13. Recursion

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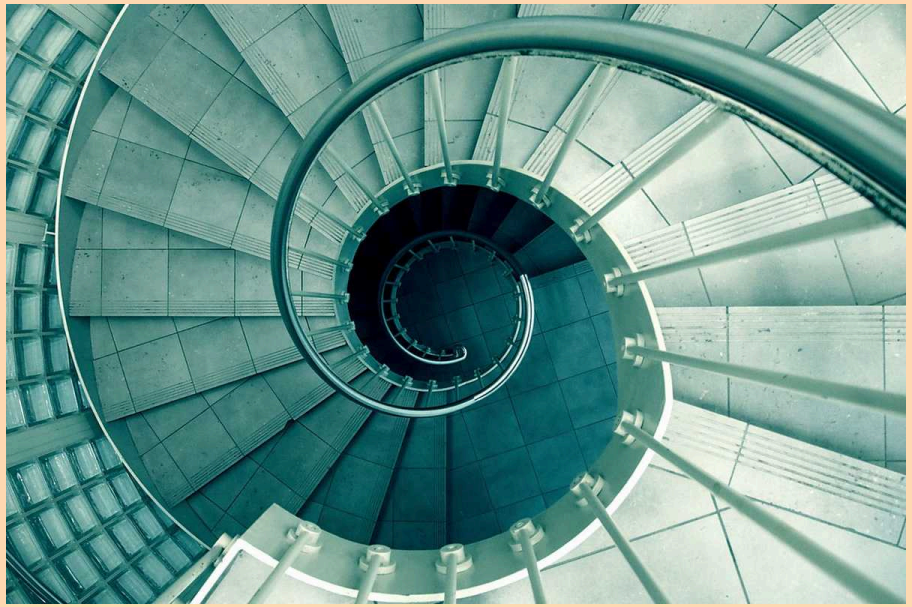
Dec. 26, 2024

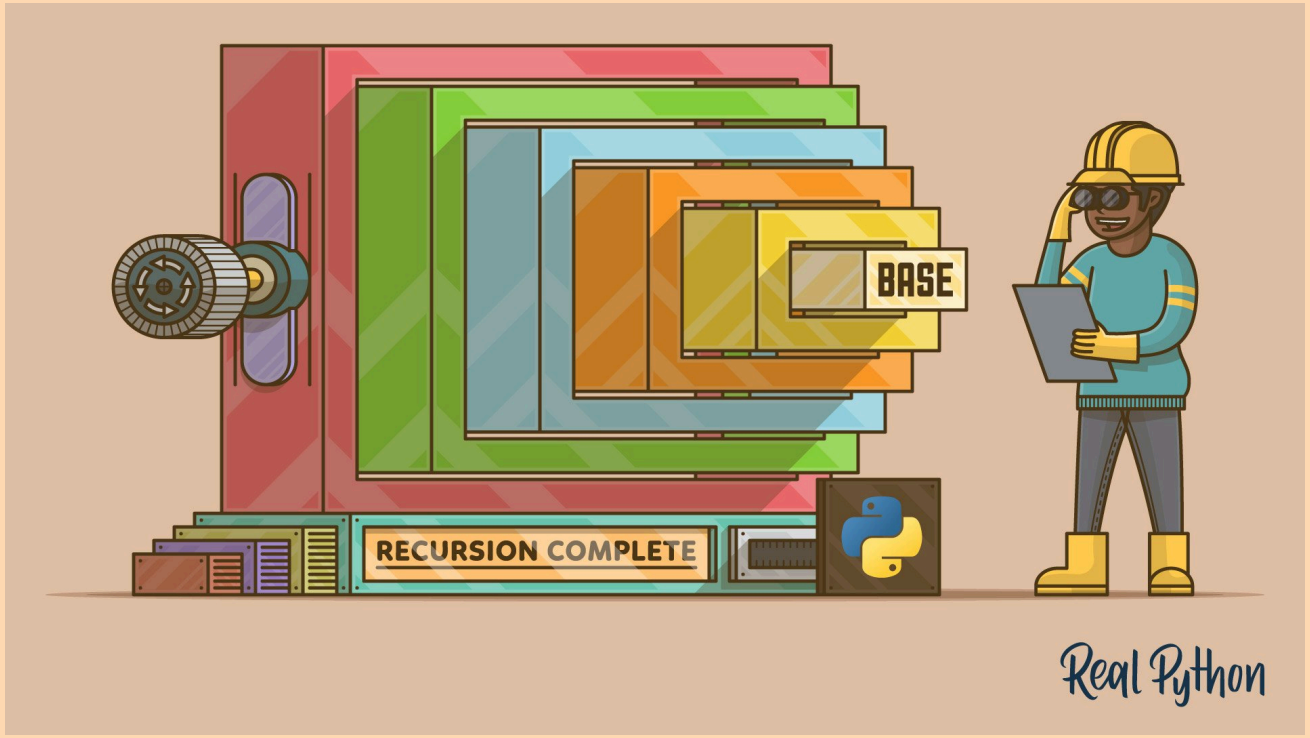
Overview

Recursive Functions (Recursion)



A function that calls itself.

(1) Thinking like a Computer Scientist



Solving a task by first solving its smaller subtasks

Mathematician: mathematical induction!!!

(1) Thinking like a Computer Scientist

You want to solve a task and suppose you have the Mirror.

The Mirror can solve the smaller task for you magically.

(1) Thinking like a Computer Scientist

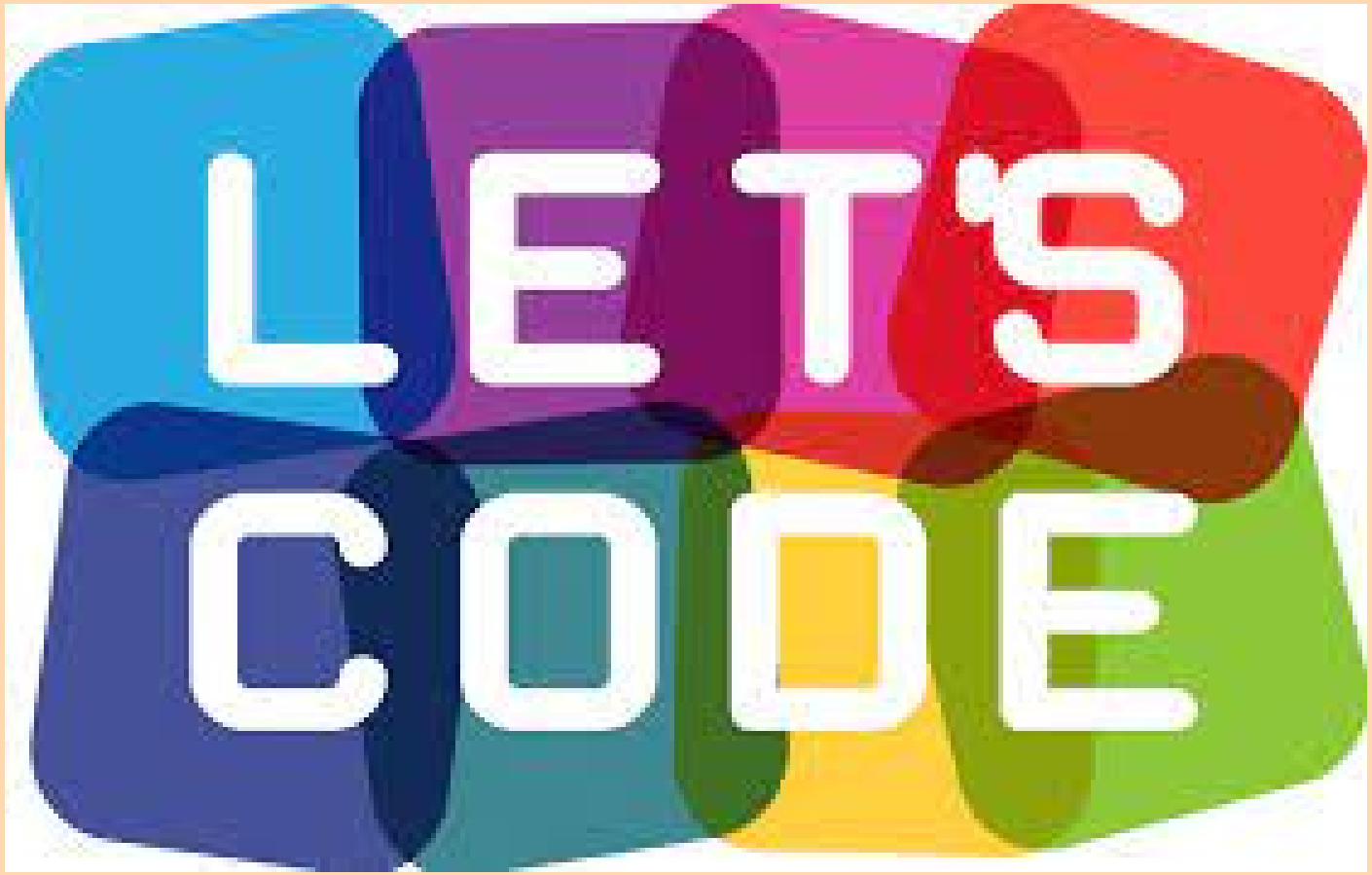
- What is a smaller task? (★★★★★)
- How to reduce the original task into the smaller task? (★★★)
- How to solve the task given the solution to the smaller one? (★★★)
- What is the smallest task? (★)

Thinking Recursively

It will be a looooooooooong way to go to master RECURSION!!!

(2) Thinking like a Computer

min.c



min-re.c sum-re.c fib-re.c gcd-re.c

bsearch-re.c mergesort.c

Min (min-re.c)

Min (min-re.c)

$$
\begin{aligned}
\mathrm{Min}(3,5,2,7) &= \min(7, \mathrm{Min}(3,5,2)) \\
&= \min(7, \min(2, \mathrm{Min}(3,5))) \\
&= \min(7, \min(2, \min(5, \mathrm{Min}(3)))) \\
&= \min(7, \min(2, \min(5,3))) \\
&= \min(7, \min(2,3)) \\
&= \min(7,2) \\
&= 2
\end{aligned}
$$

Fibonacci Sequence (fib-re.c)

$$F_0 = 0$$

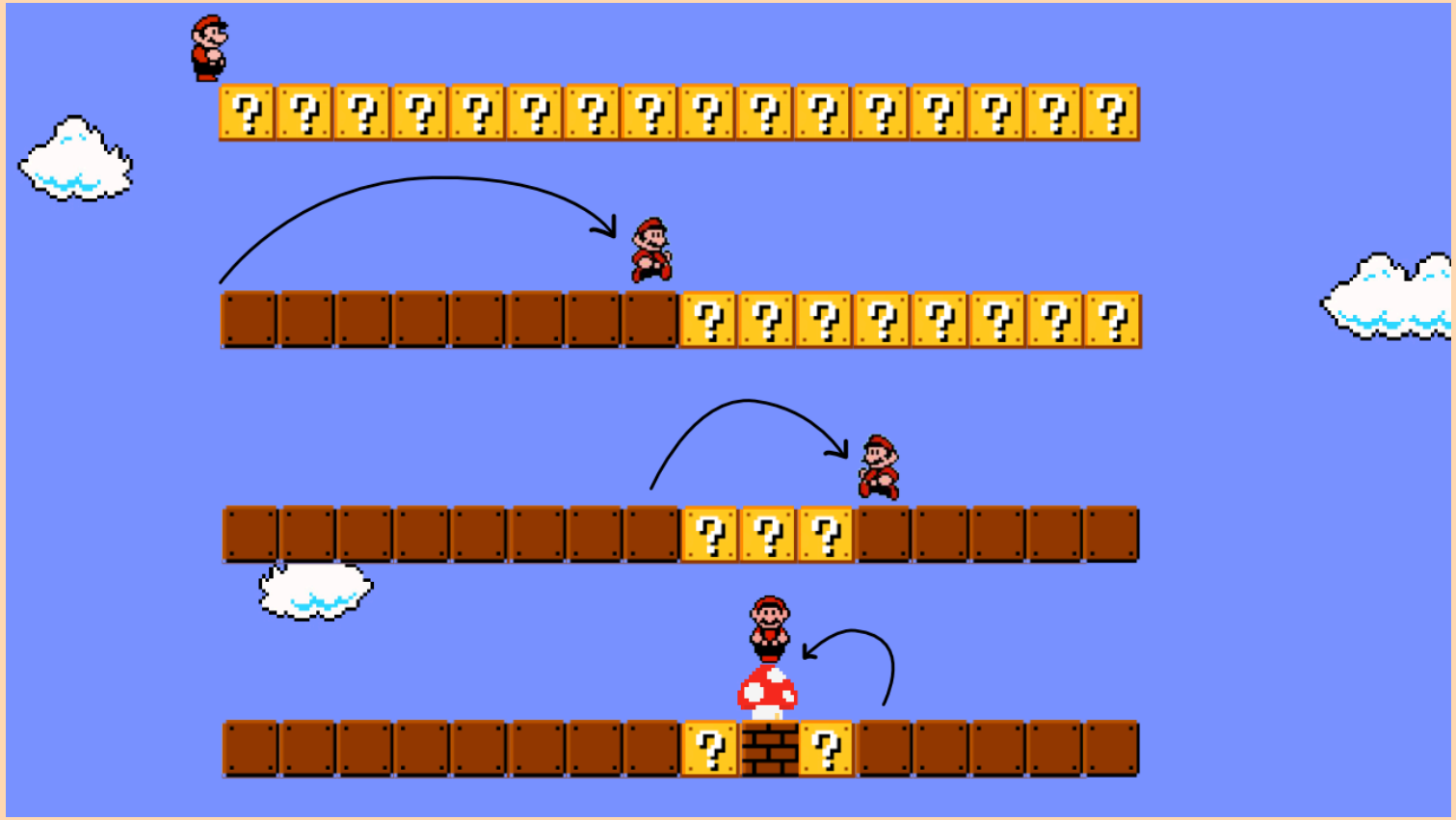
$$F_1 = 1$$

$$F_n = F_{n-1} + F_{n-2} \quad (n > 1)$$

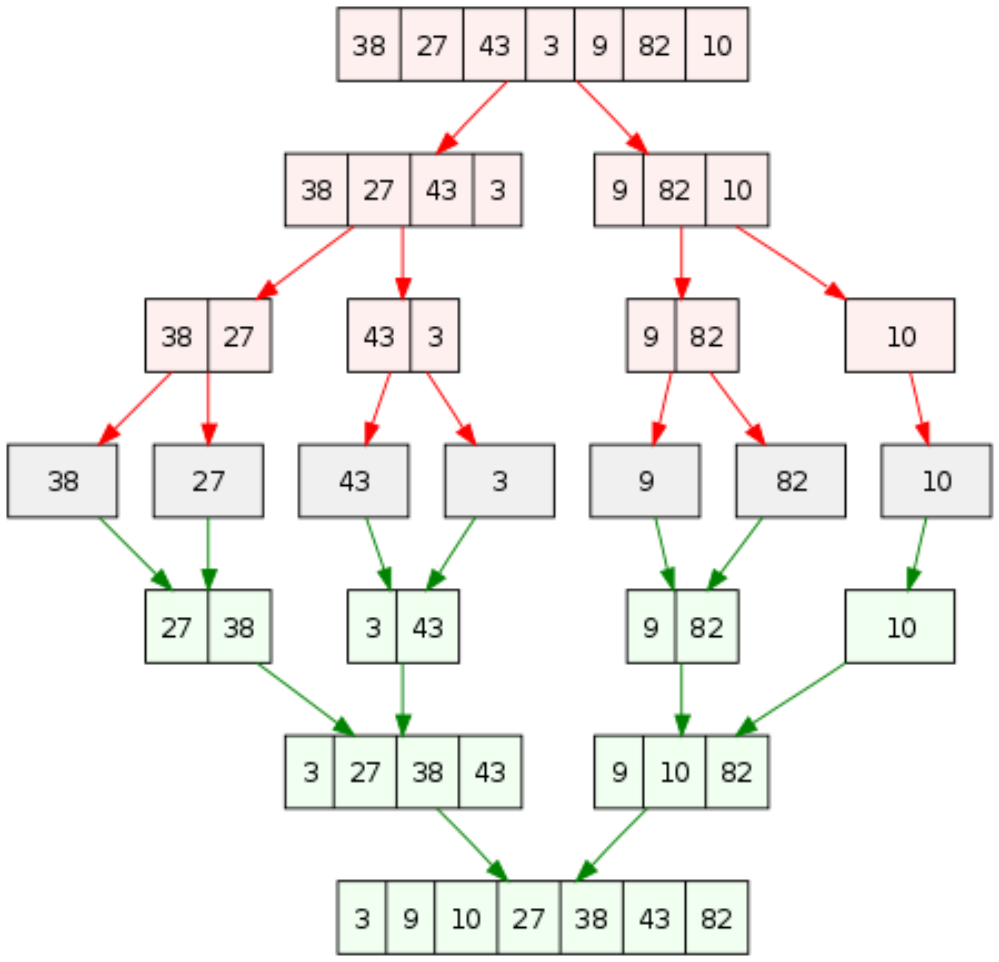
Greatest Common Divisor (gcd-re.c)

$$\gcd(a, b) = \gcd(b, a \,\%\, b)$$

Binary Search (bsearch-re.c)



MergeSort (mergesort.c)



6 5 3 1 8 7 2 4


4
2
8
6
0
5
1
7
3
9


SEE
YOU
NEXT
WEEK