

# SUMMARY

**QUESTION-1:** Write a generic function which will find all 4, 8 & m-paths between two points (x1, y1) & (x2, y2) in an image using python.

Language/Libraries Used: → Python  
→ NumPy  
→ CV2 (OpenCV)

Description of Variables Used:

- **I:** An Image as 2D matrix:

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 0 | 3 | 2 | 4 |
| 4 | 3 | 4 | 0 | 2 |
| 2 | 2 | 1 | 3 | 0 |
| 2 | 4 | 0 | 2 | 3 |
| 3 | 2 | 4 | 1 | 0 |

- **x1, y1, x2, y2:** Coordinates of start point P(x1, y1) & end point Q(x2, y2). For an example we have taken P(3, 0) & Q(1, 4) for the testing purpose.
- **V:** A set of values of Intensities which are considered Foreground. For an example we have taken  $V = \{4, 2\}$  for the testing purpose.
- **path\_type:** A variable which can takes values as 4, 8 or 10 for 4-path, 8-path and m-path respectively. We have tested the code on all 3 types of paths.

- Input Image Matrix (I)

|   |  |
|---|--|
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |

|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 0 | 3 | 2 | 4 |
| 4 | 3 | 4 | 0 | 2 |
| 2 | 2 | 1 | 3 | 0 |
| 2 | 4 | 0 | 2 | 3 |
| 3 | 2 | 4 | 1 | 0 |

- Input Image Matrix with  $V = \{4, 2\}$  as foreground.

FOREGROUND  
BACKGROUND



|   |   |   |   |   |
|---|---|---|---|---|
| 1 | 0 | 3 | 2 | 4 |
| 4 | 3 | 4 | 0 | 2 |
| 2 | 2 | 1 | 3 | 0 |
| 2 | 4 | 0 | 2 | 3 |
| 3 | 2 | 4 | 1 | 0 |

# OUTPUT ANALYSIS

For the Path Type: 10

↳ Path Type: 10

Length of Path #1: 6

Path #1: (3,0):2 -> (2,0):2 -> (2,1):2 -> (1,2):4 -> (0,3):2 -> (0,4):4 -> (1,4):2

Length of Path #2: 6

Path #2: (3,0):2 -> (3,1):4 -> (2,1):2 -> (1,2):4 -> (0,3):2 -> (0,4):4 -> (1,4):2

Total 2 10-path exists.

Length of Shortest Path: 6

Shortest Path #1: (3,0):2 -> (2,0):2 -> (2,1):2 -> (1,2):4 -> (0,3):2 -> (0,4):4 -> (1,4):2

Shortest Path #2: (3,0):2 -> (3,1):4 -> (2,1):2 -> (1,2):4 -> (0,3):2 -> (0,4):4 -> (1,4):2

| PATH-1 |   |   |   |   |
|--------|---|---|---|---|
| 1      | 0 | 3 | 2 | 4 |
| 4      | 3 | 4 | 0 | 2 |
| 2      | 2 | 1 | 3 | 0 |
| 2      | 4 | 0 | 2 | 3 |
| 3      | 2 | 4 | 1 | 0 |

| PATH-1   |       |       |
|----------|-------|-------|
| Step No. | From  | To    |
| 1        | (3,0) | (2,0) |
| 2        | (2,0) | (2,1) |
| 3        | (2,1) | (1,2) |
| 4        | (1,2) | (0,3) |
| 5        | (0,3) | (0,4) |
| 6        | (0,4) | (1,4) |

| PATH-2 |   |   |   |   |
|--------|---|---|---|---|
| 1      | 0 | 3 | 2 | 4 |
| 4      | 3 | 4 | 0 | 2 |
| 2      | 2 | 1 | 3 | 0 |
| 2      | 4 | 0 | 2 | 3 |
| 3      | 2 | 4 | 1 | 0 |

| PATH-2   |       |       |
|----------|-------|-------|
| Step No. | From  | To    |
| 1        | (3,0) | (3,1) |
| 2        | (3,1) | (2,1) |
| 3        | (2,1) | (1,2) |
| 4        | (1,2) | (0,3) |
| 5        | (0,3) | (0,4) |
| 6        | (0,4) | (1,4) |

## For the Path Type: 8

Path Type: 8

Length of Path #1: 4

Path #1: (3,0):2 → (2,1):2 → (1,2):4 → (0,3):2 → (1,4):2

Length of Path #2: 5

Path #2: (3,0):2 → (2,0):2 → (2,1):2 → (1,2):4 → (0,3):2 → (1,4):2

Length of Path #3: 5

Path #3: (3,0):2 → (2,1):2 → (1,2):4 → (0,3):2 → (0,4):4 → (1,4):2

Total 3 8-path exists.

Length of Shortest Path: 4

Shortest Path #1: (3,0):2 → (2,1):2 → (1,2):4 → (0,3):2 → (1,4):2

| PATH-1 |   |   |   |   |
|--------|---|---|---|---|
| 1      | 0 | 3 | 2 | 4 |
| 4      | 3 | 4 | 0 | 2 |
| 2      | 2 | 1 | 3 | 0 |
| 2      | 4 | 0 | 2 | 3 |
| 3      | 2 | 4 | 1 | 0 |

| PATH-1   |       |       |
|----------|-------|-------|
| Step No. | From  | To    |
| 1        | (3,0) | (2,1) |
| 2        | (2,1) | (1,2) |
| 3        | (1,2) | (0,3) |
| 4        | (0,3) | (1,4) |

| PATH-2 |   |   |   |   |
|--------|---|---|---|---|
| 1      | 0 | 3 | 2 | 4 |
| 4      | 3 | 4 | 0 | 2 |
| 2      | 2 | 1 | 3 | 0 |
| 2      | 4 | 0 | 2 | 3 |
| 3      | 2 | 4 | 1 | 0 |

| PATH-2   |       |       |
|----------|-------|-------|
| Step No. | From  | To    |
| 1        | (3,0) | (2,0) |
| 2        | (2,0) | (2,1) |
| 3        | (2,1) | (1,2) |
| 4        | (1,2) | (0,3) |
| 5        | (0,3) | (1,4) |

| PATH-3 |   |   |   |   |
|--------|---|---|---|---|
| 1      | 0 | 3 | 2 | 4 |
| 4      | 3 | 4 | 0 | 2 |
| 2      | 2 | 1 | 3 | 0 |
| 2      | 4 | 0 | 2 | 3 |
| 3      | 2 | 4 | 1 | 0 |

| PATH-3   |       |       |
|----------|-------|-------|
| Step No. | From  | To    |
| 1        | (3,0) | (2,1) |
| 2        | (2,1) | (1,2) |
| 3        | (1,2) | (0,3) |
| 4        | (0,3) | (0,4) |
| 5        | (0,4) | (1,4) |

### For the Path Type: 4

- No path found.



## RESULTS

- The total number of **m-path between P & Q is 2.**
- M-Path\_1 is  $(3,0) \Rightarrow (2,0) \Rightarrow (2,1) \Rightarrow (1,2) \Rightarrow (0,3) \Rightarrow (0,4) \Rightarrow (1,4)$  and has length of path as 6.
- M-Path\_2 is  $(3,0) \Rightarrow (3,1) \Rightarrow (2,1) \Rightarrow (1,2) \Rightarrow (0,3) \Rightarrow (0,4) \Rightarrow (1,4)$  and has length of path as 6.
- Since we have two m-paths of same length, both m-path\_1 and m-path\_2 are the shortest m-paths between P & Q
- The total number of **8-path between P & Q is 3.**
- 8-Path\_1 is  $(3,0) \Rightarrow (2,1) \Rightarrow (1,2) \Rightarrow (0,3) \Rightarrow (1,4)$  and has length of path as 4.
- 8-Path\_2 is  $(3,0) \Rightarrow (2,0) \Rightarrow (2,1) \Rightarrow (1,2) \Rightarrow (0,3) \Rightarrow (1,4)$  and has length of path as 5.
- 8-Path\_3 is  $(3,0) \Rightarrow (2,1) \Rightarrow (1,2) \Rightarrow (0,3) \Rightarrow (0,4) \Rightarrow (1,4)$  and has length of path as 5.
- The shortest 8-path is the '8-Path\_1' and its length is 4.
- The **4-path between P & Q does not exist** for the given image matrix as both possible 4-paths across  $(2,1)$  and  $(4,2)$  does not have any 4-adjacent pixel next to them.

## **QUESTION 2: Digital Image Creation (non-overlapping rectangles) using Python.**

Language/Libraries Used: → Python  
→ NumPy  
→ CV2 (OpenCV)

### Description of Variables Used:

**M x N** -- Is the image size.

**Border** -- Black Border of thickness (Border).

**n** -- Number of non-overlapping rectangles.

**[w1, w2]** -- Width uniformly distributed in range [w1, w2] for rectangles.

**Alpha** -- Rectangles height to width ratio.

**Orientation** -- Landscape (1) or Portrait (2).

**Vf and Vb** -- Foreground and background intensity (optional).

**M\_total, N\_total** -- Final dimension after adding border.

```
M_total = M + 2 * (border)
N_total = N + 2 * (border)
```

**corner\_i, corner\_j** -- Corner pixel point of the rectangles to be drawn.

## Discussion Related to Function Used in the Code:

```
def valid_rectangle(image_bg, M_total, N_total, height, width, border, Vf, rect_orientation, corner_i, corner_j):
```

→ Above function is used in our code to check if the new rectangle to be drawn has valid and non-overlapping corners with any other existing rectangle.

→ In this function, code for both landscape and portrait orientation has written.

→ This function is recursively called to find out non-overlapping space for the new rectangle.



```
def create_rectangles(M, N, border, n, w1, w2, alpha, orientation, Vf=[0], Vb=[255]):
```

→ This function is used in our code to draw valid rectangles and to create final image using `cv2.imwrite()` OpenCV function.

→ Vf and Vb values are passed in function argument itself in case if Vf(black) and Vb(white) values are not passed by the user.

→ In case of exception *RecursionError* i.e., if the condition of non-overlapping rectangles is not satisfied, we increase the size of the image to  $(2*M) \times (2*N)$  and redraw the rectangles.



```
def main():
```

→ In `main()` function all the value of parameter is passed and under this function only `create_rectangles` function is called.

# OUTPUT ANALYSIS

**CASE-I:** All the parameters are passed along with  $V_f = [0, 128]$  and  $V_b = [129, 255]$

## INPUT

```
M = 300          # no of rows
N = 200          # no of columns
border = 5       # size of the border
n = 50           # number of rectangles to fit
w1 = 20          # lower bound for the width of rectangle
w2 = 30          # upper bound for the width of rectangle
alpha = 2        # fixed [height, width] ratio of
rectangle
orientation = [1, 2] # uniformly distributed orientation of
rectangle [portrait, landscape]
Vf = [0, 128]     # foreground colors distributed
uniformly, if not provided then default = 0
Vb = [129, 255]   # background colors distributed
uniformly, if not provided then default = 255
```

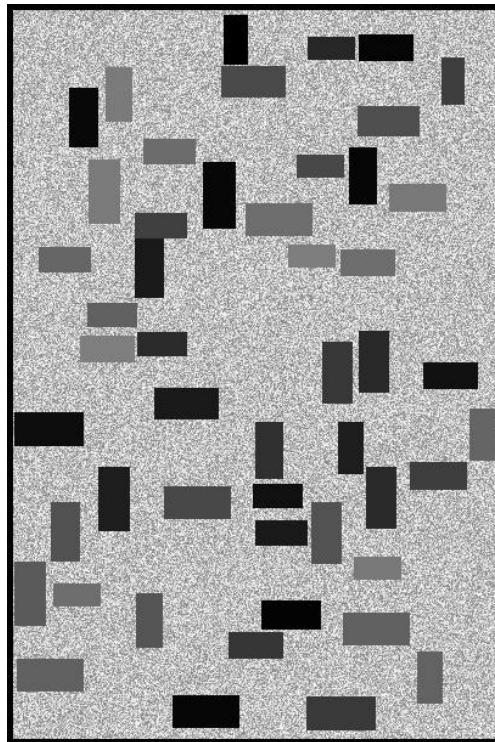
### Function Call:

```
create_rectangles(M, N, border, n, w1, w2, alpha, orientation,
Vf, Vb)
```



## **RESULT CASE-I:**

**Final shape of the image: (610, 410)**



- From this output, we can see all the rectangles are non-overlapping.
- Rectangles colour intensity is uniformly distributed over range  $V_f$  given, also same for the  $V_b$ .

**CASE-II:** All the parameters are same as previous case except **Vf** and **Vb** values not being passed as they are optional.

## INPUT

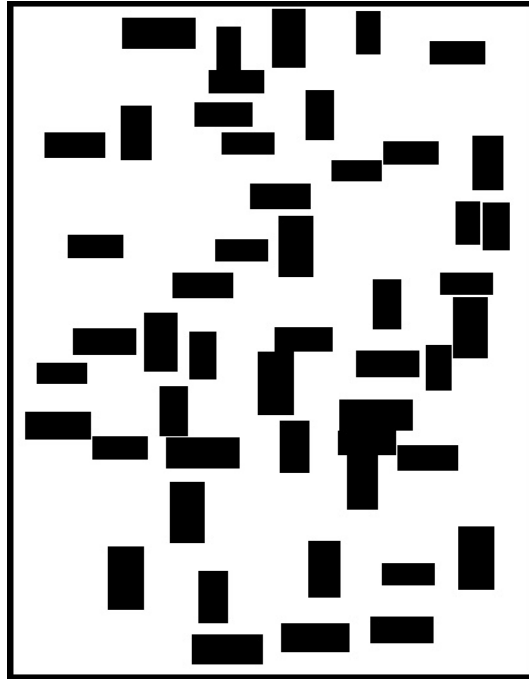
```
M = 300          # no of rows
N = 200          # no of columns
border = 5       # size of the border
n = 50           # number of rectangles to fit
w1 = 20          # lower bound for the width of rectangle
w2 = 30          # upper bound for the width of rectangle
alpha = 2        # fixed [height, width] ratio of
rectangle        #
orientation = [1, 2] # uniformly distributed orientation of
rectangle [portrait, landscape]
```

### Function Call:

```
create_rectangles(M, N, border, n, w1, w2, alpha, orientation)
```

## RESULT CASE-II:

**Final shape of the image: (610, 410)**



- From this image, it is clear when  $V_f$  and  $V_b$  values are not provided we get non-overlapping rectangles with  $V_f=0$  and  $V_b=255$  along with black border.