

People Meet People - A Microlevel Approach to Predicting the Effect of Policies on the Spread of Covid-19 *

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In the second year of the pandemic, governments worldwide have been adopting diverse and nuanced policy measures to contain the spread of Covid-19. Examples are targeted contact reduction policies, mask mandates and other hygiene measures, vaccinations and large scale rapid testing. Standard epidemiological models are not designed to predict the effect of very fine grained policies, nor to model the effect of many interacting measures at a time. We propose a novel simulation-based model to address these shortcomings. We build on state-of-the-art agent-based simulation models, greatly increasing the amount of detail and realism with which contacts take place. Firstly, we allow for different contact types (such as work, school, households or leisure), distinguish recurrent and non-recurrent contacts and allow the infectiousness of meetings to vary between contact types. Secondly, we allow agents to seek tests and react to information, such as experiencing symptoms, receiving a positive test or a known case among their contacts, by reducing their own contacts. The model is able to explain the surprising drop in case numbers observed in many european countries in the spring of 2021 as the combined effect of seasonality, vaccinations, contact reduction policies and rapid testing and allows to quantify the contribution each policy measure has.

JEL Classification: C63, I18

Keywords: Covid-19, agent based simulation model, public health measures

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1 Introduction

The first wave of the Covid-19 pandemic prompted strict lockdowns and restrictions across the world. The reaction to second waves consisted of more targeted policy measures such as splitting school classes, closing restaurants and encouragement of home office. To combat the third and fourth waves, that were triggered by the spread of more infectious variants, governments relied on the same targeted measures and previously non-available tools such as large scale rapid testing and vaccinations.

While this multitude of policy measures has led to declining case numbers in most countries, it becomes harder and harder to evaluate the contribution each policy had on the overall outcome. Moreover, the longer the pandemic lasts, the more important it becomes to accurately model heterogeneities in contact behavior and a realistic network of recurrent contacts because some sub-populations might develop herd immunity even though the full population does not.

The workhorse model of epidemiology, the S(E)IR model as well as many recent extensions to it are not up to this task. We develop an agent-based simulation model that has been designed from the ground up to predict and quantify the effects of contact reducing policies, vaccinations and testing strategies in a constantly changing policy environment. It has the following features:

- (1) At the core of the model, people meet people based on a matching algorithm. We distinguish various types of contacts. The contact types are households, leisure activities, schools, preschools, and nurseries and several types of contacts at the workplace. Contact types can be random or recurrent and vary in frequency and infectiousness.
- (2) Policies can be implemented as shutting down contact types entirely or partially. The reduction of contacts can be random or systematic. For example, it is possible to implement split class schooling where only one half of each class attends and the attending half switches on a weekly bases. The extent to which contacts are reduced can be calibrated from observed data or estimated inside the model.
- (3) Infection probabilities vary across contact types and reflect properties of the contact like the location (indoor/outdoor) and the kind of interaction (duration, physical contact). The probabilities are independent from the number of contacts and, thus, policy-invariant.
- (4) We distinguish detected and undetected cases. The share of detected cases varies over time and across age groups. Moreover, it can be influenced by rapid testing policies.
- (5) High quality Python code for the model is freely available on Github, well documented and very flexible¹. We are actively looking for researchers who want to use our model for their projects and apply it to other contexts.

The model achieves a good fit on German data of infection and fatality rates, even though most parameters are calibrated from the literature and observable datasets and only a few parameters are estimated inside the model. At accurately predicts the rise of the B117 mutation in spring 2020. It can also explain the surprising decline of case numbers at the end of April, without making ad hoc assumptions on behavioral changes at the time.

The model has previously been applied to predict the effect of schooling policies, contact tracing policies over the Christmas holidays and the effect of work from home (Dorn, Gabler, Gaudecker, Peichl, Raabe, et al. (2020), Gabler, Raabe, Röhrl, and Gaudecker (2020), and Gabler, Raabe, Röhrl, and Gaudecker (2021)).

[Summary of the main results](#)

The remainder is structured as follows: In Section 2, we give a short overview of epidemiological models. Section 3 summarizes the policy environments and dynamic of the Covid-19 pandemic in Europe, with a special focus on Germany. We continue with a general description of our modelling framework as well as a specialization to the German context in section 4. Section 5 describes our empirical datasets, sources of calibrated parameters and estimation procedure. [describe result section](#). We conclude in section 9.

2 Literature Review

We build on two strands of literature: Recent extensions of the epidemiological SEIR model and agent-based simulation models.

The traditional SEIR model is not fine-grained enough to model nuanced policies. This has motivated a large number of researchers to extend the standard model to allow for more heterogeneity and flexibility. Examples are Grimm, Mengel, and Schmidt (2020), Donsimoni, Glawion, Plachter, and Wälde (2020) and Acemoglu, Chernozhukov, Werning, and Whinston (2020) who develop multi group SEIR models to analyze the effects of targeted lockdowns and Berger, Herkenhoff, and Mongey (2020) who extend the SEIR model to analyze testing and conditional quarantines. For a more comprehensive review see Avery, Bossert, Clark, Ellison, and Ellison (2020). Others have used the results of a standard SEIR model as input for economic models that estimate the cost of policies (e.g. Dorn, Khailaie, Stöckli, Binder, Lange, et al. (2020)).

While the popularity of the SEIR model is mainly due to its simplicity, the extensions are quite complex. It is unlikely that there will be a SEIR model that combines all proposed extensions. Moreover, the extensions do not address other key issues: The main parameter of the SEIR model, the basic reproduction number (R_0), is not

1. The code can be found under <https://github.com/covid-19-impact-lab/sid> and the documentation with tutorials and background information under <https://sid-dev.readthedocs.io/>.

policy-invariant. It is a composite of the number of contacts each person has and the infection probability of the contacts. In fact, policy simulations are done by setting R_0 to a different value but it is hard to translate a real policy into the value of R_0 it will induce. In other words, SEIR models are not suited for evaluating the effect of policies which have never been experienced before.

Another commonly used model class in epidemiology are agent-based simulation models. In these models individuals are simulated as moving particles. Infections take place when two particles come closer than a certain contact radius (e.g. Silva, Batista, Lima, Alves, Guimarães, et al. (2020) and Cuevas (2020)). While the simulation approach makes it easy to incorporate heterogeneity in disease progression, it is hard to incorporate heterogeneity in meeting patterns. Moreover, policies are modeled as changes in the contact radius or momentum equation of the particles. The translation from real policies to corresponding model parameters is a hard task.

Hinch, Probert, Nurtay, Kendall, Wymatt, et al. (2020) is a recent extension of the prototypical agent-based simulation model that replaces moving particles by contact networks for households, work and random contacts. This model is similar in spirit to ours but focuses on contact tracing rather than social distancing policies.

The above assessment of epidemiological models is not meant as a critique. We are aware that these models were not designed to predict the effect of fine-grained social distancing policies in real time and are very well suited to their purpose. We invite epidemiologists to provide feedback and collaborate to improve our model.

3 Background: The Situation in Germany

4 Model

4.1 Summary

To predict and quantify the effects of a wide variety of fine-grained social distancing policies, vaccinations and rapid testing, we propose a different model structure. Our model inherits many features from prototypical agent-based simulation models but replaces the contacts between moving particles by contacts between individuals who work, go to school, live in a household and enjoy leisure activities.

The structure of the model is depicted in Figure 1.

The background characteristics include age, county and occupation of each simulated individual. Contact models are functions that map individual characteristics into a predicted number of contacts. Currently, we distinguish between eight types of contact models which are all listed in Figure 1: households, recurrent and random work contacts, recurrent and random leisure contacts, and nursery, preschool, and school contacts.

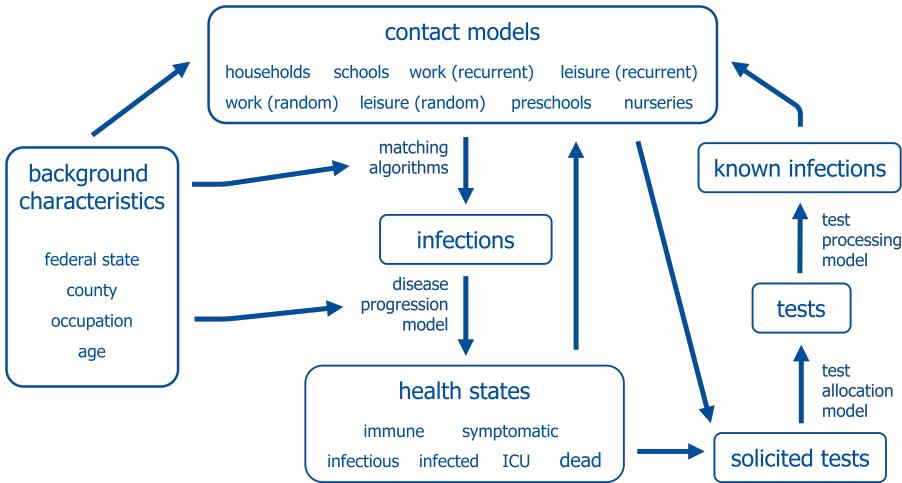


Figure 1. Simplified graph of the model.

The predicted number of contacts is translated into infections by a matching algorithm. There are different matching algorithms for recurrent contacts (e.g. classmates, family members) and non-recurrent contacts (e.g. clients, contacts in supermarkets). The infection probability can differ for each contact type. All types of contacts can be assortative with respect to geographic and demographic characteristics.

The infection probabilities of contacts vary with contact type, age of the susceptible person, and the virus strain of the infected person. Moreover, they follow a seasonal pattern. The strength of the seasonality effect is higher for contacts that are easy to be moved to an outside location in summer (such as leisure contacts) and smaller for contacts that take place inside even in summer (e.g. work contacts).

Once a person is infected, the disease progresses in a fairly standard way which is depicted in Figure 2. Asymptomatic cases and cases with mild symptoms are infectious for some time and recover eventually. Cases with severe symptoms additionally require hospitalization and lead to either recovery or death.

After rapid tests become available, people who work or go to school can receive rapid tests there. Moreover, people can decide to make a rapid test if they develop symptoms, have many planned contacts or observe cases in their contact network. People who have a positive rapid test demand a confirmatory PCR test with a certain probability. Moreover, PCR tests can be demanded because of symptoms or randomly.

This rich model of PCR and rapid tests leads to a share of detected cases that varies over time and across age groups. It also allows to quantify the effect of changes in testing policies on the dynamic of infections.

People who have symptoms, received a positive test, or had a risk contact can reduce their number of contacts across all contact types endogenously. The extent to which this is done is calibrated from survey data.

The model makes it very simple to translate policies into model quantities. For example, school closures imply the complete suspension of school contacts. A strict lockdown implies shutting down work contacts of all people who are not employed in a systemically relevant sector. It is also possible to have more sophisticated policies that condition the number of contacts on observable characteristics, risk contacts or health states.

Another key advantage of the model is that the number of contacts an individual has of each contact type can be calibrated from publicly available data (Mossong, Hens, Jit, Beutels, Auranen, et al., 2008). This in turn allows us to estimate policy-invariant infection probabilities from time series of infection and death rates using the method of simulated moments (McFadden, 1989). Since the infection probabilities are time-invariant, data collected since the beginning of the pandemic can be used for estimation. Moreover, since we model the testing strategies that were in place at each point in time, we can correct the estimates for the fact that not all infections are observed.

Last but not least, performing simulations whose starting point is set amidst the pandemic requires special adjustments to arrive at a realistic distribution of courses of diseases. We solve the initial conditions problem by matching reported infections to individuals in our data while also correcting for reporting lag and undetected cases.

In the following sections we describe each of the model components in more detail.

4.2 Modeling Numbers of Contacts

Consider a hypothetical population of 1,000 individuals in which 50 were infected with a novel infectious disease. From this alone, it is impossible to say whether only those 50 people had contact with an infectious person and the disease has an infection probability of 1 in each contact or whether everyone met an infectious person but the disease has an infection probability of only 5 percent per contact. SEIR models do not distinguish contact frequency from the infectiousness of each contact and combine the two in one parameter that is not invariant to social distancing policies.

To model social distancing policies, we need to disentangle the effects of the number of contacts of each individual and the effect of policy-invariant infection probabilities specific to each contact type. Since not all contacts are equally infectious, we distinguish different contact types.

The number and type of contacts in our model can be easily extended. Each type of contacts is described by a function that maps individual characteristics, health

states and the date into a number of planned contacts for each individual. This allows to model a wide range of contact types.

In our empirical application we distinguish the following types of contacts:

- Households: Each household member meets all other household members every day. The household sizes and structures are calibrated to be representative for Germany.
- Random non-work contacts: Each person has contacts with randomly drawn other people which are assortative with respect to region and age group. This contact type reflects contacts during pure leisure activities as well as non leisure activities such as grocery shopping or medical appointments.
- Recurrent daily non-work contacts: Each person has daily recurring contacts which allows to model close relationships other than families between individuals.
- Recurrent weekly non-work contacts: Each person has weekly recurring contacts like sports groups or other weekly activities.
- Random work contacts: Each working adult has contact to randomly drawn other people at work.
- Recurrent daily work contacts: Each working adult meets other workers every day. This is meant to capture work colleagues.
- Recurrent weekly work contacts: Each working adult meets other workers once per week. We randomize over the days on which the meetings take place. This is meant to capture meetings with clients, superiors or other colleagues which happen infrequently.
- Schools: Each student meets all of his classmates every day. Class sizes are calibrated to be representative for Germany and students have the same age. Schools are closed on weekends and during vacations, which vary by states. School classes also meet three pairs of teachers every school day. The pairs are meant to represent interactions between teachers.
- Preschools: Children who are at least three years old and younger than six may attend preschool. Each group of nine children interacts with the same two adults every day. The children in each group are of the same age. The remaining mechanics are similar to schools.
- Nurseries: Children younger than three years may attend a nursery and interact with one adult. The age of the children varies within groups. The remaining mechanics are similar to schools.

The number of random and recurrent contacts at the workplace, during leisure activities and at home is calibrated with data provided by Mossong et al. (2008). For details see Section 4.2. In particular, we sample the number of contacts or group

sizes from empirical distributions that sometimes depend on age. It is also possible to use economic or other behavioral models to predict the number of contacts.

Theoretically, each contact type can have its own infection probability. However, to reduce the number of free parameters and thus avoid a potential over-fitting we only estimate different infection probabilities for the areas work, school, preschool and nurseries, households and other contacts.

4.3 Reducing Numbers of Contacts Through Policies

The main motivation of our model is to predict the effect of policies that affect the number of contacts people have. Examples range from school closures and lockdowns to more nuanced policies such as mandatory quarantines for symptomatic individuals or a class splitting policy where only half of the students come to school in person and the other half joins digitally with weekly rotation.

Instead of thinking of policies as completely replacing how many contacts people have, it is often more helpful to think of them as adjusting the pre-pandemic number of contacts.

Therefore, we implement policies as a step that happens after the number of contacts is calculated but before individuals are matched.

On an abstract level, a policy is a function that modifies the number of contacts of one contact type. For example, school closures simply set all school contacts to zero. A lockdown where only essential workers are allowed to work means that approximately two thirds of the working population have zero work contacts and the rest has the same number of contacts as before.

This, in conjunction with our fine-grained contact types, allows us to easily implement a wide variety of policies. Allowing policies to depend on the health states of the entire population means that adaptive lockdowns where, for example, schools close when a certain threshold of infections is surpassed at the county level would be as simple as determining which counties are above the threshold and then setting all school contacts in these counties to zero.

The dependency of policies on health states also makes it possible to model contact tracing. For example, a policy could check whether each child has a classmate who's received a positive test result and then bar all children of that class from attending school.

Some policies can be easily implemented if the background characteristics are suitably extended. For example, a schooling policy of splitting and rotating classes, where each half attends school every other week can be implemented by storing whether the child would attend in even or odd weeks in the background characteristics and then using that information in the policy function.

For some policies the exact effect on each contact type is not easy to determine. If this refers to a policy during the estimation period, it is possible to estimate such parameters by fitting the model to time series data of infection rates. This is only

possible if the policy was not active during the whole estimation period and thus the infection probabilities can be identified separately. If instead it refers to a policy that we want to simulate, we make a scenario analysis in which the model is simulated with several assumptions about how the policy affects the number of contacts.

4.4 Endogenous Contact Reductions

Policies are not the only way in which the number of contacts are reduced compared to the pre-pandemic level. It is important to model those other channels. Otherwise, the effect of policies would be overestimated and policy recommendations based on the model would be biased.

Examples of endogenous contact reductions are manifold: symptomatic people stay at home; Members of risk groups try to reduce their number of contacts more strongly than others; People self-isolate if they know they had a risk contact.

Since we model the number of contacts as arbitrary functions of background characteristics and health states, it is easy to implement such considerations.

In our current empirical application we only model that symptomatic people reduce their number of contacts across all contact types (except for households) by 70 %. Within households they reduce contacts by 50%. We are working on extending this to allow for formal and informal contact tracing as well as quarantines after positive test results. For an application of our model showcasing private contact tracing in the context of the Christmas holidays see Gabler, Raabe, Röhrl, et al. (2020).

4.5 Matching Individuals

The empirical data described above only allows to estimate the number of contacts each person has. In order to simulate transmissions of Covid-19, the numbers of contacts has to be translated into actual meetings between people. This is achieved by our matching algorithm:

As described in section 4.2, some contact types are recurrent (i.e. the same people meet regularly), others are non-recurrent (i.e. it would only be by accident that two people meet twice). The matching process is different for recurrent and non recurrent contact models.

Recurrent contacts are described by two components: 1) A variable in the background characteristics. An example would be a school class identifier which could come from actual data or be drawn randomly to achieve representative class sizes. 2) A deterministic or random function that takes the value 0 (non-participating) and 1 (participating) and can depend on the weekday, date and health state. This can be used to model vacations, weekends or symptomatic people who stay home (see section 4.4 for details).

The matching process for recurrent contacts is then extremely simple: On each simulated day, every person who does not stay home meets all other group members who do not stay home. The assumption that all group members have contacts

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while are_unmatched_contacts_left:

    contact_type, i = draw_contact_type_and_individual()

    for _ in remaining_contacts[i, contact_type]:

        group_j = draw_group_of_other_person()
        j = draw_other_person_from_that_group(group_j)

        if infection_takes_place(i, j):
            update_health_state_of_freshly_infected()

        remaining_contacts[i, contact_type] -= 1
        remaining_contacts[j, contact_type] -= 1

```

Listing 1. Pseudo-code of the matching algorithm for non-recurrent contacts.

with all other group members is not fully realistic, but seems like a good approximation to reality, especially in light of the suspected role of aerosol transmission for Covid-19 (Anderson, Turnham, Griffin, and Clarke, 2020; Morawska, Tang, Bahnfleth, Bluyssen, Boerstra, et al., 2020).

The matching in non-recurrent contact models is more difficult and implemented in a two stage sampling procedure to allow for assortative matching. Currently most contact models are assortative with respect to age (it is more likely to meet people from the same age group) and county (it is more likely to meet people from the same county) but in principle any set of discrete variables can be used. This set of variables that influence matching probabilities introduce a discrete partition of the population into groups. The first stage of the two stage sampling process samples on the group level. The second stage on the individual level.

Below, we first show pseudo code for the non-recurrent matching algorithm and then describe how the algorithm works in words.

We first randomly draw a contact type and individual. For each contact of the drawn contact type that person has, we first draw the group of the other person (first stage). Next, we calculate the probability to be drawn for each member of the group, based on the number of remaining contacts, i.e. people who have more remaining contacts are drawn with a higher probability. This has to be re-calculated each time because with each matched contact, the number of remaining contacts changes. We then draw the other individual, determine whether an infection takes place and if so update the health state of the newly infected person. Finally, we reduce the number of remaining contacts of the two matched individuals by one.

The recalculation of matching probabilities in the second stage is computationally intensive because it requires summing up all remaining contacts in that group.

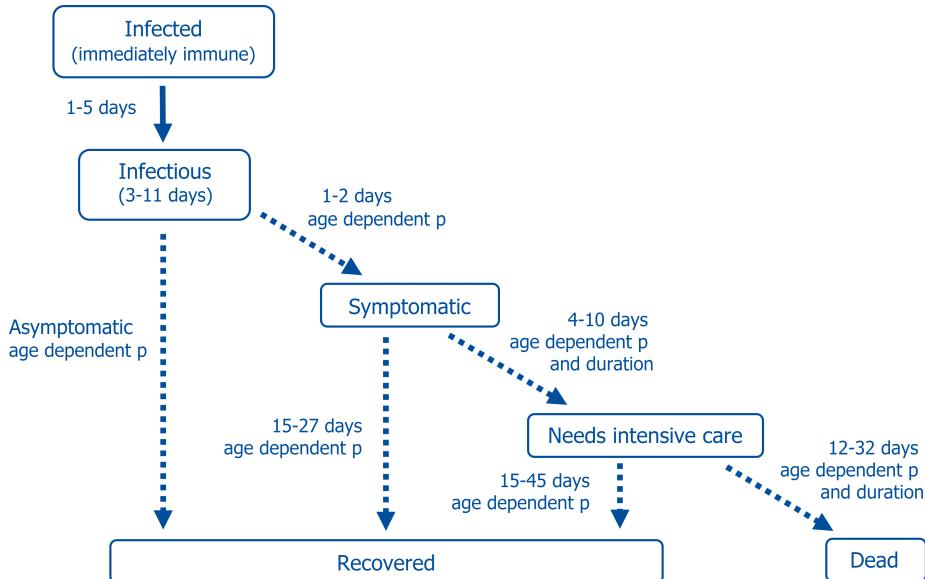


Figure 2. Course of Disease in the model.

Notes: The figure depicts the course of the disease from infection to either the state of recovery or death.

Using a two stage sampling process where the first stage probabilities remain constant over time makes the matching computationally much more tractable because the number of computations increases quadratically in the second stage group size.

4.6 Course of the Disease

The following medical parameters describing the progression of the disease are taken from systematic reviews (e.g. He, Lau, Wu, Deng, Wang, et al. (2020)). After an infection occurs, the disease progresses in the way depicted in Figure 2.

First, infected individuals will become infectious after one to five days. About one third of people remain asymptomatic. The rest develop symptoms about one to two days after they become infectious. Modeling asymptomatic and pre-symptomatic cases is important because those people do not reduce their contacts or demand a test and can potentially infect many other people (Donsimoni et al., 2020). The probability to develop symptoms with Covid-19 is highly age dependent with 75% of children not developing symptoms (Davies, Klepac, Liu, Prem, Jit, et al., 2020).

A small share of symptomatic people will develop strong symptoms that require intensive care. The exact share and time span is age-dependent. An age-dependent share of intensive care unit (ICU) patients will die after spending up to 32 days in intensive care. Moreover, if the ICU capacity was reached, all patients who require intensive care but do not receive it die.

It would be easy to make the course of disease even more fine-grained. For example, we could model people who require hospitalization but not intensive care. So far we opted against that because only the intensive care capacities are feared to become a bottleneck in Germany.

We allow the progression of the disease to be stochastic in two ways: Firstly, state changes only occur with a certain probability (e.g. only a fraction of infected individuals develops symptoms). Secondly, the number of periods for which an individual remains in a state is drawn randomly. The parameters that govern these processes are taken from the literature² and age-dependent.

4.7 Testing

We support to model testing as consisting of three stages. Firstly, we model who demands a test. Demand functions map from individual characteristics to a probability which is the probability for this individual to demand a test. There can be multiple demand functions where each function may describe a different channel. For example, individuals who experience symptoms or have a risk contact may ask for a test. Or, the ministry of education requires a negative test result from every teacher every second week. After the probabilities for each individual and every demand model are computed, individuals who demand a test as well as the channel is sampled.

The second stage is the allocation phase in which demand and supply for tests are matched. The number of available tests can be inferred from official data and used to model shortages in supply. When demand exceeds supply, some individuals might be given preferred access to tests because of their own vulnerability or their potential to become a super-spreader.

In the last and third phase, administered tests are processed. This step can become a bottleneck in the testing process if there are not enough laboratories or necessary resources available to evaluate all tests.

In our empirical estimation we use a very simplified testing model where the number of tests to be distributed is calculated from estimates for the ratio of known to all infections.³ Using these estimates as well as data on the test distribution over age groups by the RKI⁴ we allocate tests firstly among the symptomatic and then randomly allocate tests to newly infected to fit the German test distribution.

4.8 Initial Conditions

Consider a situation where you want to start a simulation with the beginning set amidst the pandemic. It means that several thousands of individuals should already

2. Detailed information on the calibration of the disease parameters is available as part of our [online documentation](#).

3. The Dunkelziffferradar project publishes daily estimates of the dark figure of infections under <https://covid19.dunkelziffferradar.de/>

4. <https://ars.rki.de/Content/COVID19/Main.aspx>

have recovered from the disease, be infectious, symptomatic or in intensive care at the start of your simulation. Additionally, the sample of infectious people who will determine the course of the pandemic in the following periods is likely not representative of the whole population because of differences in behavior (number of contacts, assortativity), past policies (school closures), etc.. The distribution of courses of diseases in the population at the begin of the simulation is called initial conditions.

To come up with realistic initial conditions, we match reported infections from official data to simulated individuals by available characteristics like age and geographic information. The matching must be done for each day of a longer time frame like a month to have individuals with possible health states. Then, health statuses evolve until the begin of the simulation period without simulating infections by contacts. We also correct reported infections for a reporting lag and scale them up to arrive at the true number of infections.

5 Calibration and Estimation

The model is described by a large number of parameters that govern the number of contacts a person has, the likelihood of becoming infected on each contact, the likelihood of developing light or strong symptoms or even dying from the disease as well as the duration each stage of the disease takes.

Most of these parameters can be calibrated from existing datasets or the medical literature. Only the infection probabilities have to be estimated inside the model by fitting it to time series data of case numbers and fatality rates.

5.1 Medical Parameters

This section discusses the medical parameters used in the model, their sources and how we arrived at the distributions used in the model.⁵ See Figure 2 for a summary of our disease progression model.

5.1.1 Duration until Infectiousness and Symptoms. The first medical parameter we need is the length of the period between infection and the start of infectiousness, the so called latent period. We infer it from two other measures that are more common in the medical literature: Firstly, the time between infection and the onset of symptoms, the incubation period. Secondly, the time between the start of infectiousness and the onset of symptoms. We assume that the latency period is the same for symptomatic and asymptomatic individuals.

5. Additional information can be found in the [online documentation](#).

Once individuals become infectious a share of them goes on to develop symptoms while others remain asymptomatic. We rely on data by Davies et al. (2020) for the age-dependent probability to develop symptoms. It varies from 25% for children and young adults to nearly 70% for the elderly.

The incubation period is usually estimated to be two to twelve days. A meta analysis by McAlloon, Collins, Hunt, Barber, Byrne, et al. (2020) comes to the conclusion that “The incubation period distribution may be modeled with a lognormal distribution with pooled μ and σ parameters (95% CIs) of 1.63 (95% CI 1.51 to 1.75) and 0.50 (95% CI 0.46 to 0.55), respectively.” For simplicity we discretize this distribution into four bins.

The <https://bit.ly/3pi18Ax> reports that people become infectious between one and two days before symptoms start.⁶

Taking these estimates together, we arrive at a latent period of one to five days.

5.1.2 Duration of Infectiousness. We assume that the duration of infectiousness is the same for both symptomatic and asymptomatic individuals as evidence suggests little differences in the transmission rates between symptomatic and asymptomatic patients (Yin and Jin (2020)) and that the viral load between symptomatic and asymptomatic individuals are similar (Zou, Ruan, Huang, Liang, Huang, et al. (2020), Byrne, McEvoy, Collins, Hunt, Casey, et al. (2020), Singanayagam, Patel, Charlett, Bernal, Saliba, et al. (2020)).

Our distribution of the duration of infectiousness is based on Byrne et al. (2020).

For symptomatic cases they arrive at 0-5 days before symptom onset (figure 2) and 3-8 days of infectiousness afterwards.⁷ Thus, we arrive at 0 to 13 days as the range for infectiousness among individuals who become symptomatic (see also figure 5). This duration range is very much in line with the meta-analysis' reported evidence for asymptomatic individuals (see their figure 1).

Following this evidence we assume the following discretized distribution of the infectiousness period: 10% of individuals are infectious for three days, 25% for five days, another 25% for seven days, 20% for nine days and 20% for eleven days.

5.1.3 Duration of Symptoms. We use the duration to recovery of mild and moderate cases reported by Bi, Wu, Mei, Ye, Zou, et al. (2020, Figure S3, Panel 2) for the duration of symptoms for asymptomatic and non-ICU requiring symptomatic cases.

We collapse the data to the following distribution: 10% recover after 15 days and 30% require 18, 22 or 27 days respectively.

These numbers are only used for mild cases. We do not disaggregate by age. Note that the length of symptoms is not very important in our model given that individuals stop being infectious before their symptoms cease.

6. This is similar to He et al. (2020) and in line with Peak, Kahn, Grad, Childs, Li, et al. (2020).

7. Viral loads may be detected much later but 8 days seems to be the time after which most people are culture negative, as also reported by Singanayagam et al. (2020).

Table 1. Shares of symptomatic patients who will require ICU care by age groups.

Age Group	Share
0-9	0.00005
10-19	0.00030
20-29	0.00075
30-39	0.00345
40-49	0.01380
50-59	0.03404
60-69	0.10138
70-79	0.16891
80-100	0.26871

Notes: The data is taken from Stokes et al. (2020) and [the OpenABM-Project](#).

5.1.4 Time from Symptom Onset to Admission to ICU. The data on how many percent of symptomatic patients will require ICU is pretty thin. We rely on data by the US CDC (Stokes, Zambrano, Anderson, Marder, Raz, et al. (2020)) and [the OpenABM-Project](#). Table 1 shows our derivations for the probabilities of requiring intensive care per age group.

For those who will require intensive care we follow Chen, Qi, Liu, Ling, Qian, et al. (2020) who estimate the time from symptom onset to ICU admission as 8.5 ± 4 days.

This aligns well with numbers reported for the time from first symptoms to hospitalization: Gaythorpe, Imai, Cuomo-Dannenburg, Baguelin, Bhatia, et al. (2020) report a mean of 5.76 with a standard deviation of 4. This is also in line with the durations collected by [the Robert-Koch-Institut](#).

We assume that the time between symptom onset and ICU takes 4, 6, 8 or 10 days with equal probabilities. These times mostly matter for the ICU capacities.

5.1.5 Death and Recovery from ICU. We take the survival probabilities and time to death and time until recovery from [the OpenABM Project](#).

They report time until death to have a mean of 11.74 days and a standard deviation of 8.79 days. Approximating this with the normal distribution, we have nearly 10% probability mass below 0. We use it nevertheless as several other distributions (such as chi squared and uniform) were unable to match the variance. Discretizing the distribution leads to 41% of individuals who will die from Covid-19 after one day in intensive care, 22% day after 12 days, 29% after 20 days and 7% after 32 days. Again, we rescale this for every age group among those that will not survive.

They report a mean duration of 18.8 days until recovery and a standard deviation of 12.21 days. Approximating this with the normal distribution, we have over 5% probability mass below 0. Of those who recover in intensive care, 22% do so after one day, 30% after 15 days, 28% after 25 days and 18% after 45 days.

5.2 Number of Contacts

We calibrate the parameters for the predicted numbers of contacts from contact diaries of over 2000 individuals from Germany, Belgium, the Netherlands and Luxembourg (Mossong et al., 2008). Each contact diary contains all contacts an individual had throughout one day, including information on the other person (such as age and gender) and information on the contact. Importantly, for each contact individuals entered of which type the contact (school, leisure, work etc.) was and how frequent the contact with the other person is.

Thus, we can use the empirical distributions from this data as pre-pandemic number of contacts.

5.3 Assortative Matching

As mentioned in section 4.5, the probability that two individuals are matched can depend on background characteristics. In particular, we allow this probability to depend on age and county of residence. While we do not have good data on geographical assortativity and just roughly calibrate it such that 60 % of contacts are within the same county, we can calibrate the assortative mixing by age from the same data we use to calibrate the number of contacts.

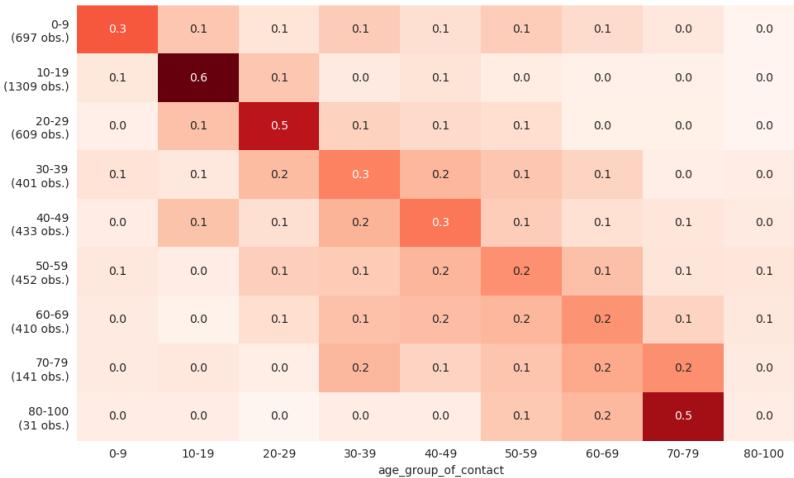


Figure 3. Distribution of random non-work contacts by age of participants.

Notes: The figure shows the distribution of random non-work contacts by age groups. A row shows the share of contacts a certain age group has with all other age groups. Higher values are colored in darker red tones. The diagonal represents the share of contacts with individuals from the same age group.

Figure 3 shows that assortativity by age is especially strong for children and younger adults. For older people, the pattern becomes more dispersed around their own age group, but within-age-group contacts are still the most common contacts.

5.4 Infection Probabilities

To calibrate infection probabilities outside of the model, it would be important to know the exact duration and distance of each contact type as well as viral loads. Since this is not available in any dataset, we estimate those parameters inside the model with the method of simulated moments (McFadden, 1989) by minimizing the distance between simulated and observed infection rates. Since our model includes a lot of randomness, we average simulated infection rates over several model runs.

Currently, we use data for Germany from August until November. We do not use earlier periods to save computational time. Moreover, we would be worried that there are seasonal effects that we currently do not model.

To avoid overfitting and simplify the numerical optimization problem, we only allow for four different probabilities: 1) for contacts in schools, preschools and nurseries. 2) for work contacts. 3) for households. 4) for leisure activities.

5.5 Policies

In our empirical application we distinguish four groups of contact types: households, education, work and other contacts. For households we assume that the individuals' contacts in their households do not change over our estimation period. For nurseries, preschools and schools we implement vacations as announced by the German federal states as well as school closures. For the moment we ignore both emergency childcare and that lack of childcare leads working parents to stay home. For our work models⁸we use the reductions in work mobility reported in the Google Mobility Data (LLC, 2021) to calibrate our work policies. Reductions in work contacts are not random but governed through a work contact priority where the policy changes the threshold below which workers stay home. Figure 4 shows the share of workers that go to work in our model over time.

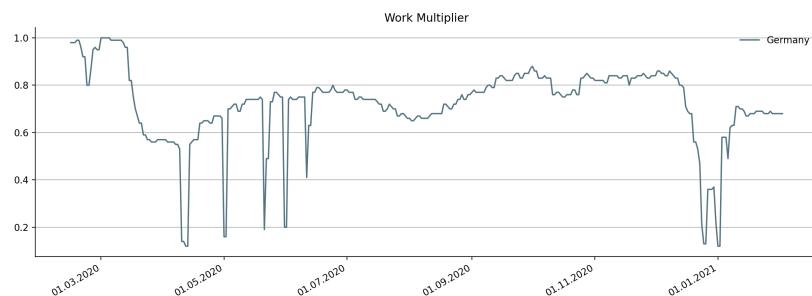


Figure 4. Share of workers attending work normally.

Notes: The figure shows the percentage of pre-pandemic work mobility taking place since the start of the pandemic. In our model this is used as a proxy for the share of workers that attend work as usual. Workers are ordered with the importance of personal contacts for their work. Thus, if the share of

For the last group of contacts which cover things like leisure activities, grocery shopping etc. we have no reliable data by how much policies reduce them. In addition, they are likely to be affected by social and psychological factors such as pandemic fatigue and vacations. Because of this we estimate them like the infection probabilities to fit the time series data. We use very few change points and tie them to particular events such as policy announcements or particular holidays.

6 Model Validation

This compares simulated data from our model with empirical data from Germany. We at observed infections, fatality rates, the spread of the B117 mutation, vaccinations and rapid test demands. Where available we do not only look at aggregated statistics but also analyze the model fit for age groups.

summarize the fit

6.1 Observed Infections

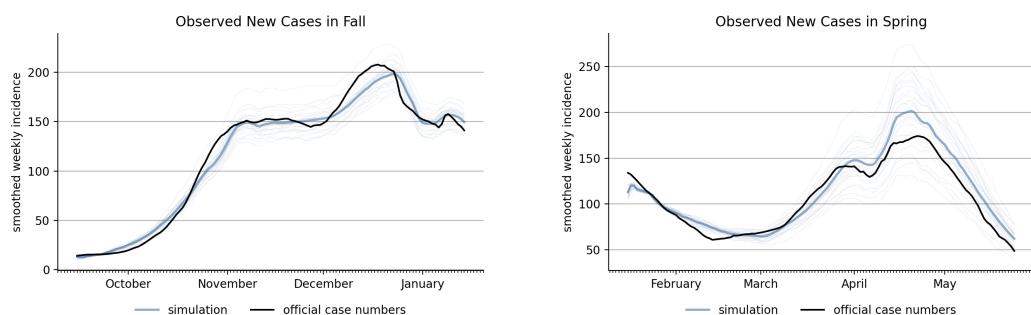


Figure 5. Simulated and Empirical Infections

Notes: The figure shows the weekly incidence rates per 100,000 people for the reported versus the simulated infections rates.

8. We distinguish non-recurrent work contacts, daily work contacts and weekly work contacts.

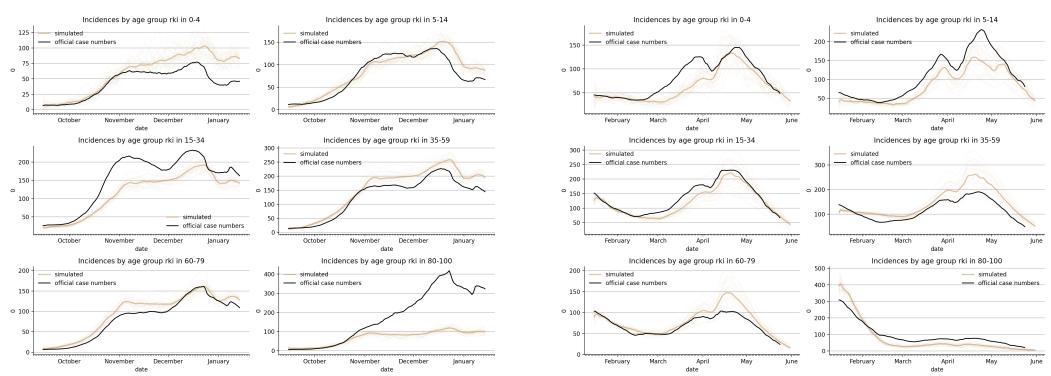


Figure 6. Simulated and Empirical Infections by Age Group

Notes: The figure shows the weekly incidence rates per 100,000 people for the reported versus the simulated infections rates for different age groups.

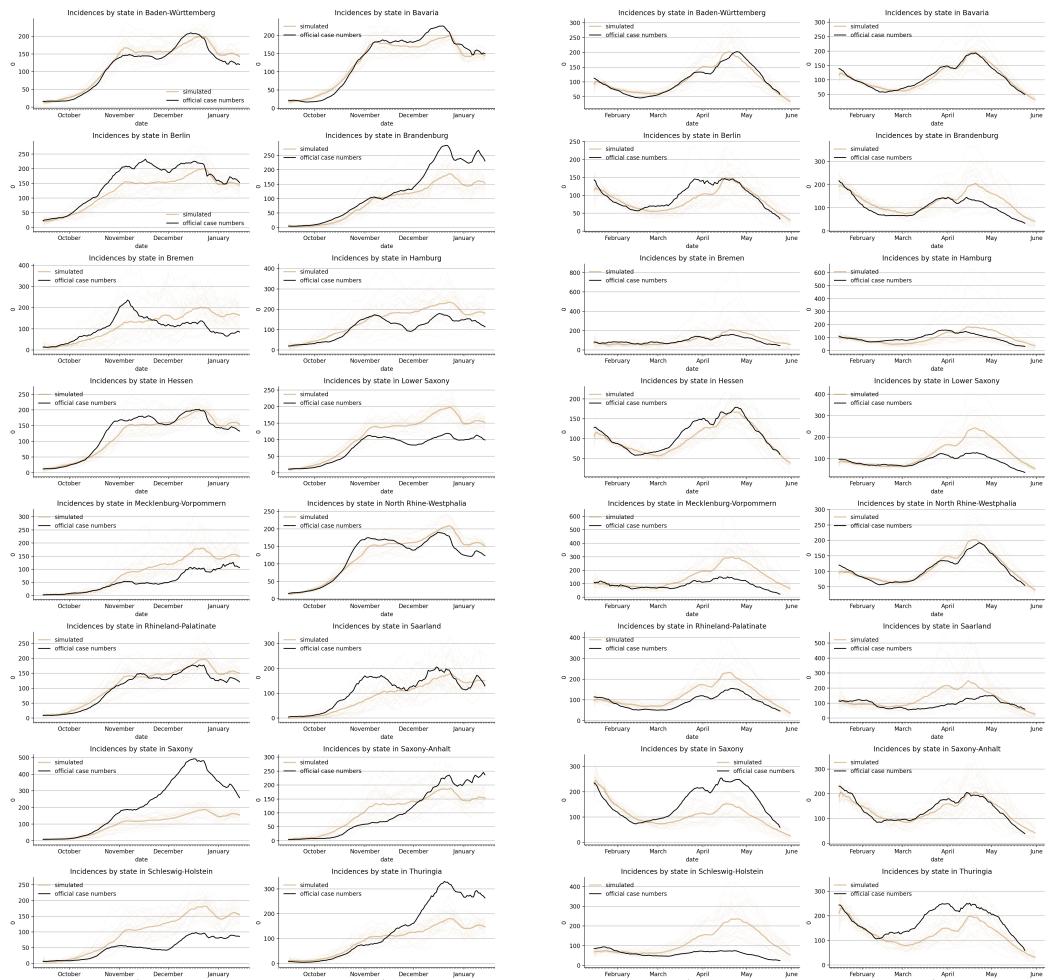


Figure 7. Simulated and Empirical Infections by Age Group

Notes: The figure shows the weekly incidence rates per 100,000 people for the reported versus the simulated infections rates for different federal regions.

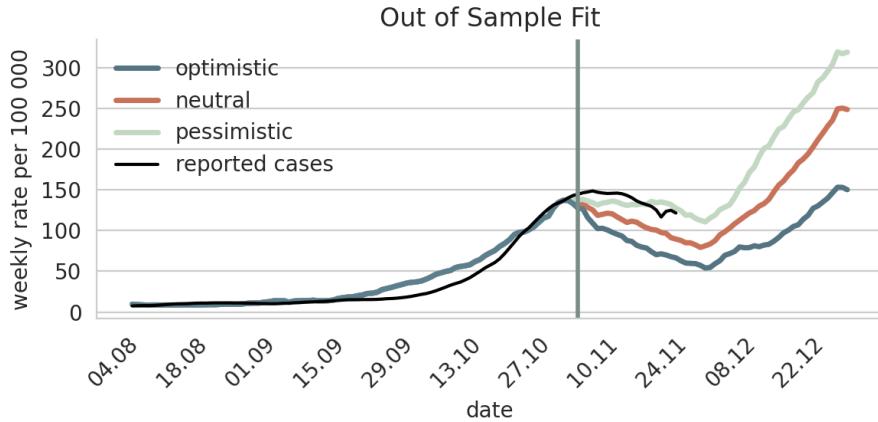


Figure 8. Predicted effect of the "Lockdown Light" on infection rates.

Notes: For the time period until the beginning of November, the figure shows the weekly incidence rates of infections per 100,000 people from reported (black) versus simulated (blue) data. With the start of November, the projections of the three scenarios, optimistic (blue), neutral (red), and pessimistic (mint green), are shown until the beginning of the Christmas holidays. The actual incidence rates (black) are reported until the 24th November.

7 The Spread of the B117 Mutation

We don't have this figure in the repo yet, but the fit is perfect

7.1 Out-of-Sample Fit

We can assess the out-of-sample fit by projecting the effect of the lockdown light and comparing it to case numbers until mid of November. It is important to note that this is not just a simple extrapolation of a time trend because the lockdown light only started after the estimation period. The out-of-sample fit can be assessed in Figure 8.

The model correctly predicts the effect of the lockdown light with reasonable accuracy. In particular, the actual case numbers are between our neutral and pessimistic projection. The plot also shows that ending the lockdown light on November 30, as was originally planned, would lead to an explosive growth in case numbers in all scenarios.

8 Results

This is the results section.

The results can be found in 'figures/results'. This includes both figures and tables for lookup of numbers and summary tables

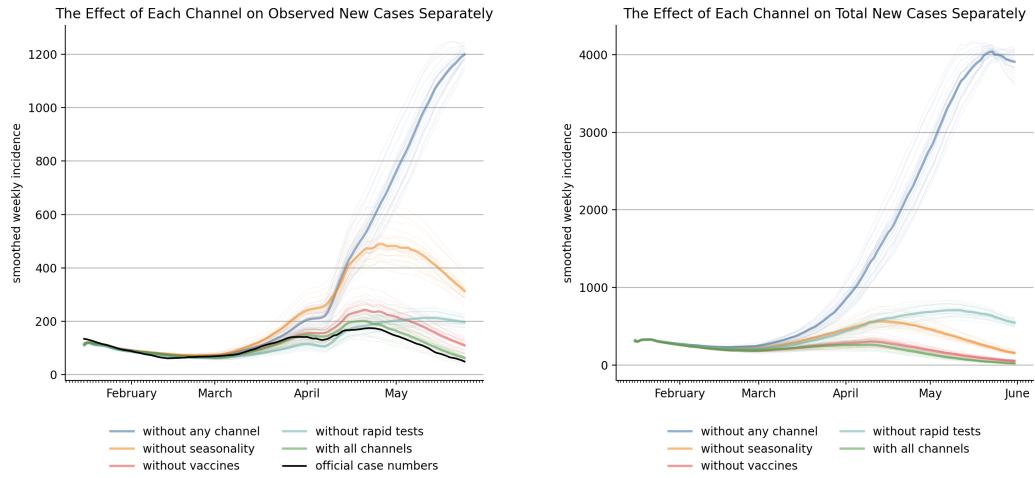


Figure 10. The Effect of Policies on Observed and Unobserved Cases

Notes: ...

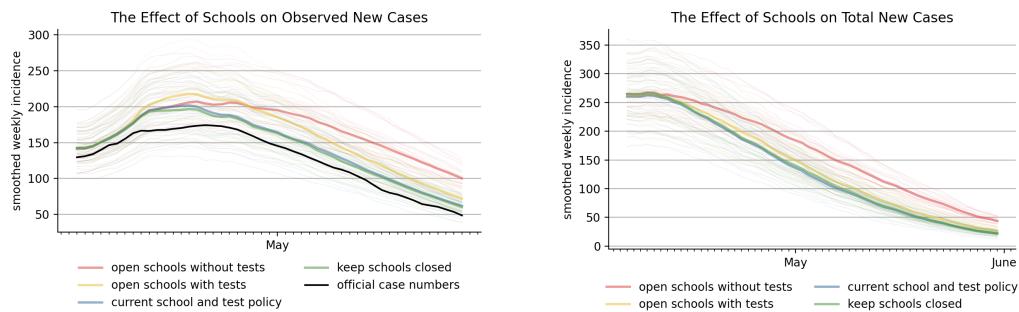


Figure 11. The Effect of Different School Scenarios on Observed and Unobserved Cases

Notes: ...

predicted total infections among 5-14 year olds from Easter until 2021 scenario	
educ open after easter without tests	8
educ open after easter with tests	6
baseline	4
close educ after easter	4

9 Conclusion

We propose a simulation based model of infectious disease transmission that is designed to predict the effects of fine-grained social distancing policies. In particular,

the model can be used to model policies such as several ways of splitting school classes or work reduction policies that affect essential and non-essential workers differentially. Both policies would be hard to implement in standard SEIR or agent based simulation models.

To predict the effects of such policies, it is not only important to have a way of expressing such flexible policies in terms of model quantities, but also to incorporate heterogeneity in disease progression as well as meeting patterns. We calibrate age dependent disease progression parameters from the medical literature and age dependent contact frequencies from contact diaries. Moreover, we distinguish ten types of contacts out of which some are only relevant for certain age groups.

The model has a good fit on past German case numbers and passes an out of sample validation despite a drastic change in the policy environment between the estimation period and the validation period.

Despite these encouraging results we still see the model as work in progress. We plan to implement more features, in particular allowing age and symptoms to affect the probability to seek and receive a test, opening the way to show the effect of different testing policies, such as those proposed by Tröger et al. (2020). Moreover, the estimation of the infection probabilities and the model fit will improve as more data becomes available.

We invite researchers from any discipline, but particularly epidemiologists to provide feedback on the model and welcome collaborations.

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