

Hammer Calculations

For these calculations it is assumed that the main air tank is equipped with a high-delivery regulator and that the hammer cycle consists of applying the output of this regulator to the air cylinder for a preset fraction of the cylinder's stroke.

The force exerted on the piston is constant for the fraction f of the stroke. Then the force on the piston declines according to the laws of thermodynamics for an adiabatic expansion.

The drives system is a cylinder with a piston attached to chain wrapped around a sprocket on the hammer axle.

Cylinder

$$A_{throw} := \pi \cdot \left(\left(\frac{d_{throw}}{2} \right)^2 - \left(\frac{d_{rod}}{2} \right)^2 \right) = 26.507 \text{ in}^2 \quad Vol_{throw} := A_{throw} \cdot stroke$$

Mechanism

$$J_{hammer} := m_{head} \cdot len_{arm}^2 + m_{arm} \cdot \left(\frac{len_{arm}}{2} \right)^2 \quad \text{rotational inertia of the arm+hammer}$$

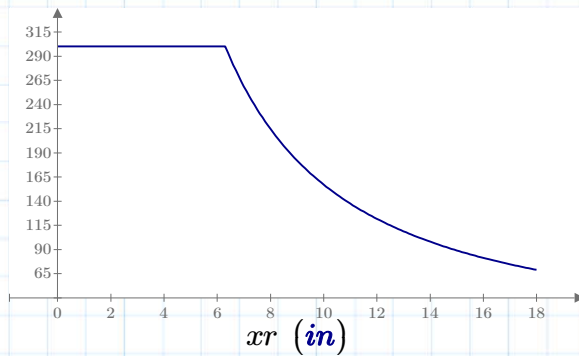
Thermodynamics

$$const(ff) := P_0 \cdot (ff \cdot Vol_{throw})^{1.4} \quad \text{this is the constant required for the adiabatic expansion calc, as a function of fill fraction ff}$$

$$V_{stroke}(x) := A_{throw} \cdot x \quad \text{volume expression for the stroke}$$

$$P(x, ff) := \text{if} \left(\left(\frac{V_{stroke}(x)}{Vol_{throw}} \leq ff \right), P_0, \frac{const(ff)}{V_{stroke}(x)^{1.4}} \right) \quad \text{the complete expression for the pressure}$$

$$xr := 0 \cdot \text{in}, 1 \cdot \text{in} \dots stroke$$



$$P(xr, ffd) \text{ (psi)}$$

Motion

$$r_{\text{sprocket}} := \frac{\text{stroke}}{\theta_{\text{max}}} = 3.82 \text{ in}$$

$$x_{\text{cyl}}(\theta) := \theta \cdot r_{\text{sprocket}}$$

$$x_{\text{cyl}}(180 \cdot \text{deg}) = 12 \text{ in}$$

$$\theta_{\text{hammer}}(x) := \frac{x}{r_{\text{sprocket}}}$$

$$\theta_{\text{stroke}} := \theta_{\text{hammer}}(\text{stroke}) = 270 \text{ deg}$$

$$T_{\text{axle}}(\theta, ff) := P(x_{\text{cyl}}(\theta), ff) \cdot A_{\text{throw}} \cdot r_{\text{sprocket}} \quad \text{torque applied by cylinder on crank}$$

$$\alpha_{\text{hammer}}(\theta, ff) := \frac{T_{\text{axle}}(\theta, ff)}{J_{\text{hammer}}} \quad \text{acceleration of hammer}$$

$$E_{\text{hammer}}(\theta, ff) := \int_0^{\theta} T_{\text{axle}}(\theta, ff) d\theta$$

$$E_{\text{hammer}}(\theta_{\text{max}}, ffd) = (1.051 \cdot 10^4) \text{ J}$$

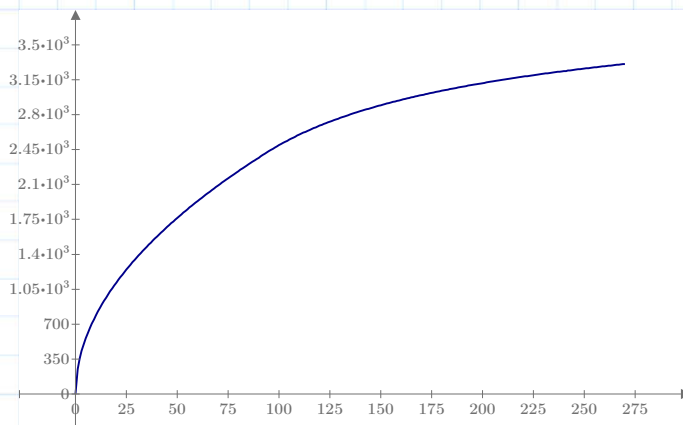
$$\omega_{\text{hammer}}(\theta, ff) := \sqrt{2 \cdot \int_0^{\theta} \alpha_{\text{hammer}}(\theta, ff) d\theta}$$

angular velocity of hammer

$$t(\theta, ff) := \int_0^{\theta} \frac{2}{\omega_{\text{hammer}}(\theta, ff)} d\theta$$

time to get to an angle

$$\theta r := 0 \cdot \text{deg}, 1 \cdot \text{deg} \dots \theta_{\text{max}}$$



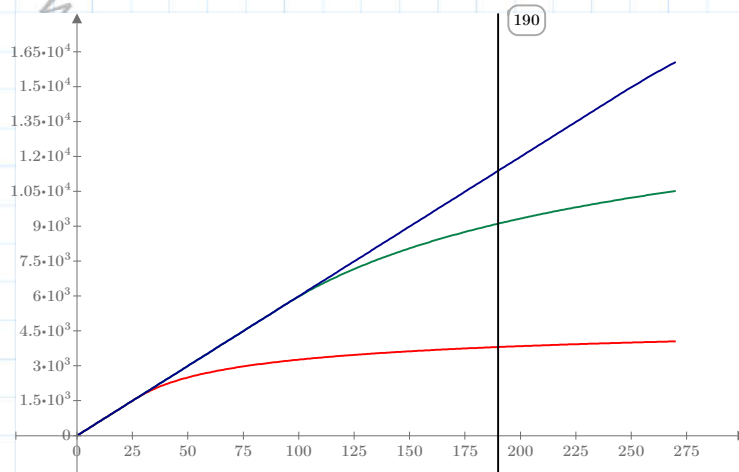
$$\omega_{\text{hammer}}(\theta r, ffd) \left(\frac{\text{deg}}{\text{s}} \right)$$

$$\theta r \text{ (deg)}$$

System

$$V_{shot} := Vol_{throw} \cdot ffd \cdot \frac{P_0}{1 \cdot atm}$$

volume of air at STP consumed per shot



$$E_{hammer}(\theta_r, 0.1) \text{ (J)}$$

$$E_{hammer}(\theta_r, ffd) \text{ (J)}$$

$$E_{hammer}(\theta_r, 0.9) \text{ (J)}$$

θ_r (deg)

Parameters

$$V_{tank} := 87 \cdot ft^3$$

$$P_0 \equiv 300 \cdot psi$$

hammer cylinder pressure

$$ffd \equiv 35\%$$

default fill fraction

$$\theta_{max} \equiv 270 \cdot deg$$

maximum hammer angle

$$\theta_{hit} := 190 \cdot deg$$

hammer angle at impact

$$d_{throw} \equiv 6 \cdot in$$

hammer cylinder diameter

$$d_{rod} \equiv 1.5 \cdot in$$

hammer rod diameter

$$stroke \equiv 18 \cdot in$$

hammer cylinder stroke

$$m_{head} \equiv 26 \cdot lb$$

hammer head mass

$$m_{arm} \equiv 6 \cdot lb$$

hammer arm mass

$$len_{arm} \equiv 28 \cdot in$$

hammer arm length

Results

$$r_{\text{sprocket}} = 3.82 \text{ in}$$

$$t(\theta_{\text{hit}}, \text{ffd}) = 0.224 \text{ s}$$

swing time

$$E_{\text{hammer}}(\theta_{\text{hit}}, \text{ffd}) = 9109.5 \text{ J}$$

terminal swing energy

$$t_{\text{chain}} := A_{\text{throw}} \cdot P_0 = (7.952 \cdot 10^3) \text{ lbf}$$

$$w_{\text{max}} := \omega_{\text{hammer}}(180 \cdot \text{deg}, \text{ffd}) = 506.516 \text{ rpm}$$

$$n_{\text{shots}} := \frac{V_{\text{tank}}}{V_{\text{shot}}} = 44.1$$

$$F_{\text{max}} := P_0 \cdot A_{\text{throw}} = (7.952 \cdot 10^3) \text{ lbf}$$

peak force from fire cylinder

$$F_{\text{hammer}} := \frac{T_{\text{axle}}(0, \text{ffd})}{\text{len}_{\text{arm}}} = (1.085 \cdot 10^3) \text{ lbf}$$

force at hammer head

$$T_{\text{max}} := T_{\text{axle}}(0, \text{ffd}) = (2.531 \cdot 10^3) \text{ ft} \cdot \text{lbf}$$

peak torque on hammer axle

Retract pulse considerations

$$d_{\text{retract}} \equiv 4 \text{ in} \quad d_{\text{retract.rod}} \equiv 0.75 \text{ in}$$

$$A_{\text{retract}} := \pi \cdot \left(\left(\frac{d_{\text{retract}}}{2} \right)^2 - \left(\frac{d_{\text{rod}}}{2} \right)^2 \right) = 10.799 \text{ in}^2$$

$$V_{\text{retract}} := A_{\text{retract}} \cdot \frac{\text{stroke}}{3}$$

volume of retract side at 180 degrees

$$T_{\text{retract}}(P) := A_{\text{retract}} \cdot P \cdot r_{\text{sprocket}}$$

$$A_{\text{retract}} := \pi \cdot \left(\left(\frac{d_{\text{retract}}}{2} \right)^2 - \left(\frac{d_{\text{retract.rod}}}{2} \right)^2 \right) = 12.125 \text{ in}^2$$

$$F_{\text{max.retract}} := P_0 \cdot A_{\text{retract}} = (3.637 \cdot 10^3) \text{ lbf}$$

$$F_{\text{min.retract}} := \frac{T_{\text{retract}}(40 \cdot \text{psi})}{\text{len}_{\text{arm}}} = 58.929 \text{ lbf}$$

$$Q_{retract} := 14 \cdot \text{cfm}$$

flow rate of tiny valve from McMaster at 3000psi

$$t(P) := \frac{P \cdot V_{e_{retract}}}{1 \cdot \text{bar} \cdot Q_{retract}}$$

time to fill to a given pressure

$$t(100 \cdot \text{psi}) = 1.108 \text{ s}$$

Hammer axle and bearing

$$F_{perBearing} := \frac{F_{max}}{2} = (3.976 \cdot 10^3) \text{ lbf}$$

$$d_{axle} := 55 \text{ mm} = 2.165 \text{ in}$$

$$l_{axle} := 120 \text{ mm} = 4.724 \text{ in}$$

$$A_{effAxle} := d_{axle} \cdot l_{axle} = 10.23 \text{ in}^2$$

$$P_{effAxle} := \frac{F_{perBearing}}{A_{effAxle}} = 388.668 \text{ psi}$$

$$v_{surf} := \omega_{hammer}(180 \cdot \text{deg}, ffd) \cdot \frac{d_{axle}}{2} = 1.459 \frac{\text{m}}{\text{s}}$$

$$\omega_{hammer}(180 \cdot \text{deg}, ffd) = 506.516 \text{ rpm}$$

$$PV := P_{effAxle} \cdot v_{surf} = (1.116 \cdot 10^5) \frac{\text{ft}}{\text{min}} \cdot \text{psi}$$

that's too small a diameter for an aluminum axle

$$\tau_{y2_6061} := 30 \cdot \text{ksi}$$

$$\tau_{y1_6061} := 27 \text{ ksi}$$

$$A_{double} := 2 \cdot \pi \cdot \left(\frac{d_{axle}}{2} \right)^2 = 7.365 \text{ in}^2$$

$$P_{swing} := \frac{F_{max}}{A_{double}} = 1.08 \text{ ksi} \quad \text{ow totally fine.}$$

force on chain idlers support structure

$$\theta_{idler} := 159.2 \cdot \text{deg}$$

$$F_{halfIdler} := F_{max} \cdot \cos\left(\frac{\theta_{idler}}{2}\right) = (1.436 \cdot 10^3) \text{ lbf}$$

$$F_{idler} := 2 \cdot F_{halfIdler} = (2.871 \cdot 10^3) \text{ lbf}$$

$$\sigma_{y1_4_20bolt} := 5730 \cdot \text{lbf per bolt area}$$

according to wikipedia it's approximately true that

$$\tau_{y1_4_20bolt} := 0.58 \cdot \sigma_{y1_4_20bolt} = (3.323 \cdot 10^3) \text{ lbf}$$

$$SF_{idlerbolt} := \frac{\tau_{y1_4_20bolt}}{F_{halfIdler}} = 2.315$$

$$\sigma_{y6061} := 42 \cdot \text{ksi}$$

$$\tau_{y6061} := 0.55 \cdot \sigma_{y6061} = 23.1 \text{ ksi}$$

$$e_{dist} := 1.492 \cdot \text{in}$$

$$F_{tearout} := \tau_{y6061} \cdot e_{dist} \cdot 0.25 \text{ in} = (8.616 \cdot 10^3) \text{ lbf}$$

$$SF_{tearout} := \frac{F_{tearout}}{F_{halfIdler}} = 6.002$$

drive dog shear and bearing loads

$$A_{shear.sprocket} := 1.3 \text{ in}^2$$

$$A_{shear.shaft} := 1.286 \text{ in}^2$$

$$n_{dog.sprocket} := 6$$

$$r_{dog.shaft} := 1.286 \text{ in}$$

$$r_{dog.sprocket} := 1.8 \text{ in}$$

$$F_{dog.sprocket} := \frac{T_{axle}(0, ffd)}{r_{dog.sprocket}} = (1.688 \cdot 10^4) \text{ lbf}$$

$$P_{shear.sprocket} := \frac{F_{dog.sprocket}}{n_{dog.sprocket} \cdot A_{shear.sprocket}} = 2.163 \text{ ksi}$$

$$F_{dog.shaft} := \frac{T_{axle}(0, ffd)}{r_{dog.shaft}} = (2.362 \cdot 10^4) \text{ lbf}$$

$$P_{shear.shaft} := \frac{F_{dog.shaft}}{n_{dog.sprocket} \cdot A_{shear.shaft}} = 3.061 \text{ ksi}$$

$$r_{bearing.shaft} := 1.5 \text{ in}$$

$$t_{shaft} := 0.7 \text{ in} \quad l_{shaft} := 0.54 \text{ in}$$

$$F_{bearing.shaft} := \frac{T_{axle}(0, ffd)}{r_{bearing.shaft}} = (2.025 \cdot 10^4) \text{ lbf}$$

$$P_{bearing.shaft} := \frac{F_{bearing.shaft}}{n_{dog.sprocket} \cdot t_{shaft} \cdot l_{shaft}} = 8.929 \text{ ksi}$$

Shear Stress on Fasteners Sprocket and Hammer

$$r_{bolt.sprocket} := \frac{2.5}{2} \text{ in} = 1.25 \text{ in} \quad \text{bolt radius}$$

$$F_{bolt.sprocket} := \frac{T_{axle}(0, ffd)}{r_{bolt.sprocket}} = (2.43 \cdot 10^4) \text{ lbf} \quad \text{force per bolt}$$

$$d_{bolt.sprocket} := 0.25 \text{ in} \quad \text{diameter of bolt}$$

$$A_{bolt.sprocket} := \pi \cdot \left(\frac{d_{bolt.sprocket}}{2} \right)^2 = 0.049 \text{ in}^2 \quad \text{area per bolt}$$

$$n_{bolt} := 12 \quad \text{number of bolts}$$

$$\tau_{Gr.8.bolt} := 150 \text{ ksi} \quad \text{grade 8 bolt yield}$$

$$P_{bolt.sprocket} := \frac{F_{bolt.sprocket}}{n_{bolt} \cdot A_{bolt.sprocket}} = 41.253 \text{ ksi} \quad \text{Stress per bolt}$$

$$FoS := \frac{\tau_{Gr.8.bolt}}{P_{bolt.sprocket}} = 3.636 \quad \text{Factor of Safety}$$

$$r_{bolt.hammer} := \frac{4.5}{2} \text{ in} = 2.25 \text{ in}$$

$$F_{bolt.hammer} := \frac{T_{axle}(0, ffd)}{r_{bolt.hammer}} = (1.35 \cdot 10^4) \text{ lbf}$$

$$n_{bolt.hammer} := 12$$

$$P_{bolt.hammer} := \frac{F_{bolt.hammer}}{n_{bolt.hammer} \cdot A_{bolt.sprocket}} = 22.918 \text{ ksi}$$

Hammer xle Torsional Stress and Stiffness

$$r_{axle.o} := 1.8 \text{ in}$$

axle outside radius

$$r_{axle.i} := \frac{2.9}{2} \text{ in} = 1.45 \text{ in}$$

axle inside radius

$$l_{axle.hollow} := 3.3 \text{ in}$$

length of axle that's hollow

$$J_{axle} := 2 \cdot \pi \cdot \left(r_{axle.o}^4 - r_{axle.i}^4 \right)$$

Polar moment of inertia

$$\tau_{shear.mod.7075} := 3900 \text{ ksi}$$

Shear modulus of 7075

$$\tau_{shear.axle} := \frac{r_{axle.o} \cdot T_{axle}(0, ffd)}{J_{axle}} = 1.432 \text{ ksi}$$

Shear stress

$$\theta_{axle} := \frac{T_{axle}(0, ffd) \cdot l_{axle.hollow}}{J_{axle} \cdot \tau_{shear.mod.7075}} = 0.039 \text{ deg}$$

Torsional deflection