## 0.1 netpoisson: Network Poisson Regression for Event Count Proximity Matrix Dependent Variables

Use network Poisson regression analysis for a dependent variable that represents the number of events that occur during a fixed period of time as a proximity matrix (a.k.a. sociomatricies, adjacency matrices, or matrix representations of directed graphs).

#### Syntax

```
> z.out <- zelig(y ~ x1 + x2, model = "netpoisson", data = mydata)
> x.out <- setx(z.out)
> s.out <- sim(z.out, x = x.out)</pre>
```

### **Additional Inputs**

In addition to the standard inputs, zelig() takes the following additional options for network poisson regression:

• LF: specifies the link function to be used for the network poisson regression. Default is LF="log", but LF can also be set to "sqrt" by the user.

#### Examples

1. Basic Example

Load the sample data (see ?friendship for details on the structure of the network dataframe):

```
> data(friendship)
```

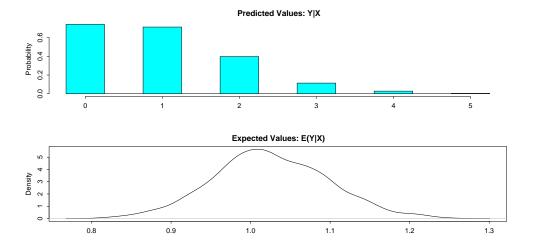
Estimate model:

> plot(s.out)

```
> z.out <- zelig(count ~ advice + prestige + perpower, model = "netpoisson",
+ data = friendship)
> summary(z.out)
```

Setting values for the explanatory variables to their default values:

```
> x.out <- setx(z.out)
Simulate fitted values.
> s.out <- sim(z.out, x = x.out)
> summary(s.out)
```



#### Model

The netpoisson model performs a Poisson regression of the proximity matrix  $\mathbf{Y}$ , a  $m \times m$  matrix representing network ties, on a set of proximity matrices  $\mathbf{X}$ . This network regression model is directly analogous to standard Poisson regression element-wise on the appropriately vectorized matrices. Proximity matrices are vectorized by creating Y, a  $m^2 \times 1$  vector to represent the proximity matrix. The vectorization which produces the Y vector from the  $\mathbf{Y}$  matrix is performed by simple row-concatenation of  $\mathbf{Y}$ . For example, if  $\mathbf{Y}$  is a  $15 \times 15$  matrix, the  $\mathbf{Y}_{1,1}$  element is the first element of Y, and the  $\mathbf{Y}_{2,1}$  element is the second element of Y and so on. Once the input matrices are vectorized, standard Poisson regression is performed.

Let  $Y_i$  be the dependent variable, produced by vectorizing an event count proximity matrix, for observation i.  $Y_i$  is thus the number of independent events that occur during a fixed time period. This variable can take any non-negative integer.

• The Poisson distribution has stochastic component

$$Y_i \sim \text{Poisson}(\lambda_i)$$
,

where  $\lambda_i$  is the mean and variance parameter.

• The *systematic component* is given by:

$$\lambda_i = \exp(x_i \beta).$$

where  $x_i$  is the vector of explanatory variables and  $\beta$  is the vector of coefficients.

#### Quantities of Interest

The quantities of interest for the network Poisson regression are the same as those for the standard Poisson regression.

• The expected value (qi\$ev) for the netpoisson model is the mean of simulations from the stochastic component,

$$E(Y) = \lambda_i = \exp(x_i \beta),$$

given draws of  $\beta$  from its sampling distribution.

- The predicted value (qi\$pr) is a random draw from the Poisson distribution defined by mean  $\lambda_i$ .
- The first difference (qi\$fd) for the network Poisson model is defined as

$$FD = \Pr(Y|x_1) - \Pr(Y|x)$$

#### **Output Values**

The output of each Zelig command contains useful information which you may view. For example, you run z.out <- zelig(y ~ x, model = "netpoisson", data), then you may examine the available information in z.out by using names(z.out), see the coefficients by using z.out\$coefficients, and a default summary of information through summary(z.out). Other elements available through the \$ operator are listed below.

- From the zelig() output stored in z.out, you may extract:
  - coefficients: parameter estimates for the explanatory variables.
  - fitted values: the vector of fitted values for the systemic component  $\lambda$ .
  - residuals: the working residuals in the final iteration of the IWLS fit.
  - linear.predictors: the vector of  $x_i\beta$ .
  - aic: Akaikeś Information Criterion (minus twice the maximized log-likelihood plus twice the number of coefficients).
  - bic: the Bayesian Information Criterion (minus twice the maximized log-likelihood plus the number of coefficients times  $\log n$ ).
  - df.residual: the residual degrees of freedom.
  - df.null: the residual degrees of freedom for the null model.
  - zelig.data: the input data frame if save.data = TRUE
- From summary(z.out)(as well as from zelig()), you may extract:
  - mod.coefficients: the parameter estimates with their associated standard errors, p-values, and t statistics.
  - cov.scaled: a  $k \times k$  matrix of scaled covariances.
  - cov.unscaled: a  $k \times k$  matrix of unscaled covariances.
- From the sim() output stored in s.out, you may extract:

- qi\$ev: the simulated expected probabilities for the specified values of x.
- qi\$pr: the simulated predicted values for the specified values of x.
- qi\$fd: the simulated first differences in the expected probabilities simulated from x and x1.

### How to Cite

To cite the *netpoisson* Zelig model:

Skyler J. Cranmer. 2007. "netpoisson: Network Poisson Regression for Event Count Proximity Matrix Dependent Variables," in Kosuke Imai, Gary King, and Olivia Lau, "Zelig: Everyone's Statistical Software," http://gking.harvard.edu/zelig.

To cite Zelig as a whole, please reference these two sources:

Kosuke Imai, Gary King, and Olivia Lau. 2007. "Zelig: Everyone's Statistical Software," http://GKing.harvard.edu/zelig.

Kosuke Imai, Gary King, and Olivia Lau. 2007. "Toward A Common Framework for Statistical Analysis and Development," http://gking.harvard.edu/files/abs/z-abs.shtml.

#### See also

The network normal regression is part of the netglm package by Skyler J. Cranmer and is built using some of the functionality of the sna package by Carter T. Butts (Butts and Carley 2001). In addition, advanced users may wish to refer to help(netpoisson). Sample data are fictional.

# **Bibliography**

Butts, C. and Carley, K. (2001), "Multivariate Methods for Interstructural Analysis," Tech. rep., CASOS working paper, Carnegie Mellon University.