$$\frac{\partial S(\mathbf{r}, t)}{\partial t} = -\frac{1}{2m} \left[\nabla S(\mathbf{r}, t)\right]^2 - V(\mathbf{r}, t)$$