

The Pennsylvania State University  
The Graduate School  
College of Earth and Mineral Sciences

**MECHANISMS OF SINTERING AND SECOND PHASE  
FORMATION IN BAYER ALUMINA**

A Dissertation in  
Materials Science and Engineering  
by  
Tobias Frueh

© 2017 Tobias Frueh

Submitted in Partial Fulfillment  
of the Requirements  
for the Degree of

Doctor of Philosophy

September 2017

The dissertation of Tobias Frueh was reviewed and approved\* by the following:

Gary Messing

Distinguished Professor of Ceramic Science and Engineering

Thesis Advisor, Chair of Committee

James Adair

Professor of Materials Science and Engineering, Biomedical Engineering and  
Pharmacology

Optional Title Here

John Hellmann

Professor of Materials Science and Engineering

Associate Dean for Graduate Education and Research

Dogulas Wolfe

Associate Professor of Materials Science and Engineering

Department Head, Advanced Coatings at the Applied Research Laboratory

Senior Scientist

\*Signatures are on file in the Graduate School.

# Abstract

# Table of Contents

List of Figures	vi
List of Tables	vii
List of Symbols	viii
Acknowledgments	ix
<b>Chapter 1</b>	
<b>Statement of Problem</b>	<b>2</b>
1.1 section1.1 . . . . .	2
1.1.1 subsection1.1.1 . . . . .	2
<b>Chapter 2</b>	
<b>Introduction</b>	<b>3</b>
2.1 section2.1 . . . . .	3
2.2 section2.2 . . . . .	3
<b>Chapter 3</b>	
<b>The Effects of Na<sub>2</sub>O and SiO<sub>2</sub> on Liquid Phase Sintering of Bayer Al<sub>2</sub>O<sub>3</sub></b>	<b>4</b>
3.1 Introduction . . . . .	4
3.2 Experimental . . . . .	5
3.3 Results . . . . .	6
3.3.1 Effects of Na <sub>2</sub> O-doping . . . . .	6
<b>Chapter 4</b>	
<b>Powder Chemistry Effects on the Sintering Behavior of MgO-doped Bayer Alumina</b>	<b>19</b>
4.1 Introduction . . . . .	19
4.2 More Declaration . . . . .	19

4.2.1	Some nonsense here . . . . .	20
4.2.2	Some additional nonsense here . . . . .	20
<b>Chapter 5</b>		
	<b>Powder Chemistry Effects on Grain Boundaries During Densi- fication of Bayer Alumina</b>	<b>21</b>
5.1	Introduction . . . . .	21
5.2	More Declaration . . . . .	21
<b>Chapter 6</b>		
	<b><math>\beta</math>-Al<sub>2</sub>O<sub>3</sub>: A Model System for the Formation of Second Phases in Al<sub>2</sub>O<sub>3</sub></b>	<b>23</b>
6.1	Introduction . . . . .	23
6.2	More Declaration . . . . .	23
<b>Chapter 7</b>		
	<b>Summary and Future Work</b>	<b>25</b>
7.1	Introduction . . . . .	25
7.2	More Declaration . . . . .	25
	<b>Bibliography</b>	<b>27</b>

# List of Figures

3.1	SEM image of as-received chemically purified Bayer $\text{Al}_2\text{O}_3$ powder used in this study. . . . .	10
3.2	Dilatometer curves of as-received and singly $\text{Na}_2\text{O}$ -doped samples heated at $10^\circ\text{C}/\text{min}$ to $1525^\circ\text{C}$ . . . . .	11
3.3	Densification kinetics of Bayer $\text{Al}_2\text{O}_3$ doped with different $\text{Na}_2\text{O}$ concentrations and sintered at $1525^\circ\text{C}$ . . . . .	12
3.4	Microstructures of as-received and singly 529 ppm $\text{Na}_2\text{O}$ doped samples after 30 min, 3 h and 8 h at $1525^\circ\text{C}$ . . . . .	13
3.5	Dilatometer curves of as-received, singly $\text{SiO}_2$ -doped, and $\text{Na}_2\text{O}/\text{SiO}_2$ -doped Bayer $\text{Al}_2\text{O}_3$ heated at $10^\circ\text{C}/\text{min}$ to $1525^\circ\text{C}$ . . . . .	14
3.6	Densification kinetics of Bayer $\text{Al}_2\text{O}_3$ doped with different concentrations of $\text{Na}_2\text{O}$ and $\text{SiO}_2$ at $1525^\circ\text{C}$ . . . . .	15
3.7	Microstructures of Bayer $\text{Al}_2\text{O}_3$ doped with a) 603 ppm $\text{SiO}_2$ and b) 529 ppm $\text{Na}_2\text{O}$ and 603 ppm $\text{SiO}_2$ after heating at $1525^\circ\text{C}$ for 8h. . . . .	16
3.8	Micrographs of a sample doped with 1029 ppm $\text{Na}_2\text{O}$ after sintering at $1525^\circ\text{C}$ for 3 h. The micrographs were recorded using a) a secondary electron detector and b) a backscattered electron detector. The arrows point at the platelet shaped beta alumina grains that form in samples doped with $\text{Na}_2\text{O}$ . The samples were not thermally etched. . . . .	17
3.9	Liquidus projection of the $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$ - $\text{Na}_2\text{O}$ ternary phase diagram. The red solid lines are isoplethal cuts representing the samples investigated in this study. The red dashed line is the $1525^\circ\text{C}$ isotherm where $\alpha$ - $\text{Al}_2\text{O}_3$ and liquid are in equilibrium. The blue dash-dot line and green dotted line are eutectic lines at which $\alpha$ - $\text{Al}_2\text{O}_3$ and liquid is in equilibrium with $\beta$ - $\text{Al}_2\text{O}_3$ or mullite, respectively. . . . .	18

# List of Tables

3.1	Physical and chemical characteristics of the as-received Bayer Al <sub>2</sub> O <sub>3</sub> powder used in this study. . . . .	8
3.2	Calculated compositions and amounts of liquid in as-received, singly doped and co-doped samples at 1525°C ( $\alpha = \alpha$ -Al <sub>2</sub> O <sub>3</sub> , $\beta = \beta$ -Al <sub>2</sub> O <sub>3</sub> , L = liquid, M = mullite). . . . .	9

# List of Symbols

- $\alpha$  The first greek letter, p. ??
- $\alpha$  The first greek letter, p. ??
- $\alpha$  The first greek letter, but we should really add some more text, though we need it to go on two lines, p. ??
- $\alpha$  The first greek letter, p. ??
- $\alpha$  The first greek letter, p. ??
- $\alpha$  The first greek letter, p. ??
- $\alpha$  The first greek letter, p. ??
- $\alpha$  The first greek letter, p. ??



# Acknowledgments

# Dedication



# Chapter 1 |

## Statement of Problem

### 1.1 section1.1

Pestorius [200] developed an algorithm to investigate propagation of finite-amplitude noise in pipes. His algorithm, based on weak shock theory, includes the effects of nonlinearity and tube wall boundary layer attenuation and dispersion. The hybrid time-frequency domain algorithm applies nonlinearity in the time domain, applies a fast Fourier transform (FFT), and then applies attenuation and dispersion in the frequency domain. Then an inverse FFT is taken to return to the time domain to propagate to the next step.

#### 1.1.1 subsection1.1.1

# Chapter 2 | Introduction

## 2.1 section2.1

When in the Course of human events, it becomes necessary for one people to dissolve the political bands which have connected them with another, and to assume among the powers of the earth, the separate and equal station to which the Laws of Nature and of Nature's God entitle them, a decent respect to the opinions of mankind requires that they should declare the causes which impel them to the separation.

## 2.2 section2.2

# Chapter 3 |

## The Effects of $\text{Na}_2\text{O}$ and $\text{SiO}_2$ on Liquid Phase Sintering of Bayer $\text{Al}_2\text{O}_3$

### 3.1 Introduction

$\text{Al}_2\text{O}_3$  is arguably the most extensively used and researched ceramic material because it is used in many large volume applications such as high temperature refractories, technical ceramics, high voltage insulators, and functional fillers. The majority of  $\text{Al}_2\text{O}_3$  applications use synthetic or specialty aluminas derived from Bayer feedstocks, such as aluminum trihydrate ( $\text{Al}(\text{OH})_3$ ), smelter grade  $\text{Al}_2\text{O}_3$  and others. Bayer process aluminas are typically 99.0 - 99.9% pure and contain  $\text{Na}_2\text{O}$ ,  $\text{CaO}$ ,  $\text{Fe}_2\text{O}_3$ , and  $\text{SiO}_2$  impurities that originate from the bauxite ore and/or Bayer process reagents (e.g.,  $\text{NaOH}$ ). The vast majority of research on the sintering of  $\text{Al}_2\text{O}_3$ , however, focuses on ultra-high purity ( $\geq 99.99\%$ ) aluminas derived from specialty feedstocks, such as ammonium alum ( $\text{NH}_4\text{Al}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$ ), boehmite ( $\gamma\text{-AlOOH}$ ) and aluminum chloride ( $\text{AlCl}_3$ ). While ultra-high purity aluminas provide the purest platform from which to conduct fundamental sintering research, that research does not usually explore the types and amounts of impurities typical of Bayer aluminas. Commercial Bayer  $\text{Al}_2\text{O}_3$  powders exist in a range of reactive grades that differ in the amount and types of these impurities. Therefore, the evaluation of specialty reactive aluminas, within the context of previous work on ultra-high purity aluminas, is a valuable contribution to industrial users and bridges

fundamental sintering research with ultra-high purity aluminas.

## 3.2 Experimental

A chemically purified 0.4  $\mu\text{m}$  median particle size Bayer process  $\text{Al}_2\text{O}_3$  powder (Almatis, Inc., Leetsdale, PA, USA) with only 2 ppm MgO was used to study the sintering of near MgO-free Bayer  $\text{Al}_2\text{O}_3$  (Figure 3.1). The powder was chemically purified by the manufacturer so that impurity levels similar to commercial high purity Bayer process aluminas were obtained after doping with  $\text{Na}_2\text{O}$  and/or  $\text{SiO}_2$ . The physical and chemical characteristics of the as-received powder are shown in Table 3.1. Chemical analysis of the as-received  $\text{Al}_2\text{O}_3$  was performed by inductively coupled plasma (ICP) emission spectroscopy (iCap 6000, Thermo Fischer Scientific, Inc., Waltham, MA, USA) after  $\text{Al}_2\text{O}_3$  samples were acid digested in a microwave digestion unit in a Teflon<sup>TM</sup> sample holder. It should be noted that the as-received Bayer  $\text{Al}_2\text{O}_3$  contained impurity levels of 90 ppm  $\text{Fe}_2\text{O}_3$ , 62 CaO, and 22 ppm  $\text{TiO}_2$ . The  $\text{Na}_2\text{O}$  and  $\text{SiO}_2$  reported after doping include the impurity concentrations in the as-received powder (29 ppm  $\text{Na}_2\text{O}$  and 103 ppm  $\text{SiO}_2$ ).

The  $\text{Al}_2\text{O}_3$  powders were doped with up to 1000 ppm  $\text{Na}_2\text{O}$  using sodium acetate ( $\text{NaC}_2\text{H}_3\text{O}_2 \cdot 3\text{H}_2\text{O}$ , ACS grade, BDH, West Chester, PA, USA), based on the procedure reported by Louet et al. [1]. The  $\text{Al}_2\text{O}_3$  powders were dispersed in a solution of sodium acetate dissolved in de-ionized water. The suspension was stirred on a magnetic stir plate for 5 h at room temperature, and held at 80°C for 24 h while stirring until the mixture was too viscous to stir, and then dried at 100°C for 24 h.

Samples were doped with up to 500 ppm  $\text{SiO}_2$  by first dissolving tetraethyl orthosilicate (TEOS,  $\text{Si}(\text{OC}_2\text{H}_5)_4$ , 98%, Aldrich Chemical Company, Inc., Milwaukee, WI, USA) in 200 proof ethanol with a few drops of de-ionized water to hydrolyze the TEOS and immediately mixed at room temperature for 5 h with either the as-received or  $\text{Na}_2\text{O}$ -doped  $\text{Al}_2\text{O}_3$  powder. The mixture was subsequently stirred at 70°C for an additional 12 h. The powder was then dried at 100°C for 2 h, followed by crushing in a mortar and pestle, and sieving to -106  $\mu\text{m}$  (US Standard 140 mesh).

Samples were prepared for sintering studies by uniaxially dry pressing the powders at 170 MPa and then cold isostatic pressing at 200 MPa (CIP, Autoclave

Engineers, Erie, PA, USA) to obtain cylindrical samples (3.0-3.5 mm long by 12.7 mm diameter or 8.5-10 mm long by 6 mm diameter) with green densities of  $59.0\% \pm 0.5\%$  of theoretical density. To investigate the sintering process, dry pressed 8.5-10 mm long by 6 mm diameter cylinders were heated at  $10^{\circ}\text{C}/\text{min}$  to  $1525^{\circ}\text{C}$  in a thermomechanical analyzer (TMA, Linseis PT1600, Robbinsville, NJ, USA). The kinetics of sintering and grain growth were evaluated on 3.0-3.5 mm long by 12.7 mm diameter samples heated at  $10^{\circ}\text{C}/\text{min}$  to  $1200^{\circ}\text{C}$  then  $5^{\circ}\text{C}/\text{min}$  to  $1525^{\circ}\text{C}$  followed by sintering at  $1525^{\circ}\text{C}$  for up to 8 h. The density of three samples of each condition was measured by the Archimedes method according to ASTM standard B962-15 [2] and the average density reported for each sintering time and temperature. For microstructure analysis, samples were first polished to a surface finish of  $1\text{ }\mu\text{m}$  and then thermally etched in air at  $1425^{\circ}\text{C}$  for 40 min. Average grain sizes were measured on SEM (ESEM, Quanta 200, FEI Company, Hillsboro, OR, USA) micrographs using a linear intercept method (ASTM Standard E112-96) [3].

## 3.3 Results

### 3.3.1 Effects of $\text{Na}_2\text{O}$ -doping

The doping experiments were designed to uniformly distribute  $\text{Na}-2\text{O}$  and  $\text{SiO}_2$  on the surfaces of the  $\text{Al}_2\text{O}_3$  particles. Upon heating the dopant  $\text{NaC}_2\text{H}_3\text{O}_2 \cdot 3\text{H}_2\text{O}$  first dehydrates and then decomposes to form  $\text{Na}_2\text{CO}_3$  above  $385^{\circ}\text{C}$  [4]. Using a video recorder, we observed that anhydrous sodium acetate melts and rapidly spreads on the surface of an  $\text{Al}_2\text{O}_3$  substrate at  $\sim 420^{\circ}\text{C}$ .  $\text{Na}_2\text{CO}_3$  melts at  $851^{\circ}\text{C}$  and subsequently decomposes to  $\text{Na}_2\text{O}$  [4]. As a result of the rapid wetting of the  $\text{Na}_2\text{O}$  precursor on the  $\text{Al}_2\text{O}_3$  substrate we conclude that  $\text{Na}_2\text{O}$  is uniformly distributed on the powder surface by the acetate doping process.

Figure 3.2 shows the shrinkage behavior of Bayer  $\text{Al}_2\text{O}_3$  doped with different  $\text{Na}_2\text{O}$  concentrations during heating to  $1525^{\circ}\text{C}$  at  $10^{\circ}\text{C}/\text{min}$ . The as-received  $\text{Al}_2\text{O}_3$  (intrinsic impurities: 29 ppm  $\text{Na}_2\text{O}$ , 103 ppm  $\text{SiO}_2$ ) begins to shrink at  $\sim 1050^{\circ}\text{C}$ , whereas shrinkage begins at  $1100^{\circ}\text{C}$  for samples doped with 1029 ppm  $\text{Na}_2\text{O}$ . The difference in density at the beginning of densification continues throughout the heating cycle. However, above  $\sim 1350^{\circ}\text{C}$  the densification rate of the  $\text{Na}_2\text{O}$  doped samples surpasses that of the as-received sample. Overall, the  $\text{Na}_2\text{O}$ -doped samples



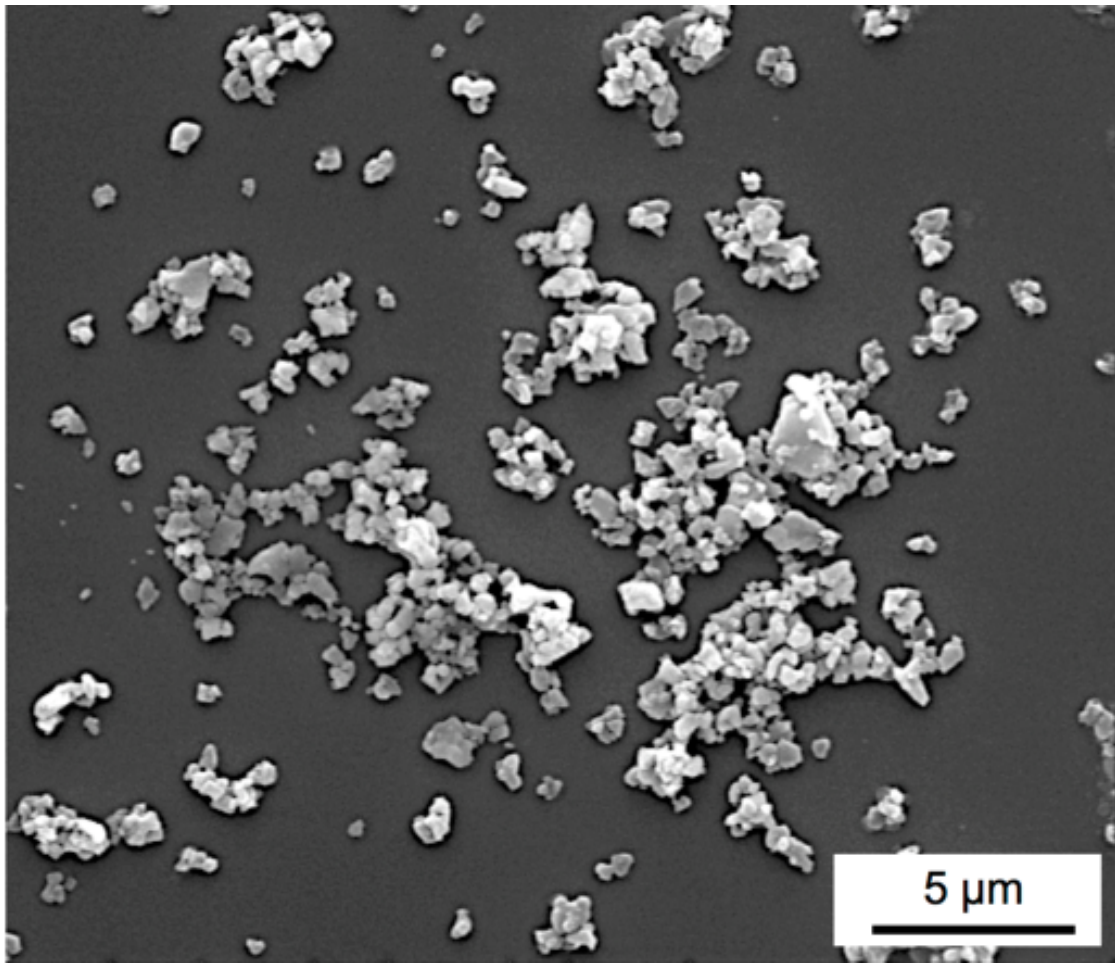
are 2.5% less dense than the as-received  $\text{Al}_2\text{O}_3$  after heating to  $1525^\circ\text{C}$ .

**Table 3.1.** Physical and chemical characteristics of the as-received Bayer Al<sub>2</sub>O<sub>3</sub> powder used in this study.

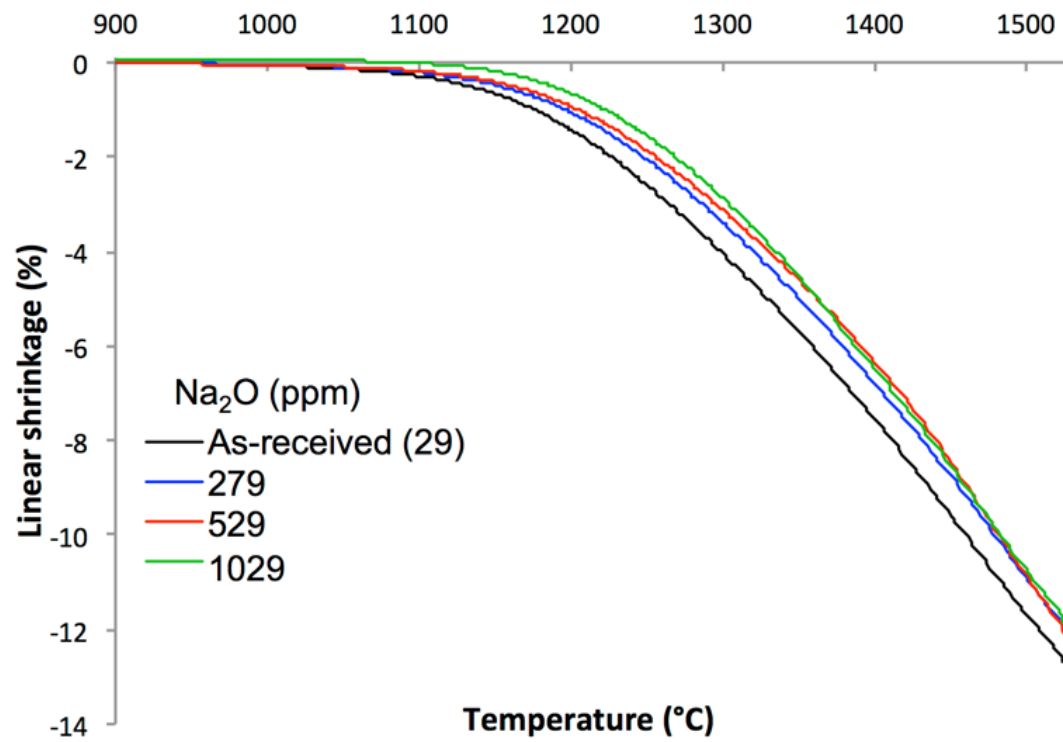
BET (m <sup>2</sup> /g)	7.4
D <sub>50</sub> (μm)	0.4
D <sub>90</sub> (μm)	1.5
	ICP (ppm)
Al <sub>2</sub> O <sub>3</sub>	99.96 %
SiO <sub>2</sub>	103
Na <sub>2</sub> O (total)	29
Fe <sub>2</sub> O <sub>3</sub>	90
CaO	62
TiO <sub>2</sub>	22
MgO	2

**Table 3.2.** Calculated compositions and amounts of liquid in as-received, singly doped and co-doped samples at 1525°C ( $\alpha = \alpha\text{-Al}_2\text{O}_3$ ,  $\beta = \beta\text{-Al}_2\text{O}_3$ , L = liquid, M = mullite).

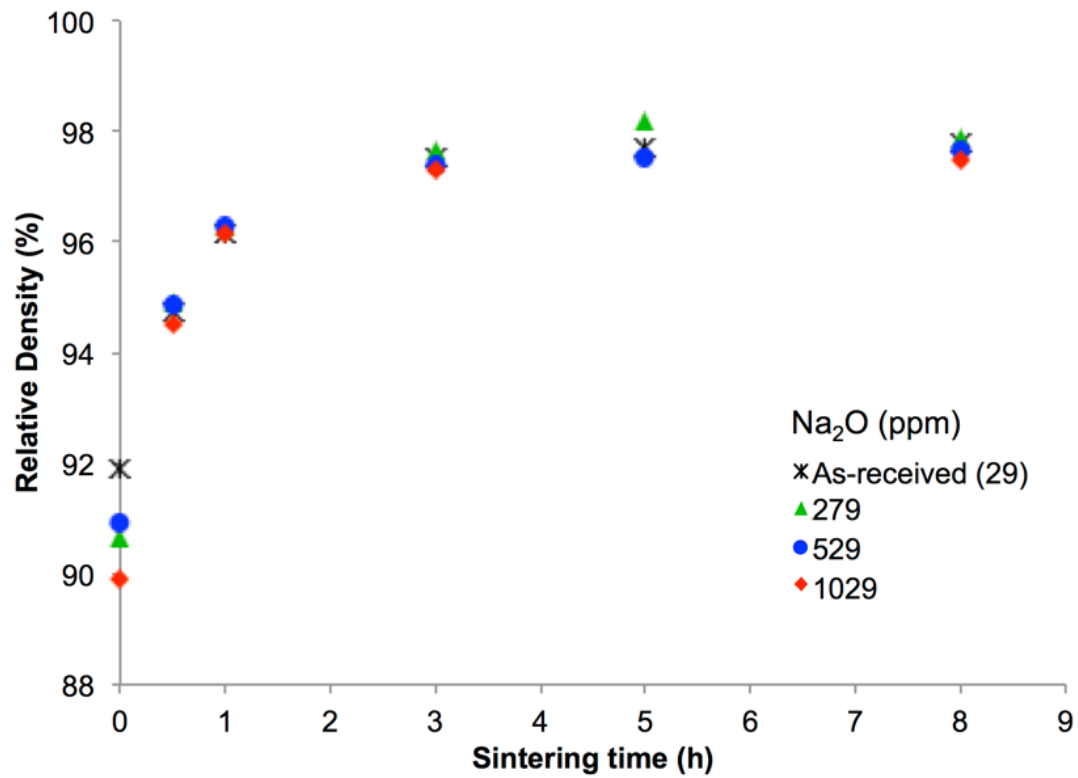
Global dopant concentration		Global $\text{Na}_2\text{O}:\text{SiO}_2$ ratio	$\text{Na}_2\text{O}:\text{SiO}_2$ ratio in Liquid	Composition of liquid (mol %)			Amount of liquid (vol. %)	Stable phases
ppm (wt.) $\text{Na}_2\text{O}/\text{SiO}_2$	ppm (mol) $\text{Na}_2\text{O}/\text{SiO}_2$			$\text{Na}_2\text{O}$	$\text{SiO}_2$	$\text{Al}_2\text{O}_3$		
As-received								
29/103	48/175	0.27	0.25	17.9	63.4	19.7	0.03%	$\alpha + \text{L}$
154/103-1029/103	253/175-1693/175	1.45-9.67	0.5	26.1	52.3	21.6	0.03%	$\alpha + \text{L} + \beta$
29/603	48/1023	0.05	0.25	16.3	65.3	18.4	0.03%	$\alpha + \text{L} + \text{M}$
154/603	253/1023	0.25	0.25	16.3	65.3	18.4	0.16%	$\alpha + \text{L}$
279/603	459/1023	0.45	0.45	24.5	54.6	20.8	0.19%	$\alpha + \text{L}$
529/603	870/1023	0.85	0.5	26.1	52.3	21.6	0.22%	$\alpha + \text{L} + \beta$
1029/603	1693/1023	1.65	0.5	26.1	52.3	21.6	0.22%	$\alpha + \text{L} + \beta$



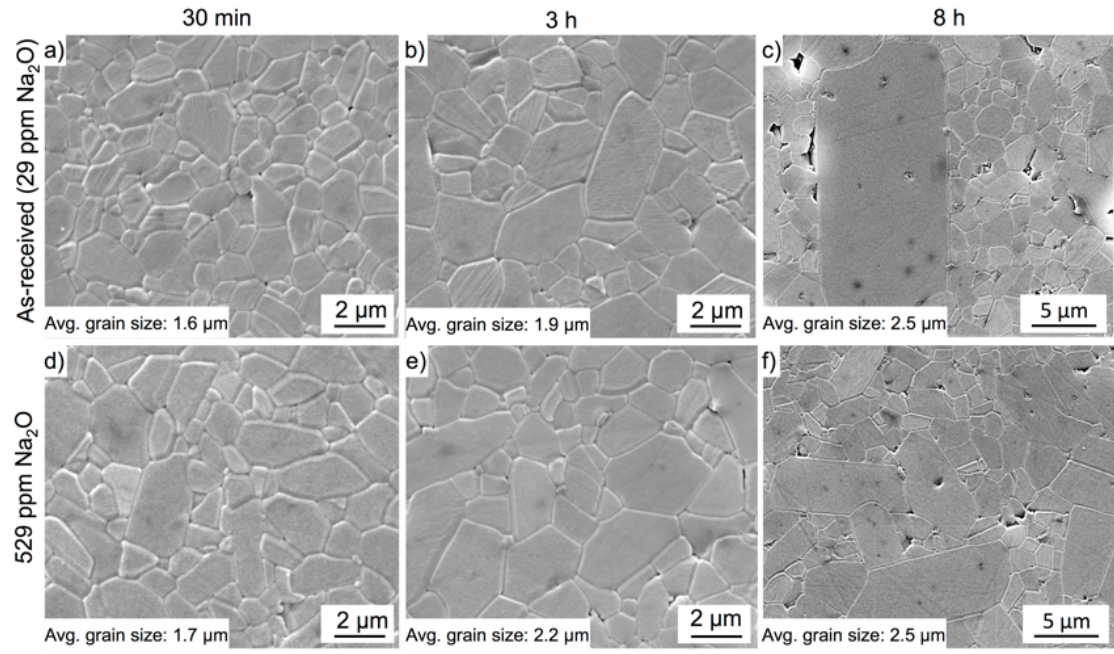
**Figure 3.1.** SEM image of as-received chemically purified Bayer Al<sub>2</sub>O<sub>3</sub> powder used in this study.



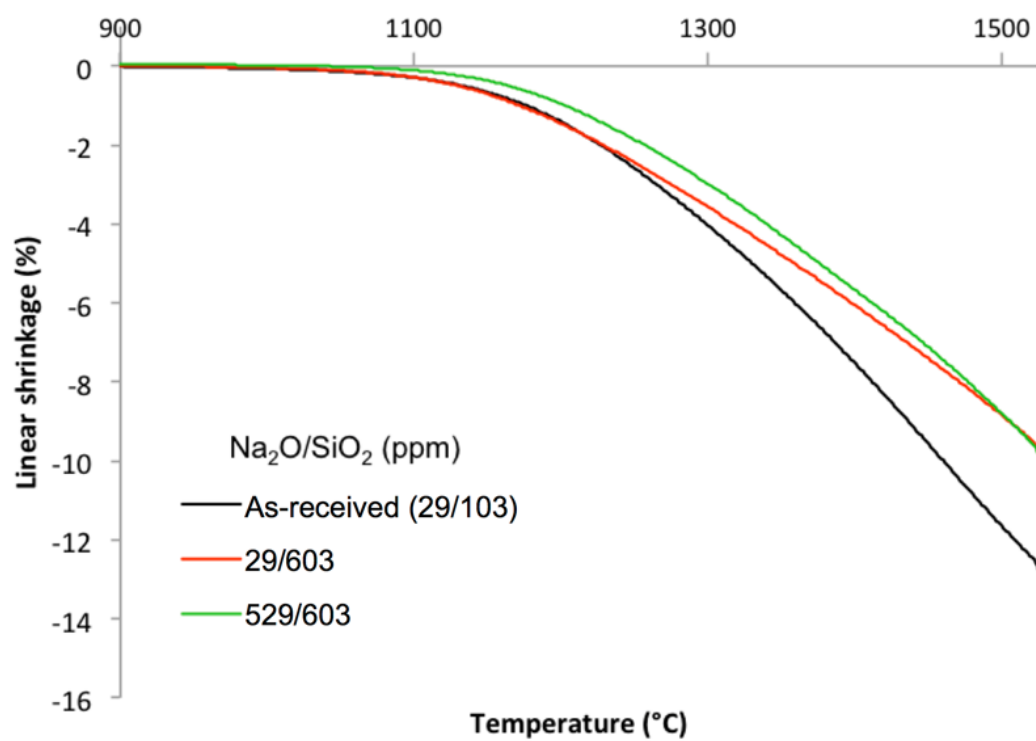
**Figure 3.2.** Dilatometer curves of as-received and singly Na<sub>2</sub>O-doped samples heated at 10°C/min to 1525°C.



**Figure 3.3.** Densification kinetics of Bayer  $\text{Al}_2\text{O}_3$  doped with different  $\text{Na}_2\text{O}$  concentrations and sintered at  $1525^\circ\text{C}$ .

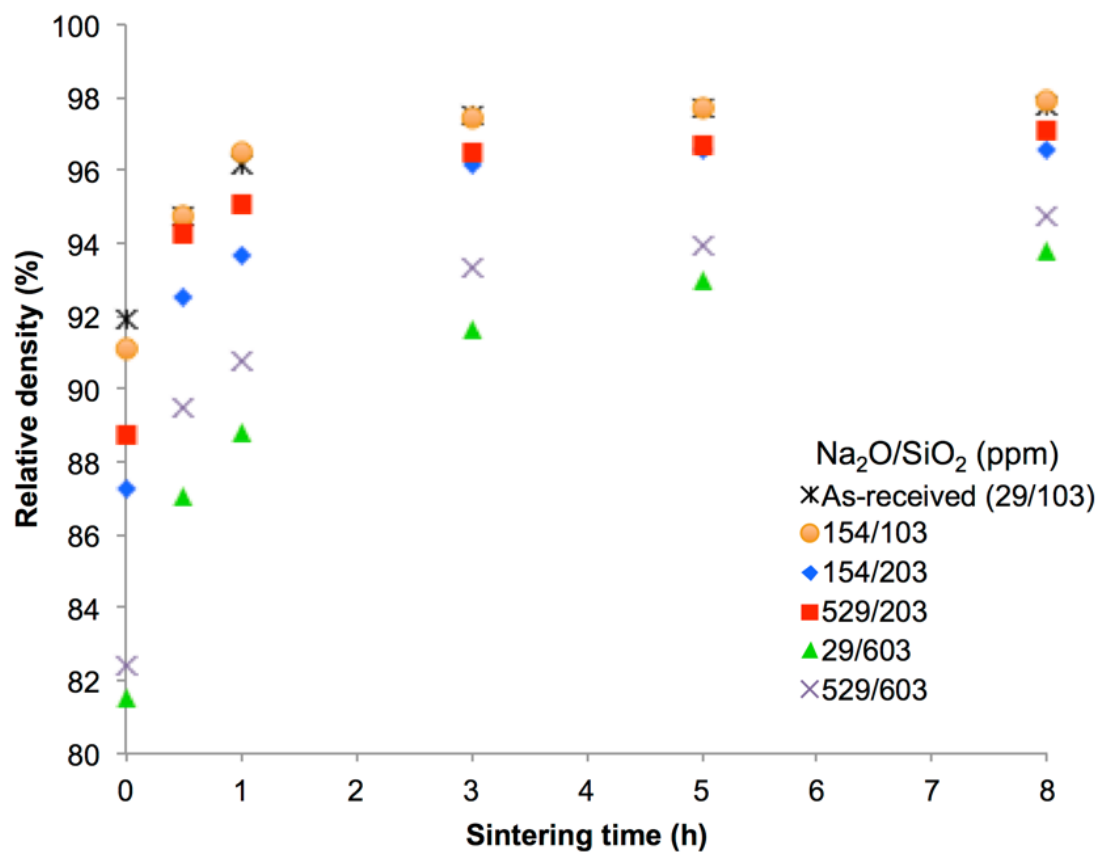


**Figure 3.4.** Microstructures of as-received and singly 529 ppm  $\text{Na}_2\text{O}$  doped samples after 30 min, 3 h and 8 h at  $1525^\circ\text{C}$ .

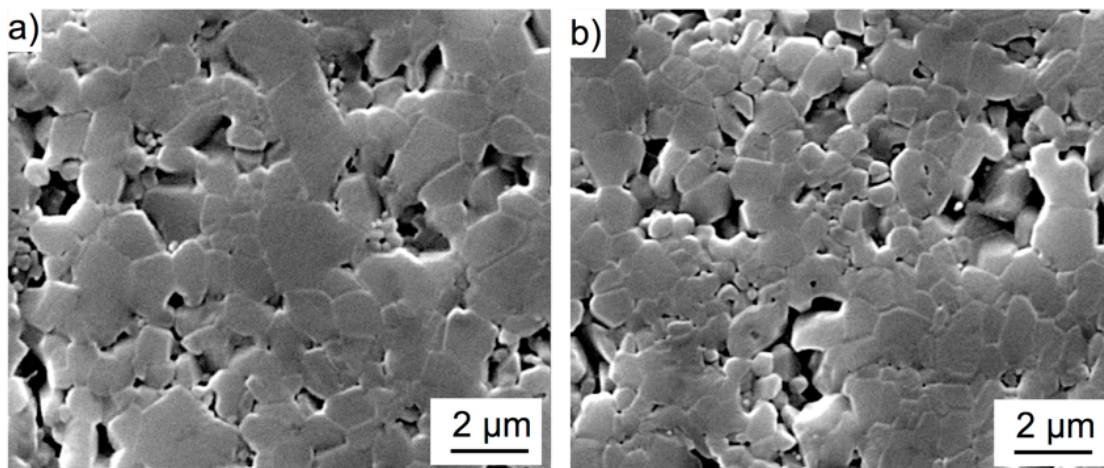


**Figure 3.5.** Dilatometer curves of as-received, singly  $\text{SiO}_2$ -doped, and  $\text{Na}_2\text{O}/\text{SiO}_2$ -doped Bayer  $\text{Al}_2\text{O}_3$  heated at  $10^\circ\text{C}/\text{min}$  to  $1525^\circ\text{C}$ .

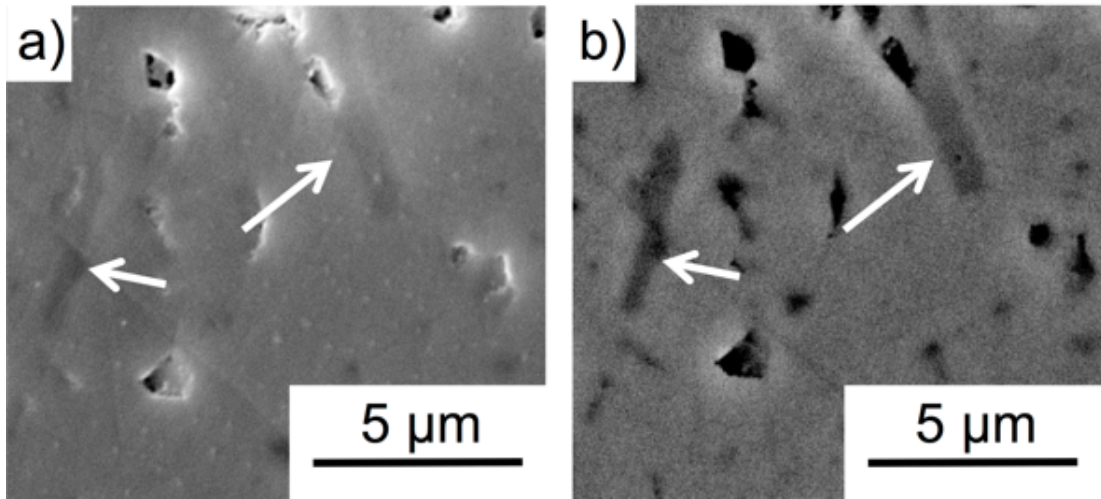




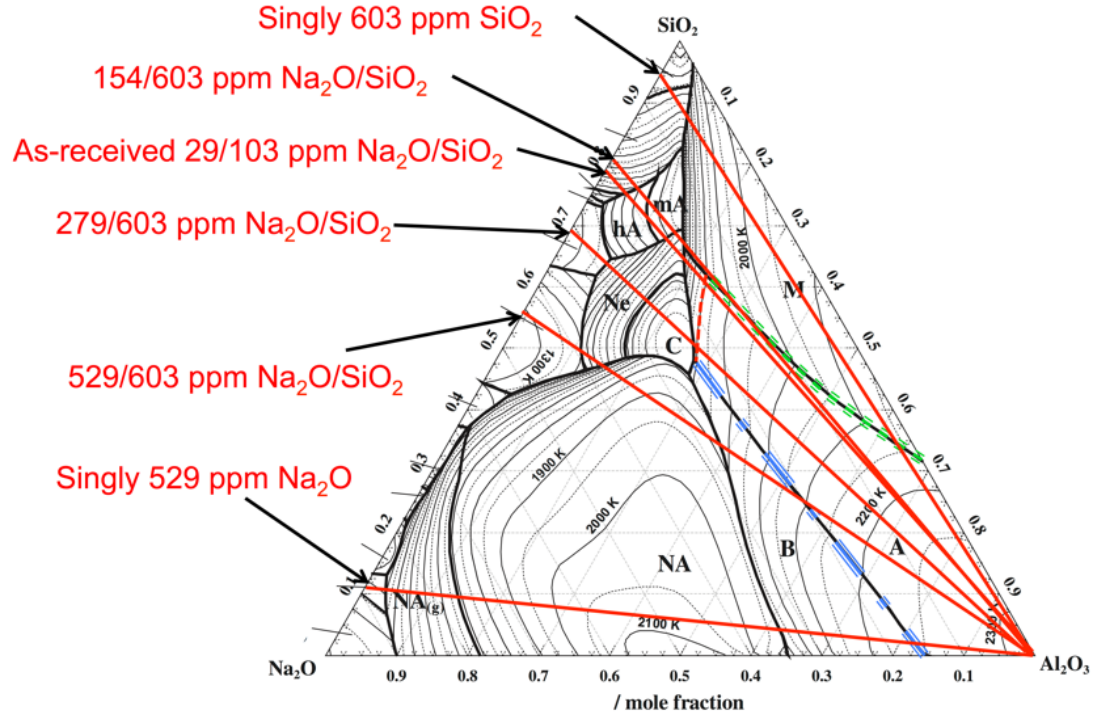
**Figure 3.6.** Densification kinetics of Bayer  $\text{Al}_2\text{O}_3$  doped with different concentrations of  $\text{Na}_2\text{O}$  and  $\text{SiO}_2$  at  $1525^\circ\text{C}$ .



**Figure 3.7.** Microstructures of Bayer Al<sub>2</sub>O<sub>3</sub> doped with a) 603 ppm SiO<sub>2</sub> and b) 529 ppm Na<sub>2</sub>O and 603 ppm SiO<sub>2</sub> after heating at 1525°C for 8h.



**Figure 3.8.** Micrographs of a sample doped with 1029 ppm  $\text{Na}_2\text{O}$  after sintering at  $1525^\circ\text{C}$  for 3 h. The micrographs were recorded using a) a secondary electron detector and b) a backscattered electron detector. The arrows point at the platelet shaped beta alumina grains that form in samples doped with  $\text{Na}_2\text{O}$ . The samples were not thermally etched.



**Figure 3.9.** Liquidus projection of the  $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$ - $\text{Na}_2\text{O}$  ternary phase diagram. The red solid lines are isoplethal cuts representing the samples investigated in this study. The red dashed line is the  $1525^\circ\text{C}$  isotherm where  $\alpha$ - $\text{Al}_2\text{O}_3$  and liquid are in equilibrium. The blue dash-dot line and green dotted line are eutectic lines at which  $\alpha$ - $\text{Al}_2\text{O}_3$  and liquid is in equilibrium with  $\beta$ - $\text{Al}_2\text{O}_3$  or mullite, respectively.

# Chapter 4 | Powder Chemistry Effects on the Sintering Behavior of MgO-doped Bayer Alumina

## 4.1 Introduction

When in the Course of human events, it becomes necessary for one people to dissolve the political bands which have connected them with another, and to assume among the powers of the earth, the separate and equal station to which the Laws of Nature and of Nature's God entitle them, a decent respect to the opinions of mankind requires that they should declare the causes which impel them to the separation.

## 4.2 More Declaration

We hold these truths to be self-evident, that all men are created equal, that they are endowed by their Creator with certain unalienable Rights, that among these are Life, Liberty and the pursuit of Happiness. –That to secure these rights, Governments are instituted among Men, deriving their just powers from the consent of the governed, –That whenever any Form of Government becomes destructive of these ends, it is the Right of the People to alter or to abolish it, and to institute new Government, laying its foundation on such principles and organizing its powers in such form, as to them shall seem most likely to effect their Safety and Happiness. Prudence, indeed, will dictate that Governments long established should not be

changed for light and transient causes; and accordingly all experience hath shewn, that mankind are more disposed to suffer, while evils are sufferable, than to right themselves by abolishing the forms to which they are accustomed.

#### **4.2.1 Some nonsense here**

But when a long train of abuses and usurpations, pursuing invariably the same Object evinces a design to reduce them under absolute Despotism, it is their right, it is their duty, to throw off such Government, and to provide new Guards for their future security. –Such has been the patient sufferance of these Colonies; and such is now the necessity which constrains them to alter their former Systems of Government.

#### **4.2.2 Some additional nonsense here**

The history of the present King of Great Britain [George III] is a history of repeated injuries and usurpations, all having in direct object the establishment of an absolute Tyranny over these States. To prove this, let Facts be submitted to a candid world.

# Chapter 5 | Powder Chemistry Effects on Grain Boundaries During Den-sification of Bayer Alumina

## 5.1 Introduction

When in the Course of human events, it becomes necessary for one people to dissolve the political bands which have connected them with another, and to assume among the powers of the earth, the separate and equal station to which the Laws of Nature and of Nature's God entitle them, a decent respect to the opinions of mankind requires that they should declare the causes which impel them to the separation.

## 5.2 More Declaration

We hold these truths to be self-evident, that all men are created equal, that they are endowed by their Creator with certain unalienable Rights, that among these are Life, Liberty and the pursuit of Happiness. –That to secure these rights, Governments are instituted among Men, deriving their just powers from the consent of the governed, –That whenever any Form of Government becomes destructive of these ends, it is the Right of the People to alter or to abolish it, and to institute new Government, laying its foundation on such principles and organizing its powers in such form, as to them shall seem most likely to effect their Safety and Happiness. Prudence, indeed, will dictate that Governments long established should not be

changed for light and transient causes; and accordingly all experience hath shewn, that mankind are more disposed to suffer, while evils are sufferable, than to right themselves by abolishing the forms to which they are accustomed. But when a long train of abuses and usurpations, pursuing invariably the same Object evinces a design to reduce them under absolute Despotism, it is their right, it is their duty, to throw off such Government, and to provide new Guards for their future security. —Such has been the patient sufferance of these Colonies; and such is now the necessity which constrains them to alter their former Systems of Government. The history of the present King of Great Britain [George III] is a history of repeated injuries and usurpations, all having in direct object the establishment of an absolute Tyranny over these States. To prove this, let Facts be submitted to a candid world.



## Chapter 6 |

# $\beta$ -Al<sub>2</sub>O<sub>3</sub>: A Model System for the Formation of Second Phases in Al<sub>2</sub>O<sub>3</sub>

### 6.1 Introduction

When in the Course of human events, it becomes necessary for one people to dissolve the political bands which have connected them with another, and to assume among the powers of the earth, the separate and equal station to which the Laws of Nature and of Nature's God entitle them, a decent respect to the opinions of mankind requires that they should declare the causes which impel them to the separation.

### 6.2 More Declaration

We hold these truths to be self-evident, that all men are created equal, that they are endowed by their Creator with certain unalienable Rights, that among these are Life, Liberty and the pursuit of Happiness. –That to secure these rights, Governments are instituted among Men, deriving their just powers from the consent of the governed, –That whenever any Form of Government becomes destructive of these ends, it is the Right of the People to alter or to abolish it, and to institute new Government, laying its foundation on such principles and organizing its powers in such form, as to them shall seem most likely to effect their Safety and Happiness. Prudence, indeed, will dictate that Governments long established should not be

changed for light and transient causes; and accordingly all experience hath shewn, that mankind are more disposed to suffer, while evils are sufferable, than to right themselves by abolishing the forms to which they are accustomed. But when a long train of abuses and usurpations, pursuing invariably the same Object evinces a design to reduce them under absolute Despotism, it is their right, it is their duty, to throw off such Government, and to provide new Guards for their future security. —Such has been the patient sufferance of these Colonies; and such is now the necessity which constrains them to alter their former Systems of Government. The history of the present King of Great Britain [George III] is a history of repeated injuries and usurpations, all having in direct object the establishment of an absolute Tyranny over these States. To prove this, let Facts be submitted to a candid world.

# Chapter 7 |

## Summary and Future Work

### 7.1 Introduction

When in the Course of human events, it becomes necessary for one people to dissolve the political bands which have connected them with another, and to assume among the powers of the earth, the separate and equal station to which the Laws of Nature and of Nature's God entitle them, a decent respect to the opinions of mankind requires that they should declare the causes which impel them to the separation.

### 7.2 More Declaration

We hold these truths to be self-evident, that all men are created equal, that they are endowed by their Creator with certain unalienable Rights, that among these are Life, Liberty and the pursuit of Happiness. —That to secure these rights, Governments are instituted among Men, deriving their just powers from the consent of the governed, —That whenever any Form of Government becomes destructive of these ends, it is the Right of the People to alter or to abolish it, and to institute new Government, laying its foundation on such principles and organizing its powers in such form, as to them shall seem most likely to effect their Safety and Happiness. Prudence, indeed, will dictate that Governments long established should not be changed for light and transient causes; and accordingly all experience hath shewn, that mankind are more disposed to suffer, while evils are sufferable, than to right themselves by abolishing the forms to which they are accustomed. But when a long train of abuses and usurpations, pursuing invariably the same Object evinces

a design to reduce them under absolute Despotism, it is their right, it is their duty, to throw off such Government, and to provide new Guards for their future security. —Such has been the patient sufferance of these Colonies; and such is now the necessity which constrains them to alter their former Systems of Government. The history of the present King of Great Britain [George III] is a history of repeated injuries and usurpations, all having in direct object the establishment of an absolute Tyranny over these States. To prove this, let Facts be submitted to a candid world.

# Bibliography

- [1] LOUET, N., M. GONON, and G. FANTOZZI (2005) “Influence of the amount of Na<sub>2</sub>O and SiO<sub>2</sub> on the sintering behavior and on the microstructural evolution of a Bayer alumina powder,” *Ceramics international*, **31**(7), pp. 981–987.
- [2] STANDARD, A. (2015) “B962-15 Standard Test Method for Density of Compacted or Sintered Powder Metallurgy (PM) Products Using Archimedes’ Principle,” .  
URL [www.astm.org](http://www.astm.org)
- [3] ——— (2013) “E112-13: Standard Test Methods for Determining Average Grain Size,” *West Conshocken*.  
URL [www.astm.org](http://www.astm.org)
- [4] JUDD, M., B. PLUNKETT, and M. POPE (1974) “The thermal decomposition of calcium, sodium, silver and copper (II) acetates,” *Journal of Thermal Analysis and Calorimetry*, **6**(5), pp. 555–563.

# **Vita**

**Tobias Frueh**

The details of my childhood are inconsequential.