

$$\frac{\partial A_{\epsilon}^2(\mathbf{r}, t)}{\partial t} + \nabla \cdot (\nabla S_{\epsilon}(\mathbf{r}, t) A_{\epsilon}^2(\mathbf{r}, t)) = 0$$