

TOA Assignment 01

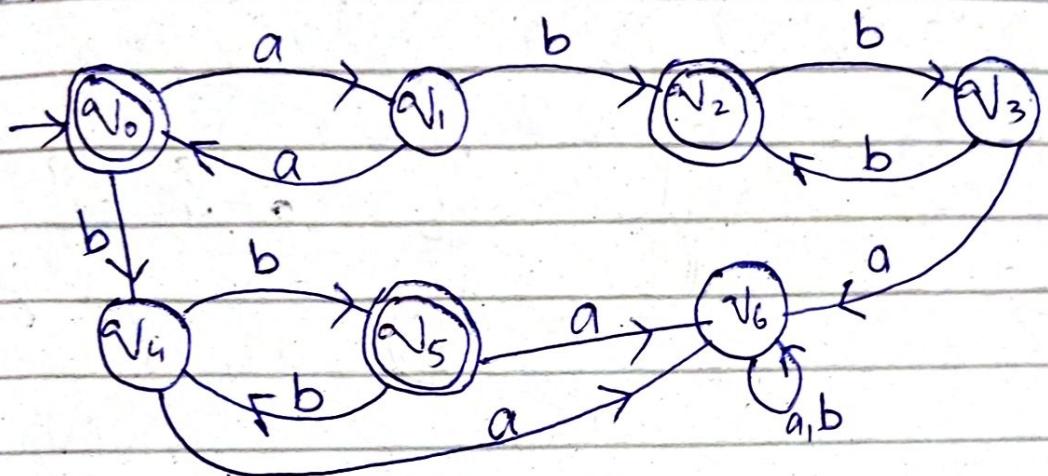
20K-0190

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$L_1 = \{ a^n b^m : (n+m) \text{ is even} \}$

$$RE = (aa)^* (bb)^* + a(aa)^* b(bb)^*$$

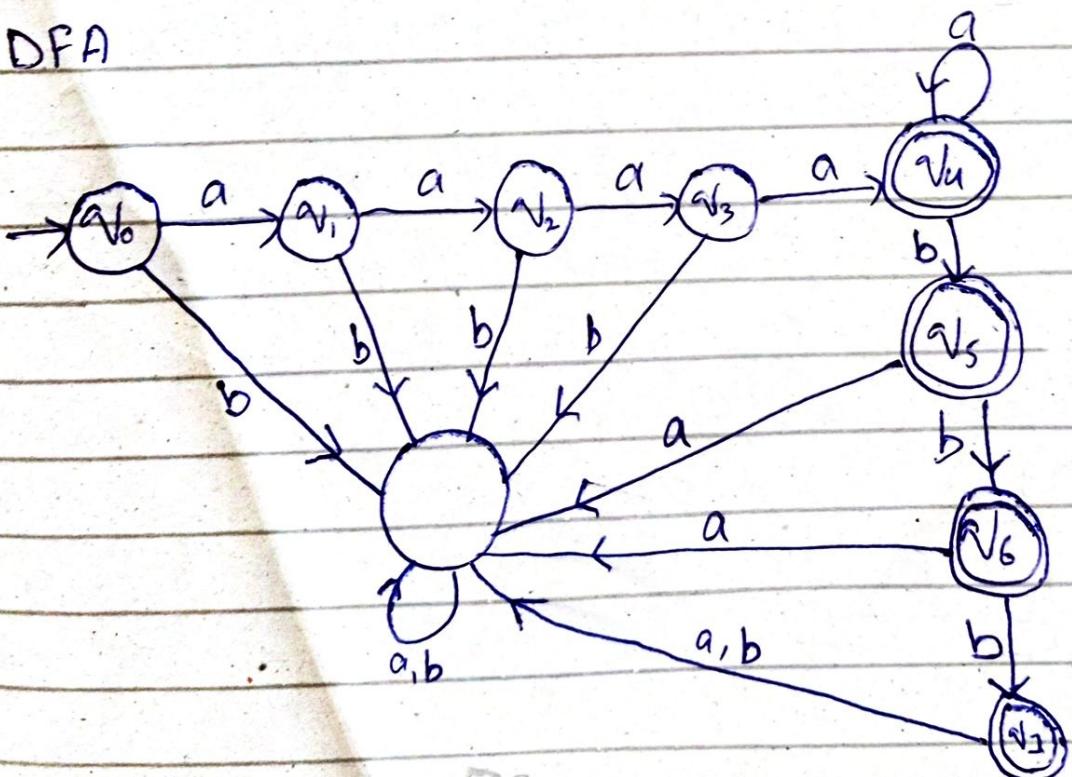
DFA



$$L_2 = \{ a^n b^m : n \geq 4, m \leq 3 \}$$

$$RE = aaaa^+ (\lambda + b + bb + bbb)$$

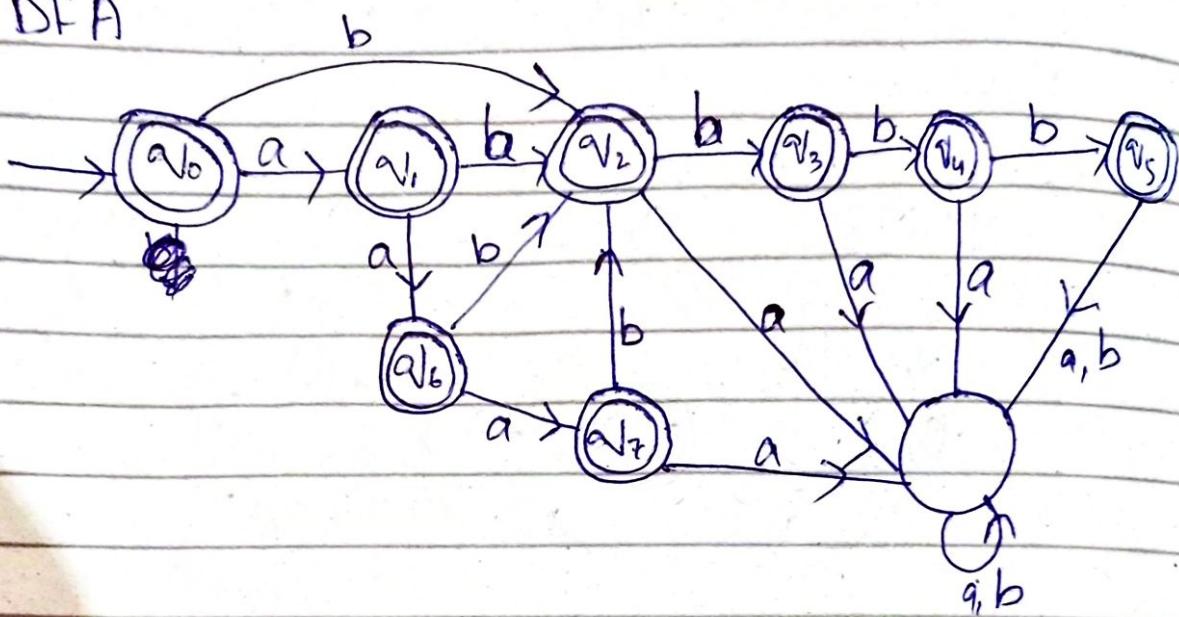
DFA



$L_3 = \{a^n b^m : n < 4, m \leq 4\}$

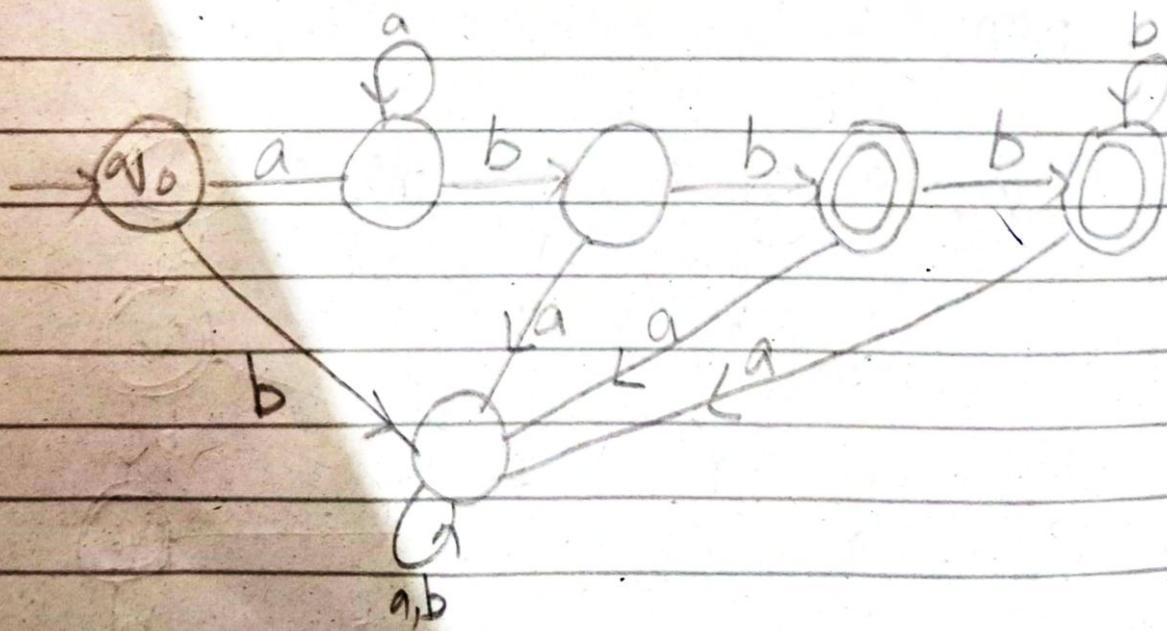
RE: $(\lambda + a + aa + aaa)(\lambda + b + bb + bbb + bbbb)$

DFA



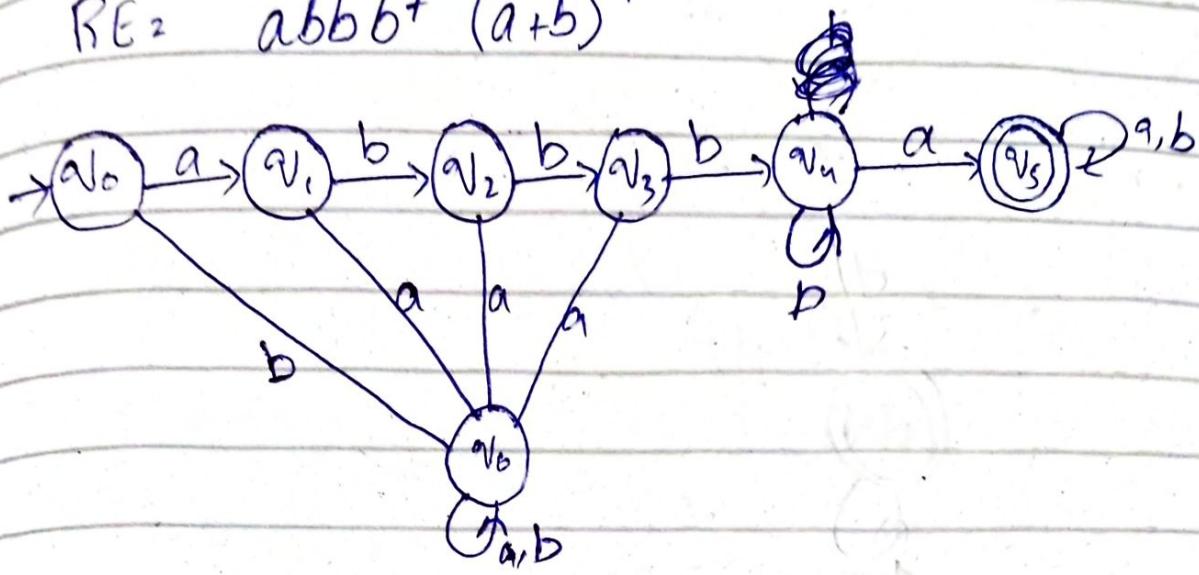
$L_4 = \{a^n b^m : n \geq 1, m \geq 1, nm \geq 3\}$

RE: $a^+ b b b^+ + a a a^+ b^+ + a a^+ b b^+$



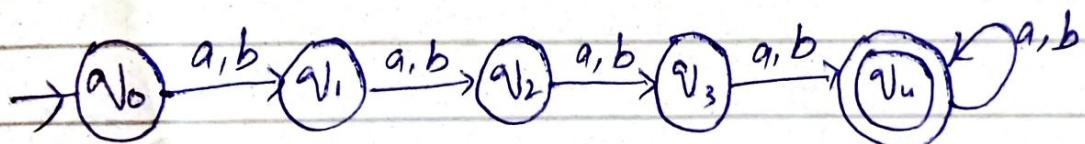
$L_5 = \{ ab^n \mid n \geq 3, w \in \{a, b\}^+ \}$

RE: $abb b^+ (a+b)^+$



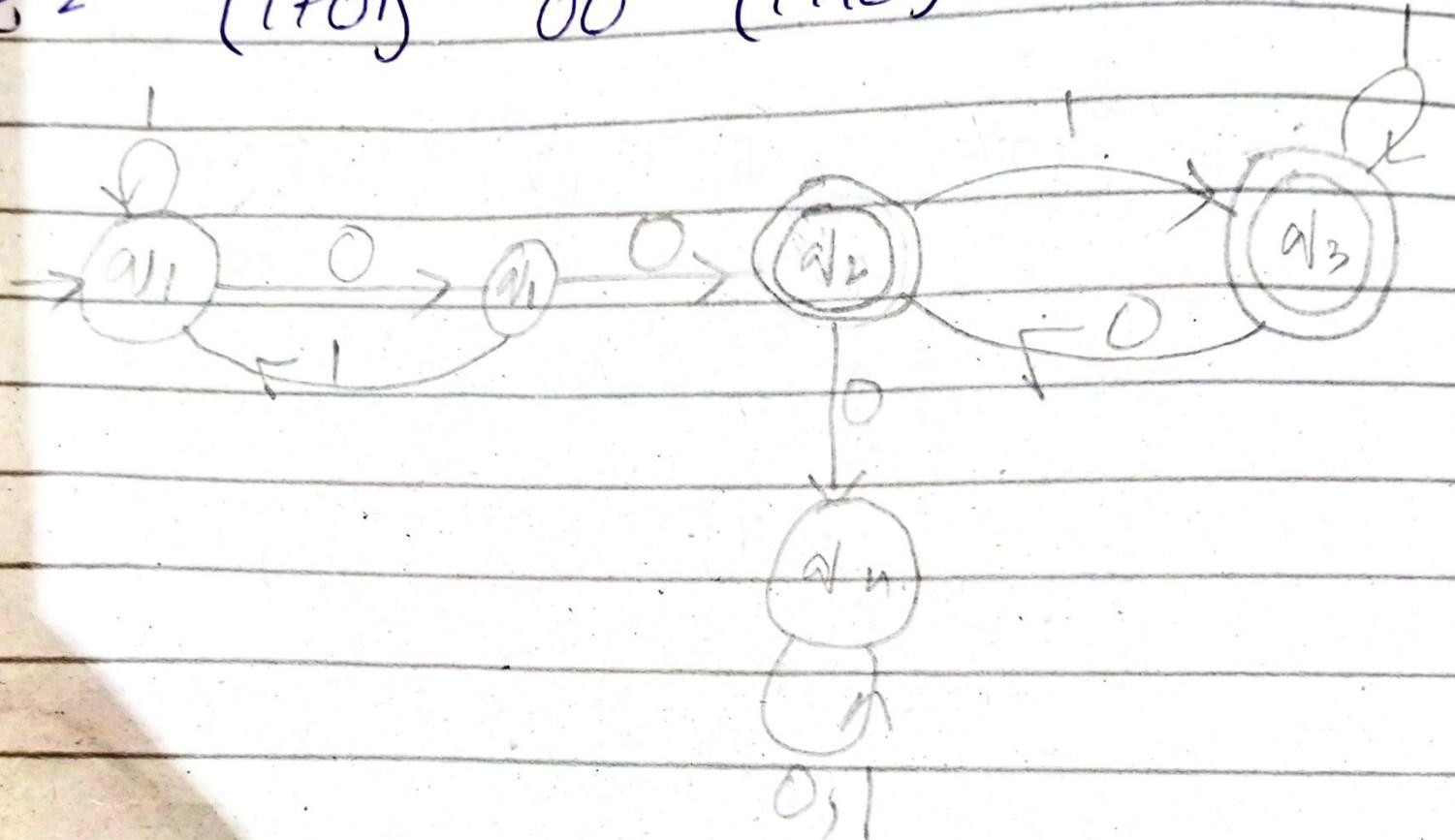
$L_6 = \{ vwv \mid v, w \in \{a, b\}^*, |w| = 2 \}$

RE: $(a+b)(a+b) \oplus (a+b)^*(a+b)(a+b)$



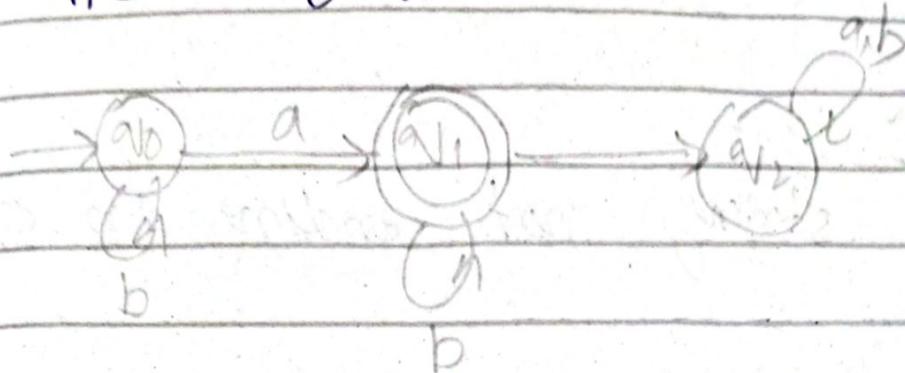
L7 Having exactly one pair of consecutive zeros

$$RB = (1+0)^* \text{ } 00 \text{ } (1+0)^*$$



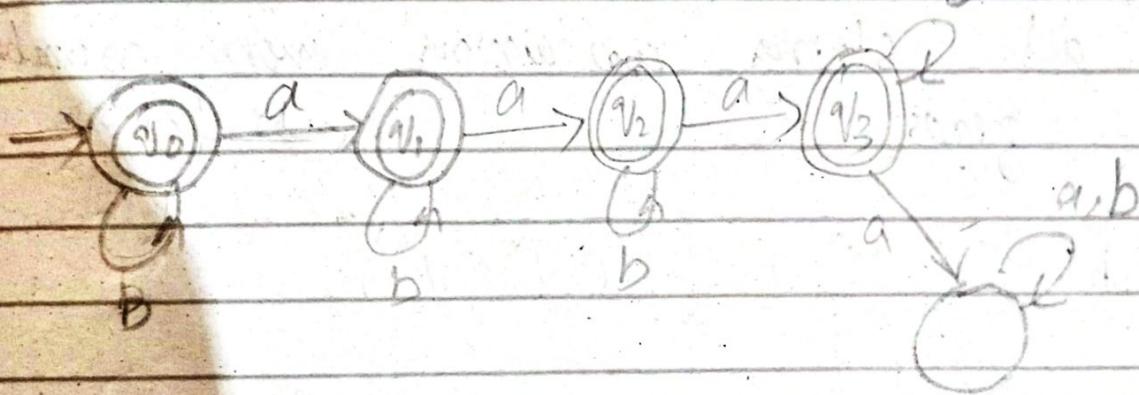
L8 having exactly one 'a'

$$RE = b^* a b^*$$



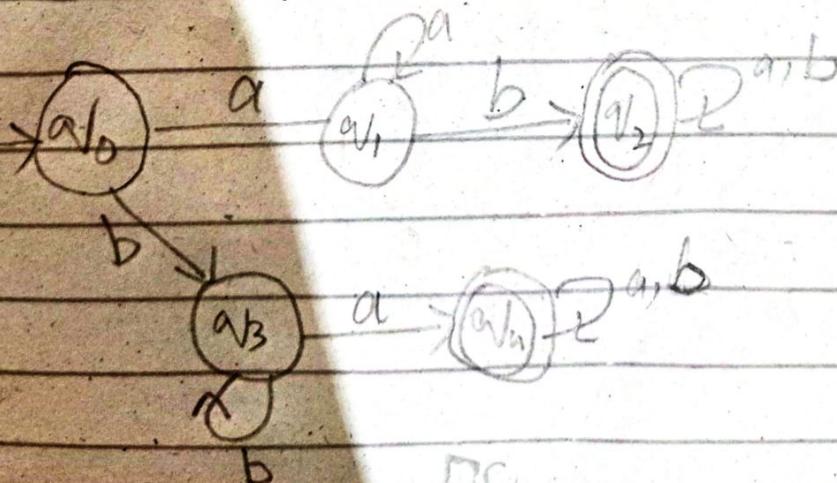
L9 strings containing no more than 3 'a's

$$RE = b^* a b^* a b^* a b^*$$



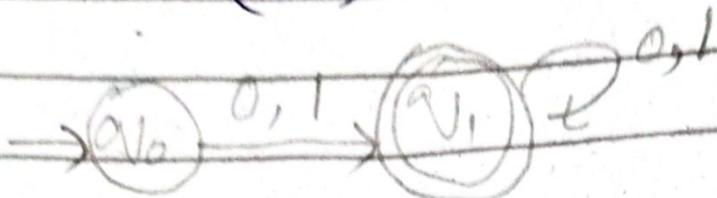
L10 All string contains at least one occurrence of each symbol in alphabet

$$RE = a(a+b)^* b + b(a+b)^* a$$



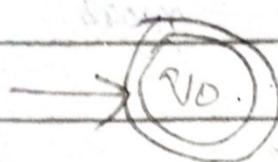
L11 all string ending in 0,1

$$RE_2 \quad (0+1)^*$$



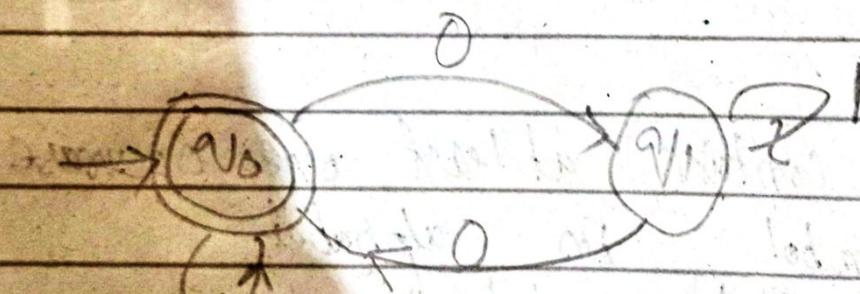
L12 all string not ending in 0,1

$$RE_2 \quad \Sigma^*$$



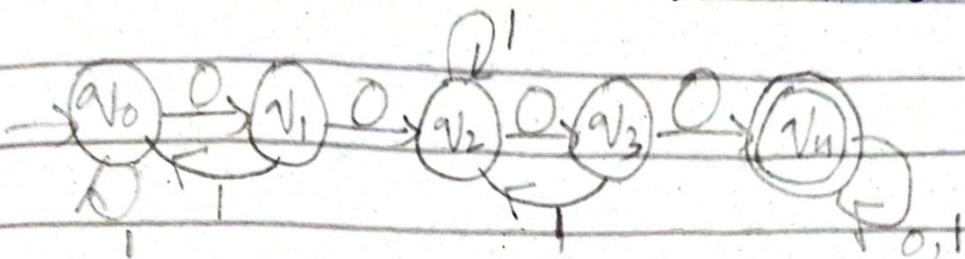
L13 all string containing even number
of zeros

$$RE_2 \quad 1^* + (1^*01^*01^*)^*$$



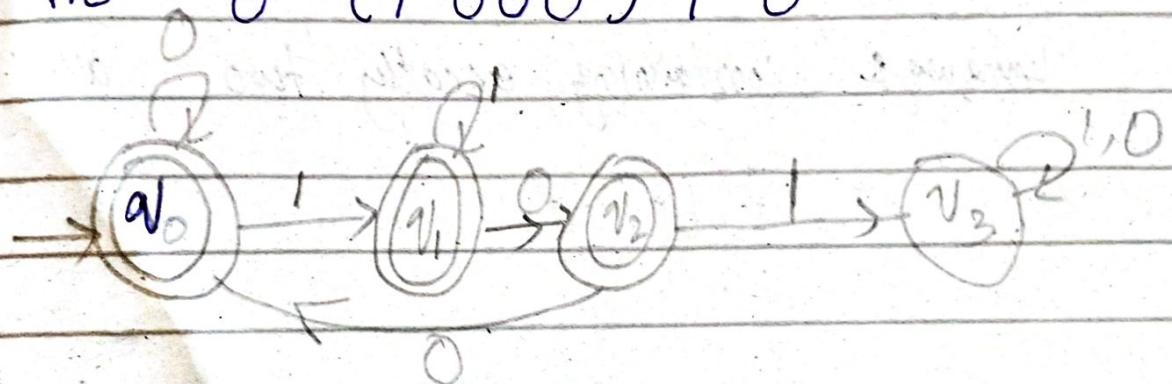
L14 strings having at least two occurrence of substring 00

$$RE = (0+1)^* 00 (0+1)^* 00 (0+1)^*$$



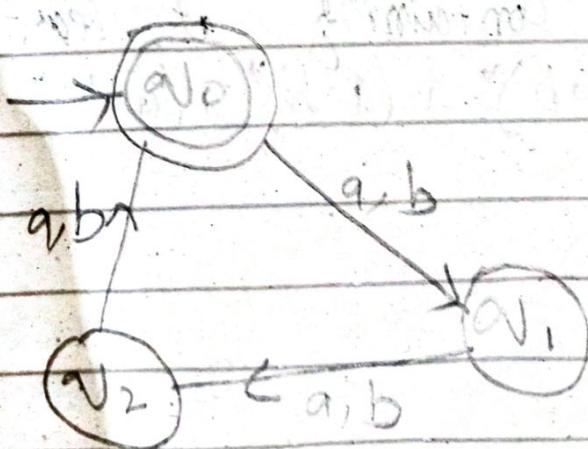
L15 all string not containing 101

$$RE = 0^* (1^* 000^*)^* 1^* 0^*$$



L16 {w: |w| mod 3 = 0}

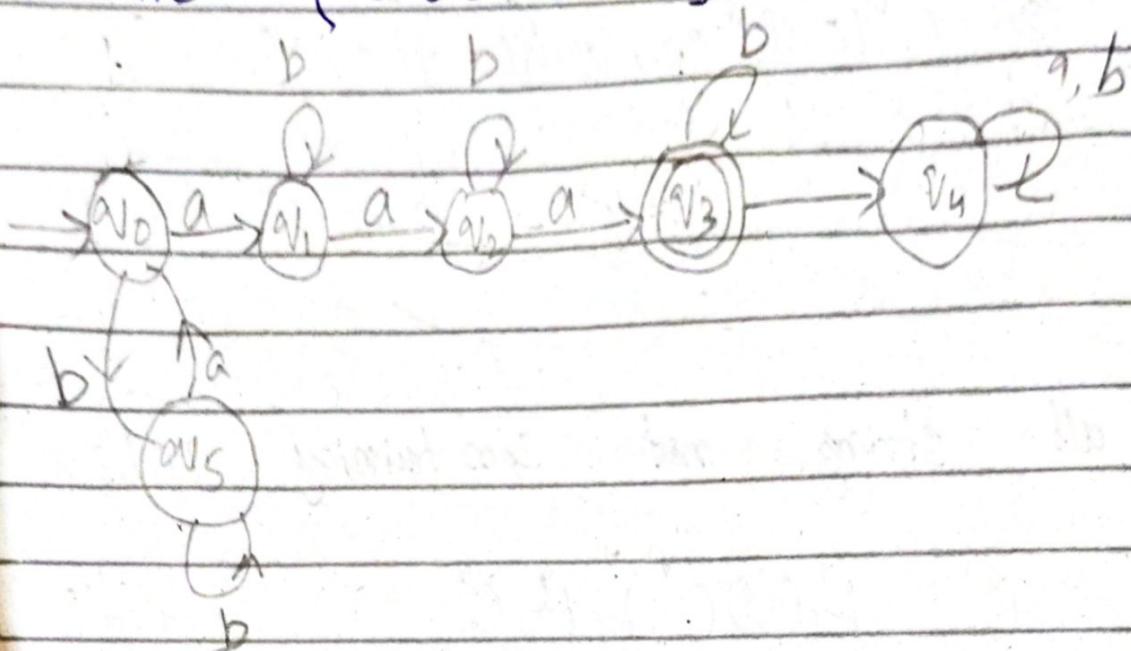
$$RE = ((a+b)^3)^*$$



Date _____

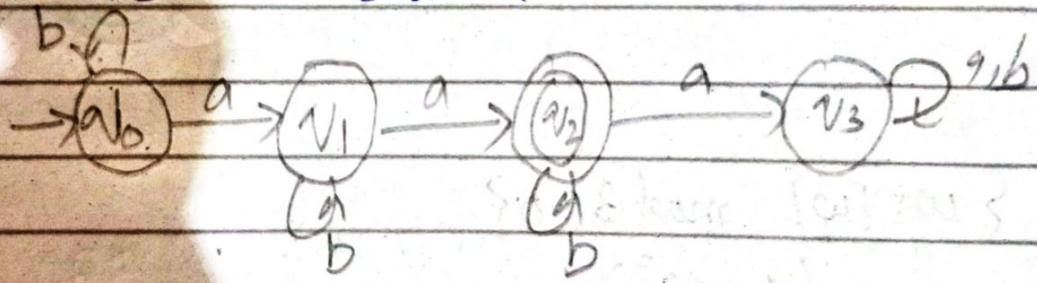
L17 $\{ w : n_a(w) \bmod 3 = 0 \}$

$$RE = (b^* a b^* a b^*)^* + b^*$$



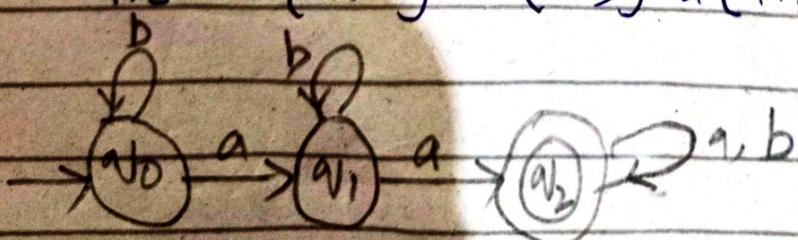
L18 Language containing exactly two a's

$$RE = b^* a b^* a b^*$$



L19 Language containing at least 2 a's

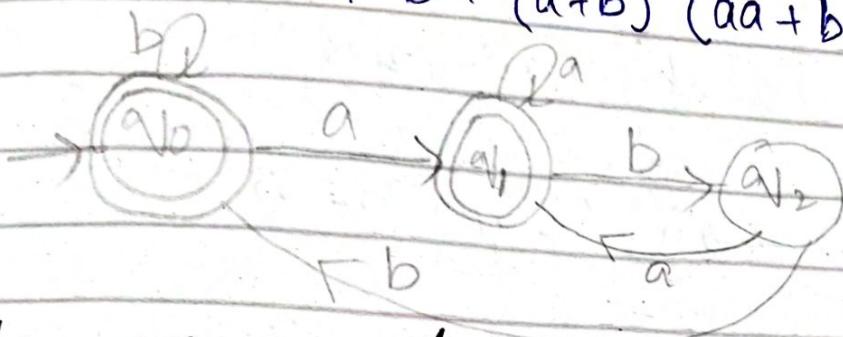
$$RE = (a+b)^* a (a+b)^* a (a+b)^*$$



L20

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 Language of all strings do not end with ab.

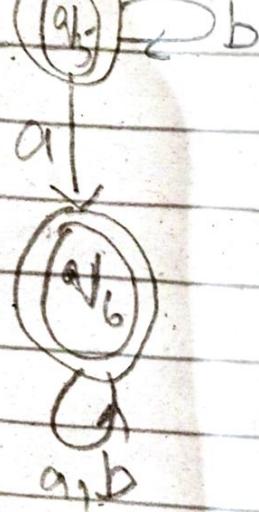
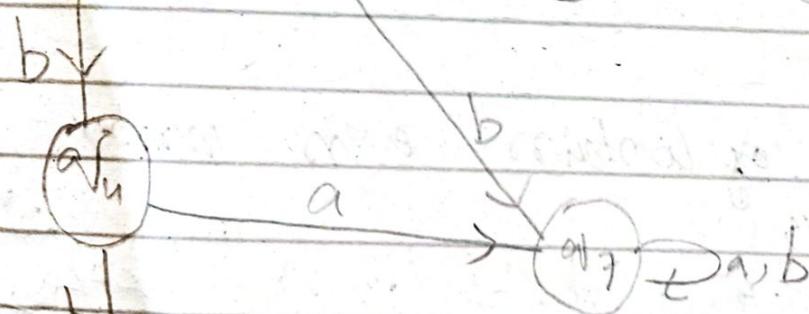
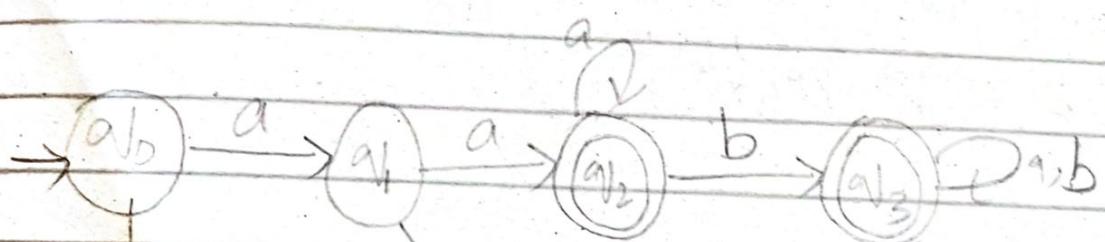
$$RE = \lambda + a + b + (a+b)^*(aa+bb+ba)$$



L21

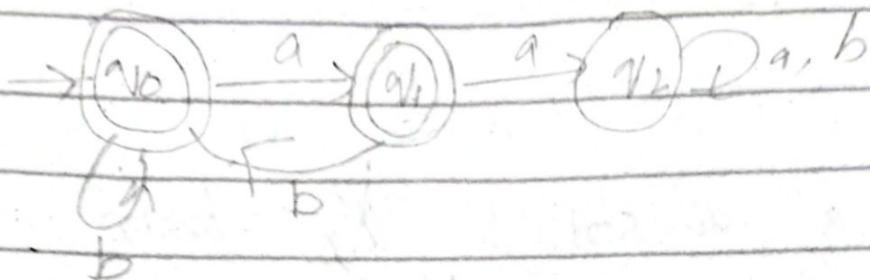
Language of all strings that begin or end with aa or bb

$$RE = aa+b^*+bb+a^*$$



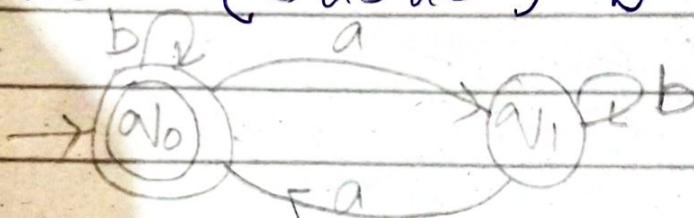
L-22 Language of all strings not containing substring aa

$$RE = (ab+b)^* (ab+ba+bb)$$



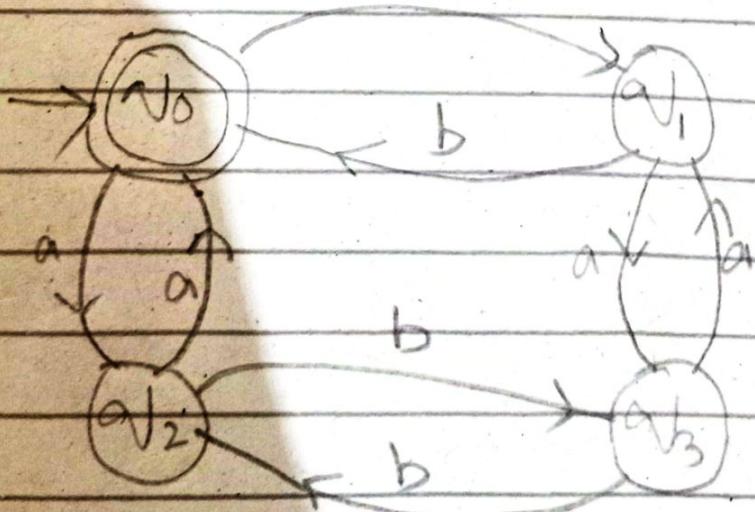
L-23 String of even number of a's

$$RE = (b^* ab^* ab^*)^* b^*$$



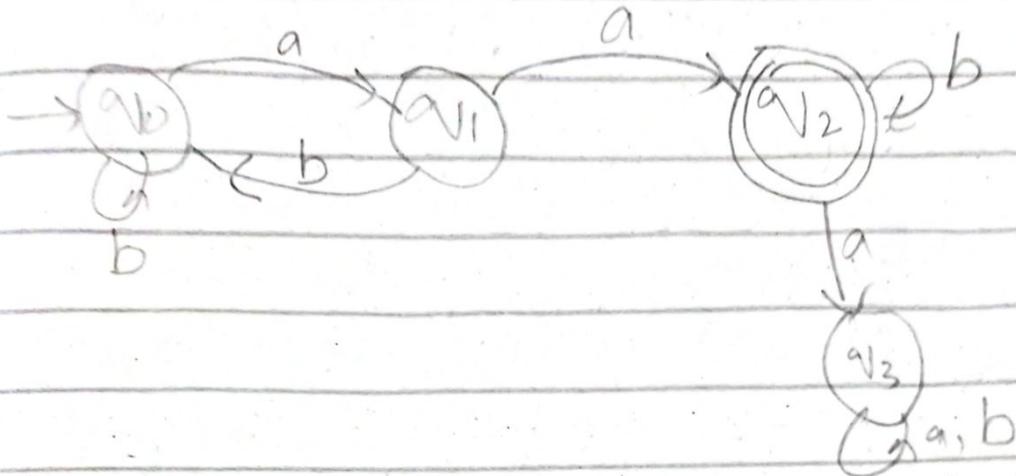
L-24 String of contain even number of a's and b's

$$RE = [aa+bb+(ab+ba)(aa+bb)^*(ab+ba)]^*$$



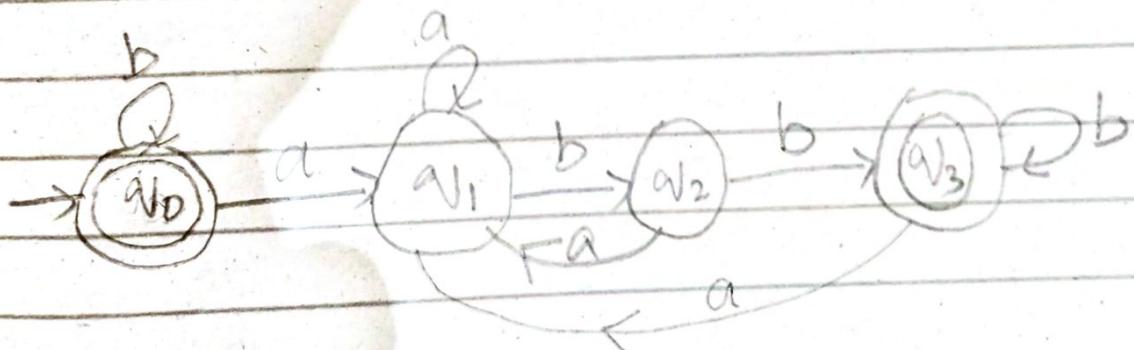
L25 String containing no more than
occurrence aa

$$RE = b^* a a b^*$$



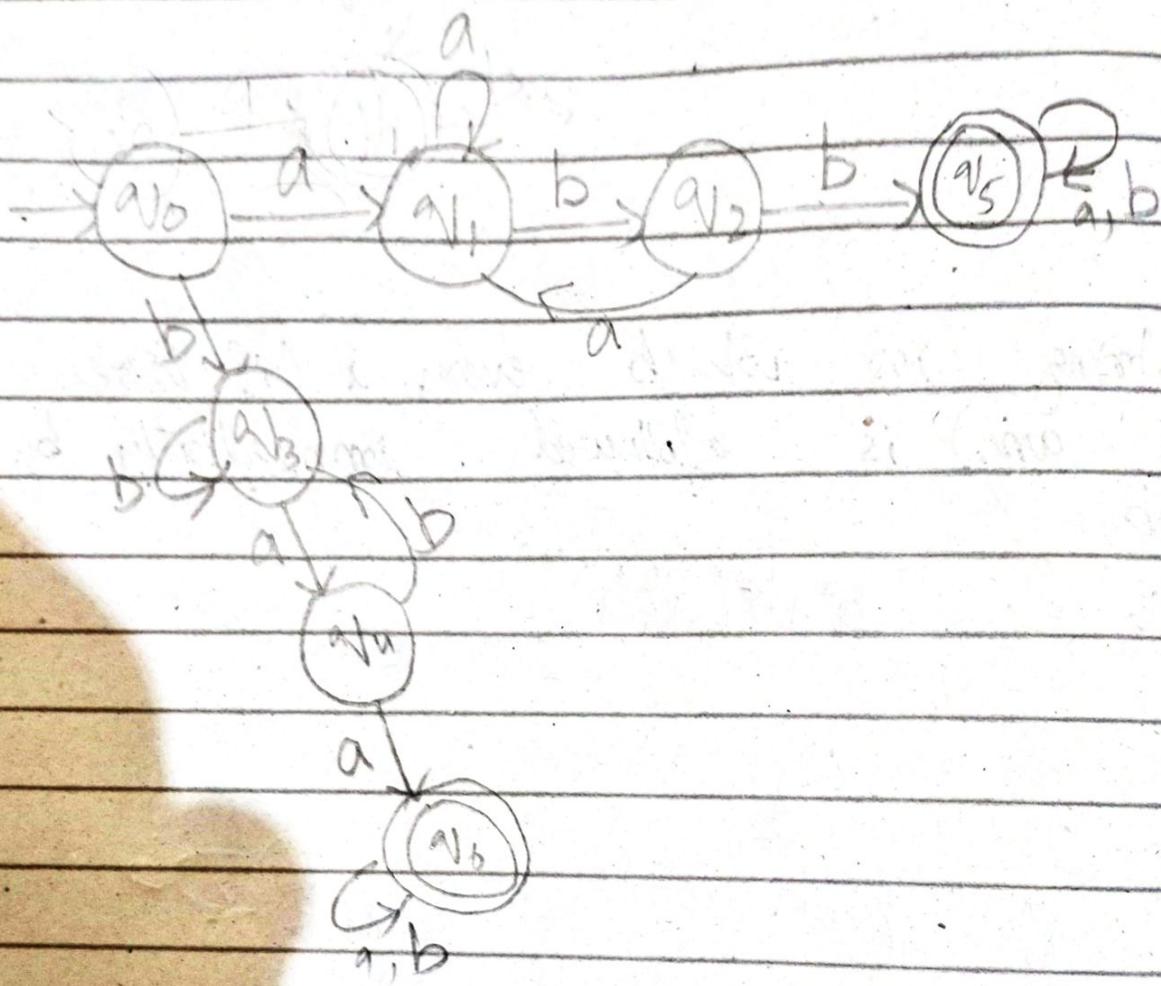
L26 string in which every a (if there are any) is followed immediately by bb

$$RE = b^* + b^* (abb)^*$$



L27 All the strings containing both bb and aa as substrings

$$RE = (a+b)^* aa (a+b)^* bb (a+b)^* + \\ (a+b)^* bb (a+b)^* aa (a+b)^*$$



Date _____

Q8 Strings containing both aba and
bab as substring

$$RE = (a+b)^* (aba + bab) (a+b)^*$$

