$$\frac{\partial S_c(\mathbf{r}, t)}{\partial t} = -\frac{1}{2m} \left[\nabla S_c(\mathbf{r}, t) \right]^2 - V(\mathbf{r}, t)$$