# Introduction to Electrodynamics by David J. Griffiths Notes

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# 1 Vector Algebra

# 1.6 The Theory of Vector Fields

#### 1.6.1 The Helmholtz Theorem

• The **Helmholtz theorem** states that a vector field  $\mathbf{F}$  is uniquely determined if you're given its divergence  $\nabla \cdot \mathbf{F}$ , curl  $\nabla \times \mathbf{F}$ , and sufficient boundary conditions.

#### 1.6.2 Potentials

• If the curl of a vector field vanishes everywhere, then it can be expressed as the gradient of a **scalar potential** 

$$\nabla \times \mathbf{F} = \mathbf{0} \Leftrightarrow \mathbf{F} = -\nabla V.$$

• If the divergence of a vector field vanishes everywhere, then it can be expressed as the curl of a **vector potential** 

$$\nabla \cdot \mathbf{F} = 0 \Leftrightarrow \mathbf{F} = \nabla \times \mathbf{A}.$$

# 2 Electrostatics

#### 2.1 The Electric Field

#### 2.1.2 Coulomb's Law

ullet Couloumb's law gives the force between two point charges q and Q

$$\mathbf{F} = \frac{1}{4\pi\epsilon_0} \frac{qQ}{\imath} \hat{\mathbf{z}}$$

where

$$\epsilon_0 = 8.85 \times 10^{-12} \, \mathrm{C}^2 / (\mathrm{N \, m}^2)$$

is the **permittivity of free space** and  $\boldsymbol{\imath}$  is the separation vector between the two charges.

#### 2.1.3 The Electric Field

- The **electric field E** is a vector field that varies from point to point and gives the force per unit charge that would be exerted on a test charge if placed at a particular point.
- For a collection of n source charges  $q_i$  at displacements  $\boldsymbol{\lambda}_i$  from a test charge, the electric field is

$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^n \frac{q_i}{\nu_i^2} \hat{\boldsymbol{\lambda}}.$$

## 2.1.4 Continuous Charge Distributions

• Couloumb's law for a continuous charge distribution is

$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \int \frac{1}{\ell^2} \hat{\boldsymbol{\lambda}} \, dq.$$