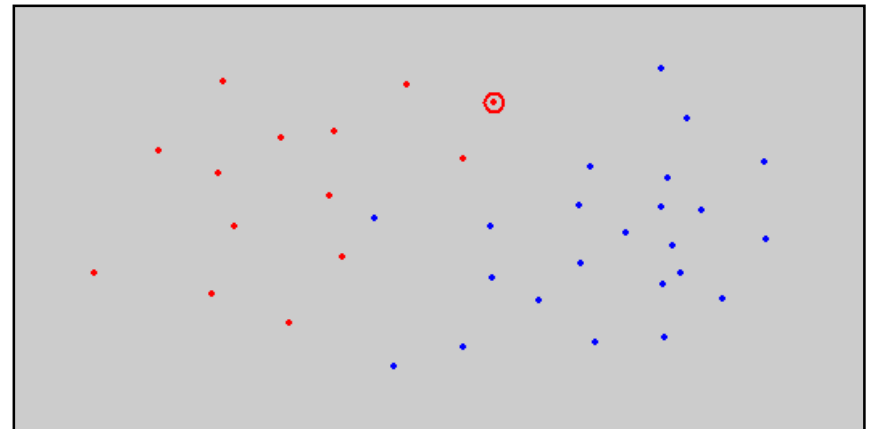
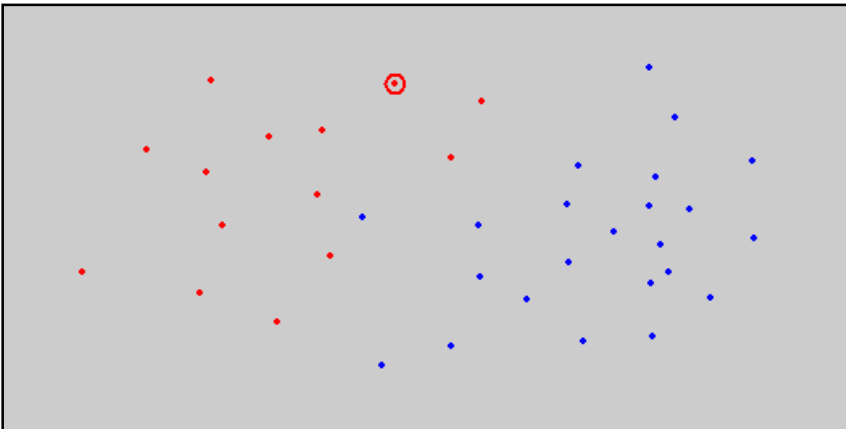
# Condensing

- Condensed Nearest Neighbour (CNN)

Hart 1968

- Incremental
- Order dependent
- Neither minimal nor decision boundary consistent
- $O(n^3)$  for brute-force method
- Can follow up with reduced NN [Gates72]
  - Remove a sample if doing so does not cause any incorrect classifications

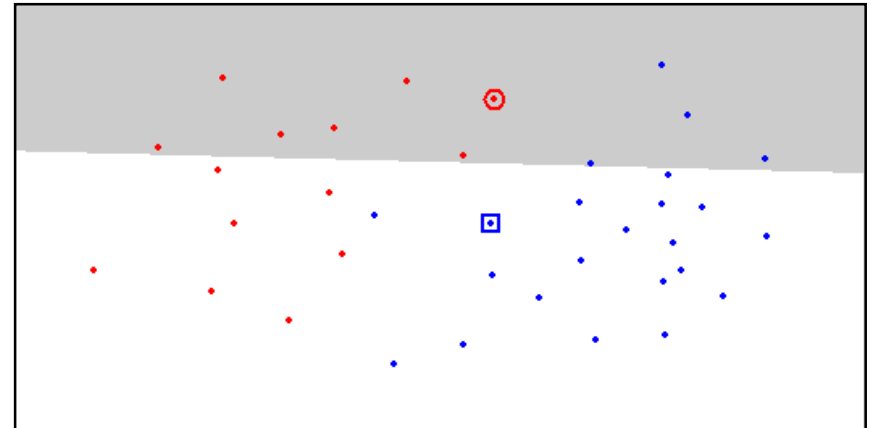
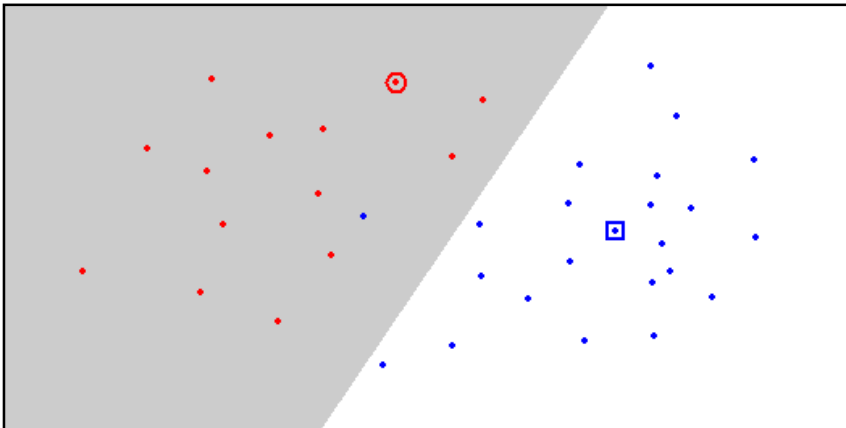
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2. Classify all remaining samples using the subset, and transfer any incorrectly classified samples to the subset
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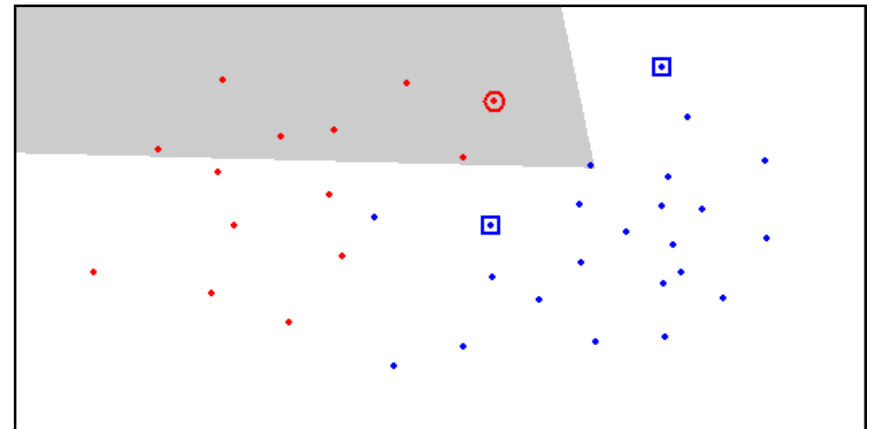
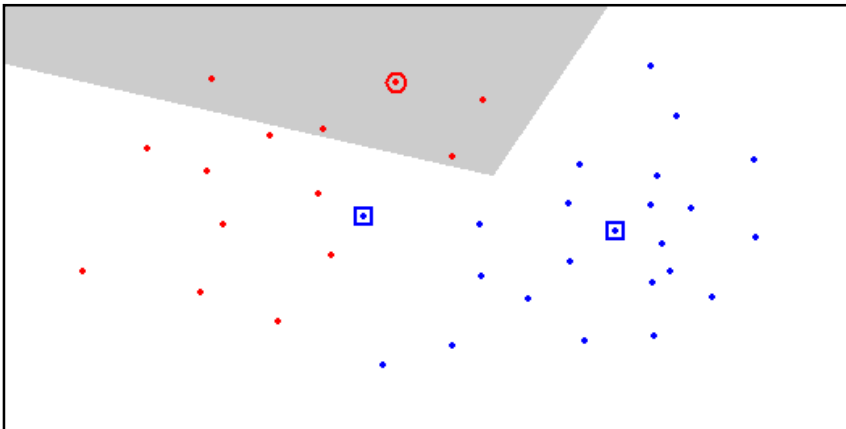


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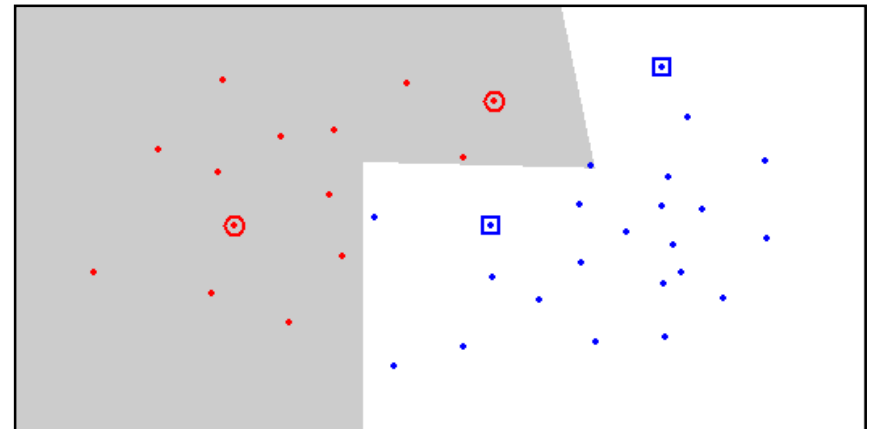
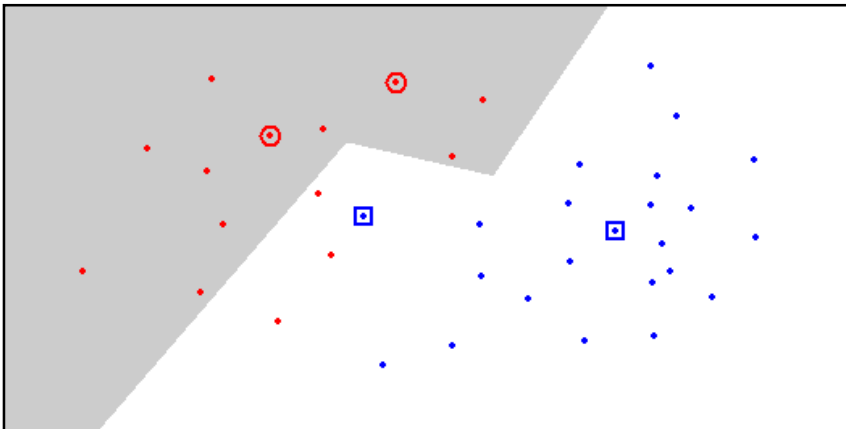
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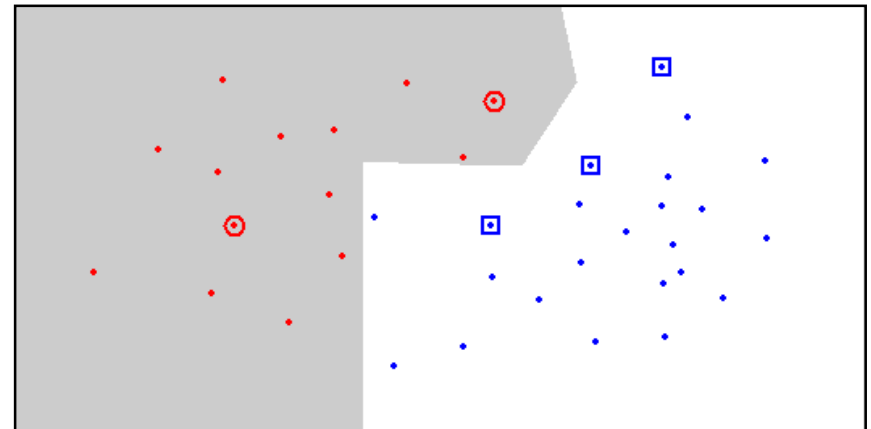
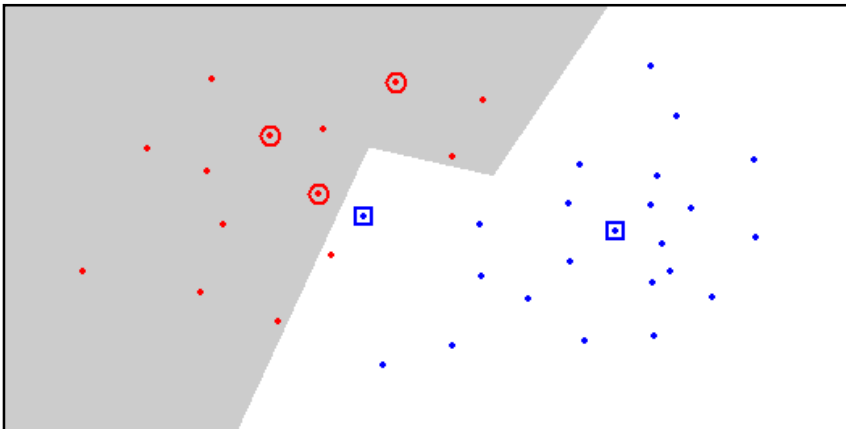
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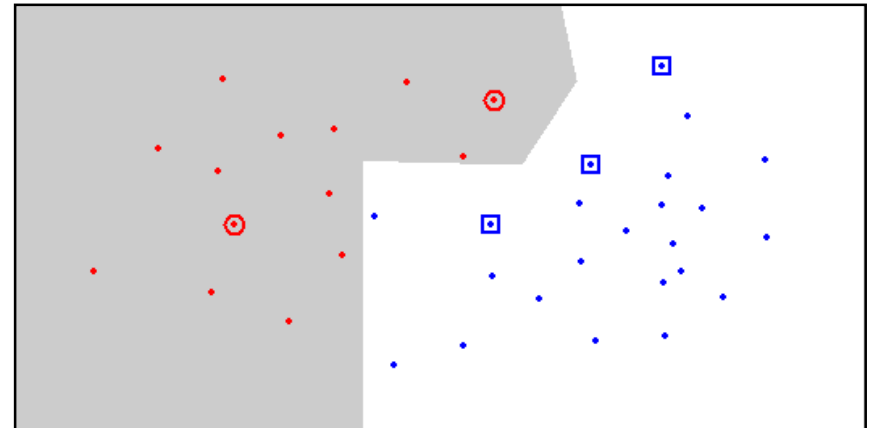
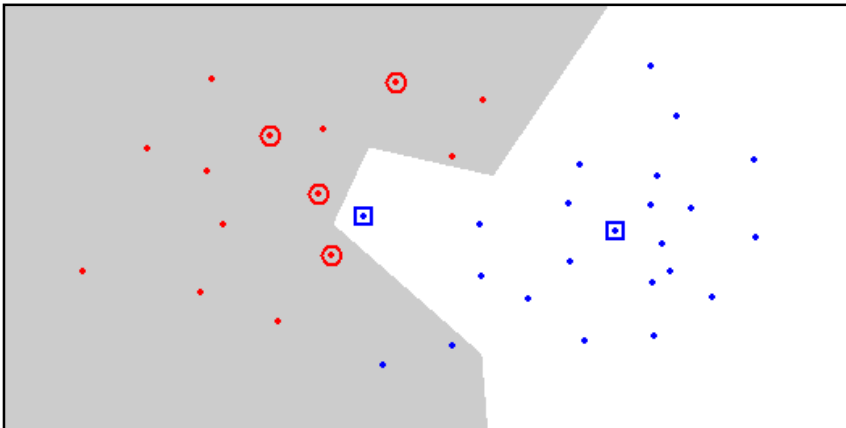
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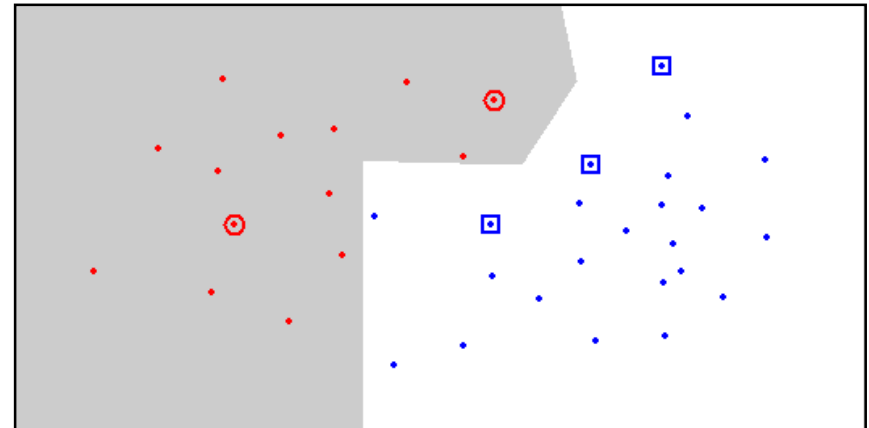
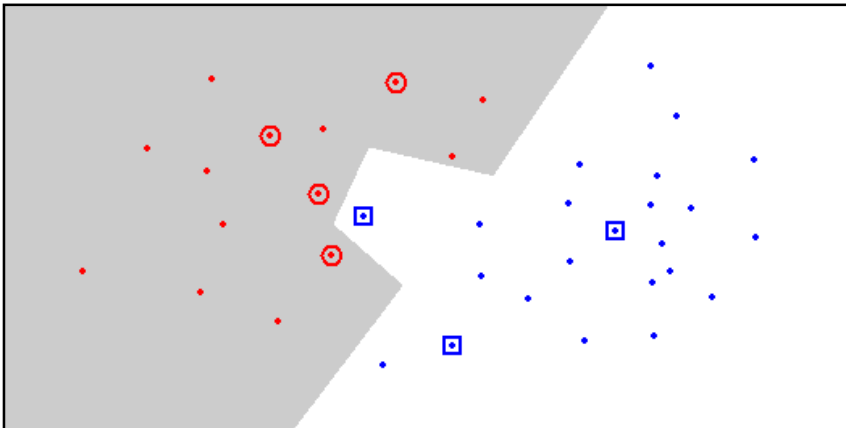
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# Nearest Neighbour Learning

- A popular learning perspective:
  - “Instance based learning”
- Lazy Learners
  - K NN and related methods
- Eager Learning Methods
  - Neural networks
  - Decision Trees
  - Support Vector Machines





# Summary

- Nearest Neighbour Methods:
  - Simple methods. Intuitive.
- Many Applications
  - Classification
  - Nearest Neighbour Graphs
  - Retrieval
  - Recommendations
- Intuitive in nature.



Thanks!!

Questions?