

$$\frac{\partial S(\mathbf{r}, t)}{\partial t} = -\frac{1}{2m} [\nabla S(\mathbf{r}, t)]^2 - [V(\mathbf{r}, t) + U(\mathbf{r}, t)]$$