Simulation of EU-SILC Population Data: Using the R Package simPopulation

Andreas Alfons

Vienna University of Technology

Matthias Templ

Vienna University of Technology, Statistics Austria

Peter Filzmoser

Vienna University of Technology

Abstract

This vignette demonstrates the use of **simPopulation** for simulating population data in an application to the EU-SILC example data from the package. It presents a wrapper function tailored specifically towards EU-SILC data for convenience and ease of use, as well as detailed instructions for performing each of the four involved data generation steps separately. In addition, the generation of diagnostic plots for the simulated population data is illustrated.

Keywords: R, synthetic data, simulation, survey statistics, EU-SILC.

1. Introduction

This package vignette is a companion to Alfons, Kraft, Templ, and Filzmoser (2010) that shows how the proposed framework for the simulation of population data can be applied in R (R Development Core Team 2010) using the package **simPopulation** (Alfons and Kraft 2010). The data simulation framework consists of four steps:

- 1. Setup of the household structure
- 2. Simulation of categorical variables
- 3. Simulation of (semi-)continuous variables
- 4. Splitting (semi-)continuous variables into components

Note that this vignette does not motivate, describe or evaluate the statistical methodology of the framework. Instead it is focused on the R code to generate synthetic population data and produce diagnostic plots. For details on the statistical methodology, the reader is referred to Alfons *et al.* (2010).

The European Union Statistics on Income and Living Conditions (EU-SILC) is panel survey conducted in European countries and serves as data basis for the estimation social inclusion indicators in Europe. EU-SILC data are highly complex and contain detailed information on the income of the sampled individuals and households. More information on EU-SILC can be found in Eurostat (2004).

In Alfons *et al.* (2010), three methods for the simulation of the net income of the individuals in the population are proposed and analyzed:

- MP Multinomial logistic regression models with random draws from the resulting categories. For the categories corresponding to the upper tail, the values are drawn from a (truncated) generalized Pareto distribution, for the other categories from a uniform distribution.
- TR Two-step regression models with trimming and random draws from the residuals.
- **TN** Two-step regression models with trimming and random draws from a normal distribution.

The first two steps of the analysis, namely the simulation of the household structure and additional categorical variables, are performed in exactly the same manner for the three scenarios. While the simulation of the income components is carried out with the same parameter settings, the results of course depend on the simulated net income.

It is important to note that the original Austrian EU-SILC sample provided by Statistics Austria and used in Alfons et al. (2010) is confidential, hence the results presented there cannot be reproduced in this vignette. Nevertheless, the code for such an analysis is presented here using the example data from the package, which has been synthetically generated itself. In fact, this example data set is a sample drawn from one of the populations generated in Alfons et al. (2010). However, the sample weights have been modified such that the size of the resulting populations is about 1% of the real Austrian population in order to keep the computation time low. Table 1 lists the variables of the example data used in the code examples.

With the following commands, the package and the example data are loaded. Furthermore, the numeric value stored in **seed** will be used as seed for the random number generator in the examples to make the results reproducible.

- > library(simPopulation)
- > data(eusilcS)
- > seed <- 1234

The rest of this vignette is organized as follows. Section 2 illustrates the use of a convenient wrapper function for the generation of EU-SILC population data. In Section 3, detailed instructions are given for each step in the data generation process as well as for the generation of diagnostic plots. The final Section 4 concludes.

2. Wrapper function for EU-SILC

A convenient way of generating synthetic EU-SILC population data is provided by the wrapper function simEUSILC(), which performs the four steps of the data simulation procedure at once. For each step, the names of the variables to be simulated can be supplied. However, the default values for the respective arguments are given by the variables names used in Alfons et al. (2010). Since the same names are used in the example data, the complex procedures for the three different methods can be carried out with very simple commands.

Variable	Name	Type	
Region	db040	Categorical 9 levels	
Household size	hsize	Categorical 9 levels	
Age	age	Categorical	
Gender	rb090	Categorical 2 levels	
Economic status	p1030	Categorical 7 levels	
Citizenship	pb220a	Categorical 3 levels	
Personal net income	netIncome	Semi-continuous	
Employee cash or near cash income	py010n	Semi-continuous	
Cash benefits or losses from self-employment	py050n	Semi-continuous	
Unemployment benefits	py090n	Semi-continuous	
Old-age benefits	py100n	Semi-continuous	
Survivor's benefits	py110n	Semi-continuous	
Sickness benefits	py120n	Semi-continuous	
Disability benefits	py130n	Semi-continuous	
Education-related allowances	py140n	Semi-continuous	
Household sample weights	db090	Continuous	
Personal sample weights	rb050	Continuous	

Table 1: Variables of the EU-SILC example data in **simPopulation**.

Note that the default is to use the MP procedure. An upper bound for the net income is supplied using the argument upper, while the argument equidist is set to FALSE so that the breakpoints for the discretization of the net income are given by quantiles with non-equidistant probabilities as described in Alfons et al. (2010). The twostep regression approaches are performed by setting method = "twostep", in which case the logical argument residuals specifies whether variability should be added by random draws from the residuals (TR method, the default) or from a normal distribution (TN method). In both cases, the default trimming parameter alpha = 0.01 is used.

The synthetic populations generated with the wrapper function are not further evaluated here, instead a detailed illustration of each step along with diagnostic plots is provided in the following section.

3. Step by step instructions and diagnostics

As for the wrapper function simEUSILC(), the variable names of the example data set are used as default values for the corresponding arguments of the functions for the different steps of the procedure. Nevertheless, in order to demonstrate how these arguments are used, the names of the involved variables are always supplied in the commands shown in this section.

The first step of the analysis is to set up the basic household structure using the function simStructure(). Note that a variable named "hsize" giving the household sizes is generated automatically in this example, but the name of the corresponding variable in the sample data can also be specified as an argument. Furthermore, the argument additional specifies the variables that define the household structure in addition to the household size (in this case age and gender).

```
> eusilcP <- simStructure(eusilcS, hid = "db030", w = "db090", + strata = "db040", additional = <math>c("age", "rb090"))
```

For the rest of the procedure, combined age categories are used for the individuals in order to reduce the computation time of the statistical models.

```
> breaks <- c(min(eusilcS$age), seq(15, 80, 5), max(eusilcS$age))
> eusilcS$ageCat <- as.character(cut(eusilcS$age, breaks = breaks,
+ include.lowest = TRUE))
> eusilcP$ageCat <- as.character(cut(eusilcP$age, breaks = breaks,
+ include.lowest = TRUE))</pre>
```

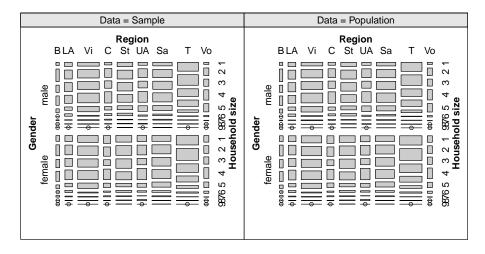
Additional categorical variables are then simulated using the function simCategorical(). The argument basic thereby specifies the already generated variables for the basic household structure (age category, gender and household size), while additional specifies the variables to be simulated in this step (economic status and citizenship).

```
> basic <- c("ageCat", "rb090", "hsize")
> eusilcP <- simCategorical(eusilcS, eusilcP, w = "rb050", strata = "db040",
+ basic = basic, additional = c("pl030", "pb220a"))</pre>
```

Mosaic plots are available as graphical diagnostic tools for checking whether the structures of categorical variables are reflected in the synthetic population. They are implemented in the function spMosaic() based on the package vcd (Meyer, Zeileis, and Hornik 2006, 2010), which contains extensive functionality for customization.

With the following commands, mosaic plots for the variables gender, region and household size are created (see Figure 1, top). The function labeling_border() from package vcd is thereby used to set shorter labels for the different regions and to display more meaningful labels for the variables.

In addition, mosaic plots for the variables gender, economic status and citizenship are produced (see Figure 1, bottom). Also in this case, labeling_border() is used for some fine tuning. In particular, the categories of citizenship are abbreviated and again more meaningful labels for the variables are set.



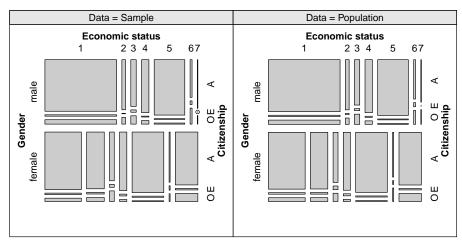


Figure 1: *Top*: Mosaic plots of gender, region and household size. *Bottom*: Mosaic plots of gender, economic status and citizenship.

```
> nam <- c(rb090 = "Gender", pl030 = "Economic status",
+     pb220a = "Citizenship")
> lab <- labeling_border(abbreviate = c(FALSE, FALSE, TRUE),
+     set_varnames = nam)
> spMosaic(c("rb090", "pl030", "pb220a"), "rb050", eusilcS,
+     eusilcP, labeling = lab)
```

Next, the function simContinuous() is used to simulate the net income according to the three proposed methods. The same parameter settings as in Section 2 are thereby used for each of the methods. In any case, the argument basic specifies the predictor variables (age category, gender, household size, economic status and citizenship), while the argument additional specifies the variable to be simulated.

Note that the current state of the random number generator is stored beforehand so that the different methods can all be started with the same seed. Furthermore, the random seed after

each of the methods has finished is stored so that the simulation of the income components can later on continue from there.

Two functions are available as diagnostic tools for (semi-)continuous variables: spCdfplot() for comparing the cumlative distribution functions, and spBwplot() for comparisons with box-and-whisker plots. Both are implemented based on the package lattice (Sarkar 2008, 2010).

The following commands are used to produce the two plots in Figure 2. For better visibility of the differences in the main parts of the cumulative distribution functions, only the parts between 0 and the weighted 99% quantile of the sample are plotted (see Figure 2, left). Furthermore, the box-and-whisker plots by default do not display any points outside the extremes of the whiskers (see Figure 2, right). This is because population data are typically very large, which almost always would result in a large number of observations ouside the whiskers. Also note that a list containing the three populations is supplied as the argument dataP of the plot functions.

One of the main requirements in the simulation of population data is that heterogeneities between subgroups are reflected (see Alfons $et\ al.\ 2010$). Since spCdfplot() and spBwplot() are based on lattice, this can easily be checked by producing conditional plots. With the following commands, the box-and-whisker plots in Figure 3 are produced. The conditioning variables gender ($top\ left$), citizenship ($top\ right$), region ($bottom\ left$) and economic status ($bottom\ right$) are thereby used. For finetuning, the layout of the panels is specified with the layout argument provided by the lattice framework.

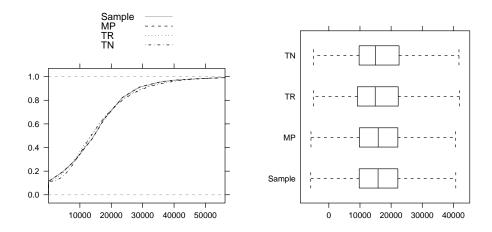


Figure 2: *Left*: Cumulative distribution functions of personal net income. For better visibility, the plot shows only the main parts of the data. *Right*: Box plots of personal net income. Points outside the extremes of the whiskers are not plotted.

```
> spBwplot("netIncome", "rb050", "rb090", dataS = eusilcS,
+ dataP = listP, pch = "|", layout = c(1, 2))
> spBwplot("netIncome", "rb050", "pb220a", dataS = eusilcS,
+ dataP = listP, pch = "|", layout = c(1, 3))
> spBwplot("netIncome", "rb050", "db040", dataS = eusilcS,
+ dataP = listP, pch = "|", layout = c(1, 9))
> spBwplot("netIncome", "rb050", "pl030", dataS = eusilcS,
+ dataP = listP, pch = "|", layout = c(1, 7))
```

The last step of the analysis is to simulate the income components. This is done based on resampling of fractions conditional on net income category and economic status. Therefore, the net income categories need to be constructed first. With the function getBreaks(), default breakpoints based on quantiles are computed. In this example, the argument upper is set to Inf to avoid problems with different maximum values in the three synthetic populations, and the argument equidist is set to FALSE such that non-equidistant probabilities as described in Alfons et al. (2010) are used for the calculation of the quantiles.

```
> breaks <- getBreaks(eusilcS$netIncome, eusilcS$rb050,
+ upper = Inf, equidist = FALSE)
> eusilcS$netIncomeCat <- getCat(eusilcS$netIncome, breaks)
> eusilcMP$netIncomeCat <- getCat(eusilcMP$netIncome, breaks)
> eusilcTR$netIncomeCat <- getCat(eusilcTR$netIncome, breaks)
> eusilcTN$netIncomeCat <- getCat(eusilcTN$netIncome, breaks)</pre>
```

Once the net income categories are constructed, the income components are simulated using the function simComponents(). The arguments total, components and conditional thereby specify the variable to be split, the variables containing the components, and the conditioning variables, respectively. In addition, for each of the three populations the seed of the random number generator is set to the corresponding state after the simulation of the net income.

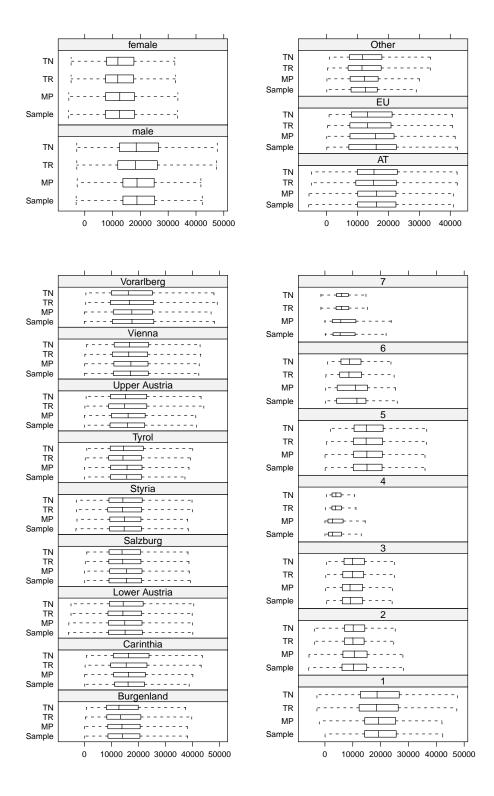


Figure 3: Box plots of personal net income split by gender (top left), citizenship (top right), region (bottom left) and economic status (bottom right). Points outside the extremes of the whiskers are not plotted.

		-10000 0 10000 20000 30000 40000 50000		
	py130n	py140n		
TN	1	py 1 1011		
TR	ı 	HED I		
MP	1	К□>1		
Sample	1	K ED- -1		
	py110n	py120n		
TN	1	¥D- ¬		
TR	1	K⊡I		
MP	1	но		
Sample	1	КШ>- ⊣		
	py090n	py100n		
TN	1	1		
TR	1	1		
MP	11	h		
Sample	1	h 1		
	py010n	py050n		
TN	11	II		
TR	,	+I		
MP	r			
Sample	r			
	-10000 0 10000 20000 30000 40000 50000			

Figure 4: Box plots of the income components. Points outside the extremes of the whiskers are not plotted.

Finally, diagnostic box-and-whisker plots of the income components are produced with the function <code>spBwplot()</code>. Since the box widths correspond to the ratio of non-zero observations to the total number of observed values and most of the components contain large proportions of zeros, a minimum box width is specified using the argument <code>minRatio</code>. Figure 4 contains the resulting plots.

```
> listP <- list(MP = eusilcMP, TR = eusilcTR, TN = eusilcTN)
> spBwplot(components, "rb050", dataS = eusilcS, dataP = listP,
+ pch = "|", minRatio = 0.2, layout = c(2, 4))
```

4. Conclusions

In this vignette, the use of **simPopulation** for simulating population data has been demonstrated in an application to the EU-SILC example data from the package. Both the simulation of synthetic population data and the generation of diagnostic plots have been illustrated in a similar analysis as in Alfons *et al.* (2010).

The code examples show that the functions are easy to use and that the arguments have sensible default values. Nevertheless, the behavior of the functions is highly customizable. In particular the functions for the diagnostic plots benefit from the implementations based on the packages **vcd** and **lattice**.

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Affiliation:

Andreas Alfons Department of Statistics and Probability Theory Vienna University of Technology Wiedner Hauptstraße 7 1040 Vienna, Austria

E-mail: alfons@statistik.tuwien.ac.at

URL: http://www.statistik.tuwien.ac.at/public/alfons/