#### Unit 0.2 C++ Review

Numerical Analysis

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## Mathematical Operations in C and C++

- In C or C++ we have the following basic numerical types defined already.
  - Integer types: int, short, long, unsigned, singed, etc.
  - Floating-point types: float, double, long double.
- Using these basic types, mathematical expressions can be coded using simple operators.
  - For example, to evaluate

$$y = \frac{x^2 + 1}{x^3 + 2x^2 + 3x + 4}.$$

One simply writes

$$y=(x*x+1)/(x*x*x+2*x*x+3*x+4);$$

- Thus, simple mathematical expressions can be coded with ease.
- This is because the operators associated with the basic types have been defined.

## Needs of Vector and Matrix Operations

- In this course, we will need to solve linear and nonlinear systems.
- Often these systems are expressed by matrices and vectors.
- Solution methods are often expressed using matrices and vectors as well.
- The vectors and matrices are not basic types in C or C++.
- And no mathematical operations defined.
- For example, given an  $n \times n$  matrix A, an n-vector x and a real number  $\lambda$ , if  $\lambda$  is an eigenvector of A and x is the associated eigenvector, then

$$\mathbf{A}\mathbf{x} - \lambda\mathbf{x} = \mathbf{0}.\tag{0.2.1}$$

- Vectors are usually defined as 1-dimensional array in C or C++; while matrices defined as 2-dimensional array. To check if Eq. (0.2.1) is satisfied, multiple loops are needed.
- Fortunately, using class in C++ one can defined mathematical operators to match mathematical equations.
- Translating numerical theories to program becomes an easy job.

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### Classes in C++

- Class in C++ is designed to provide programmers with a tool for creating new types that can be used as conveniently as the basic types.
- It needs to define two aspects: data stored and the operations associated with.
  - Data members to store necessary data for the new type.
  - Function members to define the operations.
- Data members are similar to struct in C.
  - Storage for any predefined types can be declared.
- The members of a class are further classified into two categories:
  - public: members can be accessed by any functions,
  - private: members can only be accessed by member functions.
- Using private data, data hiding is made possible.
  - Clear responsibility,
  - Easier debugging,
  - Enable better teamwork, etc.

## Class Example

```
class Complex {
  public:
    Complex(double r=0,double i=0);
                                         // constructor
                                         // copy constructor
    Complex(const Complex &C);
    double r() const;
                                         // get real part
    double i() const;
                                         // get imaginary part
                                       // C1 += C2;
    Complex& operator+= (Complex &C2);
                                         // C1 += dbl;
    Complex& operator+= (double);
    Complex& operator = (Complex &C2); // C1 -= C2;
    Complex& operator-= (double);
                                         // C1 -= dbl;
    Complex& operator*= (Complex &C2); // C1 *= C2;
    Complex& operator*= (double);
                                         // C1 *= dbl;
    Complex& operator/= (Complex &C2); // C1 *= C2;
    Complex& operator/= (double);
                                        // C1 *= dbl;
  private:
    double x,y;
};
```

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### Classes in C++, II

- Data members can be divided into public and private.
  - Data accessible by all functions should be declared public,
  - Other data declared private.
- Member functions can have public and private as well.
  - Most member functions are public to define operations on the class.
  - Private functions can be used by member functions only.
    - Utility functions.
- The struct in C is a special case of class in C++.
  - It has only public members.
  - And no member functions.
- In declaring a class, the member function should be declared.
- All members (data and function) are accessed through the member operator

   ¬¬¬ .
  - Accessing data: z1.x, z1.y,
  - Accessing function: z1.r(), z1.i()
  - If zp is a pointer to z, then
    - Accessing data: zp->x, zp->y
    - Accessing function: zp->r() , zp->i()

### Member Function Accessing

- In C or C++, a function, f, is invoked by
  - f(x), calling f with one argument.
  - f(x1,x2), calling f with two arguments.
  - f(), calling f with no argument.
  - The parentheses () are needed to signify a function call.
- When calling a member function, (assuming z is an Complex object)
  - z.r() or z.i()
  - Parentheses are still needed to signify a function all.
  - There is an implicit argument supplied, this
  - this is a pointer pointing to the object.
  - In z.r(), this = &z
  - In the function definition of r(), data member can be accessed by the name of the data or with this-> preceding the name of the data.
    - For example, the member function r() is defined as

```
double Complex::r()
{
    return x;
}

double Complex::r()
{
    return this->x;
}
```

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### Member Function Definition

- To define a member function, the name should be preceded with class name::, as the examples shown above.
  - The return type needs to precede the class name
  - Note that in C++, the return type should always be defined.
- Two special functions need no return type.
  - constructor and destructor functions.
- In C or C++, a variable is created by a declaration statement.
  - For example, two variables are declared

```
double x1,x2;
```

• In C++, an object is instantiated by declaration as

#### Complex z1;

When this declaration statement is executed, the constructor function is actually called such that the data member can be initialized (or not) properly.

### Constructors

- Three types of constructors are possible (using Complex class as an example).
  - Initialization constructor:

```
Complex z1(1.0,1.0); // initializing z1 to (1.0,1.0)
```

Uninitialization constructor, two usages:

```
Complex z2; // uninit constructor Complex z2(); // uninit constructor
```

Copy constructor, two usages:

```
Complex z3=z1; // copy constructor Complex z3(z1); // copy constructor
```

Each constructors need to declared and defined separately.

### Constructors, II

- Note that the name of the constructor functions are simply the name of the class.
  - In defining the member function, class name and scope operator :: need to precede function name.
- Constructor functions need no return type.
- Three functions defined with the same name function overload.
  - The number of arguments or the argument types need to be different.
- In C++, function arguments can have default values.

```
Complex::Complex(double r=0,double i=0) // init constructor
{
    x=r; y=i;
}
```

• In this case, when parameters are not supplied in function calls, the default values are taken.

```
Complex z1(1.0,1.0);  // initialize both real and imaginary
Complex z2(1.0);  // z2=(1.0,0)
Complex z3();  // z3=(0,0)
```

• In this case, the uninit constructor should not be declared or defined.

### Destructor

- Destructor function is called when a variable is no longer needed.
  - Local variables (automatic storage duration) going out of scope.
  - Temporary variables no longer needed.

```
z4=z1+z2*z3;
z5=sqrt(z6);
```

A temporary variable may be created in forming the product z2\*z3, and returned by a function before assignment.

- Compiler generates calls to destructor functions.
- In most cases, destructor needs no actions.
  - But, if dynamic memory is allocated by constructor then destructor should release the memory space acquired.
- ullet The name of destructor function is  $\overline{\ }\sim \overline{\ }$  preceding the class name.
- Destructor has no return type.

```
Complex::~Complex()
{ } // no action needed
```

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### References

- In C, function parameters are passed by value.
  - A copy of the variable is created and passed to the function.
  - The return value of a function is also a copy that is destroyed after its use.
  - Thus, the value of the parameter cannot be modified by a function.
  - Pointer should be passed, if its value is to be modified.
- In C++, the variable itself can be passed and returned by a function pass-by-reference.
- To do so, the parameter needs to be declared with a reference symbol & after the type name.
- Example member function declaration:

```
Complex& operator+= (Complex &C2); // C1 += C2;
```

• Example member function definition:

```
Complex & Complex::operator+=(Complex &z)
{
    x+=z.x;
    y+=z.y;
    return *this;
}
```

### References, II

- Using a referenced parameter or return, the variable itself is passed between functions.
  - No copies are created improved efficiency.
  - Variable can be modified.
- Reference can be used to create an alias for a variable.

```
Complex z1;
Complex za=&z1;
```

The variable za is an alias of z1. Modifying za changes the value of z1, vice versa.

 Note that reference can only be created for variables that are existing physically. Temporary variables created during expression evaluation may not have references.

```
z4=z1+z2*z3;
```

• The temporary variable created for z2\*z3 may not be physically present and, thus, no reference possible.

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#### const

- Using reference can increase program efficiency by eliminating the need of copying function arguments repeatedly.
- The function is also able to access the variables with the capability of modifying their values.
- To clear state that a function argument will not be modified, the const key word should be used.

```
Complex& operator+= (const Complex &C2); // C1 += C2;
```

- With const inserted, the variable C2 cannot be modified.
- Any attempts of modifying C2 will result in a compilation error.
- Note that the copy constructor should have the argument declared as a const reference of the class type.

```
class Complex {
    // ...
    Complex(const Complex &C); // copy constructor
    // ...
}
```

### const, II

- Note that const can be used for any argument, not necessary of reference type, with the same effect.
- A member function of a class that will not modify any of its data members can be declared to be a const member function.

 Note that in function definition, the const key work needs to appear after the parentheses as well.

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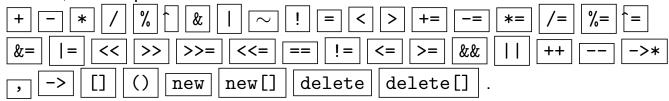
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## Defining Operators for Classes

• In C++, most operators can be defined for classes



- The following operators cannot be redefined.
  - :: scope resolution,
  - member selection,
  - .\* member selection through pointer to member,
  - ? : ternary condition expression,
  - sizeof,
  - typeid
- The first 3 operators take a name, rather than value, as the second operand.

## Defining Operators for Classes, II

- In C++, the operators are functions.
  - They have the name operator preceding the operator symbol
  - For example, operator+
- If z is an object of class Complex and operator+ function is defined as a member function of class Complex, then it is possible to use both shorthand or explicit operator function call.
- If operator+ is defined as a member function of z1.

```
z3=z1+z2;
z3=z1.operator+(z2);
```

• If operator— is defined as a nonmember function, then the following are equivalent.

```
z3=z1-z2;
z3=operator-(z1,z2);
```

• Shorthand operator symbols are usually preferred.

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### Defining Operators for Classes, III

 In defining an operator function as a member function, it should be declared in the class declaration as well, and then defined with the class name preceding the function name.

```
class Complex {
    public:
    // ...
    Complex operator+(Complex C);    // + function declaration
    // ...
};
Complex Complex::operator+(Complex C)    // + function definition
{        ... }
```

• In defining operator function as nonmember function, it follows regular function declaration and definition.

```
Complex operator-(Complex C1,Complex C2); // - function declaration

Complex operator-(Complex C1,Complex C2) // - function definition

{ ... }
```

## Defining Operators for Classes, IV

- Note in the preceding function declaration and definition, the addition of z1+z1 must have both operands of type Complex.
- If z1 or z2 is not Complex, then the addition is not defined.
- To handle the case that z2 is a double, the function needs to be overloaded by declare and define the following:

```
class Complex {
    public:
    // ...
    Complex operator+(double dbl);    // + can handle Complex + dbl
    // ...
};
Complex Complex::operator+(double dbl)    // + function definition
{ ... }
```

• But the case of *double* **z1** can only be handled by declaring a nonmember function.

```
Complex operator+(double dbl,Complex C);
```

 This is due to that the first operand of the operator defined as member function must be an implicit argument, which has the same type as the class.

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#### friend of a Class

- In C++, private members cannot be accessed by nonmember functions.
- Exceptions can be made by declaring a function as a friend.
  - friend functions can access private members (data and functions).
  - friend functions must be declared in class declaration.

- Note that sqrt() is a nonmember function but it can access class Complex's private data.
- Properties of friendship.
  - Friendship is granted not taken.
  - Friendship is not symmetric.
  - Friendship is not transitive.

### Header Files and Source Files

- A well defined class can be reused for many applications.
- It is a good practice to put the declarations associated with a class into a header file that ends with .h file extension.
- The function definitions, member and nonmember, are put into a separated source file that ends with cpp file extension.
- The source file can then be compiled by

```
$ g++ -c Complex.cpp
```

This produces a Complex.o object file that can be linked with application programs.

```
$ g++ prog.cpp Complex.o
```

- This practice saves compilation time and the header file serves as a well defined interface for the users.
- As long as the function declarations are not changed, modifying the the function definitions in Complex.cpp file does not affect the application source file.
  - But the program needs to be re-linked.

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## Complex.h (1/2)

```
// complex number class
#ifndef COMPLEX_H
#define COMPLEX H
#include <stdio.h>
#include <stdlib.h>
class Complex {
  public:
    Complex(double r=0,double i=0);
                                        // constructor
    Complex(const Complex &C);
                                         // copy constructor
    double r() const;
                                         // get real part
    double i() const;
                                         // get imaginary part
    Complex& operator+= (Complex&);
                                        // C1 += C2;
    Complex& operator+= (double);
                                         // C1 += dbl;
    Complex& operator*= (Complex&);
                                        // C1 *= C2;
    Complex& operator*= (double);
                                        // C1 *= dbl;
    Complex& operator/= (Complex&); // C1 *= C2;
    Complex& operator/= (double);
                                        // C1 *= dbl;
  private:
    double x,y;
};
```

## Complex.h (2/2)

```
// unary plus
Complex operator+(Complex);
Complex operator+(Complex, Complex);
                                           // C1 + C2
                                           // C1 + dbl
Complex operator+(Complex,double);
Complex operator+(double,Complex);
                                           // dbl + C1
Complex operator-(Complex);
                                           // unary minus
Complex operator-(Complex, Complex);
                                           // C1 - C2
Complex operator-(Complex,double);
                                          // C1 - dbl
Complex operator-(double,Complex);
                                           // dbl - C1
Complex operator*(Complex, Complex);
                                          // C1 * C2
Complex operator*(Complex,double);
                                           // C1 * dbl
Complex operator*(double,Complex);
                                          // dbl * C1
Complex operator/(Complex, Complex);
                                           // C1 / C2
Complex operator/(Complex,double);
                                          // C1 / dbl
Complex operator/(double,Complex);
                                           // dbl / C1
                                           // |C1|
double fabs(Complex z);
Complex& operator++(Complex&);
                                          // prefix increment
Complex operator++(Complex&,int);
                                          // postfix increment
int operator==(Complex,Complex);
                                          // testing for equality
int operator!=(Complex,Complex);
#endif
```

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## Complex.cpp (1/4)

```
// Function definitions
#include <math.h>
#include "Complex.h"
Complex::Complex(double r=0,double i=0) // init constructor
{
    x=r; y=i;
Complex::Complex(const Complex &z)
                                             // copy constructor
{
    x=z.x; y=z.y;
double Complex::r() const
                                             // get real part
{
    return x;
double Complex::i() const
                                             // get imaginary part
{
    return y;
}
```

## Complex.cpp (2/4)

```
Complex & Complex::operator+=(Complex &z) // C += Z;
{
    x+=z.x;
    y+=z.y;
    return *this;
}
Complex & Complex::operator+=(double d1)  // C += double;
    x+=d1;
    return *this;
}
Complex operator+(Complex z)
                                                 // unary plus
    Complex z1(z);
    return z1;
}
Complex operator+(Complex z1,Complex z2) // z1 + z2
    Complex z(z1);
    return z+=z2;
}
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```

# Complex.cpp (3/4)

```
Complex operator+(Complex z1, double d) // z1 + double
{
    Complex z(z1);
    return z+=d;
}
Complex operator+(double d,Complex z1) // double + z1
{
    Complex z(z1);
    return z+=d;
}
                                           // |z|
double fabs(Complex z)
{
    return sqrt(z.r()*z.r()+z.i()*z.i());
Complex & operator ++ (Complex & z1)
                                           // prefix increment
    return z+=1.0;
}
```

# Complex.cpp (4/4)

```
Complex operator++(Complex &z1,int)  // postfix increment
{
    Complex z(z1);
    ++z1;
    return z;
}
int operator==(Complex z1,Complex z2)  // test for equality
{
    if (z1.r()==z2.r() && z1.i()==z2.i()) return 1;
    return 0;
}
```

- With these example functions, all functions defined in Complex.h can be easily implemented.
- And coding for complex number expressions are very straightforward.
- Try to code the following expressions.

$$f(z) = \frac{3z^3 + 2z^2 + z + 1}{z^4 - z^3 + z^2 - z + 1},$$
  
$$g(z) = (z+1)(z+2)(z+3).$$

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## Summary

- Needs of classes
- Class in C++
- Member functions
- Constructor
- Destructor
- References
- Const
- Defining operator functions
- Friends
- Header and source files
- Example: Complex class