$\bullet\,$ First-order initial value problems of the form

$$\frac{dy}{dx} = f(x, y)$$

$$y(x_0) = y_0$$

are guaranteed to have a unique solution over an interval I containing x_0 if f(x,y) and $\partial f/\partial y$ are continuous