

CALCULATING PAGE NUMBER AND OFFSET FROM LOGICAL ADDRESS

Given page size which is a multiple of 2 - 2^n bytes

Virtual address space - m -bit or 2^m bytes

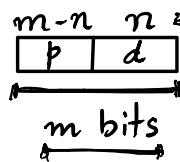
32-bit virtual/logical address space size ?

Binary number basics

Using N bits, 2^N different values can be represented including 0

Conversely, you need $\log_2(N)$ bits to represent N values from 0 to $N-1$

Logical address space -



m -bit
 $0 - 2^m - 1$

4 bits $\rightarrow 2^4$
 $0 - 2^4 - 1 \rightarrow 4$ bits

Total number of pages = logical address space size / page size

$$\underbrace{(m-n) \text{ bits}}_{\text{page number}} = \frac{2^m}{2^n} = 2^{(m-n)} \text{ pages} \quad \underbrace{0 - (2^{(m-n)} - 1)}_{\text{page offset}}$$

How many bits you require to represent $0 - 2^{(m-n)} - 1$ page numbers? 🤔

Page offset can vary from $0 - 2^n - 1$. How many bits to represent the offset?

$$0 - (2^n - 1) \rightarrow n \text{ bits}$$

How many bits are required for storing the frame number? 🤔

Depends on the size of RAM/physical address space and frame size

Frame size is same as the page size

Calculate the maximum number of frames into which physical memory can be divided (similar to calculation of number of pages)

If maximum number of frames is 2^x , then x bits are required to store the frame number

$$0 - (2^x - 1) \rightarrow x \text{ bits}$$

The size of the page table depends on the number of bits required to store frame numbers



$$\text{no of frame} = \frac{\text{physical address space size}}{\text{frame size}}$$

$$(32 \text{ bit}) \rightarrow 2^{32}$$

PRACTICE PROBLEM

Size of virtual address = 32-bit = $m = 2^{32} \text{ bytes}$

Size of physical address = 30-bit = 2^{30} bytes

Page size = 4 KB = $2^2 \times 2^{10} \text{ bytes} = 2^{12} \text{ bytes}$

2^n

Calculate the number of bits required to store page number, page offset and frame number.

$$m = 32$$

$$n = 12$$

$$\text{no of frames} = \frac{2^{30}}{2^{12}} = 2^{18}$$

$$p = 32 - 12 = 20 \text{ bits}$$

$$d = 12 \text{ bits}$$

$$\left\{ \begin{array}{c} 0 \\ \vdots \\ 2^{18} - 1 \end{array} \right\} \rightarrow (18 \text{ bits})$$