

Swansea University

College of Engineering

## EGLM03 Modern Control Systems

### Homework 3: Lag Compensation

#### Problems

1. A satellite attitude control system has an open-loop transfer function

$$G_o(s) = \frac{4(s+2)}{s}$$

determine the low frequency gain required to ensure that the steady-state error to a constant acceleration input of  $1 \text{ rad/s}^2$  is  $1/40 \text{ rad}$ . Design a lag compensator to give the required low frequency gain.

1. A plant has a transfer function

$$G(s) = \frac{K}{s(s+10)^2}$$

The velocity constant  $K_v$  of a feedback control system for this plant is to be 20, while the damping ratio  $\zeta$  of the dominant second-order closed-loop poles is to be 0.707. Design a lag compensator to achieve this specification.

1. A numerical path-controlled turret lathe control system is illustrated in Figure 1. The gear ratio is  $n = 0.1$ , the motor inertia is  $J = 10^{-3} \text{ kg.m}^2$  and the motor resistance is  $R = 10^{-2} \text{ Nm/(rad/s)}$ . It is necessary to attain an accuracy of 0.5 thousandths of an inch in the position of the cutting tool relative to the workpiece and therefore a position accuracy of 1% is required for a ramp input. Design a cascade controller, to be inserted before the silicon-controlled-rectifiers (SCRs), in order to provide a step command with an overshoot of less than 2%. A suitable damping ratio for the system is 0.8. The gain of the SCRs is  $K_r = 5$ .

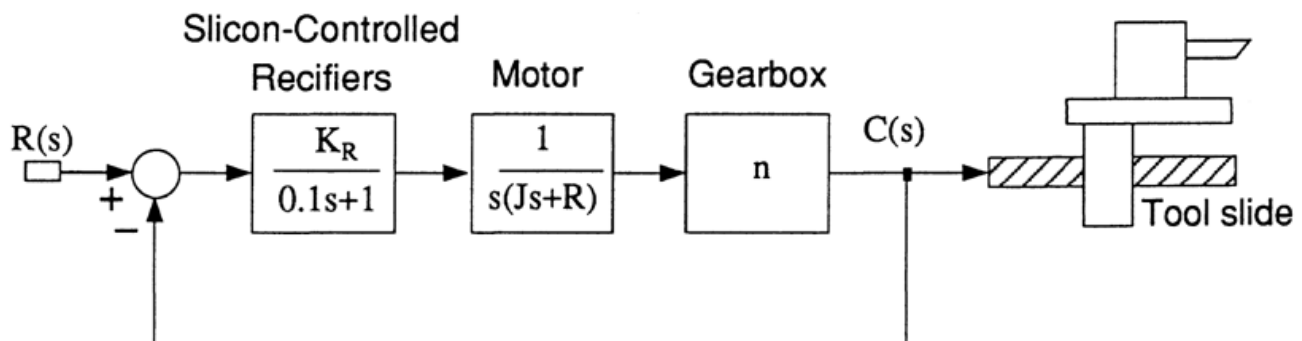


Figure 1