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Homework 1. Fixpoints and grammar filters
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Introduction
You are a reader for Computer Science 181, which asks students to submit grammars that solve various problems. However, many of the submitted grammars are trivially wrong, in several ways. Here is one. Some grammars contain blind-alley rules, that is, grammar rules for which it is
impossible to derive a string of terminal symbols. Blind-alley rules do not affect the language or parse trees generated by a grammar, so in some sense they don't make the answers wrong, but they're noise and they make grading harder. You'd like to filter out the noise, and just grade the
useful parts of each grammar.
You've heard that OCaml is a good language for writing compilers and whatnot, so you decide to give it a try for this application. While you're at it, you have a background in fixed point and periodic point theory, so you decide to give it a try too.
Definitions
fixed point
      (of a function f) A point x such that f x = x. In this description we are using OCaml notation, in which functions always have one argument and parentheses are not needed around arguments.
computed fixed point
      (of a function f with respect to an initial point x) A fixed point of f computed by calculating x, f x, f (f x), etc., stopping when a fixed point is found for f. If no fixed point is ever found by this procedure, the computed fixed point is not defined for f and x.
periodic point
      (of a function f with period p) A point x such that f (f ... (f x)) = x, where there are p occurrences of f in the call. That is, a periodic point is like a fixed point, except the function returns to the point after p iterations instead of 1 iteration. Every point is a periodic point for
      p=0. A fixed point is a periodic point for p=1.
computed periodic point
      (of a function f with respect to a period p and an initial point x) A periodic point of f with period p, computed by calculating x, f x, f (f x), f (f (f x)), etc., stopping when a periodic point with period p is found for f. The computed periodic point need not be equal to x. If no
      periodic point is ever found by this procedure, the computed periodic point is not defined for f, p, and x.
symbol
      A symbol used in a grammar. It can be either a nonterminal symbol or a terminal symbol; each kind of symbol has a value, whose type is arbitrary. A symbol has the following OCaml type:
       type ('nonterminal, 'terminal) symbol =
           N of 'nonterminal
           T of 'terminal
right hand side
      A list of symbols. It corresponds to the right hand side of a single grammar rule. A right hand side can be empty.
rule
      A pair, consisting of (1) a nonterminal value (the left hand side of the grammar rule) and (2) a right hand side.
      A pair, consisting of a start symbol and a list of rules. The start symbol is a nonterminal value.
Assignment
Let's warm up by modeling sets using OCaml lists. The empty list represents the empty set, and if the list t represents the set T, then the list h::t represents the set {h}UT. Although sets by definition do not contain duplicates, the lists that represent sets can contain duplicates. Another set
of warmup exercises will compute fixed points. Finally, you can write a function that filters blind alleys.
   1. Write a function subset a b that returns true iff (i.e., if and only if) a\subseteq b, i.e., iff the set represented by the list b. Every set is a subset of itself. This function should be curried, and should be generic to lists of any type: that is, the type of
      subset should be a generalization of 'a list -> 'a list -> bool.
   2. Write a function equal_sets a b that returns true iff the represented sets are equal.
   3. Write a function set_union a b that returns a list representing a \cup b.
   4. Write a function set_all_union a that returns a list representing \bigcup [x \in a]x, i.e., the union of all the members of the set a; a should represent a set of sets.
   5. Russell's Paradox involves asking whether a set is a member of itself. Write a function self_member s that returns true iff the set represented by s is a member of itself, and explain in a comment why your function is correct; or, if it's not possible to write such a function in OCaml,
      explain why not in a comment.
   6. Write a function computed_fixed_point eq f x that returns the computed fixed point for f with respect to x, assuming that eq is the equality predicate for f's domain. A common case is that eq will be (=), that is, the builtin equality predicate of OCaml; but any predicate can be
      used. If there is no computed fixed point, your implementation can do whatever it wants: for example, it can print a diagnostic, or go into a loop, or send nasty email messages to the user's relatives.
   7. Write a function computed_periodic_point eq f p x that returns the computed periodic point for f with period p and with respect to x, assuming that eq is the equality predicate for f's domain.
   8. Write a function whileseq s p x that returns the longest list [x; s x; s (s x); ...] such that p e is true for every element e in the list. That is, if p x is false, return []; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s x) is false, return [x]; otherwise if p (s
      example, whileseq ((+) 3) ((>) 10) 0 returns [0; 3; 6; 9]. Your implementation can assume that p eventually returns false.
   9. OK, now for the real work. Write a function filter_blind_alleys g that returns a copy of the grammar g with all blind-alley rules removed. This function should preserve the order of rules: that is, all rules that are returned should be in the same order as the rules in g.
  10. Supply at least one test case for each of the above functions in the style shown in the sample test cases below. When testing the function F, call the test cases my F test1, etc. For example, for subset your first test case should be called my subset test0. Your test
      cases should exercise all the above functions, even though the sample test cases do not.
Your code should follow these guidelines:
   1. Your code may use the <u>Stdlib</u> and <u>List</u> modules, but it should use no other modules other than your own code.
  2. It is OK (and indeed encouraged) for your solutions to be based on one another; for example, it is fine for filter_blind_alleys to use equal_sets and computed_fixed_point.
   3. Your code should prefer pattern matching to conditionals when pattern matching is natural.
   4. Your code should be free of side effects such as loops, assignment, input/output, incr, and decr. Use recursion instead of loops.
   5. Simplicity is more important than efficiency, but your code should avoid using unnecessary time and space when it is easy to do so. For example, instead of repeating a expression, compute its value once and reuse the computed value.
   6. The test cases below should work with your program. You are unlikely to get credit for it otherwise.
Assess your work by writing a brief after-action report that summarizes why you solved the problem the way you did, other approaches that you considered and rejected (and why you rejected them), and any weaknesses in your solution in the context of its intended application. This report
should be a plain text file that is no more than 2000 characters long. See Resources for oral presentations and written reports for advice on how to write assessments; admittedly much of the advice there is overkill for the simple kind of summary we're looking for here.
Submit
Submit three files. The file hw1.ml should implement the abovementioned functions, along with any auxiliary types and functions and required comments; in particular, it should define the symbol type as shown above. The file hw1.ml should contain your test cases. The file hw1.txt
should hold your assessment. Please do not put your name, student ID, or other personally identifying information in your files.
Sample test cases
See <a href="hw1sample.ml">hw1sample.ml</a> for a copy of these tests.
let subset_test0 = subset [] [1;2;3]
let subset_test1 = subset [3;1;3] [1;2;3]
let subset test2 = not (subset [1;3;7] [4;1;3])
let equal sets test0 = equal sets [1;3] [3;1;3]
let equal_sets_test1 = not (equal_sets [1;3;4] [3;1;3])
let set_union_test0 = equal_sets (set_union [] [1;2;3]) [1;2;3]
let set_union_test1 = equal_sets (set_union [3;1;3] [1;2;3]) [1;2;3]
let set_union_test2 = equal_sets (set_union [] []) []
let set_all_union_test0 =
  equal_sets (set_all_union []) []
let set_all_union_test1 =
  equal_sets (set_all_union [[3;1;3]; [4]; [1;2;3]]) [1;2;3;4]
let set_all_union_test2 =
  equal sets (set all union [[5;2]; []; [5;2]; [3;5;7]]) [2;3;5;7]
let computed_fixed_point_test0 =
  computed fixed point (=) (fun x \rightarrow x / 2) 1000000000 = 0
let computed_fixed_point_test1 =
  computed_fixed_point (=) (fun x -> x \star. 2.) 1. = <u>infinity</u>
let computed_fixed_point_test2 =
  computed_fixed_point (=) sqrt 10. = 1.
let computed_fixed_point_test3 =
  ((computed_fixed_point (fun x y \rightarrow abs_float (x \rightarrow y) < 1.)
                                (fun x -> x /_{\bullet} 2.)
    = 1.25)
let computed_periodic_point_test0 =
  computed_periodic_point (=) (fun x \rightarrow x / 2) 0 (-1) = -1
let computed_periodic_point_test1 =
  computed_periodic_point (=) (fun x \rightarrow x *. x -. 1.) 2 0.5 = -1.
(* An example grammar for a small subset of Awk. *)
type awksub_nonterminals =
   | Expr | Lvalue | Incrop | Binop | Num
let awksub_rules =
    [Expr, [T"("; N Expr; T")"];
     Expr, [N Num];
     Expr, [N Expr; N Binop; N Expr];
     Expr, [N Lvalue];
     Expr, [N Incrop; N Lvalue];
     Expr, [N Lvalue; N Incrop];
     Lvalue, [T"$"; N Expr];
     Incrop, [T"++"];
     Incrop, [T"--"];
    Binop, [T"+"];
    Binop, [T"-"];
     Num, [T"0"];
                                                                                                                            Assignment Project Exam Help
    Num, [T"1"];
     Num, [T"2"];
     Num, [T"3"];
                                                                                                                                    https://tutorcs.com
     Num, [T"4"];
     Num, [T"5"];
     Num, [T"6"];
                                                                                                                                    WeChat: cstutorcs
     Num, [T"7"];
     Num, [T"8"];
     Num, [T"9"]]
let awksub_grammar = Expr, awksub_rules
let awksub test0 =
  filter_blind_alleys awksub_grammar = awksub_grammar
let awksub_test1 =
  filter_blind_alleys (Expr, <u>List.tl</u> awksub_rules) = (Expr, List.tl awksub_rules)
let awksub_test2 =
  filter_blind_alleys (Expr,
        [Expr, [N Num];
         Expr, [N Lvalue];
         Expr, [N Expr; N Lvalue];
         Expr, [N Lvalue; N Expr];
         Expr, [N Expr; N Binop; N Expr];
         Lvalue, [N Lvalue; N Expr];
         Lvalue, [N Expr; N Lvalue];
         Lvalue, [N Incrop; N Lvalue];
         Lvalue, [N Lvalue; N Incrop];
         Incrop, [T"++"]; Incrop, [T"--"];
         Binop, [T"+"]; Binop, [T"-"];
         Num, [T"0"]; Num, [T"1"]; Num, [T"2"]; Num, [T"3"]; Num, [T"4"];
         Num, [T"5"]; Num, [T"6"]; Num, [T"7"]; Num, [T"8"]; Num, [T"9"]])
  = (Expr,
       [Expr, [N Num];
        Expr, [N Expr; N Binop; N Expr];
       Incrop, [T"++"]; Incrop, [T"--"];
        Binop, [T "+"]; Binop, [T "-"];
       Num, [T "0"]; Num, [T "1"]; Num, [T "2"]; Num, [T "3"]; Num, [T "4"];
       Num, [T "5"]; Num, [T "6"]; Num, [T "7"]; Num, [T "8"]; Num, [T "9"]])
let awksub_test3 =
  filter_blind_alleys (Expr, List.tl (List.tl (List.tl awksub_rules))) =
     filter_blind_alleys (Expr, List.tl (List.tl awksub_rules))
type giant_nonterminals =
   | Conversation | Sentence | Grunt | Snore | Shout | Quiet
let giant_grammar =
  Conversation,
   [Snore, [T"ZZZ"];
    Quiet, [];
    Grunt, [T"khrgh"];
    Shout, [T"aooogah!"];
    Sentence, [N Quiet];
    Sentence, [N Grunt];
    Sentence, [N Shout];
    Conversation, [N Snore];
   Conversation, [N Sentence; T","; N Conversation]]
let giant test0 =
  filter blind alleys giant grammar = giant grammar
let giant_test1 =
  filter blind alleys (Sentence, List.tl (snd giant grammar)) =
     (Sentence,
      [Quiet, []; Grunt, [T "khrgh"]; Shout, [T "aooogah!"];
       Sentence, [N Quiet]; Sentence, [N Grunt]; Sentence, [N Shout]])
let giant_test2 =
  filter_blind_alleys (Sentence, List.tl (List.tl (snd giant_grammar))) =
     (Sentence,
       [Grunt, [T "khrgh"]; Shout, [T "aooogah!"];
       Sentence, [N Grunt]; Sentence, [N Shout]])
Sample use of test cases
When testing on SEASnet, use one of the machines lnxsrv11.seas.ucla.edu, lnxsrv13.seas.ucla.edu, and lnxsrv15.seas.ucla.edu, and lnxsrv15.seas.ucla.edu. Make sure /usr/local/cs/bin is at the start of your path, so that you get the proper version of OCaml. To do this, append the following lines to
your $HOME/.profile file if you use bash or ksh:
export PATH=/usr/local/cs/bin:$PATH
The command ocaml should output the version number 5.1.1.
If you put the <u>sample test cases</u> into a file hw1sample.ml, you should be able to use it as follows to test your hw1.ml solution on the SEASnet implementation of OCaml. Similarly, the command #use "hw1test.ml";; should run your own test cases on your solution.
$ ocaml
OCaml version 5.1.1
Enter #help;; for help.
# #use "hw1.ml";;
type ('a, 'b) symbol = N of 'a | T of 'b
# #use "hw1sample.ml";;
val subset_test0 : bool = true
val subset test1 : bool = true
val subset test2 : bool = true
```

val set\_union\_test0 : bool = true val set\_union\_test1 : bool = true val set\_union\_test2 : bool = true val set\_all\_union\_test0 : bool = true

val set all union test1 : bool = true val set\_all\_union\_test2 : bool = true

(Conversation,

val equal\_sets\_test0 : bool = true val equal\_sets\_test1 : bool = true

val computed\_fixed\_point\_test0 : bool = true val computed\_fixed\_point\_test1 : bool = true val computed\_fixed\_point\_test2 : bool = true val computed\_fixed\_point\_test3 : bool = true

val awksub rules :

val computed\_periodic\_point\_test0 : bool = true

val computed\_periodic\_point\_test1 : bool = true type awksub\_nonterminals = Expr | Lvalue | Incrop | Binop | Num (awksub\_nonterminals \* (awksub\_nonterminals, string) symbol list) list = [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]);

(Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);

(Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]); (Lvalue, [T "\$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);

(Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]); (Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]);

(Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])]

val awksub\_grammar :

awksub\_nonterminals \* (awksub nonterminals \* (awksub nonterminals, string) symbol list) list =

(Expr, [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]); (Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);

(Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]);

(Lvalue, [T "\$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);

(Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]);

(Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]); (Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])]) val awksub\_test0 : bool = true val awksub test1 : bool = true

val awksub\_test2 : bool = true val awksub\_test3 : bool = true type giant\_nonterminals = Conversation Sentence Grunt

Snore Shout Quiet val giant\_grammar : giant\_nonterminals \*

(Conversation, [N Sentence; T ","; N Conversation])]) val giant test0 : bool = true val giant\_test1 : bool = true val giant\_test2 : bool = true

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[(Snore, [T "ZZZ"]); (Quiet, []); (Grunt, [T "khrgh"]);

(Sentence, [N Shout]); (Conversation, [N Snore]);

(giant\_nonterminals \* (giant\_nonterminals, string) symbol list) list =

(Shout, [T "aooogah!"]); (Sentence, [N Quiet]); (Sentence, [N Grunt]);