ParPyDTK2 Documentation

Release 1.1.0

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CHAPTER

ONE

INTRODUCTION

1.1 Background & Motivation

Multi-physics coupling has become one of the popular topics. People try to put different models together and simulate the behaviors in a coupled fashion. With the popularity of *partitioned approach*, i.e. solve different domains with different solvers and couple the interface conditions as those solvers boundary conditions, a robust and accurate interface solution remapping operator is needed. The solution transfer problem on its own is not an easy task, since it involves the following research aspects:

- 1. **numerical method**, i.e. consistent, conservative, high-order convergence.
- 2. **geometry and data structure**, i.e. efficient and robust treatments of *mesh association* of two (potentially more) general surfaces that come from different discretization methods (*FEM*, *FVM*, *FDM*, etc.) thus having different resolutions.
- 3. parallel rendezvous & HPC, i.e. handling migrating meshes that have different parallel partitions.

Data Transfer Kit-2.0 (DTK2) is a package that is developed at the Oak Ridge National Laboratory. DTK2 provides parallel solution transfer services with *meshless* (a.k.a. *mesh-free*) methods, which are relatively easy to implement and computational efficient. Particularly, we are interested in its *modified moving least square*¹ method that is an improvement of traditional MLS fitting in terms of robustness on featured geometries.

Mesh-Oriented datABase (MOAB) is an array-based general purpose mesh library with MPI support. Array-based mesh data structure is more efficient in both computational cost and memory usage compared to traditional pointer-based data structures. MOAB has been adapted in DTK2, so we choose to use it as our mesh database for this work.

In multi-physics coupling, a flexible software framework is must. The fact is: the physics solvers may be implemented in different programming languages or shipped as executable binaries (typically commercial codes), this makes using static languages difficult. Python, on the other hand, can easily glue different languages together and drive executable binaries smoothly. Its built-in reference counting, garbage collection, and pass-by-reference make it as one of the best choices for developing multi-physics coupling frameworks. In addition, MPI is well supported through the mpi4py package. This motivates us to develop a Python interface for DTK2!

1.2 License

This package is distributed under MIT License. For detailed information, please take a look at the LICENSE file.

¹ Slattery, S. Hamilton, T. Evans, "A Modified Moving Least Square Algorithm for Solution Transfer on a Spacer Grid Surface", ANS MC2015 - Joint International Conference on Mathematics and Computation (M&C), Supercomputing in Nuclear Applications (SNA) and the Monte Carlo (MC) Method, Nashville, Tennessee ⋅ April 19−23, 2015, on CD-ROM, American Nuclear Society, LaGrange Park, IL (2015).

1.3 About Me

I am a Ph.D. candidate who work with Dr. Jim Jiao on high-order numerical methods. This work is for testing our software framework of multi-physics coupling in general, *conjugate heat transfer* (CHT) in particular.

Note: Please be aware that I may not have time to maintain this package.

1.3. About Me 2

CHAPTER

TWO

INSTALLATION

Installing this package is not a trivial task due to its heavy dependencies. ParPyDTK2 has the following installation requirements:

- 1. C++11 compiler
- 2. MPI
- 3. MOAB
- 4. DTK2 and Trilinos
- 5. Python >= 3.5
- 6. mpi4py
- 7. NumPy
- 8. setuptools

And both MOAB and DTK2 have their own dependencies.

In addition, to build the documentation, the following packages are needed:

- 1. Sphinx
- 2. Doxygen
- 3. breathe
- 4. numpydoc

The good news is you can install these easily through pip.

2.1 Install MOAB

The MOAB official README has a very clear description of the installation process. Here we take an excerpt of our MOAB Docker image building script:

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```
F77=mpif77 \
   --enable-optimize \
   --enable-shared=yes \
   --with-blas=-lopenblas \
    --with-lapack=-lopenblas \
    --with-scotch=/usr/lib \
    --with-metis=/usr/lib/x86_64-linux-gnu \
    --with-eigen3=/usr/include/eigen3 \
    --with-x \
   --with-cgns \
   --with-netcdf \
   --with-hdf5=/usr/lib/hdf5-openmpi \
   --with-hdf5-ldflags="-L/usr/lib/hdf5-openmpi/lib" \
   --enable-ahf=yes \
   --enable-tools=ves
$ make && sudo make install
```

Notice that this is for system installation. Install to your preferred locations if you don't have the root access. Also, turn off those optional packages if you don't have them, only MPI and HDF5 are necessary.

```
Warning: You must build it into a shared object!
```

Note: If you use Ubuntu >= 17.10, all those optional packages are likely to be available through apt.

2.2 Install DTK2

DTK2 is shipped as a sub-module of Trilinos, so building Trilinos is needed. For people who are not familiar with Trilinos, this can be tricky. Therefore, an excerpt of our DTK2 Docker image building script might be helpful:

```
$ export TRILINOS_VERSION=12-12-1
$ git clone --depth 1 --branch trilinos-release-${TRILINOS_VERSION}
$ cd Trilinos
$ git clone --depth 1 --branch dtk-2.0 \
   https://github.com/unifem/DataTransferKit.git
$ mkdir build && cd build
$ cmake \
   -DCMAKE_INSTALL_PREFIX:PATH=/usr/local \
   -DCMAKE_BUILD_TYPE:STRING=RELEASE \
   -DCMAKE_VERBOSE_MAKEFILE:BOOL=OFF \
    -DCMAKE_SHARED_LIBS:BOOL=ON \
    -DTPL_ENABLE_MPI:BOOL=ON \
   -DTPL ENABLE Boost:BOOL=ON \
   -DBoost_INCLUDE_DIRS:PATH=/usr/include/boost \
   -DTPL_ENABLE_Libmesh:BOOL=OFF \
   -DTPL_ENABLE_MOAB:BOOL=ON \
   -DMOAB_INCLUDE_DIRS=$MOAB_ROOT/include \
   -DMOAB_LIBRARY_DIRS=$MOAB_ROOT/lib \
   -DTPL_ENABLE_Netcdf:BOOL=ON \
   -DTPL_ENABLE_BinUtils:BOOL=OFF \
    -DTrilinos_ENABLE_ALL_OPTIONAL_PACKAGES:BOOL=OFF \
```

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2.2. Install DTK2 4

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```
-DTrilinos_ENABLE_ALL_PACKAGES=OFF \
   -DTrilinos_EXTRA_REPOSITORIES="DataTransferKit" \
    -DTrilinos_ENABLE_EXPLICIT_INSTANTIATION:BOOL=ON \
    -DTrilinos_ASSERT_MISSING_PACKAGES:BOOL=OFF \
    -DTrilinos_ENABLE_TESTS:BOOL=OFF \
    -DTrilinos_ENABLE_EXAMPLES:BOOL=OFF
    -DTrilinos_ENABLE_CXX11:BOOL=ON \
    -DTrilinos_ENABLE_Tpetra:BOOL=ON \
    -DTpetra_INST_INT_UNSIGNED_LONG:BOOL=ON \
   -DTPL_ENABLE_BLAS:BOOL=ON \
   -DTPL_BLAS_LIBRARIES=/usr/lib/x86_64-linux-gnu/libopenblas.so \
   -DTPL_ENABLE_LAPACK:BOOL=ON \
   -DTPL_LAPACK_LIBRARIES=/usr/lib/x86_64-linux-qnu/libopenblas.so
   -DTPL_ENABLE_Eigen:BOOL=ON \
   -DTPL_Eigen_INCLUDE_DIRS=/usr/include/eigen3 \
   -DTrilinos_ENABLE_DataTransferKit=ON \
   -DDataTransferKit_ENABLE_DBC=ON \
   -DDataTransferKit_ENABLE_TESTS=ON \
    -DDataTransferKit_ENABLE_EXAMPLES=OFF \
    -DDataTransferKit_ENABLE_ClangFormat=OFF \
    -DTPL_ENABLE_BoostLib:BOOL=OFF \
    -DBUILD_SHARED_LIBS:BOOL=ON
$ make && sudo make install
```

Again, this assumes root access, adjust this based on your situation. DTK2 needs to stay in the root directory of Trilinos and be turned on through switches DTrilinos_EXTRA_REPOSITORIES and DTrilinos_ENABLE_DataTransferKit. The environment var MOAB_ROOT is the place where you install MOAB.

Note: We recommend that install DTK2 from my personal forked repo since we may add/modify the source codes to make DTK2 more advanced.

2.3 Install ParPyDTK2

Once you have the dependencies setup, installing ParPyDTK2 can be very easy. The easiest way is through PyPI:

```
$ sudo pip3 install parpydtk2
```

However, this assumes that ParPyDTK2 can find MOAB and DTK2 on the system. With different specifications of install command, ParPyDTK2 can automatically add different paths to search for MOAB and DTK2.

```
$ pip3 install parpydtk2 --user
```

will assume MOAB and DTK2 can be found in USER_BASE/{include, lib}.

```
$ pip3 install parpydtk2 --prefix=...
```

will allow ParPyDTK2 to search MOAB and DTK2 under the prefix directory.

The preferred way is to define the environment variables PARPYDTK2_MOAB_ROOT and PARPYDTK2_DTK_ROOT before you do pip install. For instance,

```
$ export PARPYDTK2_MOAB_ROOT=/path/to/moab/root
$ export PARPYDTK2_DTK_ROOT=/path/to/dtk/root
$ pip3 install parpydtk2 --user
```

Warning: We don't mark mpi4py as installation dependency, so you need to install it manually before you install ParPyDTK2. pip3 install mpi4py is just fine.

Of course, you can install from source, which can be obtained here. Just make sure you have all Python *dependencies* installed.

```
$ git clone -b parallel https://github.com/chiao45/parpydtk2.git
$ cd parpydtk2
$ python3 setup.py install --user
```

2.4 Using our Docker container

You can try the package through our pre-built Docker container. Two driver scripts are provided in order to easily use the container:

- 1. parpydtk2_desktop.py
- 2. parpydtk2_jupyter.py

The former will launch a desktop environment through VNC, while the latter will run the container as a Jupyter server.

CHAPTER

THREE

SOME DETAILS

3.1 Meshless/Mesh-free

Point clouds are easier to use (for the end user) compared to meshes. However, there are some drawbacks: 1) using meshes can achieve linear time complexity for mesh associations¹; 2) numerical integrations are not easy; 3) handling cell-averaged data fields, e.g. solutions that come from FVM, potential can lead to problems.

For 3), typically, people assume cell-averaged data to be cell-centered data, which limits to 2nd-order of accuracy. (Notice that this is actually not a big problem in practice.)

3.2 Global IDs/Handles

MOAB uses global IDs for parallel communications as well as DTK2. Therefore, ParPyDTK2 expects the user to provide this information. For most applications, this can be computed offline.

The global IDs are unique handles of the vertices in a point cloud. For instance, if one wants to distribute two triangles, then each of them has local IDs from 0 to 2, but unique global IDs that range from 1 to 4.

Note: ParPyDTK2 uses 1-based indexing for global IDs

3.3 Treatment of Empty Partitions

Both MOAB and DTK2 don't natively support empty partitions, which occur pretty frequently in practice. For instance, couple a serial solver with a parallel solver, or couple a commercial code with an open-sourced one through socket and the incoming data partition graph from the commercial code probably doesn't align with that of the open-sourced side.

To support empty partitions, we duplicate the first node in the master process to the processes that are empty. However, this is not complete yet, because the user is not aware of this, so that the values between across duplicated nodes are not synchronized. Of course, we don't want to let the user to explicitly handle this extra layer of communication. To resolve this, a member function, called $resolve_empty_partitions()$, is added to class IMeshDB and must be called **collectively** whenever the user updates the field values through $assign_field()$.

¹ Jiao X, Edelsbrunner X, Heath MT. Mesh association: formulation and algorithms. In 8th International Meshing Roundtable. Sandia Report, South Lake Tahoe, CA, 1999; 75–82.

CHAPTER

FOUR

AWLS EXTENSION

Although the *modified moving least square* in DTK2 is a very advanced data remapping method, there are still rooms for improvement.

- 1. Whenever dealing with Vandermonde systems, stability must be taken into consideration.
- 2. The local support of the Vandermonde systems should be adaptive based on the properties of local stencils.

The MLS method solves the local problem in the normal equation setting, which doubles the condition number of the system. MMLS solves the local system with *truncated singular value decomposition* (TSVD), but the problem is that the truncated terms in the Vandermonde systems cannot be controlled. Notice that in order to perform the TSVD, an condition number estimator is needed, and MMLS uses the one in LAPACK for general matrices that requires an LU factorization, which takes another $O(n^3)$ FLOPs.

Regarding implementation details, MMLS uses the global cartesian coordinates for constructing Vandermonde matrices and calls SVD incrementally to ensure the resulting systems are full rank, and this procedure is less stable and costly.

For the local stencil choice, directly using the query results is risky, because the stencil might be too large. In general, the number of points in the local stencils should be determined by the column sizes of the Vandermonde systems.

Moreover, after the data has been remapped, an intermediate target solutions are obtained. Combining with the input source data, *a posteriori* error analysis can be performed in order to fix non-smooth values.

With these considerations, we have implemented *adaptive weighted least square* (AWLS) as an extension of the **meshless** methods in DTK2.

4.1 Weighted Least Square (WLS) Formulation

4.1.1 Formulation

Given the source input discrete function values f^s and target output f^t , we want to construct a transfer operator T, s.t.

$$\boldsymbol{f}^t = \boldsymbol{T}\boldsymbol{f}^s \tag{4.1}$$

Clearly, such an operator is rectangle with sizes n by m, where n is the number of nodes in target grid while m for that of the source grid.

Therefore, for each target node i, we have an "interpolation" that reads:

$$f_i^t = T_{i,J} \boldsymbol{f}_J^s \tag{4.2}$$

where J is the local support stencil around target node i. Denote $c^T = T_{i,J}$, and localize the stencil J around the target node x_i and denote the localized stencil to be u, i.e. $u = x - x_i$, we can then build the *generalized Vandermonde system* (assume 2D):

$$V = | 1 \quad u_1 \quad u_2 \quad u_1^2 \quad u_1 u_2 \quad u_2^2 |$$
 (4.3)

So the coefficients c^T can be solved with the following fitting problem:

$$\boldsymbol{V}^T \boldsymbol{c} = \boldsymbol{e}_1 \tag{4.4}$$

If V is square system, i.e. typical Vandermonde system, then (4.4) is just an interpolation problem. When we have more points than the number of columns in V, it results a rectangle system thus requiring least square minimization.

Note that a more intuitive derivation of (4.4) is to first form a system of polynomial coefficients for J and explicitly compute the values of any points in u.

$$VC = I$$
 $C = V^+$

Where V^+ is the *pseudo-inverse* of V. Given a point p in the local coordinate system u, its Vandermonde component is:

$$\mathbf{p}_V = [1 \ p_1 \ p_2 \ p_1^2 \ p_1 p_2 \ p_2^2]^T \tag{4.5}$$

Then evaluating (4.5) in the system of polynomial coefficients, i.e. (4.1.1), is just to perform $p_V^T C$. It's worth noting that for the fitting problem, where the query point is always the center (the target node of interest) thus having the the Vandermonde component $\begin{bmatrix} 1 & 0 & 0 & 0 & 0 \end{bmatrix}^T$. Therefore, the explicit computation reduces to (4.4).

It is well-known that the Vandermonde systems are ill-conditioned, so a balancing technique is needed. A typical way is to do a column scaling: VS. Typical choices of the diagonal matrix S are 1) algebraic scaling that is based on the norms of column vectors of V and 2) geometric scaling that is based on the radii of the local stencil J. Here we choose the latter, and the local stencil radii is chosen as:

$$r = \max_{j \in J} (\max_{1 \le d \le D} (\left| \mathbf{u}_d^j \right|)) \tag{4.6}$$

Where D is the spatial dimension. Then the column scaling matrix is (assume 2D):

$$S = \begin{vmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1/r & 0 & 0 & 0 & 0 \\ 0 & 0 & 1/r & 0 & 0 & 0 \\ 0 & 0 & 0 & 1/r^2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1/r^2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1/r^2 \end{vmatrix}$$

$$(4.7)$$

Note: S doesn't affect the solution.

Now, the least square problem (4.1.1) can be formulated as:

$$\min(\|\boldsymbol{V}\boldsymbol{C} - \boldsymbol{I}\|_{\boldsymbol{W}}) \tag{4.8}$$

We choose to use the family of radius basis functions (RBF) as the diagonal row weighting matrix W.

Note: W does affect the solution.

With (4.7) and (4.8), we have a weighted and balanced generalized Vandermonde system:

$$\hat{\mathbf{V}} = \mathbf{W}\mathbf{V}\mathbf{S} \tag{4.9}$$

Plug (4.9) into (4.4) and reorganize it, we have:

$$\hat{oldsymbol{V}}^Toldsymbol{W}^{-1}oldsymbol{c} = oldsymbol{S}^{-1}oldsymbol{e}_1 \ \hat{oldsymbol{V}}^T\hat{oldsymbol{c}} = oldsymbol{e}_1$$

Where $\hat{\boldsymbol{c}} = \boldsymbol{W}^{-1} \boldsymbol{c}$.

4.1.2 Solving WLS

We follow the technique of using *truncated QR with column pivoting* (TQRCP) introduced here¹ to solve the problem (4.1.1).

The first step is to decompose \hat{V} with QRCP:

$$\hat{\mathbf{V}}\mathbf{P} = \mathbf{Q}\mathbf{R} \tag{4.10}$$

The truncation step is to utilize a condition number estimator for the upper triangular system R that will report the rank of the system—k. Combine this with (4.10) and plug into (4.1.1), we have:

$$egin{array}{ll} m{P}_{:,1:k}m{R}_{1:k,1:k}^Tm{Q}_{:,1:k}^T\hat{m{c}} &=m{e}_1 \ m{R}_{1:k,1:k}^Tm{Q}_{:,1:k}^T\hat{m{c}} &=m{P}_{:,1:k}^Tm{e}_1 \ m{Q}_{:,1:k}^T\hat{m{c}} &=m{R}_{1:k,1:k}^{-T}m{P}_{:,1:k}^Tm{e}_1 \ m{c} &=m{Q}_{:,1:k}m{R}_{1:k,1:k}^{-T}m{P}_{:,1:k}^Tm{e}_1 \ m{c} &=m{W}m{Q}_{:,1:k}m{R}_{1:k,1:k}^{-T}m{P}_{:,1:k}^Tm{e}_1 \end{array}$$

This procedure is very efficient and robust. The dominated computation cost comes from QRCP, i.e. $O(n^3)$, where n is some measure of the size of local problems. It's worth noting that QRCP is called only once for each of the local problems.

4.2 Improving the Strategy of Choosing Local Stencil

The original DTK2 stencil choice is based on a global configuration parameter of either knn (k nearest neighborhoods) or radius. Moreover, the resulting neighbors are used to be the support of the local problems, i.e. number of points used in the Vandermonde systems. This procedure is not robust for problems with point clouds that are not uniformly distributed. To overcome this, we have implemented the following three steps for querying and choosing local supports.

- 1. Perform knn search with a small number of neighborhoods to estimate the radii of the one-ring neighborhood of the local point clouds, say h.
- 2. Perform radius search with a relatively large radius so that we have enough candidates for next step. The radius is chosen as: r = ah.
- 3. Choose the support stencil, i.e. J from the candidates based on the number of columns (coefficients) in the Vandermonde systems, i.e. $|J| = \rho c_d$. Notice that c_d are 3, 6, and 10 for dimension (subscript d) 1, 2, and 3 for quadratic polynomial basis functions, respectively.

¹ R. Conley, T. J. Delaney, and X. Jiao. Overcoming element quality dependence of finite elements with adaptive extended stencil FEM (AES-FEM). Int. J. Numer. Meth. Engrg., vol. 108, pp. 1054–1085, 2016.

Note: We choose a=5 for candidate selections and observe that better results can be obtained with $\rho \approx 3$.

Note: Theoretically, steps 1 and 2 can be achieved with knn search if we can determine the number points in step 3. However, since we have ran into robustness issues with DTK2 while using knn as the primary search mechanism, we rely on the radius search.

With this strategy, the user doesn't need to provide a radius. However, we still believe using topology based query is still efficient and better, but this requires meshes, which is an arduous task for this work.

4.2.1 Automate Parallel Mesh Rendezvous

While use DTK2 in parallel, each operator is built based on the cartesian bounding box the target point cloud with an approximated extension. For this extension length, we have implemented the following strategy:

$$r = \max(\alpha h_b, \frac{\beta h_b}{N^{1/d}}, r_u) \tag{4.11}$$

Where h_b is the longest edge in the cartesian bounding box, N is the number of nodes, d is the topological dimension, and r_u is user-provided radius extension. Notice that the second term essentially tries to estimate the average cell-size of the point cloud.

Note: We choose $\alpha = 0.1$ (10%) and $\beta = 5$ as default parameters.

4.3 Adaptation with Non-smooth Functions

A common challenge of solution/data remapping is to handle non-smooth functions, i.e. avoiding Gibbs phenomenon. We apply a simple bounding strategy that enforces the transferred solutions are bounded locally with respect to the sources values in the stencil J.

Given the intermediate solutions \hat{f}_t after applying the WLS fitting, then the following limitation is performed:

$$f_i^t = \begin{cases} \hat{f}_i^t & \hat{f}_i^t \in range(\mathbf{f}_J^s) \\ \max(\mathbf{f}_J^s) & \hat{f}_i^t \approx \max \\ \min(\mathbf{f}_J^s) & ow \end{cases}$$
(4.12)

In solution transfer, the strategy above may crop high-order values to first order in smooth regions, this is particularly true when the two grids resolutions differ too much from each other. Therefore, we need a mechanism that can prescreen the non-smooth regions. We utilize a gradient based smoothness indicator, which is similar to those used in WENO schemes.

$$\frac{\left|\hat{f}_i^t - f_1^s\right|}{\epsilon h} \le \sigma \tag{4.13}$$

where $\epsilon = \max_{j \in J} (\left| f_j^s \right|)$. This scheme is efficient and doesn't require geometry data. The drawback is also obvious—it's too simple and tuning σ is not easy.

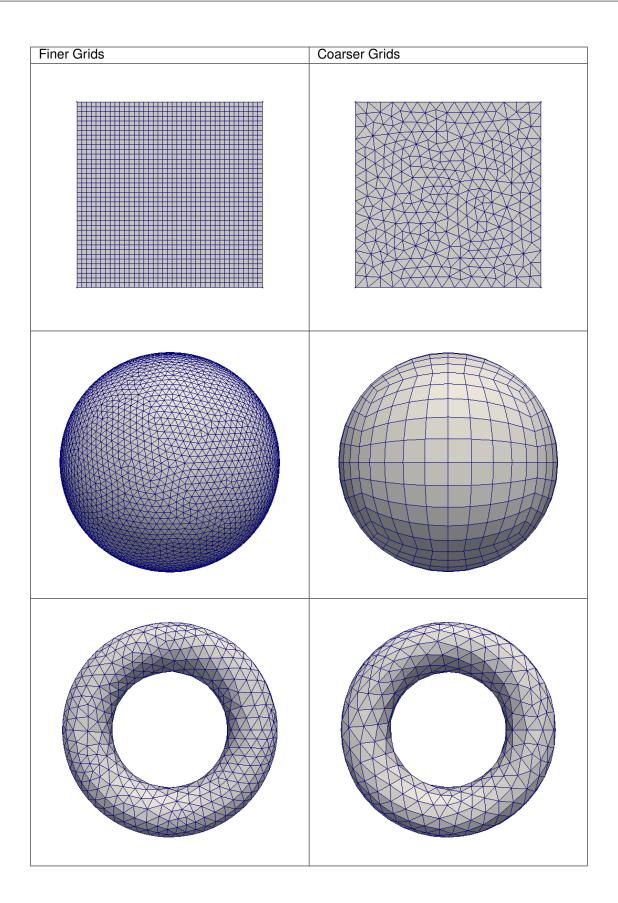
4.4 Results

4.4.1 Convergence Tests

We have tested the AWLS on the following settings:

- 1. plane surface,
- 2. spherical surface, and
- 3. torus surface.

For the plane surface, we use structured grids on one side and triangular meshes on the other side. For setting 2, we use *cubed-sphere* grids and triangular meshes. For the last case, we use triangular meshes with different resolutions. All grids are uniformly refined by three levels in order to study the convergences. Notice that only the coarsest levels are shown in the following figures and all tests are transferred from fine grids to the corresponding coarse ones.



The convergence metric is:

$$c = \left| \frac{\log_2(e_3/e_1)}{\log_2(h_3/h_1)} \right|$$

Where h is some consistent measures of the grids. The error metric we use is relative ℓ_2 errors:

$$e = \frac{\|f_h - f\|_2}{\|f\|_2}$$

For the plane surface, the following two models are tested:

- 1. $f(x,y) = e^{x+y}$, and
- 2. $f(x,y) = \sin(\frac{\pi x}{2})\cos(\frac{\pi y}{2}).$

We use WENDLAND21 as weighting scheme and choose $\rho = 3$ (18 points in stencils), the results are:

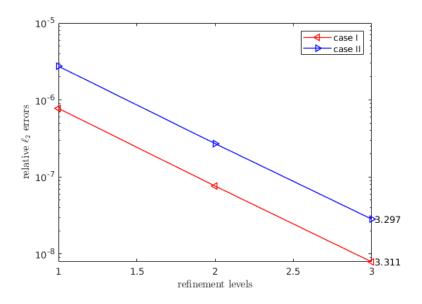


Fig. 1: Convergence of the plane surface

For the 3D cases, we choose the following models:

- 1. $f(x, y, z) = (\sin(x) + \cos(y))z$, and
- 2. $f(x, y, z) = e^{x+y+z}$.

We use WENDLAND21 as weighting scheme and choose $\rho=3.2$ (32 points in stencils) for the spherical surface and $\rho=2.3$ (23 points in the stencils) for the torus surface, the results are:

Note that for all cases, the super-convergence phenomenon is observed, i.e. the convergence rate is greater than (p+1)-st order.

The torus program script can be obtained here, and the corresponding grids are stored in compressed npz file that can be obtained here.

Since the spherical surface is really special due to its smoothness and symmetry, an almost-(p+2)-nd order super-convergence can be obtained with large stencils and WU2 weighting schemes. The following results are with $\rho=6.8$ (68 points in stencils):

However, this is less practical and hard to apply on general surfaces. As a matter of fact, we didn't observe this with the torus setting.

You can obtain the test grids in VTK here.

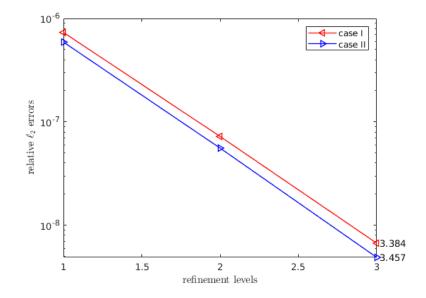


Fig. 2: Convergence of the spherical surface

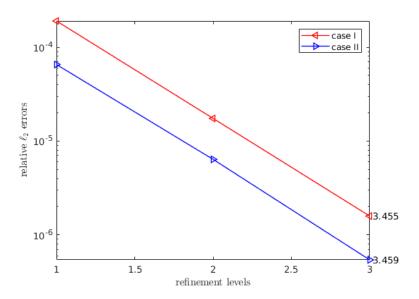
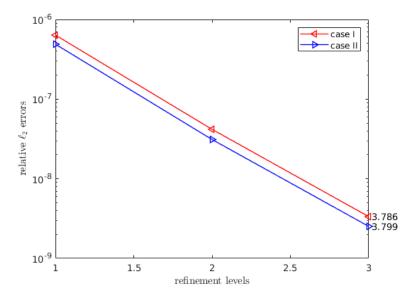


Fig. 3: Convergence of the torus surface



4.4.2 Non-smooth Functions

As a preliminary report, we perform the discontinuous test with the heaviside function on the plane surface with $\sigma=2$. The results are:

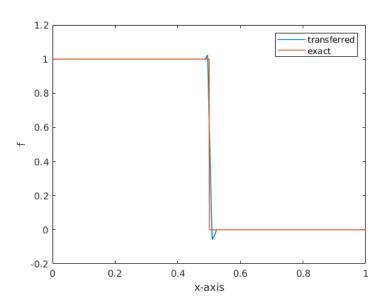


Fig. 4: Heaviside function w/o resolving non-smooth regions

4.5 Usage

In order to use AWLS, you need to install the DTK2 package from my personal forked version.

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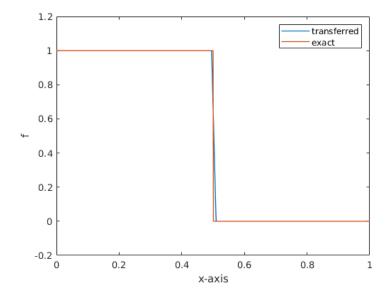


Fig. 5: Heaviside function with resolving non-smooth regions

Note: I didn't decide to make a PR due to DTK2 is probably deprecated in the official repository???

To determine the backend DTK2, a static member function is implemented:

```
>>> from parpydtk2 import *
>>> assert not Mapper.is_dtk2_backend()
```

To enable AWLS support, you just need to call awls_conf():

```
>>> mapper.awls_conf()
```

The default settings are:

- 1. method is set to AWLS,
- 2. basis is set to WENDLAND21,
- 3. α is set to 0.1 in (4.11),
- 4. β is set to 5 in (4.11),
- 5. ρ is set to 3 for *choosing local stencils*

A complete list of parameters are:

```
>>> mapper.awls_conf(
... ref_r_b=...,
... ref_r_g=...,
... dim=...,
... alpha=...,
... beta=...,
... basis=...,
... rho=...,
... verbose=True,
... )
```

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Where ref_r_b and ref_r_g are r_u in (4.11) for blue and green participants. dim is the topological dimension used in (4.11), which is important if you need to transfer surface data (90% cases) in 3D space in order to estimate the proper of mesh cell sizes.

In order to resolve discontinuous solutions, you need to pass in at least one additional parameter $resolve_disc$ to $transfer_data()$:

```
>>> bf_tag, gf_tag = 'foo', 'bar'
>>> mapper.transfer_data(bf_tag, gf_tag, direct=B2G, resolve_disc=True)
```

The default is σ in (4.13) is 2. To use another value, simply do:

```
>>> mapper.transfer_data(...,resolve_disc=True, sigma=...)
```

Note: Resolving discontinuous solutions only works with AWLS method under CHIAO45 backend.

4.5. Usage 18

CHAPTER

FIVE

A DEMO

Here, we show a demo for transferring solutions between two meshes of the unit square. We let the blue mesh participant run in parallel with two cores, while the green side is treated as a serial mesh.

```
import numpy as np
from mpi4py import MPI
from parpydtk2 import *

comm = MPI.COMM_WORLD

blue, green = create_imeshdb_pair(comm)

assert comm.size == 2
rank = comm.rank
```

For demo purpose, we construct the meshes globally.

```
# create blue meshes on all processes
12
   cob = np.empty(shape=(16, 3), dtype=float, order='C')
13
   index = 0
15
   x = 0.0
16
   for i in range(4):
17
       y = 0.0
18
       for j in range (4):
19
20
           cob[index] = np.asarray([x, y, 0.0])
           index += 1
21
           y += dh
22
       x += dh
23
24
   # global IDs, one based
25
   bgids = np.arange(16, dtype='int32')
26
   bgids += 1
```

The blue side has 16 nodes, the following is for the green side:

```
# create green meshes on all processes
29
   cog = np.empty(shape=(36, 3), dtype=float, order='C')
30
   dh = 0.2
31
   index = 0
32
   x = 0.0
33
   for i in range(6):
34
       y = 0.0
35
       for j in range(6):
36
            cog[index] = np.asarray([x, y, 0.0])
```

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```
index += 1
    y += dh
    x += dh

// ggids = np.arange(36, dtype='int32')
ggids += 1
```

The green participant has 36 nodes. The next step is to put the data in the two mesh databases.

```
# creating the mesh database
   blue.begin_create()
   # local vertices and global IDs
48
   lcob = cob[8 * rank:8 * (rank + 1), :].copy()
49
   lbgids = bgids[8 * rank:8 * (rank + 1)].copy()
50
   blue.create_vertices(lcob)
51
   blue.assign_gids(lbgids)
52
   # do not use trivial global ID strategy
53
   blue.finish_create(False)
54
   blue.create_field('b')
```

As we can see, we equally distributed the mesh into the two cores as well as the corresponding global IDs. In line 54, the False flag indicates that the mesh database should use the user-provided global IDs.

Warning: Creating vertices and assigning global IDs must be called between <code>begin_create()</code> and <code>finish_create()!</code> Otherwise, exceptions are thrown.

```
Warning: Creating fields must be done after finish_create()!
```

Here is the treatment for the "serial" participant:

```
# NOTE that green is assumed to be serial mesh
green.begin_create()
# only create on master rank
if not rank:
    green.create_vertices(cog)
# since green is serial, we just use the trivial global IDs
green.finish_create() # empty partition is resolve here
green.create_field('g') # must after finish create

assert green.has_empty()
```

As we can see, only the master process has data.

Note: The *duplicated* node is handled inside *finish_create()*

With the two participants ready, we can now create our *Mapper*.

```
# create our analytical model, i.e. 10+sin(x)*cos(y)

bf = 10.0 + np.sin(lcob[:, 0]) * np.cos(lcob[:, 1])

gf = np.sin(cog[:, 0]) * np.cos(cog[:, 1]) + 10.0
```

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```
72
   # Construct our mapper
73
   mapper = Mapper(blue=blue, green=green)
74
75
   # using mmls, blue radius 1.0 green radius 0.6
76
   mapper.method = MMLS
77
   mapper.radius_b = 1.0
78
   mapper.radius_q = 0.6
79
   mapper.dimension = 2
80
81
   # Mapper initialization region
82
   mapper.begin_initialization()
   mapper.register_coupling_fields(bf='b', gf='g', direct=B2G)
  mapper.register_coupling_fields(bf='b', qf='q', direct=G2B)
85
  mapper.end_initialization()
```

Line 69-70 just create an analytic model for error analysis. Line 77-80 are for parameters, for this case, we use MMLS (default) with blue side radius 1.0 and green side radius 0.6 for searching.

The important part is from line 83 to 86. Particularly speaking, the function $register_coupling_fields()$. It takes three parameters, where the first two are string tokens that represents the data fields in blue and green. The direct is to indicate the transfer direction, e.g. B2G stands for blue to green.

Warning: register_coupling_fields() must be called within begin_initialization() and end_initialization().

```
# NOTE that the following only runs on green master mesh
if not rank:
green.assign_field('g', gf)
# Since green is serial and has empty partition, we must call this to
# resolve asynchronous values
green.resolve_empty_partitions('g')
```

The above section is to assign values on the green participant. Notice that it is a "serial" mesh, so we only assign values on the master process. But resolve the *duplicated* node is needed, this is done in line 93.

Finally, the solution transfer part is pretty straightforward:

```
# solution transfer region
94
   mapper.begin_transfer()
95
   mapper.transfer_data(bf='b', gf='g', direct=G2B)
   err_b = (bf - blue.extract_field('b'))/10
   mapper.transfer_data(bf='b', gf='g', direct=B2G)
   err_g = (gf - green.extract_field('g'))/10
   mapper.end_transfer()
100
101
   comm.barrier()
102
103
   print(rank, 'blue L2-error=%.3e' % (np.linalg.norm(err_b)/np.sqrt(err_b.size)))
   if rank == 0:
       print(0, 'green L2-error=%.3e' % (np.linalg.norm(err_g)/np.sqrt(err_g.size)))
106
```

This code can be obtained here parallel2serial.py.

CHAPTER

SIX

API

6.1 ParPyDTK2 Python API

6.1.1 Default

```
Main module interface of ParPyDTK2
```

```
parpydtk2.B2G
```

bool – boolean flag of True denotes transferring direction from blue to green

parpydtk2.G2B

bool – boolean flag of False denotes transferring direction from green to blue

parpydtk2.MMLS

int – flag (0) represents using modified moving least square method

parpydtk2.**SPLINE**

int – flag (1) represents using spline interpolation method

parpydtk2.N2N

int – flag (2) represents using nearest node projection method

parpydtk2.AWLS

int – flag (3) represents using adaptive weighted least square method

parpydtk2.N2N_MATCH

int – flag (4) represents using matching n2n method

parpydtk2.WENDLAND2

int – flag (0) represents using Wendland 2nd-order RBF weights

parpydtk2.WENDLAND4

int – flag (1) represents using Wendland 4th-order RBF weights

parpydtk2.WENDLAND6

int – flag (2) represents using Wendland 6th-order RBF weights

parpydtk2.WU2

int – flag (3) represents using Wu 2nd-order RBF weights

parpydtk2.WU4

int - flag (4) represents using Wu 4th-order RBF weights

parpydtk2.WU6

int – flag (5) represents using Wu 6th-order RBF weights

parpydtk2.BUHMANN3

int - flag (6) represents using Buhmann 3rd-order RBF weights

```
parpydtk2.WENDLAND21
```

int – flag (7) represents using Wendland 2nd-order 1st dimension RBF weights

```
parpydtk2.create_imeshdb_pair(comm=None)
```

Create a pair of interface mesh databases

This is a convenient and safe way to create a pair of imeshdbs, i.e. blue and green participants with a unified communicator. Please use this API instead of directly creating *IMeshDB*.

```
Parameters comm (MPI.Comm (optional)) - MPI communicator, default is None or MPI_COMM_WORLD.
```

Returns blue and green participants

Return type tuple of IMeshDB

Examples

Create mesh databases with MPI_COMM_WORLD

```
>>> from parpydtk2 import *
>>> blue, green = create_imeshdb_pair()
```

Create mesh databases with explicit communicator

```
>>> from mpi4py import *
>>> from parpydtk2 import *
>>> comm = MPI.COMM_WORLD
>>> blue, green = create_imeshdb_pair(comm)
```

```
parpydtk2.get_include()
```

Get the abs include path

6.1.2 Error Handling

The error handler module

```
parpydtk2.error_handle.ERROR_CODE
```

int – set this to nonzero values one exceptions have been raised

Examples

```
>>> import parpydtk2 as dtk
>>> try:
...  # your programs here
... except Expection:
...  dtk.error.ERROR_CODE = 1
... raise
```

6.1.3 Interface Mesh & Mapper

```
class parpydtk2.IMeshDB(comm=None)
Interface mesh database
```

ParPyDTK2 utilizes MOAB as the underlying mesh database. MOAB is an array based mesh library that is adapted by DTK2. With array based mesh library, the memory usage and computational cost are lower than typical pointer based data structure. The mesh concept in this work is simple since only meshless methods are ultilized, the only additional attribute one needs is the global IDs/handles, which are used by both MOAB and DTK2. For most applications, the global IDs can be computed offline.

One thing is not directly supported by IMeshDB is I/O. However, since this is a Python module and only points clouds are needed, one can easily uses a tool (e.g. meshio) to load the mesh.

```
comm
     MPI.Comm - MPI communicator
ranks
     int – size of comm
rank
     int - rank of comm
size
     int – point cloud size, i.e. number of vertices
gsize
     int – global point cloud size
bbox
     np.ndarray – local bounding box array of shape (2,3)
```

appox

np.ndarray – global bounding box array of shape (2,3)

Constructor

Parameters comm (MPI. Comm (optional)) - if no communicator or None is passed in, then MPI_COMM_WORLD will be used

Examples

```
>>> # implicit communciator
>>> import parpydtk2 as dtk
>>> mdb = dtk.IMeshDB()
```

```
>>> # explicit communicator
>>> from mpi4py import MPI
>>> import parpydtk2 as dtk
>>> mdb = dtk.IMeshDB(MPI.COMM_WOLRD)
```

Notes

Since the mesh database participants appear at least in pairs, a prefered way to construct IMeshDB is to use the wrapper API create_imeshdb_pair(), e.g.

```
>>> from parpydtk2 import *
>>> blue, green = create_imeshdb_pair()
```

```
assign_field(self, unicode field_name, ndarray values)
     Assign values to a field
```

Note: values size must be at least size*dim

Parameters

- field name (str) name of the field
- values (np.ndarray) input source values

See also:

```
extract_field() extract value from a field
size check the size of a mesh set
```

```
assign_gids (self, __Pyx_memviewslice gids)
```

Assign global IDs

Internally, both DTK and MOAB use so-called global IDs/handles communications. Each node has its own local IDs/handles and a unique global ID.

```
Parameters gids (np.ndarray) - global IDs
```

See also:

```
create_vertices() create vertices
extract_gids() extract global IDs
```

bbox

np.ndarray – local bounding box

The bounding box is stored simply in a 2x3 array, where the first row stores the maximum bounds while minimum bounds for the second row.

Warning: Bounding box is valid only after finish_create().

See also:

gbbox global bounding box

begin_create(self)

Begin to create/manupilate the mesh

This function must be called in order to let the mesh databse be aware that you will create meshes.

See also:

```
finish_create() finish creating mesh
```

comm

MPI.Comm - communicator

```
create_field (self, unicode field_name, int dim=1)
```

Create a data field for solution transfer

This is the core function to register a field so that you can then transfer its values to other domains. The dim parameter determines the data type of the field. By default, it's 1, i.e. scalar fields. For each node, a tensor

of (1x"dim") can be registered. For instance, to transfer forces and displacements in FSI applications, dim is 3 (for 3D problems).

Parameters

- **field_name** (str) name of the field
- dim (int) dimension of the field, i.e. scalar, vector, tensor

Examples

```
>>> from parpydtk2 import *
>>> mdb1 = IMeshDB()
>>> mdb1.begin_create()
>>> # creating the meshdb
>>> mdb1.finish_create()
>>> mdb1.create_field('heat flux')
```

create_vertices (self, __Pyx_memviewslice coords)

Create a set of coordinates

Note: The coords must be C-ordering with ndim=2!

Parameters coords (np.ndarray) - nx3 coordinates in double precision

See also:

```
assign_gids() assign global IDs
extract_vertices() extract vertex coordinates
```

Examples

```
>>> from parpydtk2 import *
>>> import numpy as np
>>> mdb1 = IMeshDB()
>>> mdb1.begin_create()
>>> verts = np.zeros((2,3)) # two nodes
>>> verts[1][0] = 1.0
>>> mdb1.create_vertices(verts)
```

created(self)

Check if the mesh database has been created or not

Returns True if finish_create() has been called

Return type bool

empty (self)

Check if this is an empty partition

```
extract_field (self, unicode field_name, __Pyx_memviewslice buffer=None, reshape=False) Extact the values from a field
```

Warning: if buffer is passed in, it must be 1D

Parameters

- field_name (str) name of the field
- buffer (np.ndarray) 1D buffer
- **reshape** (bool) *True* if we reshape the output, only for vectors/tensors

Returns field data values

Return type np.ndarray

extract_gids (self)

Extract global IDs/handles

Warning: This function should be called once you have finished assign_gids().

Returns array of size that stores the integer IDs

Return type np.ndarray

extract_vertices (self)

Extract coordinate

Warning: This function should be called once you have finished create_vertices().

Returns (nx3) array that stores the coordinate values

Return type np.ndarray

See also:

size get the mesh size

field_dim(self, unicode field_name)

Check the field data dimension

Parameters field_name (str) – name of the field

Returns data field dimension of *field_name*

Return type int

finish_create (self, trivial_gid=True)

finish mesh creation

This method finalizes the interface mesh database by communicating the bounding boxes and empty partitions. Also, setting up the DTK managers happens here.

Warning: You must call this function once you have done with manupilating the mesh, i.e. vertices and global IDs.

Parameters trivial_gid (bool) - True if we use MOAB trivial global ID computation

Notes

By trivial_gid, it means simply assigning the global IDs based on the size of the mesh. This is useful in serial settings or transferring solutions from a serial solver to a partitioned one.

gbbox

np.ndarray – global bounding box

The bounding box is stored simply in a 2x3 array, where the first row stores the maximum bounds while minimum bounds for the second row.

Warning: Bounding box is valid only after finish_create().

See also:

bbox local bounding box

gsize

int – Get the global point cloud size

 $has_empty(self)$

Check if an empty partition exists

has_field(self, unicode field_name)

Check if a field exists

Parameters field_name (str) - name of the field

Returns *True* if this meshdb has *field_name*

Return type bool

rank

int – get the rank

ranks

int – Get the communicator size

resolve_empty_partitions (self, unicode field_name)

Resolve asynchronous values on empty partitions

ParPyDTK2 doesn't expect <code>assign_field()</code> should be called collectively. Therefore, a collective call must be made for resolving empty partitions.

Warning: This must be called collectively even on empty partitions

Note: You should call this function following assignment

Parameters field_name (str) – name of the field

Examples

```
>>> if rank == 0:
... mdb.assign_field('flux', values)
>>> mdb.resolve_empty_partitions('flux')
```

Notes

This API is not available in C++ level, therefore, one needs to implement this if he/she wants to use the C++ API.

size

int – Get the size of a set

class parpydtk2.Mapper(blue, green, profiling=True, verbose=True, **kwargs)
DTK2 wrapper

The meshless methods in DTK2, including *modified moving least square*, *spline interpolation* and *nearest node projection* methods are wrapped within this class.

In addition, if you build DTK2 from UNIFEM/CHIAO45 forked verions, then you can use the *adaptive weighted least square* fitting method.

blue_mesh

IMeshDB - blue mesh participant

green_mesh

IMeshDB – green mesh participant

comm

MPI.Comm - MPI communicator

ranks

int – size of comm

rank

int - rank of comm

dimension

int – spatial dimension

method

int - method flag, either MMLS, SPLINE, or N2N

basis

int – flag of basis function for weighting schemes used by MMLS and SPLINE

radius b

float – radius used for searching on blue_mesh

radius_g

float – radius used for searching on green_mesh

leaf_b

int – kd-tree leaf size of blue_mesh

leaf_g

int – kd-tree leaf size of green_mesh

rho

double - local Vandermonde system row scaling factor

Constructor

Parameters

- blue_mesh (IMeshDB) blue mesh participant
- green_mesh (IMeshDB) green mesh participant
- profiling (bool (optional)) whether or not do timing report, default is True.
- **verbose** (bool (optional)) whether or not verbose printing, default is True.
- **stat_file** (str (optional)) file for storing profiling information

Examples

```
>>> from parpydtk2 import *
>>> blue, green = IMeshDB(), IMeshDB()
>>> # initialize blue and green
>>> mapper = Mapper(blue=blue,green=green)
>>> # do work with mapper
```

awls conf (self, **kwargs)

Configuration of Adaptive Weighted Least Square Fitting

Parameters

- basis (int (optional)) basis weighting scheme, default is WENDLAND21
- rho (float (optional)) number of rows in the local Vandermonde system, i.e. rho*col
- $ref_rb(float (optional))$ reference user-specified blue radius, i.e. r_u for blue
- $ref_rg(float (optional))$ reference user-specified green radius, i.e. r_u for green
- dim (int (optional)) topological dimension, default is the surface dimension
- **verbose**(bool (optional))-print verbose information/warning messages, default is False
- alpha (float) the α parameter
- **beta** (float) the β parameter
- _ind_file (str (optional)) indicator result file, used in chiao45 dtk

Notes

_ind_file is for internal use to fine tune the parameter sigma. It will not be enabled in release build.

See also:

```
enable_mmls_auto_conf() configure radius for parallel
mesh()
```

basis

int – Get the basis function flag

See also:

method get the method tag

begin_initialization (self, **kwargs)

Initialization starter

This is a must-call function in order to indicate mapper that you are about to initialize/register coupling fields

See also:

```
register_coupling_fields() register coupled fields
end_initialization() finish initialization
```

begin_transfer (self, **kwargs)

Transfer starter

This is a must-call function to inidate the beginning of a transferring block

See also:

```
end_transfer() transfer closer
```

tranfer_data() transfer a coupled data fields

blue_mesh

IMeshDB - blue mesh

comm

MPI.Comm - Get the communicator

See also:

ranks get the total communicator size
rank "my" rank

dimension

int – Get the problem dimension

Note: this is the spacial dimension

Automatically set up radius parameter for MMLS

Warning: This method should be used only when the underlying DTK2 installation is from CHIAO45 forked version. Otherwise, you should **always** manully configure the radius parameters.

The following strategy is performed:

$$r = \max(\alpha h_b, \frac{\beta h_b}{N^{1/d}}, r_u)$$

where h_b is the the maximum edge length of the global bounding box (gbbox); α is some ratio, say 0.1 (10%); β is the scaling factor the estimated mesh size, which is given by $\frac{h_b}{N^{1/(d-1)}}$ and N is the

global mesh size (gsize); d is the spatial dimension; the last parameter r_u is provided by the user thus optional.

For UNIFEM/CHIAO45 DTK2, this parameter should be relatively large, because the final points in the Vandermonde system is determined by the column size, so that larger radius means that the system has larger candidate pool.

Warning: Regarding the spatial dimension, since this packages is mainly for interface/surface coupling thus the actual dimension is assumed to be one less than the spatial dimension, i.e. surface topological dimension. If this is not the case, the user needs to explicit pass in the dimension to override this default behavior.

Parameters

- $ref_rb(float (optional))$ reference user-specified blue radius, i.e. r_u for blue
- ref_rg (float (optional)) reference user-specified green radius, i.e. r_u for green
- dim (int (optional)) topological dimension, default is the surface dimension
- **verbose**(bool (optional))-print verbose information/warning messages, default is False
- alpha (float) the α parameter
- **beta** (float) the β parameter

See also:

```
is_dtk2_backend() check backend installation of DTK2
```

```
end_initialization (self, **kwargs)
```

Initialization closer

This is a must-call function in order to tell the mapper we are ready

See also:

```
begin_initialization() initialization starter
```

```
end_transfer (self, **kwargs)
```

Transfer closer

This is a must-call function to indicate we have finished a sequence of transferring requests

See also:

```
begin_transfer() transfer starter
```

green_mesh

```
IMeshDB - green mesh
```

has_coupling_fields (self, unicode bf, unicode gf, bool direct)

Check if a coupled fields exists

Returns True if (bf,gf) exists in the direct direction

Return type bool

static is dtk2 backend()

Check if the underlying DTK2 library is chiao45 forked version

Returns False if the user's DTK2 is from chiao45 forked repo

Return type bool

leaf b

int – get the leaf size of blue mesh for kd-tree

Warning: This attribute only works when the underlying DTK2 is installed from UNIFEM or CHIAO45 forked versions.

See also:

leaf_g green leaf size of kd-tree

leaf_g

int - get the leaf size of the green mesh for kd-tree

Warning: This attribute only works when the underlying DTK2 is installed from CHIAO45 forked versions.

See also:

leaf b blue leaf size of kd-tree

method

int – Get the method tag

See also:

basis the basis function and order attribute

static parameter_keys()

radius b

float – physical domain radius support for blue mesh

Note: if blue does not use RBF-search, then -1.0 returned

See also:

radius_g green radius

radius_g

float - physical domain radius support for green mesh

Note: if green does not use RBF-search, then -1.0 returned

See also:

```
radius_b blue radius
rank
     int - Check "my" rank
     See also:
     ranks get the total communicator size
     comm MPI communicator
ranks
     int - Check the total process number
     See also:
     rank "my" rank
register_coupling_fields (self, unicode bf, unicode gf, bool direct, **kwargs)
     register a coupled fields
     Note: we use boolean to indicate direction
         Parameters
             • bf (str) – blue mesh field name
             • gf (str) – green mesh field name
             • direct (bool) – True for blue->green, False for the opposite
     See also:
     transfer_data() transfer a coupled data fields
rho
    float - local scaling factor
set_matching_flag_n2n (self, bool matching)
     Set the matching flag for N2N
     Note: this function will not throw even if you dont use n2n
         Parameters matching (bool) – True if the interfaces are matching
transfer_data (self, unicode bf, unicode gf, bool direct, **kwargs)
     Transfer (bf, gf) in the direct direction
```

Note: Parameters resolve_disc and sigma only work with UNIFEM/CHIAO45 DTK and AWLS

Parameters

method.

- **bf** (str) blue mesh field name
- **gf** (str) green mesh field name
- direct (bool) True for blue->green, False for the opposite
- resolve_disc (bool (optional)) True if do post-processing for resolving non-smooth functions
- sigma (float (optional)) threshold used in smoothness indicator

See also:

register_coupling_fields() register coupled fields

6.2 ParPyDTK2 C++ API

6.2.1 Common Definitions

group common

Defines

```
handle_moab_error(__ret)
    macro to handle moab error
throw_error(__msg)
    throw runtime_error exception
throw_error_if (__cond, __msg)
    conditionally error throw
throw_noimpl(__what)
    throw not implemented feature error
throw_noimpl_if (__cond, __what)
    throw not implemented feature error with condition
\verb"show_warning" (\__msg")
    log warning message in stderr
show_warning_if (__cond, __msg)
    log warning with condition
show_experimental(__msg)
    log experimental warning in stderr
show_experimental_if(__cond, __msg)
    log experimental warning in stderr with condition
show_info(__msg, __rank)
    show information in parallel
show_info_master(__msg, __rank)
    show information only on master rank
streamer(__rank)
    streaming message with specific rank
```

```
streamer_master (__rank)
streaming messages only on the master process
```

Typedefs

typedef entity_t

MOAB entity handle.

Enums

enum [anonymous]

root set

Values:

 $root_set = 0$

6.2.2 Field Variables

class FieldData

a representation of MOAB tag for field data

Public Functions

FieldData (moab::Core &mdb, const std::string &field_name, int dim = 1) constructor with moab instance

Note set is not the same as mesh set in MOAB

Parameters

- mdb: moab instance
- field name: field name
- dim: field dimension

void assign (const moab::Range &range, const double *values) assign values

Parameters

- range: entity ranges, for this work, it should be vertices
- values: data values, for vector/tensor, C order is expected

void assign_1st (const moab::Range &range, const double *values)
 assign to first node

This function is used by Python for handling empty partitions

Parameters

• range: entity ranges

• values: values for the first node, at least size of dim

void extract (const moab::Range &range, double *values) const
extract values

Parameters

- range: entity ranges, for this work, it should be vertices
- values: data values, for vector/tensor, C order is expected

void **extract_1st** (**const** moab::Range & range, double *values) **const** extract the value from the first node

Parameters

- range: entity ranges
- values: values for the first node, at least size of dim

```
operator const std::string&() const
```

brief implicitly cast to string

```
int dim() const
```

check the dimension

int set () const

check the set ID

const moab::Tag &tag() const
 get MOAB tag

Protected Attributes

```
moab::Core &mdb_
```

reference to moab instance

std::string fn_

field name

int set_

set count

int dim

field dimension

moab::Tag tag_ moab tag

class FieldDataSet

a set of field data

Public Types

typedef base_t::iterator iterator
interator type

```
typedef base_t::const_iterator const_iterator
     constant iterator
Public Functions
virtual ~FieldDataSet()
     destructor
bool has_field(const std::string &fn) const
     check if a field exist
     Parameters
           • fn: field name
void create (moab::Core &mdb, const std::string &field_name, int dim = 1)
     create an data field
     Note set is not the same as mesh set in MOAB
     Parameters
           • mdb: moab data base
           • field_name: field name
           • dim: field dimension
FieldData &operator[] (const std::string &fn)
     get a reference to a field data
     Note this overloads the base operator[]
     Parameters
           • fn: field name
const FieldData &operator[] (const std::string &fn) const
     get a const reference to a field data
     Parameters
           • fn: field name
iterator begin()
     get the first iterator
iterator end()
     get the end iterator
const_iterator begin() const
     get the constant iterator
const_iterator end() const
     get the constant end iterator
```

```
const_iterator cbegin() const
    get the constant iterator

const_iterator cend() const
    get the constant end iterator
```

Protected Attributes

```
base_t fs_
fields
```

Private Types

typedef std::unordered_map<std::string, FieldData *> base_t
 data structure

6.2.3 Interface Mesh Database

class IMeshDB

interface mesh database, build on top of MOAB

imesh_py_interface

```
bool created() const
    check created mesh database

void begin_create()
    begin to create mesh

void create_vset()
    create a new vertex set

void create_vertices(int nv, const double *coords)
    create vertices
```

Parameters

- nv: number of vertices
- coords: coords values

```
void extract_vertices (double *coords) const extract assigned coordinates
```

Note coords must be at least n*3 where n is the size of the mesh

Parameters

• coords: coordinates

```
void assign_gids (int nv, const int *gids) assign global IDs
```

Note gids should be one-based indices

Parameters

- nv: number of local vertices
- gids: global IDs

void extract_gids (int *gids) const

extract global IDs

Parameters

• gids: global IDs

void finish_create (bool trivial_gid = true)

finish manupilating the mesh

NOTE that if your input mesh is element-based partition and the vertices you create are mesh nodes, then you have to specify the correct global IDs in parallel. However, if the coordinates are face centres, then the global IDs can be trivially computed by MOAB since there are no shared entities cross different processes.

Parameters

• trivial_gid: true if we let MOAB to compute the GID

bool empty() const

check if empty partition

bool has_empty() const

check if any of the process has an empty partition

const std::vector<int> &_m2s() const

get a reference to the m2s pattern

Note This is used in Python level as "private" thus having "_"

int size() const

check mesh size

int gsize() const

check the global mesh size

void get_bbox (double *v) const

get bounding box

Parameters

• v: values

void get_gbbox (double *v) const

get global bounding box

Parameters

• v: values

```
void create_field(const std::string &field_name, int dim = 1)
```

create a field

Parameters

- field name: field name
- dim: field dimension

bool has_field(const std::string & field_name) const

check if we have a field

Parameters

• field name: field name

int field_dim(const std::string &field_name) const

check field dimension

Parameters

• field_name: field name

void assign_field(const std::string &field_name, const double *values)

assign a value to a field

Parameters

- field_name: field name
- values: field data values

void _assign_1st (const std::string &field_name, const double *values)

assign to the first node

This function is used by Python to resolve the issues when empty empty partitions happen. Therefore, this function has an "_" prefix to indicate "private" usage!

Parameters

- field_name: field name
- values: field data values, at least size of field dimension

void extract_field(const std::string &field_name, double *values) const

extract value

Parameters

- field_name: field name
- values: field data values

void _extract_1st (const std::string &field_name, double *values) const

extract first value

This function is used by Python to resolve the issues when empty empty partitions happen. Therefore, this function has an "_" prefix to indicate "private" usage!

Parameters

- field_name: field name
- · values: field data values

Public Functions

```
\mathbf{IMeshDB} \; (\mathbf{MPI\_Comm} \; comm = \mathbf{MPI\_COMM\_WORLD})
     constructor with communicator
     Parameters
           • comm: communicator
int ranks () const
     get total ranks
int rank() const
     get my rank
MPI_Comm comm() const
     get the communicator
Teuchos::RCP<moab::ParallelComm> pcomm() const
     get mesh
std::vector<DataTransferKit::MoabManager> &mangers ()
     get the manger
void set_dimension (int dim)
     set geometry dimension
     Parameters
           • dim: dimension
bool ready() const
     check if ready
dtk_field_t &dtk_fields()
     get the dtk fields
```

Protected Types

typedef std::unordered_map<std::string, std::pair<int, Teuchos::RCP<Tpetra::MultiVector<double, int, DataTransferKit::Suphandy typedef

Protected Attributes

```
std::vector<std::array<double, 6>> bboxes_
     bounding boxes
std::vector<std::array<double, 6>> gbboxes_
     global bounding boxes
FieldDataSet fields
     field data set
bool created
     flag to indicate whether users are done with creating mesh
moab::Tag gidtag_
     global ID tag
moab::Tag parttag_
     partition tag
bool usergid_
     flag to indicate if we have user computed global ID
std::vector<DataTransferKit::MoabManager> mngrs_
     DTK MOAB manager.
dtk_field_t dtkfields_
     DTK multi vector for MOAB tags.
bool empty
     check empty partition
bool has_empty_
     check if any process is empty
std::vector<int> m2s_
     comm pattern for master2slaves for handling empty partitions
int gsize_
     global size
Private Functions
void init_ (bool del = false)
     helper for clean up mesh
     Parameters
           • del: whether or not delete mesh
void reset vecs ()
     handle all vectors
void init\_bbox\_ (int i = -1)
     initialize empty bounding boxes
     Parameters
           • i: index if < 0 then init all
void cmpt_bboxes_()
     compute all bounding box
```

6.2.4 Solution Mapper

```
class Mapper
     the mapper interface for interface solution transfer
     mapper_py_interface
     int ranks() const
          get the ranks
     int rank () const
          get my rank
     MPI_Comm comm() const
          get the communicator
     void set dimension (int dim)
          set dimension
          Parameters
                • dim: geometry dimension
     void use_mmls()
          use moving least square, this is the default method
          See use_spline, use_n2n
     void use_spline()
          use spline interpolation method
          See use_mmls, use_n2n
     void use_n2n (bool matching = false)
          use node 2 node project
          See use_mmls, use_spline
          Parameters
                • matching: are the interfaces mathing?
     void use_awls()
          use adaptive weighted least square fitting
```

${\tt void} \; \textbf{set_basis} \; (\mathsf{int} \; \mathit{basis})$

See use mmls

set basis function, default is Wendland 4th order

See BasisFunctions

Parameters

• basis: basis function and order

```
void use knn b (int)
    use knn for blue mesh
void use_knn_g (int)
    use knn for green mesh
void use radius b (double r)
    use radius for blue
    See use_knn
     Parameters
           • r: physical domain radius support
void use\_radius\_g (double r)
    use radius for green
    See use_knn
    Parameters
           • r: physical domain radius support
int check_method() const
     check method
int check basis() const
    check basis
int knn_b() const
    check blue knn
    Note if blue does not use knn, then negative value returned
int knn_g() const
    check green knn
double radius_b() const
    check blue radius
     Note if blue does not use radius, then -1.0 is returned
double radius_g() const
    check green radius
int dimension() const
    get the dimension
QRCP_ONLY
void set_leaf_b (int size)
    set the leaf size
```

Warning This method only works with unifem or chiao45 forked backend

Parameters

• size: the leaf size in kd-tree

```
void set_leaf_g (int size)
set the leaf size for green database
```

Warning This method only works with unifem or chiao45 forked backend

Parameters

• size: the leaf size in kd-tree

```
int leaf_b() const
    get the blue leaf size

int leaf_g() const
    get the green leaf size

void _set_ind_file(const std::string &fn)
    set the indicator tuning filename
```

Note internal use

Note This only works with QRCP implementation, or AWLS method

Parameters

• fn: filename

```
void _wipe_ind_file()
    wipe indicator file

void set_rho (double rho)
    set local scaling rho
```

Note This only works with QRCP implementation, or AWLS method

Parameters

• rho: scaling factor

```
double rho() const
get local scaling rho
```

Public Functions

```
Mapper (std::shared_ptr<IMeshDB> B, std::shared_ptr<IMeshDB> G, const std::string &version = "", const std::string &date = "", bool profiling = true, const std::string &stat_file = "", bool verbose = true) constructor
```

Parameters

- B: input blue mesh
- G: input green mesh

- version: passed from Python inteface
- date: passed from Python interface
- profiling: whether do simple profiling, i.e. wtime
- stat_file: statistics filename
- verbose: doing verbose information printing

```
std::shared_ptr</br>
JMeshDB> blue_mesh()
get blue mesh
```

```
std::shared_ptr<IMeshDB> green_mesh() const get green mesh
```

void begin_initialization()

begin initialization

void register_coupling_fields (const std::string &bf, const std::string &gf, bool direct) register coupling fields

Parameters

- bf: blue meshdb field data
- qf: green meshdb field data
- direct: true for b->g, false for g->b

bool has_coupling_fields (const std::string &bf, const std::string &gf, bool direct) check if a coupling data fields exists

Parameters

- bf: blue meshdb field data
- qf: green meshdb field data
- direct: true for b->g, false for g->b

void end_initialization()

end initialization

void begin_transfer()

begin to transfer data

void **transfer_data** (**const** std::string & bf, **const** std::string & gf, bool direct, bool resolve_disc = false, double sigma = -1.0)

transfer data

Notice that internally, the unifem backend occupies the mode parameter to indicate whether or not do post processing to resolve non-smooth solutions. Set mode == Teuchos::TRANS

Parameters

- bf: blue meshdb field data
- qf: green meshdb field data
- direct: true for b->g, false for g->b
- resolve_disc: (optional) if true, then try to resolve disc

• sigma: (optional) indicator threshold

```
void end_transfer()
  end transfer
```

Public Static Functions

```
static bool is_dtk2_backend()
```

check the backend

In chiao45 version of DTK2, we modified the exception class to add a prefix of "chiao45", so it's feasible to query this information w/o adding a new API

Return if the underlying DTK2 is using in chiao45 forkedversion, then return true

Protected Attributes

```
std::shared_ptr<IMeshDB> B_
     blue mesh
std::shared_ptr<IMeshDB> G_
     green mesh
int dim
     dimension
bool ready_
     flag to indicate the mapper is ready for transfering
bool profiling_
     whether do simple profiling
bool verbose
     verbose output
std::unique_ptr<Teuchos::ParameterList> opts_[2]
     parameter list
std::map<std::string, std::string>, Teuchos::RCP<DataTransferKit::MapOperator>> operators_[2]
     transfer operators references
Teuchos::RCP<DataTransferKit::MapOperator> optrs_[2]
     actual transfer operators
std::map<std::pair<std::string, std::string>, std::vector<StatInfo>> info_[2]
     information box for each of the registered pair of fields
std::map<std::pair<std::string, std::string>, unsigned long> counts_[2]
     total transfer counter
std::unique_ptr<std::ofstream> stat_
     the statistics file handle
int stat_write_freq_counter_
     statistics file dump freq counter
```

Protected Static Attributes

```
DataTransferKit::MapOperatorFactory factory_
    map factory
const std::string title_ = std::string(LEN1, '-')
    title of verbose printing
const std::string indentation_ = std::string(LEN2, ' ')
    indentation
Private Functions
void init_parlist_()
    initialize parameter list
template <bool _Dir, typename _V>
void set_search (const std::string &type, const std::string &value, const _V &v)
     helper for set local search
     Template Parameters
           • _Dir: direction
           • _V: value type
     Parameters
           • type: search type
           • value: tag for value
           • v: actual value
template <bool _Dir, typename _V>
_V get_search (const std::string &type, const std::string &value, const _V &dft) const
     helper for get search info
     Template Parameters
           • _Dir: direction
           • _V: value type
     Parameters
           • type: search type
           • value: tag for value
```

void _dump_stats()

• dft: default value

helper function for writing outputs

Private Static Functions

static std::string parse_list_ (Teuchos::ParameterList &list)
parse and formatting a parameter list

Parameters

• list: parameter list

struct StatInfo

a simple structure to store discontinuous points and timing results

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