

True problem:

$$\max_{x, y, r, s, u, v} \sum_{t \in T} (R_t x_t - E[B_t(y_t^w + g r_t^w)])$$

$$\text{s.t.} \quad x_t \leq y_t + g r_t + w_t^w + M_t^w z^w$$

$$\sum_{w \in \Omega} z^w \leq \lfloor N\epsilon \rfloor$$

$$z^w \in \{0, 1\},$$

$$\forall w \in \Omega$$

$$x_t, s_t^w \geq 0$$

$$\forall t \in T, \forall w \in \Omega$$

$$(y^w, r^w, u^w, v^w) \in \gamma$$

$$\forall w \in \Omega$$

Lagrangian Relaxation:

$$L(\lambda) = \max \sum_{t \in T} (R_t x_t - E[B_t(y_t^w + g r_t^w)]) + \lambda (\lfloor N\epsilon \rfloor - \sum_{w \in \Omega} z^w)$$

$$\text{s.t.} \quad x_t \leq y_t + g r_t + w_t^w + M_t^w z^w$$

$$z^w \in \{0, 1\}$$

$$\forall w \in \Omega$$

$$x_t^w, s_t^w \geq 0$$

$$\forall t \in T, \forall w \in \Omega$$

$$(y^w, r^w, u^w, v^w) \in \gamma$$

$$\forall w \in \Omega$$

Lagrangian Dual:

$$\min L(\lambda)$$

$$\text{s.t.} \quad \lambda \geq 0$$