

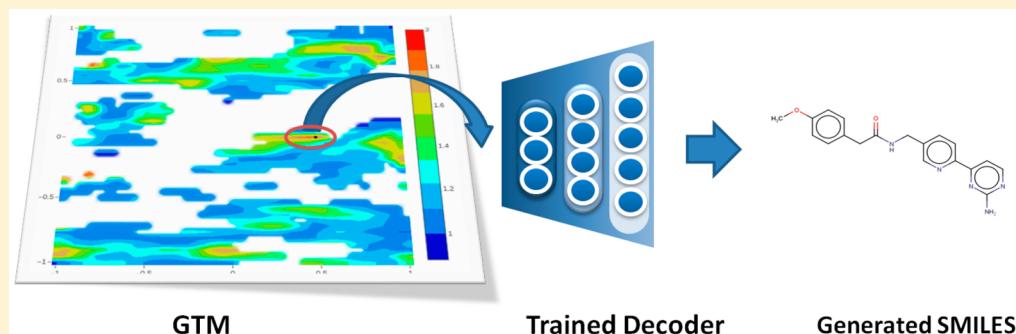
# De Novo Molecular Design by Combining Deep Autoencoder Recurrent Neural Networks with Generative Topographic Mapping

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**ABSTRACT:** Here we show that Generative Topographic Mapping (GTM) can be used to explore the latent space of the SMILES-based autoencoders and generate focused molecular libraries of interest. We have built a sequence-to-sequence neural network with Bidirectional Long Short-Term Memory layers and trained it on the SMILES strings from ChEMBL23. Very high reconstruction rates of the test set molecules were achieved (>98%), which are comparable to the ones reported in related publications. Using GTM, we have visualized the autoencoder latent space on the two-dimensional topographic map. Targeted map zones can be used for generating novel molecular structures by sampling associated latent space points and decoding them to SMILES. The sampling method based on a genetic algorithm was introduced to optimize compound properties “on the fly”. The generated focused molecular libraries were shown to contain original and *a priori* feasible compounds which, pending actual synthesis and testing, showed encouraging behavior in independent structure-based affinity estimation procedures (pharmacophore matching, docking).

## 1. INTRODUCTION

The development of new chemical compounds with desired properties drives the field of chemoinformatics.<sup>1</sup> The two main approaches to solve this problem are *virtual screening*,<sup>2–5</sup> which is based on the processing of sets of preprepared molecules (e.g., databases of already synthesized or easily synthesizable compounds, virtual combinatorial libraries), and *de novo* design,<sup>6–8</sup> which involves the generation of new molecules. The *de novo* design can be either *receptor-based*, which requires knowledge of the spatial structure of protein receptors (biological targets) and in which new molecules are assembled within receptor binding pockets, or *ligand-based*, which does not require such knowledge. The latter approach is at the focus of this publication. Methods involving the use of pseudoreceptors can be considered as a combination of both approaches.<sup>9</sup>

The field of ligand-based *de novo* design is currently rather broad. The first-generation research in this area began with the advent of the “inverse QSAR” concept.<sup>10–17</sup> Within the framework of this methodology, the model allowing the prediction of the property/activity value for a compound is

used in the “reverse direction” to restore the structures of compounds possessing, according to this model, a given property/activity value. Inverse QSAR methods are usually based on topological (including fragment) descriptors and include the use of either an exhaustive or a stochastic molecular graph generator.

The second-generation methods in ligand-based *de novo* design are of a broader nature.<sup>8</sup> They are based on the use of general-purpose scoring functions, which can also include similarity measures with respect to active compounds assessed at either topological or 3D levels, in combination with predominantly stochastic search procedures, such as genetic algorithm, genetic programming, Monte Carlo techniques, etc. New molecules can be generated in this case by applying formal molecular-graph mutation operations and recombining

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atoms and fragments (building blocks), as well as combining synthetic reactions.<sup>18</sup>

The third-generation methods have recently been developed under the influence of deep learning approaches,<sup>19</sup> which enabled novel opportunities for drug discovery.<sup>20,21</sup> Most of such methods are based on the use of recurrent neural networks (RNNs) for generating SMILES strings, which encode chemical structures.<sup>22</sup> An alternative approach based on directly generating molecular graphs instead of SMILES should also be mentioned.<sup>23–25</sup> Although SMILES were used in several earlier publications to represent molecules in QSAR modeling,<sup>26–29</sup> only since 2017 they are actively used to generate chemical structures.<sup>30–37</sup> In order to perform structure generation, an RNN learns to predict the probability of the next character (or token) in a current SMILES, given the previous ones.<sup>30</sup> Sampling characters (tokens) from predicted probability distributions using a temperature parameter can be used to control the diversity of the molecules being generated.<sup>33</sup> A large number of SMILES strings are needed for training such networks in order to be able to generate correct SMILES strings, because the grammar of the SMILES language is not encoded explicitly in RNNs and needs to be learned. Once trained, such RNN can generate SMILES strings corresponding to new molecules resembling training set examples. A practical procedure for generating focused libraries of chemical compounds active against a chosen target consists of two stages. First, a network is trained on a large amount of data to generate correct SMILES strings. Then, the pretrained network is fine-tuned using chemical structures of compounds known to be active with respect to a certain target, and the resulting network acquires the ability to generate focused libraries of compounds being active against the same target.<sup>30,33</sup> New molecules can be generated in this case not only from scratch but also by growing specified seed fragments.<sup>33</sup>

A more powerful approach to perform *de novo* design of molecules with desired properties is based on the use of Reinforcement Learning (RL)<sup>38</sup> in conjunction with RNNs. RL is a general machine-learning framework that considers “agents” taking “actions” to maximize “rewards”. In this case, the “agent” is a RNN being used to generate SMILES strings, the “action” is appending a new character (token) to a partially formed SMILES string, while the “reward” is gained whenever a completely formed SMILES string corresponds to a molecule with desired properties. Unlike the aforementioned approach requiring fine-tuning of pretrained networks, the use of RL offers the additional opportunity to drive inverse QSAR studies in association with quantitative QSAR modes. Olivecrona et al. applied RL to tune a RNN toward generating compounds predicted to be active against a certain target.<sup>34</sup> Popova et al. suggested to integrate two deep neural networks—generative and predictive—for this purpose.<sup>36</sup> The generative network is trained to generate correct SMILES strings, the predictive network is trained to predict desired properties, and then both networks are trained jointly with RL in order to generate molecules with desired properties. In several other publications the same goal was reached by combining RL with the Generative Adversarial Net (GAN) framework. GANs is a recently introduced class of unsupervised machine learning algorithms enabling generating new samples from the distribution represented by the training examples without the need to define and manipulate the corresponding probability distribution explicitly.<sup>39</sup> This makes this approach very

attractive for generating high-dimensional or unstructured data, such as high-resolution images in computer vision and molecules in chemoinformatics. This is achieved by combining two neural networks, so-called “generator” and “discriminator” nets, competing with each other (by trying to “fool” each other) in a zero-sum game. The “generator” net generates new molecules, while the “discriminator” net tries to detect whether it belongs to the same distribution as the molecules from the training set, e.g. the distribution of correct SMILES for drug-like and synthesizable compounds. The role of the RL in this case is to tune the “generator” to generate molecules with desired properties. RL was combined with GANs for performing *de novo* design of molecules by Guimaraes et al. in the ORGAN (Objective-Reinforced Generative Adversarial Networks) system<sup>40</sup> and in the RANC (Reinforced Adversarial Neural Computer) system.<sup>35</sup>

Although the use of RL in conjunction with the formation of SMILES using RNN is a universal approach to the design of chemical compounds with desired properties, it has certain drawbacks. It cannot be expected that a very indirect association of the property of compounds with the next added symbol to a gradually growing SMILES can be comparable, in predictive performance and interpretability, with the models obtained in a more traditional way (by directly correlating the property with molecular descriptor values). Moreover, the use of molecular descriptors would make it possible to involve a rich arsenal of chemoinformatics tools and methodologies in the *de novo* design of new compounds and materials.

A fundamental alternative to the use of RL in *de novo* molecular design is the schemes based on the formation of “revertible” molecular descriptors, which, on the one hand, could be used to construct structure–property models, and on the other hand, could be used to reconstruct structures of chemical compounds from their values. Such descriptors can be produced by a special architecture of neural networks – autoencoders.<sup>41,42</sup> An autoencoder encodes an initial object to its higher-level compressed representation (code, i.e. descriptors), while its associated decoder would have the ability to reconstruct the initial object from its code. The code produced by an autoencoder for a molecule can be considered as a fixed-length vector of “revertible” descriptors, further referred to as “seq2seq” or “latent” descriptors. A simple autoencoder was already used earlier for performing virtual screening based on one-class classification with traditional molecular descriptors.<sup>43</sup> Xu et al. suggested, following the guidelines of the sequence-to-sequence learning model in neural machine translation,<sup>44</sup> to form such “revertible” descriptors by extracting the values of hidden units of RNNs after perception of its entire SMILES string.<sup>45</sup> An important modification of this methodology was recently reported by Winter et al., who designed a neural network that translates between alternative string representations (alternative SMILES, canonical SMILES, InChI) and simultaneously predicts several basic molecular properties by feeding latent descriptors into an additional feed-forward multilayer neural network.<sup>46</sup> It was demonstrated that in this case the continuous data-driven representation of molecules produced by latent descriptors is more adequate for molecular properties modeling, because this network does not focus on syntactic features of a single type of string representations of molecules. A similar idea of using heteroencoders for translating between different SMILES strings as a source of the data-driven descriptors suitable for building QSAR models

was reported by Bjerrum et al.<sup>47</sup> The possibility to use such latent descriptors for generating new molecules in *de novo* design is, however, not discussed in the cited papers. For this purpose, autoencoders (or heteroencoders) should be generative, i.e. should be able to generate new objects. The most popular way to do this is to use “variational autoencoders” (VAE),<sup>48</sup> in which the codes of training objects are fitted to a multidimensional Gaussian probability distribution, which can be sampled to generate new objects. VAEs were proposed by Gómez-Bombarelli et al.<sup>49</sup> for finding new chemical compounds with desired properties using the “data-driven continuous representation”. An adversarial modification of VAE (adversarial autoencoders, AAE),<sup>50</sup> in which an autoencoder is coupled with GANs, was suggested by Blaschke et al.<sup>32</sup> as a general approach to *de novo* design.

Nevertheless, despite the great success in using VAEs and its modifications in various application areas, including generation of new texts, images, sounds, music, and other types of objects, one should be aware of the potential danger of the mechanical transfer of this method to the domain of molecular design. The “property-molecule” relation in the general case is “one-to-many”, because the same property value(s) may be possessed by very dissimilar chemical structures. This results in multimodal statistical distributions of the molecules possessing the desired properties, as it was shown.<sup>51</sup> However, the mathematical theory of VAE, in which any point distribution is approximated by a single Gaussian function, implies the unimodality of this distribution. This contradiction can potentially lead to a sharp deterioration in the results. In any case, the problem of the multimodality of statistical distributions in *de novo* molecular design should be addressed.

In this Article, we put forward a new method of *de novo* molecular design based on combining autoencoder RNNs with Generative Topographic Mapping (GTM). We believe that this method can cope with the problems discussed above for the use of VAEs and RL in molecular design. GTM is a dimensionality reduction and data visualization technique based on variational Bayesian statistics.<sup>52,53</sup> This method has been successfully used in a variety of studies related to the visualization of chemical data, mapping chemical space, analyzing and comparing chemical databases, building classification and regression QSAR models, visualizing activity landscapes, performing inverse QSAR, etc.<sup>51,54–59</sup> The ability to replace VAE with GTM follows from the similarity of underlying mathematical theory of both methods based on variational Bayesian statistics. Unlike VAE, GTM can successfully be used to approximate multimodal distributions, which is very important for performing *de novo* molecular design. In this case, the application of GTM will allow using the strong features and advantages of this approach in the design of new molecules with the desired properties.

This paper starts with the description of our approach, followed by the analysis and verification of the results obtained in a case study.

## 2. METHODS

## 2.1. Molecular Representation and Data Preprocess-

**21 Molecular Representation and Data Preprocess-  
ing.** To be processed by seq2seq models, molecules must be represented as sequences of characters—such as the Simplified Molecular-Input Line-Entry System (SMILES) strings.<sup>22</sup> SMILES were recently used as input for generative autoencoder models, which proved to be able to generate new drug-like hits.<sup>49</sup> Besides, a seq2seq model was applied to

SMILES strings to extract data-driven molecular descriptors.<sup>45</sup> Although in principle one canonical SMILES string is enough for an unambiguous description of molecule, in practice, however, different canonization algorithms produce different canonical representations. We used RDKit<sup>60</sup> canonical SMILES in this study.

Since neural networks can process only numeric data, some initial preprocessing of alphanumeric SMILES strings is required. “One-hot” encoding is a technique that converts categorical variables into arrays of binary values (“1” and “0”) with strictly a single ‘1’ in each of them (because exactly one value in the array is “hot”).<sup>61</sup> Each SMILES string can be represented in this case as a matrix of binary values, in which each row corresponds to an item in the dictionary of valid symbols, each column corresponds to a character in the SMILES string, and ‘1’ at their intersection denotes the correspondence between them ([Figure 1](#)).

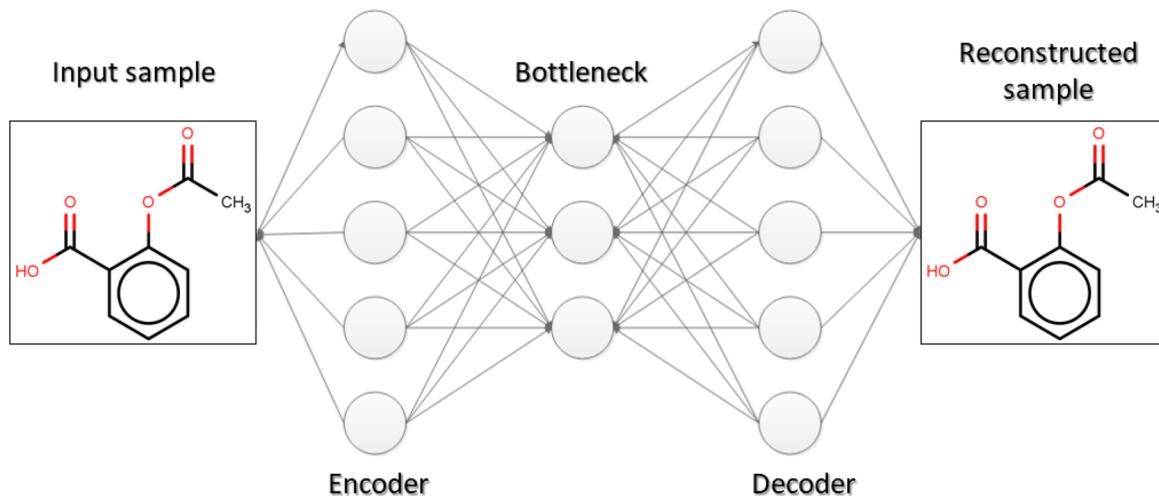
SMILES string														
C	h	a	r	a	c	t	e	r	e	r	o	o	C	
c	0	1	c	(	c	c	c	c	1	)	C			
c	0	0	1	0	1	1	1	1	0	0	0			
1	0	1	0	0	0	0	0	0	1	0	0			
(	0	0	0	0	1	0	0	0	0	0	0			
)	0	0	0	0	0	0	0	0	0	1	0			
o	1	0	0	0	0	0	0	0	0	0	0			
C	0	0	0	0	0	0	0	0	0	0	1			

**Figure 1.** “One-hot” encoding of a SMILES string.

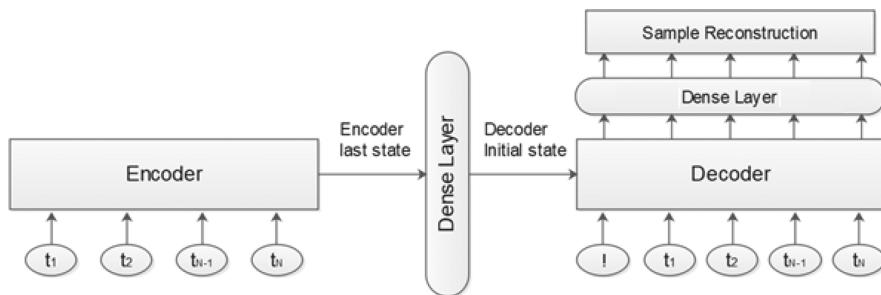
Atomic symbols (tokens) that contain two characters are encoded as a single special character,<sup>62</sup> for example, the chlorine symbol, "Cl", is represented as "X". This significantly simplifies data processing by avoiding the misuse of the "I" character in interpreting and generating SMILES strings.

For each canonical SMILES string two sequences of characters were created: the initial sequence, which is a reversed SMILES string padded to the constant size of 100, and the teacher forcing sequence with the offset by 1 character. Padding to a constant size is needed to allow training neural networks in batch mode. Application of the “one-hot” encoding turns the sequences into numerical matrices with 41 rows (by the number of possible characters in SMILES strings) and 100 columns (by the maximum constant size of SMILES strings after padding).

**2.2. Autoencoders.** An autoencoder is a neural network that can learn to produce an internal representation of an input sample in the form of a vector, called *code*, from which the sample can be reconstructed with the smallest possible error (Figure 2).<sup>41,42</sup> A part of the autoencoder called *encoder* computes the function  $\mathbf{d} = f_\varphi(s)$  for each sample  $s$ , where  $\mathbf{d}$  is the code, called also *latent vector*, which is the internal representation of the sample  $s$  in the *latent space* of the autoencoder. The second part of the autoencoder called *decoder* tries to reconstruct the sample from its code using the function:  $s' = g_\theta(\mathbf{d})$ . The encoder and the decoder are trained jointly by learning the joint parameter set  $(\varphi, \theta)$  to achieve the lowest possible value of the reconstruction loss function  $R(s, s')$ , which is the measure of the discrepancy between the sample  $s$  and its reconstruction  $s'$ .<sup>42</sup> It should be emphasized, however, that not all solutions that can be obtained by minimizing  $R(s, s')$  are of practical value. For example, there is a trivial solution for this minimization problem when the



**Figure 2.** General scheme of the autoencoder neural network architecture.



**Figure 3.** General scheme of a sequence-to-sequence autoencoder.

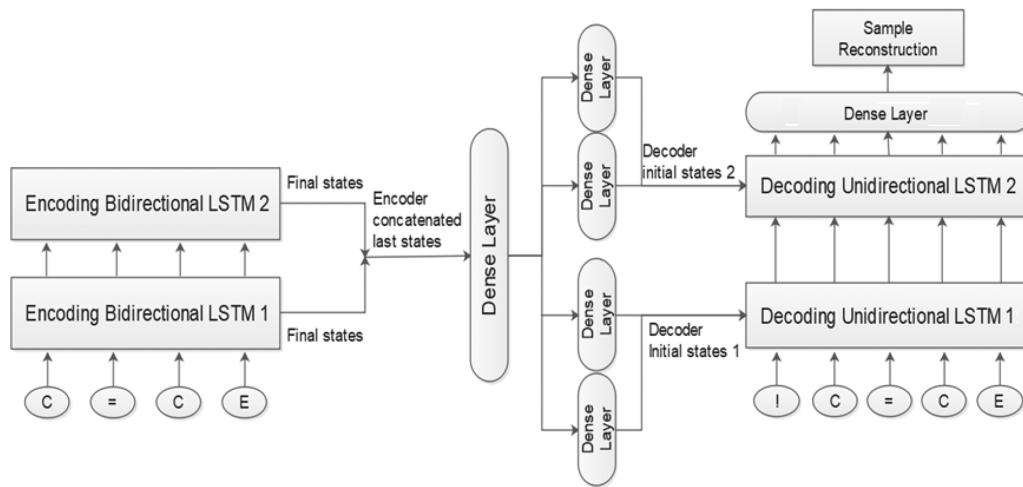
network simply learns to copy  $s$  to  $s'$  without doing anything else. Obviously, the operation of copying objects could be carried out much easier without any machine learning. Therefore, it is always necessary to avoid obtaining such trivial and useless solutions when training an autoencoder. Therefore, along with the task of minimizing the reconstruction loss function  $R(s, s')$ , the task of obtaining internal representations  $d$  that maximally facilitate the solution of additional practically important problems must also be solved.

In most practical applications, autoencoders work with data represented as vectors in a multidimensional space. To avoid the trivial solution, the dimensionality of the autoencoder latent space, which is equal to the number of neurons in the code layer, should be lower than the dimensionality of the data. The autoencoder performs in this case data compression from  $s$  to  $d$  and decompression from  $d$  to  $s'$ . If the dimensionality of the latent space is equal or higher than some “intrinsic” data dimensionality, the decompression is lossless. Otherwise, the code layer with too small number of neurons becomes the information “bottleneck” of the network, and the loss of information becomes inevitable. The neural network tries in this case to minimize the loss of the information that is important for data reconstruction by performing analysis of data structure, revealing hidden patterns, disentangling hidden factors, and performing noise-signal separation.<sup>42</sup> A new data representation formed in this case in the code layer of the autoencoder can be very useful for further data processing. A similar effect can also be achieved by introducing regularization terms into the minimized function without reducing the actual number of neurons in the code layer.<sup>63</sup> In the latter case, the

effective dimension of the latent space of the autoencoder decreases.

Autoencoders based on neural networks with special architecture can also be used to process complex discrete structures with a variable number of elements, such as graphs and sequences of characters. In this case, the formation of vectors in the code layer can be considered as an embedding of such structures into the Euclidean space of fixed dimensionality. In chemoinformatics, the latent vectors  $d$  are viewed in this case as “revertible” data-driven molecular descriptors, which form a continuous representation of discrete chemical objects, e.g. molecules and chemical reactions.

**2.3. Sequence-to-Sequence Models.** The autoencoders used by us in this study belong to the family of sequence-to-sequence (seq2seq) encoders-decoders, which first encode an input sequence (e.g., a sequence of characters) into a latent vector of fixed size (a code), and then decodes it to an output sequence.<sup>44</sup> This architecture has proven to be very efficient in natural language processing tasks, such as English-French translation<sup>44</sup> and conversational modeling.<sup>64</sup> If such an encoder-decoder learns to reproduce the input sequences at its output, it is called a seq2seq autoencoder. A general scheme of the seq2seq autoencoders is represented in Figure 3.<sup>65</sup> An input sequence is fed to the encoder based on a recurrent neural network (RNN). The encoder updates its internal state after reading and processing each element of the input sequence, so the last state of the encoder will contain information about the whole input sequence. This state is then passed to the decoder RNN through a fully connected layer, which serves as an information bottleneck and recombines the state into the latent vector (code). This latent



**Figure 4.** Architecture of the sequence-to-sequence autoencoder used in this study.

vector is used as an initial state for the decoder, which carries out reconstruction of the sequence. At the first time step, a dummy input character is fed to the decoder. At each next time step, the expected target sequence character at the previous time step is fed as an input to the decoder. This technique is widely used in sequence-to-sequence learning and called “teacher forcing”.<sup>66</sup> The outputs of the decoder are passed to the fully connected layer with the “softmax” activation function at every time step to match the size of the target sequence. After the model converges, the outputs of the dense layer between the encoder and the decoder act as a learned representation of the sequence, its embedding into the latent space of the autoencoder.

In this study, we used a variation of the SMILES-based seq2seq autoencoder architecture introduced by Xu et al. for seq2seq fingerprint extraction.<sup>45</sup> Molecules were represented as sequences of one-hot encoded SMILES characters and fed to the encoder. Sequences were padded with a special end-symbol “E” at the end to a constant length. This padding enables network training in batch mode and acts as a stop symbol when new sequences are being generated. Besides, the dummy symbol “!” was added to the beginning of each input sequence to enable the teacher forcing by offsetting the input from the target sequence by 1 character step.

The encoder in our implementation contains two Bidirectional Long Short-Term Memory (LSTM) layers (Figure 4).<sup>67,68</sup> While the ordinary LSTM networks are only able to utilize information from the previous context in the sequence learning, the Bidirectional LSTM<sup>68</sup> can also take advantage of the future context, by processing the sequences in both directions (using two isolated hidden layers connected to the same output). The decoder is composed of two ordinary LSTM layers with a same number of neurons as the encoder. At the end of the sequence, final cell states and hidden states of both layers are concatenated and passed to a dense layer. The outputs of this layer form the latent vector for the input sequence. Subsequently, it is decoded by four parallel dense layers to form the initial cell and hidden states for each LSTM layer of the decoder. The number of nodes in the bottleneck dense layer is lower than the dimensionality of the LSTM states to avoid obtaining trivial solutions. Application of each nonlinear activation function was followed by Batch Normalization (BN),<sup>69</sup> which was shown to accelerate training by reducing internal covariance shift. The code implementing this

architecture of the autoencoder was written using the Keras deep-learning library.<sup>70</sup>

The autoencoder was trained in the batch mode, where batches of “one-hot”-encoded sequences (initial, target, and teacher forcing) were generated on-the-fly from training-set SMILES strings. The Adam optimizer was used for training, initial learning rate was set to 0.005, and batch size was set to 256 samples per batch. The learning rate was reduced during training if there were no improvement in the validation loss for two epochs. The training was terminated if no improvements in validation-set reconstruction accuracy were observed for 5 epochs. Then, the final reconstruction accuracy was estimated using a separate held-out set composed of 10000 molecules.

**2.4. Generative Topographic Mapping.** Generative Topographic Mapping (GTM) was introduced by C. Bishop as probabilistic counterpart of Self-Organizing Maps (SOM) based on Bayesian learning.<sup>52,53</sup> It has proven to be an effective tool for chemical space analysis,<sup>57–59,71–75</sup> comparing chemical databases,<sup>54</sup> building classification<sup>56,58,59,73</sup> and regression<sup>55,76</sup> models, building and analyzing structure–activity landscapes,<sup>55,58,59,76</sup> and solving the “inverse” QSAR problem.<sup>51</sup>

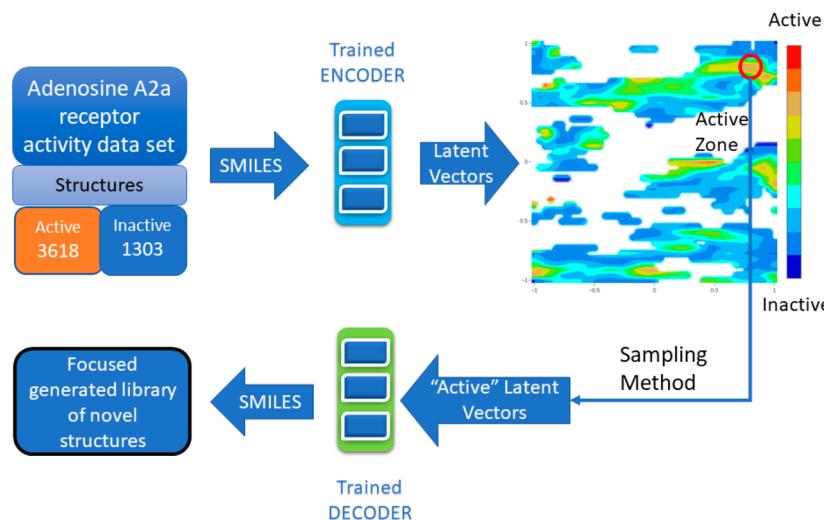
The GTM algorithm operates by embedding a nonlinear two-dimensional manifold into a  $D$ -dimensional descriptor space. First, a squared grid with  $K$  nodes is created in a two-dimensional GTM latent space, called also a *map*, in which the position of the  $k$ -th node of the grid is defined by its 2D coordinates  $x_k = (l_x, l_y)$ . Each node  $x_k$  is mapped to its image  $y_k$  on the manifold using a nonlinear function  $y(x; W)$ , which is approximated as a linear combination of several predefined Radial Basis Functions (RBF)  $\varphi(x)$

$$y(x; W) = W\varphi(x)$$

where  $W$  is a matrix of the tunable parameters that define the manifold. Each point  $y_k$  serves as a center of a multidimensional isotropic Gaussian function for approximating the distribution of data points (e.g., molecules) around it

$$p(\mathbf{d}|k) = \left( \frac{\beta}{2\pi} \right)^{D/2} \exp \left\{ -\frac{\beta}{2} \|\mathbf{d} - y(x_k, W)\|^2 \right\}$$

where  $\beta$  is the inverse variance of this distribution. Sampling from it allows generating new data points, e.g. molecules in the descriptor space. GTM implies that all data points have nonzero probability to be generated from the image of any



**Figure 5.** Generation of the focused library of novel active structures of A2a ligands using the GTM map and the encoder/decoder parts of trained autoencoder.

node and hence be mapped to any node on the map, which is “responsible” for it. This probability is called responsibility  $R_{nk}$ ,  $k$  being the index of the node, and  $n$  being the index of the data point  $d_n$ . It can be calculated using the Bayes’ theorem:

$$R_{nk} = p(k|d_n) = \frac{\exp\left\{ \frac{-\beta}{2} \| d_n - y(x_k, W) \|^2 \right\}}{\sum_{k'=1}^K \exp\left\{ \frac{-\beta}{2} \| d_n - y(x_k, W) \|^2 \right\}}$$

The compliance of the GTM model with data is measured by  $L$ , log(likelihood), calculated as the logarithm of the probability with which the data could be generated using the model, which is a function of two parameters:  $W$  and  $\beta$

$$L(W, \beta) = \sum_{n=1}^N \log\left( \frac{1}{K} \sum_{k=1}^K \exp\left\{ \frac{-\beta}{2} \| d_n - y(x_k, W) \|^2 \right\} \right)$$

The optimal values of these parameters can be found by maximizing this function for fixed set of hyperparameters using a special modification of the EM algorithm.<sup>52</sup> The aforementioned set of the hyperparameters includes the number of grid nodes,  $K$ , the number and the half-width of the basis functions,  $\varphi(x)$ , and a regularization coefficient. The optimal values of these hyperparameters, as well as optimal descriptor sets, can be found by maximizing a “usefulness” score of GTM models, such as an average predictive performance of regression or classification models based on them.<sup>59,76</sup> The simplest way to deduce such models from GTM models is to use so-called *activity landscapes* as support for regression and, respectively, *class landscapes* supporting classification models.<sup>55,59,77</sup> Besides visualization, such landscapes can be used for predicting the activity values or class labels for new molecules by projecting their descriptors onto the GTM and taking the local average property as predicted value.<sup>55,77</sup> Several benchmarking studies performed on different data sets (biological activities, aqueous solubility, stability of metal complexes, pharmacokinetic parameters)<sup>55,56,59,73</sup> demonstrated that GTM as a regression and classification tool is competitive with the most popular machine-learning methods like Random Forest, Naïve Bayes, and SVM. It has also been demonstrated that GTM separates different activity classes

from the DUD data set much better than PCA and Kohonen maps.<sup>73</sup>

Activity landscapes are typically visualized by associating coloring each map point according to a spectrum matching the mapped property range, while the local transparency (alpha channel) is modulated to reflect data density (cumulated responsibility over training set compounds at that point). This allows defining both the model applicability domain and revealing the zones highly enriched with active molecules. Generating new molecules within the latter zones leads to production of focused virtual libraries.

In this study, the GTM technology was used to create maps using the latent vectors  $\mathbf{d}$  of the above-discussed SMILES-based autoencoder as “revertible” molecular descriptors. The strategy used to create “universal” maps<sup>59</sup> based on classical fragment descriptors has been re-enacted using the latent vectors instead. The initial descriptor space being fixed, the evolutionary algorithm only searched through the space of GTM hyperparameters in order to create manifolds with optimal propensity to “host” predictive fuzzy class landscapes for 236 randomly selected ChEMBL activities. For a given manifold, the quality of the predictive fuzzy class landscape of every target is estimated by the cross-validated balanced accuracy  $BA_{CV}$ . Two thirds of the associated ligand set are projected on the manifold and serve to “color” the landscape by the relative density of actives vs inactives residing at each map point. Then, the kept-out tier is projected *a posteriori*, to read predicted activity class assignments of its ligands from the landscape. The three tiers are iteratively kept out, and then the procedure is repeated four more times, with reshuffling of the ligand set (varying the way in which ligands are being regrouped into the cross-validation tiers).  $BA_{CV}$  is estimated by comparing actual and map-read activity labels for kept-out compounds. The top map is the manifolds allowing for a maximal mean  $\langle BA_{CV} \rangle$  over all the 236 considered biological activities. It was then challenged to also host predictive landscapes of the remaining 618–236 structure–activity class series, associated with targets that were in part completely unrelated to the 236 “selection” sets.

The calculations were performed using the ISIDA/GTM package (<http://infochim.u-strasbg.fr/spip.php?rubrique41>).

Its evaluation version is available from the authors upon request.

**2.5. Structure Generation.** Given a latent vector, it can be interpreted by the trained decoder to produce a SMILES string for a new molecule. Since the GTM activity landscapes allows us to locate zones enriched with molecules with properties of interest, we can generate new latent vectors for them and, hence, the SMILES strings of novel molecules with desired properties (Figure 5). Taking into account good predictive performance of GTM, one can expect that new structures generated from the zones populated by highly active molecules with reasonable probability will also be active.

In this study, we have generated two libraries of putative A2a ligands, using two different sampling methods of the latent space – Genetic Algorithm (GA-sampling) and GTM node-based sampling ( $\beta$ -sampling). Several properties of the libraries, such as synthetic accessibility and internal diversity of compounds, were assessed and compared with corresponding properties of the ChEMBL23 database.

Each of these sampling algorithms generates new latent vectors that might correspond to active molecules. These vectors are decoded into the SMILES strings, which are then checked for validity. The percent of valid structures was estimated using the ChemAxon's structure checker with default settings.

For each valid chemical structure, the Synthetic Accessibility score (SA) was estimated according to P. Ertl's method<sup>78</sup> as implemented in RDKit. The SA score indicates how difficult it would be to synthesize a given compound, 1 being very easy and 10—almost impossible. The ChemAxon's Structure Checker was then used to discard molecules with reactive or “unwanted” groups. The remaining compounds were collected as potential A2a ligand candidates.

**2.5.1. Genetic Algorithm-Based Sampling (GA-Sampling).** The GA-sampling explores the latent space by means of the genetic algorithm with the latent-space vectors coded as chromosomes. The fitness function for the GA algorithm was taken to consist of several terms. Its first term verifies the compliance to the applicability domain (AD) of the A2a GTM landscape, including two aspects. First, manifold-based log-(likelihood), which evaluates whether the latent space point encoded by the chromosome is close to the GTM manifold (at least 5% of frame set compounds must be further away from the manifold, or otherwise the current point is considered an “outlier” and its fitness evaluation stops, returning a default minimal score). Second, it is verified whether the projection of the latent point on the map matches an area populated (with sufficient density) by A2A training set compounds, in order to ensure a meaningful prediction of its probability to be active (default density threshold of the GTM tool being applied). If the above closeness criteria are met, the second term is responsible for checking whether the SMILES strings decoded from the latent vector represent valid molecules, as assessed using RDKit. Should the second check point be passed (otherwise, default minimal fitness returned), the third term evaluates probability  $P_{\text{A}2\text{A}}$  of the sample to be of desired class (A2A active) according to the activity class landscape zone into which it is projected. The last two terms of the fitness score are the synthetic accessibility score SA and, respectively, the number UNW of “unwanted” groups found by the ChemAxon structure checker in the decoded molecules. By trial and error, the fitness score  $Fit$  was empirically defined such as to increase with  $P_{\text{A}2\text{A}}$ , all while being penalized with increasing SA scores

and abruptly decreasing with the number of detected unwanted groups:  $Fit = P_{\text{A}2\text{A}}(1 - \text{SA}/100)e^{-\text{UNW}}$ . Following this fitness score, the evolutionary simulation was seen to progress toward latent space zones that are in the well-sampled neighborhood of the manifold, project into GTM areas predominantly populated by A2A actives, have a low SA score, and are void of unwanted groups.

**2.5.2. Random Normal Node-Based Sampling ( $\beta$ -Sampling).** This is a normal sampling of the initial latent space using coordinates of the GTM nodes as the mean and the GTM parameter  $1/\beta$  as the variance. Since this method can be applied to any node on the map, only the top 8 active nodes of the A2A landscape were selected for sampling. The sampled latent vectors were decoded, and only SMILES strings corresponding to valid molecules were selected.

**2.5.3. Scaffold Analysis.** The RDKit software<sup>60</sup> was used to extract scaffolds and frameworks from chemical structures represented by SMILES strings.

**3.6. Pharmacophore Screening.** Using LigandScout 4.2.1, we have analyzed several PDB structures of the A2A receptor with cocrystallized ligands: 3EMI, 3UZC, 3UZA, SUIG, SOLH, SIUA. Then key pharmacophore features were identified for every structure, and corresponding pharmacophore models were created. The pharmacophores were aligned, and a single consensus pharmacophore (containing only the common features) was constructed.

**3.7. Candidate Validation by Docking.** Two different docking approaches were applied: the in-house program S4MPLE,<sup>79–81</sup> a general tool which handles docking simulations as a special case of the wider range of conformational sampling problems it may tackle, versus the state-of-art FlexX<sup>82</sup> docking software licensed by BioSolveIT. A subset of randomly selected 1900 ligands of the herein extracted CHEMBL251 (A2a) structure–activity set served as a benchmark in order to verify whether either of these programs is able to effectively discriminate between A2a “actives” and “inactives”. If the actives are indeed assigned more favorable docking scores, this is reflected by an increased area-under-the-curve (AUC) value of the resulting Receiver Operating Characteristic (ROC) curve. Both tools were used in default configurations.

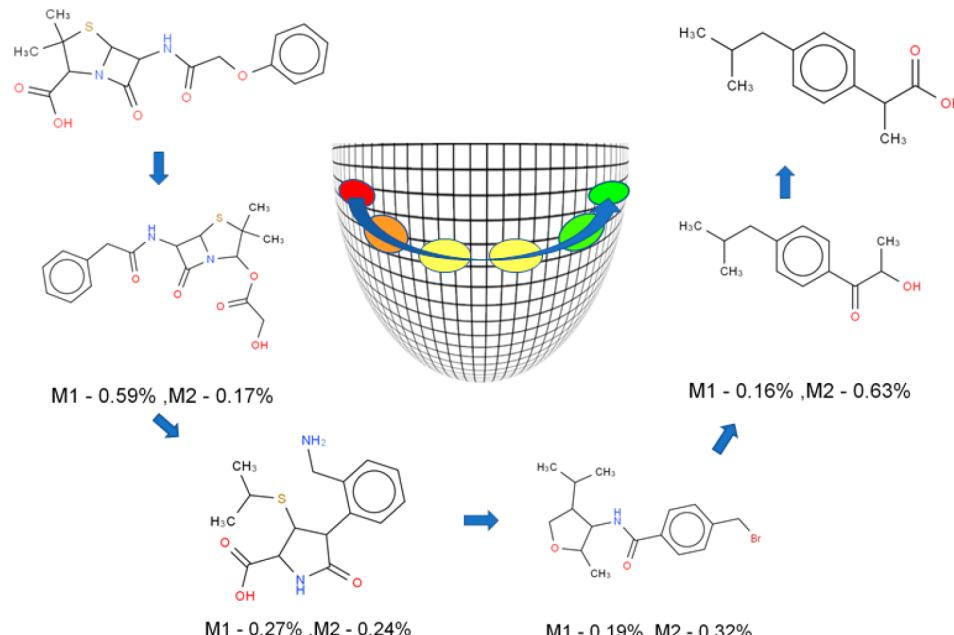
**3.7.1. Protein Preparation.** LeadIt 2.3.2 (BioSolveIT) tools were used to prepare the 2YDO structure of the A2a receptor from the Protein Data Bank.<sup>83</sup> The standard workflow for protein site curation was followed, all water molecules were removed, and amino acid side chain protonation states were fixed.

**3.7.2. Ligand Preparation.** The 1900 ChEMBL251 ligands selected for docking were subjected to an automated conversion to protonated initial 3D structures, by means of an in-house tool developed on the basis of the ChemAxon API. The tool relies on the tautomer<sup>84</sup> and pK<sub>a</sub> plugins<sup>85</sup> to generate the most probable microspecies of the expected main tautomer. Explicit hydrogen atoms were added, and a single conformer was then generated using the conformer plugin. Eventually, the charge plugin<sup>86</sup> was used to assign Gasteiger charges to all atoms in this structure (to be used by S4MPLE but not by FlexX). Last, the tool detected flexible rings and proposed the single bonds to be formally “broken” in order to enable intracyclic torsional axes to be driven by S4MPLE (macrocyclic sampling was, by contrast, disabled in FlexX, as its default setting prone). Next, antechamber<sup>87</sup> and other utilities, as called by GAFF pilot scripts, were used to assign

**Table 1.** SMILES Reconstruction Accuracy (ACC) and Percentage of Valid Generated SMILES Strings (VAL) Provided by Different Autoencoder Architectures

LSTM type	enc\dec layers	units in encoder	bottleneck layer	units in decoder	ACC, %	VAL, %
unidirectional	2	256 + 256 <sup>a</sup>	128	256 + 256 <sup>a</sup>	95.80	96.5
bidirectional	2	(128 + 128) + (128 + 128) <sup>b</sup>	256	256 + 256 <sup>a</sup>	99.71	99.65

<sup>a</sup>Two layers with 256 units in each of them. <sup>b</sup>Two layers each consisting of two sublayers with 128 units in each of them (see description in text).



**Figure 6.** Interpolation between the penicillin V and the ibuprofen molecules in the latent space. When the smallest distance path from one molecule to another is sampled, new molecules between them can be discovered. M1 – Tanimoto similarity of the given decoded structure to penicillin, M2 – to ibuprofen.

GAFF<sup>88</sup> ligand types and to automatically set associated FF parameters to the internal coordinates found in the ligands. The FF types and Gasteiger charges were added as data S4MPLE-readable fields to the MDL sd file used to store the proposed initial conformer of the ligand. The same sd files were used by docking with FlexX, which however ignores the S4MPLE-specific parameters and uses its internal parameters for docking.

**3.7.3. Active Site Specifications.** The docking program S4MPLE uses a predefined cutoff of 12 Å for nonbonded interactions. Therefore, a selection of relevant residues that have at least one atom at less than 10 Å from any of the cocrystallized 2YOD ligand was used as site model for S4MPLE calculations. Protein atoms were explicitly declared as fixed (by default, all degrees of freedom are considered in S4MPLE). Moreover, S4MPLE requires the user-specified input of “hot spots”, which are used for random prepositioning of the ligand into the active site. These were site atoms seen to make contacts to the cocrystallized PDB ligand, including the aromatic ring of Phe168 and His250, the hydrophobic pocket defined by Leu249, plus the key hydrogen bond donor/acceptor Asn253. Their choice has no impact on the docking energy function (they are not used to tether the ligand).

For FlexX, the active site was automatically defined by the subset of protein residues interacting with the adenosine ligand present in 2YDO according to the procedure implemented in LeadIt.

**3.7.4. Docking Protocols.** Docking and scoring with FlexX was driven by the batch file dock\_list taken from the program

distribution. The only nondefault option it includes is a user-imposed pose optimization of 500 steps. Docking with S4MPLE followed the published<sup>89</sup> standard protocol. Therefore, the docking score  $\Delta E$  for the current ligand can be directly estimated as the energy difference between the lowest energy levels of bound and respectively free ligand geometries,  $\min\langle E_i \rangle_{\text{ligand@site}} - \min\langle E_i \rangle_{\text{ligand}}$ . Based on benchmarking results, S4MPLE has been used to dock a library of 394 *de novo* candidates that successfully passed the pharmacophore matching test. Their docking scores were compared to the scores of known A2a actives and inactives from the benchmark set, respectively.

### 3. RESULTS AND DISCUSSION

**3.1. Data Preparation.** The ChEMBL23 database was used both as source of SMILES strings for autoencoder and labeled data for GTM landscapes and framesets. Before training, molecules from ChEMBL23 were standardized as already described by Klimenko et al.<sup>59</sup> This resulted in 1514188 unique molecules. For the autoencoder training, an ensemble of “one-hot”-encoded canonical SMILES strings was divided into the training set with 1211352 molecules and the validation set with 302836 molecules, from which 10000 molecules were drawn to perform an unbiased test of reconstruction accuracy after training.

The adenosine A2a receptor (CHEMBL251) was chosen as the target for this *de novo* design simulation. The activity cutoff for A2a was set to 50 nM. An uncertainty corridor from 50 to 500 nM was allowed, and molecules with  $K_i$  inside this range

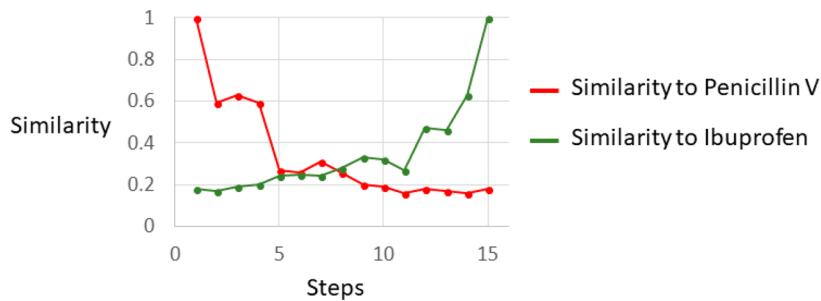


Figure 7. Similarity of the two terminal compounds to molecules generated along the path in the latent space from penicillin V to ibuprofen.

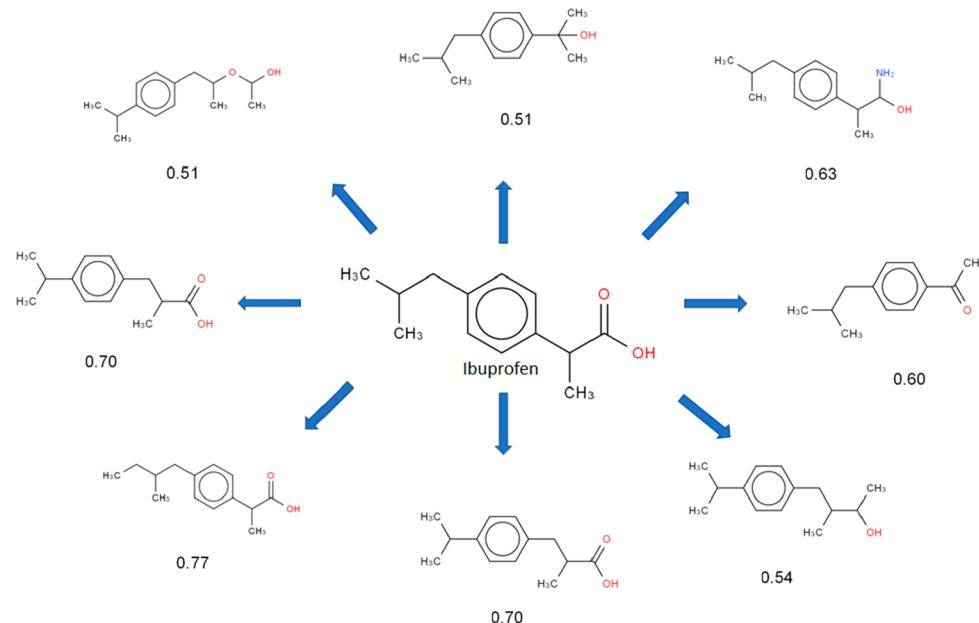


Figure 8. Molecules generated by perturbing the latent vector representation of ibuprofen using random values sampled from the normal distribution with very small standard deviation. A number below each structure indicates the values of the Tanimoto coefficients with respect to ibuprofen.

were discarded. Molecules with  $K_i > 500$  nM were treated as inactives. Further 617 ChEMBL ligand sets, each associated with a distinct *H. sapiens* single protein with available  $K_i$  or  $IC_{50}$  values, were extracted and subjected to a similar conversion of activity values into active/inactive labels, for a more general assessment of the predictive power of latent descriptors, beyond the current design problem.

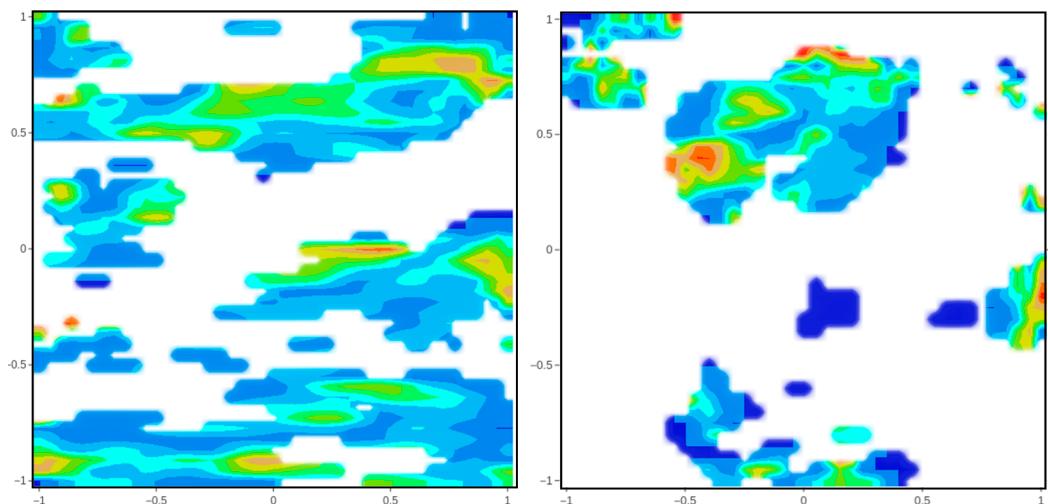
**3.2. Autoencoder Architectures and Reconstruction Errors.** Different architectures of the neural sequence-to-sequence autoencoders for SMILES string were developed and tested, see Table 1. Reconstruction accuracies were accessed and compared. We have found out that bidirectional LSTM encoders demonstrate the highest SMILES reconstruction accuracies (ACC) and the optimal architectures should contain 2 hidden layers in both encoder and decoder. Besides, it turned out that Batch Normalization is crucial for reaching the highest reconstruction rates in a reasonable time of training (<10 h on Nvidia GTX1080) for this type of autoencoders. High reconstruction accuracies achieved on the test set imply that the autoencoder is well generalized and can effectively be used for representing most of the SMILES strings of ChEMBL23 molecules.

Latent descriptors provided by the trained autoencoder represent a relevant chemical space, in which it is possible to simulate “walks” from one point (chemical structure) to

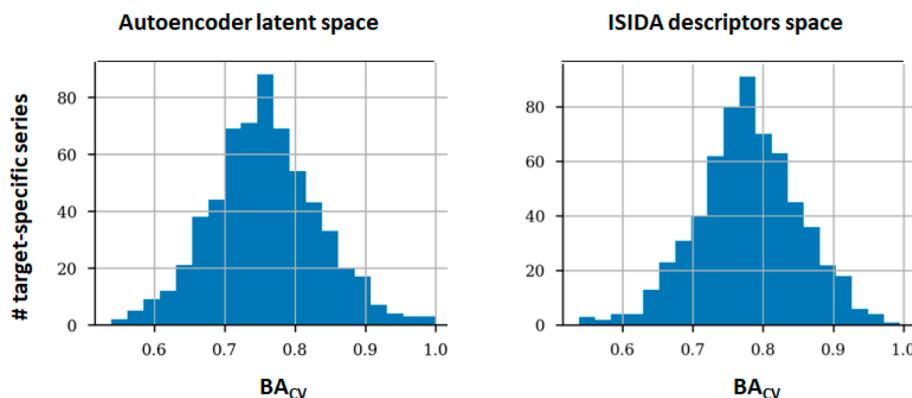
another by visiting interpolated latent space points which translate to hybrid structures “mixing” features of departure and arrival compound. We simulated a “walk” in the latent vector space, from penicillin V to ibuprofen, see Figure 6. Latent space points along the path were sampled and decoded into corresponding SMILES strings. Out of the 22 sampled latent points, 19 corresponded to valid molecules. This simulation is a chemical version of the popular “morphing” of one portrait into another in image processing, so the intermediate molecules can be considered in this sense as “imorph frames” between penicillin and ibuprofen.

We have tracked the similarity (Tanimoto coefficient over all pairs of molecules using ECFC4-like Morgan circular fingerprint hashed to 1024-bit vectors as implemented in RDKit) of each structure picked along the path from penicillin V to the ibuprofen with respect to both of these molecules. Figure 7 indicates that when moving from the penicillin to the ibuprofen the similarity with respect to the penicillin continuously decreases, while the similarity to the ibuprofen decreases. This test proves that in the latent space similar molecules are indeed located close to each other.

We have also checked whether minor random changes of latent vectors result in minor structural changes in molecular structures. Eight chemical structures generated by perturbing the latent vector representation of ibuprofen using random



**Figure 9.** GTM class landscapes based on the latent vectors (left) compared to one example of a “universal” map based on ISIDA fragment descriptors (right). The blue zones on the maps indicate mostly inactive compounds, while the red zones indicate mostly active compounds.



**Figure 10.** Comparison of the  $BA_{cv}$  (Cross-Validated Balanced Accuracy) histograms for classification models built on 617 ChEMBL target series using latent vector-based GTM (on the left) and the “universal” map 1 based on ISIDA fragment descriptors (on the right).

values sampled from the normal distribution with very small standard deviation are shown in Figure 8, along with the values of the Tanimoto coefficients for them with respect to ibuprofen. One can see that all eight molecules are indeed rather similar to ibuprofen, with the average value of the Tanimoto coefficient being 0.62.

The results of the above tests indicate a good neighborhood behavior of the space, determined by latent vectors, and the possibility of using it as a continuous representation of molecules both to solve the problem of optimizing the target property and to generate focused libraries of compounds with the desired properties.

**3.3. GTM Built on Latent Descriptors.** Using the GTM methodology, we have built “universal maps” for the same sets of ChEMBL compounds using both (a) the latent vectors produced by the autoencoder with the chosen architecture and (b) standard ISIDA fragment descriptors<sup>90</sup> successfully used in most previous applications concerning the use of GTM for chemical data analysis. Then the same set of A2a binders CHEMBL251 was used to color the maps to produce the class activity landscapes. The activity landscape for the autoencoder latent vectors is depicted at the left side of Figure 10, whereas one of the analogous activity landscapes built using ISIDA fragment descriptors is given at the right side of Figure 9. Both descriptor types appear to produce landscapes with com-

parable predictive performance—the cross-validated balanced accuracy,  $BA_{cv}$ , values are 0.72 for the latent vector map versus 0.68–0.76, depending on the specific ISIDA “universal” map based on fragment descriptors. Note that the target of interest, A2A (CHEMBL251), is an “external” set, which was never used for map selection (neither for latent-vector nor for ISIDA descriptor maps). The  $BA_{cv}$  values for the remaining 617 ChEMBL activity sets are also distributed very similarly, as indicated in Figure 10. This indicates that the latent vectors are competitive with respect to ISIDA molecular descriptors for building structure–activity models.

As can be seen from the comparison of the two landscapes shown in Figure 9, when using latent vectors instead of fragment descriptors, a much larger part of the map turns out to be colored, which makes the map much more informative. Perhaps this is because the descriptors learned from data are generally better suited for describing data distribution, because some of the details of this distribution are implicitly embedded in the descriptors themselves.

**3.4. Generation of the Focused Libraries of A2a-Receptor Binders.** The process of generating focused schematic libraries described above is shown in Figure 5. Projection of the generated compounds back on the A2A landscape based on the GTM map built using autoencoder

latent vectors indicates that the generated structures expectedly fall into the selected active zone on the map.

Assessment of the properties of the generated focused libraries for the A2a receptor has shown that the compounds generated using the genetic algorithm (GA-sampling) are significantly easier accessible synthetically than the  $\beta$ -sampled ones, the former being almost equal to the ChEMBL23 baseline (see Table 2), which can be explained by the fact that the fitness function of the genetic algorithm explicitly favored low SA scores (i.e., more synthetically accessible).

**Table 2. Comparison of Synthetic Accessibility and Diversity of the Compounds in Generated Libraries vs Compounds from the ChEMBL23 Data Set<sup>a</sup>**

	GA-sampling	$\beta$ -sampling	ChEMBL23 baseline
average SA score	2.94	4.59	2.99
average diversity	0.78	0.85	0.88

<sup>a</sup>Average diversity refers to the Soergel distance (1-Tanimoto coefficient) over all pairs of molecules using an ECFC4-like Morgan circular fingerprint hashed to 1024-bit vectors as implemented in RDKit.

Besides synthetic accessibility, it is also important to assess the diversity of the generated focused libraries, because for discovering new drugs by screening the focused libraries of generated compounds it is necessary to be able to obtain new chemotypes with possible new modes of action. Since molecules were generated to cover A2a active zones of the chemical space, the increase in the average pairwise similarity in comparison with ChEMBL baseline is completely expected. However, as it follows from Table 2, the library generated by  $\beta$ -sampling is more diverse than the other one produced by genetic algorithm and almost as diverse as the compounds extracted randomly from ChEMBL23. Thus, as follows from Table 2, the synthetic availability and diversity of the generated focused libraries is comparable to the similar characteristics of compounds from ChEMBL, which indicates the possibility of

using them instead of the sets of known compounds in the process of virtual screening.

**3.5. Validation of the Generated Compounds Using Structure-Based Methods.** Pending real synthesis and experimental validation, we have applied alternative chemoinformatics approaches that do not rely on machine-learned models (pharmacophore screening and docking) to validate that the generated compounds could be binders to the adenosine A2A receptor.

**3.5.1. Pharmacophore Screening.** The structure-based pharmacophore model built by us for A2A binders includes 4 features that are crucial for the activity and are present in all cocrystallized A2A ligands (see Figure 11 for a protein–ligand complex overlapped with the pharmacophore features):

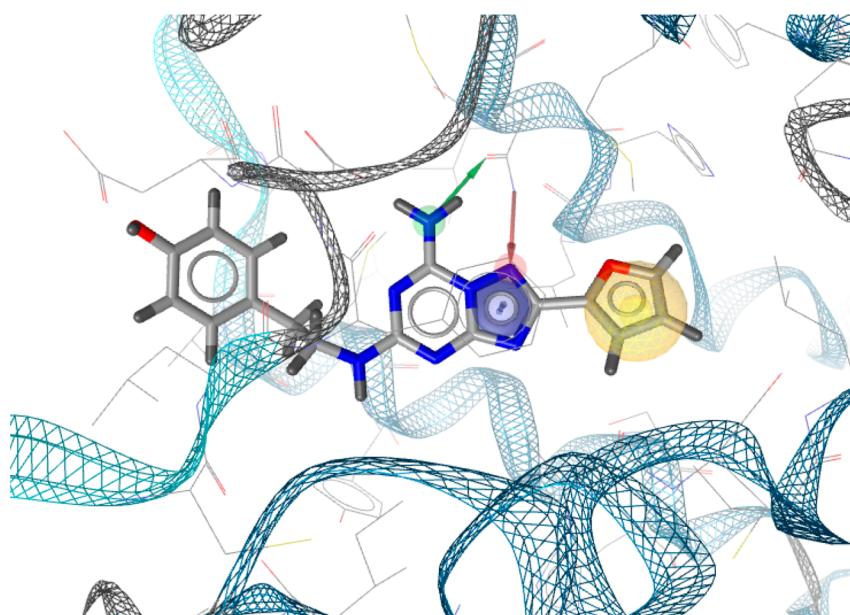
1. hydrogen-bond donor interacting with ASN253A;
2. acceptor interacting with ASN253A;
3. aromatic ring interacting with PHE168A;
4. hydrophobic group interacting with the hydrophobic part of the binding pocket (LEU85A, LEU249A, MET177A, VAL84A).

We have observed that compounds from the focused libraries are approximately three times more likely to comply with this pharmacophore model, as compared to the compounds selected randomly from the ChEMBL database (see Table 3). This suggests that developed workflow could produce focused libraries enriched with compounds potentially possessing the desired biological activity.

**Table 3. Percentage of Molecules Complying with the Developed Pharmacophore**

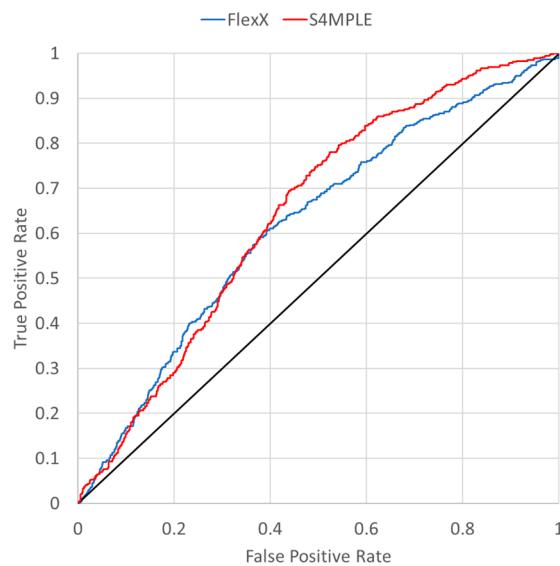
parameter	source of molecules	remarks	
pharmacophore hit rate, in %	$\beta$ -sampling	GA-sampling	ChEMBL

**3.5.2. Docking of Ligands to Protein.** The Receiver Operating Characteristic (ROC) curves for our docking experiments for the benchmark subset of 1900 ChEMBL



**Figure 11.** Binding site of the A2a receptor cocrystallized with ligand (3EML PDB structure) overlapped with the developed pharmacophore filter.

A2a binders are presented in Figure 12. As can be seen, both FlexX and S4MPLE are better-than-random selectors of active



**Figure 12.** ROC curves for docking experiments with the benchmark set with 1900 compounds with annotated A2a activity selected at random from ChEMBL.

A2a ligands. However, their performance is not high. According to the Area Under the Curve (AUC), S4MPLE ( $AUC = 0.64$ ) slightly outperforms FlexX ( $AUC = 0.62$ ). We have also found that S4MPLE reproduces correct binding modes of ligands in the crystal structures 2YDO, 4EIY, 3EML, SIU4, and 2YDV but fails with the highly flexible ligand in 3QAK, for which the standard 500 evolutionary generations are clearly not sufficient to discover its native pose.

Since protein–ligand docking is a time-consuming process, only a subset of 394 compounds produced by the GA-sampling method and passed the pharmacophore matching tests were docked using the S4MPLE program. The GA-sampling was chosen because of the higher pharmacophore hit rate and better synthetic accessibility in comparison with the  $\beta$ -sampling. The S4MPLE docking method was chosen because of the higher values of AUC in the above-discussed benchmarking tests.

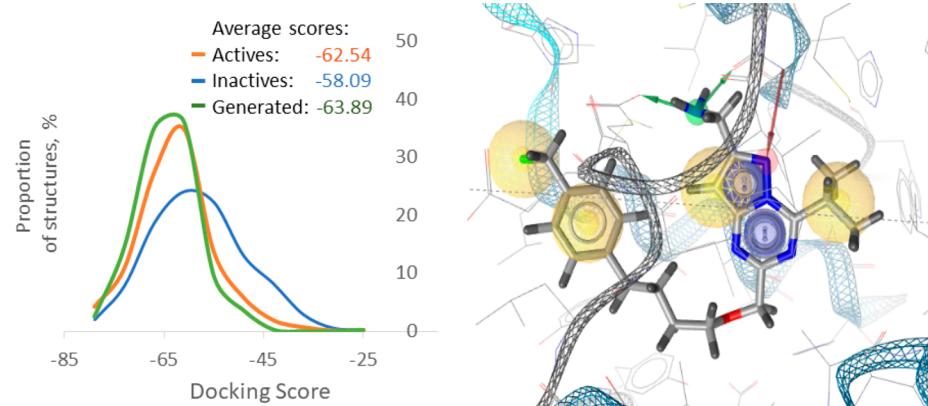
The results of the docking studies given in Figure 13 (at left) show that the average docking score of the generated compounds ( $-63.89$ ) is slightly better than the average score of the active molecules from ChEMBL23 ( $-62.54$ ), which means that the generated library is enriched with potential A2a binders. Visual pose analysis of the top-ranked generated compounds shows the interaction pattern (with ASN253, PHE168A and hydrophobic parts of the pocket) is similar to that in the PDB structures of the complexes of the A2a receptors with the active ligands used by us for developing the pharmacophore model.

With the help of RDKit software<sup>60</sup> 320 Bemis-Murcko scaffolds and 203 frameworks were generated for a docked subset of 394 compounds. Comparison with the ChEMBL251 (A2a) set used for identification of the sampled area on GTM shows that all generated molecules, scaffolds, and 197 frameworks were new which demonstrates a high *de novo* potential of the given methodology.

#### 4. CONCLUSIONS

We have developed a method of *de novo* design of biologically active molecules based on the autoencoder sequence-to-sequence neural network and Generative Topographic Mapping. The latter served to select an area in the space of autoencoder latent variables which sampling results in generation of a focused library of compounds with desirable activities. We believe that GTM is a good choice for such constrained structures generation for the following reasons: (i) GTM is a generative method which allows for the automatic creation of new objects residing in selected areas in the 2D space, (ii) due to its prediction potency the generated library is enriched with compounds possessing desired activities, and (iii) it allows for the visualization of activity landscapes which facilitates taking decision concerning the choice of the sampled region in the chemical space. At the same time, a benchmarking study comparing performance of GTM to generate the desired focused library with some other generative dimensionality reduction methods (e.g., different variants of Variational Autoencoder) could be useful.

Encoding of SMILES strings into a latent space of about 100 dimensions has been proven to occur with virtually no information loss (excellent SMILES reconstruction rates). Furthermore, this work showed that the obtained “latent” vectors are molecular descriptors on par with any chemical



**Figure 13.** (Left) Histogram of docking scores of the generated compounds and compounds with experimentally measured activity for the binding pocket of the adenosine receptor A2a (PDB 2YDO). (Right) An example of the top-scored docking pose of one of the generated molecules.

relevant, information-rich molecular descriptors, such as ISIDA fragment counts. They are equally able to support highly predictive, polypharmacologically competent “universal” maps as the latter. Thus, the herein constructed latent-space-driven “universal” map GTM provided a direct and intuitive access to the latent descriptor space, which means that sampling of chemical space can be “driven” by the map, toward the highly relevant zones of a drug discovery project. Chemical space sampling can be intuitively “monitored” in 2D on the map. Driving through the chemical space can be achieved both by stochastic methods (here, an evolutionary algorithm) guided by the GTM manifold or by direct normal sampling of the neighborhood of relevant GTM nodes, having predominantly active ligands as residents. The robust link from the herewith visited latent space zones to actual SMILES strings is provided by a well-trained decoder, with very high propensity to generate chemically valid structures. The unique combination of these two features promised to generate *de novo* focused molecular libraries, the quality of which can be rigorously tuned according to multiple criteria:

- proximity to the GTM manifold, as an implicit check of the AD of the GTM model (the activity class landscape)
- the probability to be active, returned as a function of the likelihood to encounter confirmed A2a actives in the area of projection of the new candidate (with implicit rejection of candidates projected in empty zones of the GTM landscape, as a second AD criterion)
- synthetic accessibility, as encoded by Peter Ertl’s SA criterion
- absence of “unwanted” reactive groups

For the herein addressed study case, the A2A receptor, *de novo* compounds of correct synthetic accessibility (both by score and by human evaluation) were discovered to reside in chemical space zones predominantly populated by A2A actives, all the while not being structurally redundant (in terms of Tanimoto dissimilarity) to the latter. Pending real synthesis and experimental validation, alternative chemoinformatics approaches that do not rely on machine-learned models (pharmacophore screening and docking) seem to corroborate the high likelihood of real, original actives being present in these focused libraries.

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### Notes

The authors declare no competing financial interest.

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