

## EDA and Descriptive Statistics using RStudio

Course Taught at SUAD

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## What we quest to achieve through the sessions

- Data Pre-processing
- Playing around Email dataset
- Exploratory Data Analysis



Data Pre-processing



## **DATA PREPROCESSING**

- 1. Missing value replenishment
- 2. Transformation or normalization
- 3. Random Sampling



Example: Suppose a telecom company wants to analyze the performance of its circles based on the following parameters

- 1. Current Month's Usage
- 2. Last 3 Month's Usage
- 3. Average Recharge
- 4. Projected Growth

The data set is given in next slide. (Missing\_Values\_Telecom Data)



## Example: Circle wise Data

	Current	Last 3			
	Month's	Month's	Average	Projected	
SL No.	Usage	Usage	Recharge	Growth	Circle
1	5.1	3.5	99.4	99.2	Α
2	4.9	3	98.6	99.2	Α
3		3.2		99.2	Α
4	4.6	3.1	98.5	92	Α
5	5		98.4	99.2	Α
6	5.4	3.9	98.3	99.4	Α
7	7	3.2	95.3	98.4.	В
8	6.4	3.2	95.5	98.5	В
9	6.9	3.1	95.1	98.5	В
10		2.3	96	98.3	В
11	6.5	2.8	95.4	98.5	В
12	5.7		95.5	98.3	В
13	6.3	3.3		98.6	В
14	6.7	3.3	94.3	97.5	С
15	6.7	3	94.8	97.3	С
16	6.3	2.5	95	98.9	С
17		3	94.8	98	С
18	6.2	3.4	94.6	97.3	С
19	5.9	3	94.9	98.8	С



## Example: Read data and variables to R

- > mydata = Missing\_Values\_Telecom
- > cmusage = mydata[,2]
- > I3musage = mydata[,3]
- > avrecharge = mydata[,4]



## Option 1: Discard all records with missing values

>newdata = na.omit(mydata)

>write.csv(newdata,"E:/SUAD/newdata.csv")

SL.No.	Current.Month.s.Usage	Last.3.Month.s.Usage	Average.Recharge	Projected.Growth	Circle
1	5.1	3.5	99.4	99.2	Α
2	4.9	3	98.6	99.2	Α
4	4.6	3.1	98.5	92	Α
6	5.4	3.9	98.3	99.4	Α
7	7	3.2	95.3	98.4.	В
8	6.4	3.2	95.5	98.5	В
9	6.9	3.1	95.1	98.5	В
11	6.5	2.8	95.4	98.5	В
14	6.7	3.3	94.3	97.5	С
15	6.7	3	94.8	97.3	С
16	6.3	2.5	95	98.9	С
18	6.2	3.4	94.6	97.3	С
19	5.9	3	94.9	98.8	С



Option 2: Replace the missing values with variable mean, median, etc

Replacing the missing values with mean

Compute the means excluding the missing values

- >cmusage\_mean = mean(cmusage, na.rm = TRUE)
- >l3musage\_mean = mean(l3musage, na.rm = TRUE)
- > avrecharge\_mean = mean(avrecharge, na.rm = TRUE)

Replace the missing values with mean

- > cmusage[is.na(cmusage)]=cmusage\_mean
- > I3musage[is.na(I3musage)]= I3musage\_mean
- >avrecharge[is.na(avrecharge)]=avrecharge\_mean



Option 2: Replace the missing values with variable mean, median, etc Replacing the missing values with mean

Replace the missing values with mean

- > cmusage[is.na(cmusage)]=cmusage\_mean
- > I3musage[is.na(I3musage)]= I3musage\_mean
- >avrecharge[is.na(avrecharge)]=avrecharge\_mean

## Making the new file

- > mynewdata = cbind(cmusage, I3musage, avrecharge, mydata[,5],mydata[,6])
- > write.csv(mynewdata, "E:/SUAD/mynewdata.csv")



Option 2: Replace the missing values with variable mean, median, etc Replacing the missing values with men

SL No	cmusage	l3musage	avrecharge	Proj Growth	Circle
1	5.1	3.5	99.4	11	1
2	4.9	3	98.6	11	1
3	5.975	3.2	96.14117647	11	1
4	4.6	3.1	98.5	1	1
5	5	3.105882353	98.4	11	1
6	5.4	3.9	98.3	12	1
7	7	3.2	95.3	6	2
8	6.4	3.2	95.5	7	2
9	6.9	3.1	95.1	7	2
10	5.975	2.3	96	5	2
11	6.5	2.8	95.4	7	2
12	5.7	3.105882353	95.5	5	2
13	6.3	3.3	96.14117647	8	2
14	6.7	3.3	94.3	3	3
15	6.7	3	94.8	2	3
16	6.3	2.5	95	10	3
17	5.975	3	94.8	4	3
18	6.2	3.4	94.6	2	3
19	5.9	3	94.9	9	3



#### TRANSFORMATION / NORMALIZATION

## z transform:

Transformed data = (Data – Mean) / SD

Exercise: Normalize the variables in the Supply\_Chain.csv?

Read the files
>mydata = Supply\_Chain
> mydata = mydata[,2:7]

Normalize or standardize the variable >mystddata = scale(mydata)



#### RANDOM SAMPLING

Example: Take a sample of size 60 (10%) randomly from the data given in the file bank data.csv and save it as a new csv file?

#### Read the files

```
>mydata = bank data
```

- > mysample = mydata[sample(1:nrow(mydata), 60, replace = FALSE),]
- >write.csv(mysample,"E:/SUAD/mysample.csv")

Example: Split randomly the data given in the file bank data.csv into sets namely training (75%) and test (25%)?

#### Read the files

```
>mydata = bank data
```

>sample = sample(2, nrow(mydata), replace = TRUE, prob = c(0.75, 0.25))

- > sample1 = mydata[sample ==1, ]
- > sample2 = mydata[sample ==2,]



## PLAY WITH YOUR DATA



#### WHAT WE WILL LEARN IN THIS?

- Tools for data exploration and transformation
- Intuitive to write and easy to read
- Super-fast on data frames



#### **INSTALLATION OF PACKAGES**

We will use the 'dplyr' package in R. Since it is a part of 'tidyverse' package installing 'dplyr' separately is not mandatory.

library(tidyverse)

#### LOAD AN EXAMPLE DATASET

suppressMessages(library(dplyr))

install.packages("hflights")

library(hflights)

data(hflights) # hflights is flights departing from two Houston airports in 2011



## head(hflights)

	Year	Month	Dayof	Month Day	/OfWeek	DepTime	ArrTime	Unique	eCarrier	FlightNum	TailNum	ActualEla	apsedTime
5424	2011	1		1	6	1400	1500		AA	428	N576AA		60
5425	2011	1		2	7	1401	1501		AA	428	N557AA		60
5426	2011	1		3	1	1352	1502		AA	428	N541AA		70
5427	2011	1		4	2	1403	1513		AA	428	N403AA		70
5428	2011	1		5	3	1405	1507		AA	428	N492AA		62
5429	2011	1		6	4	1359	1503		AA	428	N262AA		64
	AirTi	ime Ar	rDelay	DepDelay	/ Origin	Dest D	istance	TaxiIn	TaxiOut	Cancelled	Cancella	ationCode	Diverted
5424	AirTi	ime Ar 40	rDelay -10		/ Origin )     IAH		istance 224	TaxiIn 7	TaxiOut 13	Cancelled 0	Cancella	ationCode	Diverted 0
5424 5425	AirTi		-		_	l DFW		TaxiIn 7 6		Cancelled 0 0	Cancella	ationCode	Diverted 0 0
	AirTi	40	-10		) IAH L IAH	I DFW I DFW	224	7		Cancelled 0 0	Cancella	ationCode	Diverted 0 0 0
5425	AirTi	40 45	-10 -9	-{	) IAH L IAH	I DFW I DFW I DFW	224 224	7 6	13 9	Cancelled 0 0 0	Cancella	ationCode	Diverted 0 0 0 0
5425 5426	AirTi	40 45 48	-10 -9	-{ -{	IAH L IAH B IAH	DFW DFW DFW DFW	224 224 224	7 6 5	13 9 17	Cancelled 0 0 0 0 0	Cancella	ationCode	Diverted 0 0 0 0 0 0

as\_tibble creates a "local data frame", which is just a wrapper for a data frame that prints nicely.

# convert to local data frame

flights <- as\_tibble(hflights)</pre>



## flights

```
## A tibble: 227,496 × 21
    Year Month DayofMonth DayOfWeek DepTime ArrTime UniqueCarrier FlightNum TailNum
    <int> <int> <int>
                                                 <int>
                                                              <chr>
                                                                          <int>
                                                                                  <chr>
                                <int>
                                         <int>
## 1 2011
                                 6
                                                                AA
                                                                          428
                                                                                 N576AA
                                         1400
                                                 1500
                                                                                 N557AA
## 2 2011 1
                                                               AA
                                                                          428
                                         1401
                                                 1501
                                                               AA
                                                                                 N541AA
## 3 2011
                                                                          428
                                                 1502
                 3
                                 1
                                         1352
                                                                                 N403AA
                                                                AA
## 4 2011
                                                                          428
                 4
                                 2
                                         1403
                                                 1513
                                                               AA
                                                                                 N492AA
## 5 2011
                                                                          428
                                         1405
                                                 1507
                                 3
                                                               AA
                                                                                 N262AA
## 6 2011
                                                                          428
                                 4
                                         1359
                                                 1503
                                                               AA
                                                                                 N493AA
## 7 2011
                                                                          428
                                                 1509
                                         1359
                                 5
## 8 2011
                                                               AA
                                                                                 N477AA
                                                                          428
                                         1355
                                                 1454
                                                               AA
                                                                                 N476AA
## 9 2011
                                                                          428
                                         1443
                                                 1554
                 9
                                                                AA
                                                                                 N504AA
## 10 2011
                                                                          428
                 10
                                         1443
                                                  1553
## ... with 227,486 more rows, and 12 more variables: ActualElapsedTime <int>,
   AirTime <int>, ArrDelay <int>, DepDelay <int>, Origin <chr>, Dest <chr>,
    Distance <int>, TaxiIn <int>, TaxiOut <int>, Cancelled <int>,
    CancellationCode <chr>, Diverted <int>
```

This prints the data nicely with 10 rows and as many columns that fits the screen.



## # Revert to the original data frame to view all the columns head(data.frame(flights))

	Year	Month	DayofMo	onth Day	OfWeek	DepTim	ne Arr	Time U	niqueCa	arrier Fl	ightNum	TailNum
1	2011	1		1	6	140	00	1500		AA	428	N576AA
2	2011	1		2	7	140	)1	1501		AA	428	N557AA
3	2011	1		3	1	135	2	1502		AA	428	N541AA
4	2011	1		4	2	140	3	1513		AA	428	N403AA
5	2011	1		5	3	140	)5	1507		AA	428	N492AA
6	2011	1		6	4	135	9	1503		AA	428	N262AA
	Actua	alElaps	sedTime	AirTime	ArrDel	ay Dep	Delay	Origi	n Dest	Distance	TaxiIn	TaxiOut
1			60	40	-	10	0	IA	H DFW	224	7	13
2			60	45		-9	1	IA	H DFW	224	6	9
3			70	48		-8	-8	IA	H DFW	224	5	17
4			70	39		3	3	IA	H DFW	224	. 9	22
5			62	44		-3	5	IA	H DFW	224	. 9	9
6			64	45		-7	-1	IA	H DFW	224	6	13
	Cance	elled (	Cancella	ationCod	e Diver	ted						
1		0				0						
2		0				0						
3		0				0						
4		0				0						
5		0				0						
6		0				0						



## Functions in dplyr:

- Pick observations by their values: filter()
- Reorder the rows: arrange().
- Pick variables by their names: select().
- Create new variables with functions of existing variables: mutate()
- Collapse many values down to a single summary: summarise()
- These can all be used in conjunction with *group\_by()* which changes the scope of each function from operating on the entire dataset to operating on it group-by-group.

These six functions provide the verbs for a language of data manipulation.



*filter*: Keep rows matching criteria

- Base R approach to filtering forces you to repeat the data frame's name
- dplyr approach is simpler to write and read
- Command structure (for all dplyr verbs):
  - irst argument is a data frame
  - return value is a data frame
  - nothing is modified in place

**Qn:** Extract details of flights operating on January 01.

```
# base R approach to view all flights on January 1 flights[flights$Month==1 & flights$DayofMonth==1, ]
```

```
# try the filter function of dplyr for the same question
# dplyr approach
# note: you can use comma or ampersand to represent AND condition
filter(flights, Month==1, DayofMonth==1)
```



Qn: Extract details of flights operated by American Airlines or United Airlines.

```
# use pipe for OR condition
filter(flights, UniqueCarrier=="AA" | UniqueCarrier=="UA")
# you can also use %in% operator
filter(flights, UniqueCarrier %in% c("AA", "UA"))
# Check the two answers
```



```
select: Pick columns by name
Qn: Show flight details with Dep/Arr times along with flight numbers only.
# Show flight details with Dep/Arr times alongwith flight numbers only.
# base R approach to select DepTime, ArrTime, and FlightNum columns
flights[, c("DepTime", "ArrTime", "FlightNum")]
# dplyr approach
select(flights, DepTime, ArrTime, FlightNum)
# Check the two answers
# Use colon to select multiple contiguous columns, and use contains to match
columns by name
select(flights, Year:DayofMonth, contains("Taxi"), contains("Delay"))
# starts_with, ends_with, and matches (for regular expressions) can also be used
to match columns by name
select(flights, Year:DayofMonth, starts_with("Taxi"), ends_with("Delay"))
# Check the two answers
```

# 9

#### **EXPLORE THE DATA**

## "Chaining" or "Pipelining"

Usual way to perform multiple operations in one line is by nestingCan write commands in a natural order by using the %>% infix operator (pipes, which can be pronounced as "then")

# Show unique carrier details for flights having departure delays of more than 1 hour. # nesting method

filter(select(flights, UniqueCarrier, DepDelay), DepDelay > 60)

### # chaining method

flights %>% select(UniqueCarrier, DepDelay) %>% filter(DepDelay > 60)

- Chaining increases readability significantly when there are many commands
- Operator is automatically imported from the magrittr package
- Can be used to replace nesting in R commands outside of dplyr

#### # create two vectors and calculate Euclidian distance between them

```
x1 <- 1:5; x2 <- 2:6

sqrt(sum((x1-x2)^2))

# chaining method

(x1-x2)^2 %>% sum() %>% sqrt()

## [1] 2.236068
```



*arrange*: Reorder rows

Qn: Extract flight carrier details and show departure delays only sorted by delay lengths.

```
# base R approach
```

flights[order(flights\$DepDelay), c("UniqueCarrier", "DepDelay")]

## # dplyr approach

flights %>% select(UniqueCarrier, DepDelay) %>% arrange(DepDelay)

# arrange(desc(DepDelay)) for descending order



mutate: Add new variables

Qn. Find mean speed of flights.

### # base R approach

flights\$Speed <- flights\$Distance / flights\$AirTime\*60 flights[, c("Distance", "AirTime", "Speed")]

### # dplyr approach (prints the new variable but does not store it)

flights %>%
select(Distance, AirTime) %>%
mutate(Speed = Distance/AirTime\*60)

## # storing the speed variable

flights <- flights %>% mutate(Speed = Distance/AirTime\*60) flights



**summarise**: Reduce variables to values

- Primarily useful with data that has been grouped by one or more variables
- group\_by creates the groups that will be operated on
- summarise uses the provided aggregation function to summarise each group

Qn. Find average delay to each destination.

# dplyr approach: create a table grouped by Dest, and then summarise each group by taking the mean of ArrDelay

flights %>% group\_by(Dest) %>% summarise(avg\_delay = mean(ArrDelay, na.rm=TRUE))



### group\_by function

Qn. For each day of the year, count the total number of flights and sort in descending order.

flights %>% group\_by(Month, DayofMonth) %>% summarise(flight\_count = n()) %>% arrange(desc(flight\_count))

## `summarise()` has grouped output by 'Month'. You can override using the ## `.groups` argument.

*n\_distinct* (vector): counts the number of unique items in the vector

Qn. For each destination, count the total number of flights and the number of distinct planes that flew there.

flights %>% group\_by(Dest) %>% summarise(flight\_count = n(), plane\_count = n\_distinct(TailNum))



#### Window Functions

- Aggregation function (like mean ) takes \$n\$ inputs and returns 1 value
- Window function takes n inputs and returns n values
- Includes ranking and ordering functions (like min\_rank), offset functions (lead and lag), and cumulative aggregates (like cummean).

Qn. For each carrier, calculate which two days of the year they had their longest departure delays.

## # Note: smallest (not largest) value is ranked as 1, so you have to use `desc` to rank by largest value

flights %>% group\_by(UniqueCarrier) %>% select(Month, DayofMonth, DepDelay) %>% filter(min\_rank(desc(DepDelay)) <= 2) %>% arrange(UniqueCarrier, desc(DepDelay))

## # rewrite more simply with the `top\_n` function

flights %>% group\_by(UniqueCarrier) %>% select(Month, DayofMonth, DepDelay) %>% top\_n(2) %>% arrange(UniqueCarrier, desc(DepDelay))



#### **Useful Convenience Functions**

# randomly sample a fixed number of rows, without replacement flights %>% sample\_n(5)

# randomly sample a fraction of rows, with replacement flights %>% sample\_frac(0.25, replace=TRUE)

# base R approach to view the structure of an object str(flights)

# dplyr approach: better formatting, and adapts to your screen width glimpse(flights)

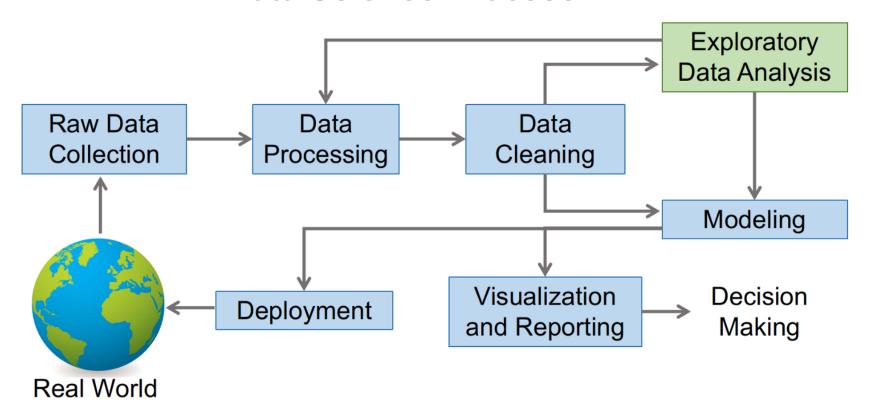


# EXPLORATORY DATA ANALYSIS (EDA)



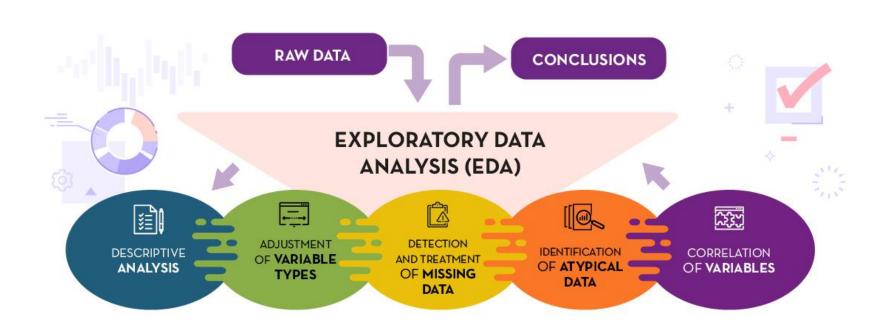
## WHAT IS EDA IN DATA SCIENCE?

## **Data Science Process**





## WHAT IS EDA?





#### WHAT IS EDA?

- Exploratory Data Analysis, or EDA in short, use visualization and transformation to explore data in a systematic way. It is an iterative cycle where one
  - Generates questions about the data.
  - Search for answers by visualizing, transforming, and modelling the data.
  - Use what we learn to refine our questions and/or generate new questions.
- EDA is not a formal process with a strict set of rules. During the initial phases of EDA one should feel free to investigate every idea that occurs.
- Some of these ideas will pan out, and some will be dead ends. As our exploration continues, we will home in on a few particularly productive areas that you'll eventually write up and communicate to others.
- EDA is an important part of any data analysis, even if the questions are handed to you on a platter, because you always need to investigate the quality of your data.
- Data cleaning is just one application of EDA: we ask questions about whether our data meets our expectations or not.
- To do data cleaning, we'll need to deploy all the tools of EDA: visualisation, transformation, and modelling.



## **EDA Case Study**

## Let's begin with the *email* dataset



- These data represent incoming emails for the first three months of 2012 for an email account.
- The data frame has 3921 observations on 21 variables.
- Some of the variables are:
  - **spam**: Indicator for whether the email was spam.
  - to multiple: Indicator for whether the email was addressed to more than one recipient.
  - *from*: Whether the message was listed as from anyone (this is usually set by default for regular outgoing email).
  - **dollar**: The number of times a dollar sign or the word "dollar" appeared in the email.
  - winner: Indicates whether "winner" appeared in the email.
  - *inherit*: The number of times "inherit" (or an extension, such as "inheritance") appeared in the email.
  - num\_char: The number of characters in the email, in thousands.
  - urgent\_subj : Whether the word "urgent" was in the email subject.



## **EDA Case Study**

## Loading the dataset

library(tidyverse)
library(openintro) #for loading our case study dataset
data(email)
email

Can you tell the format of the dataset?



## **EDA Case Study**

#### **Possible Questions for EDA:**

- How is the length of an email related to an email being a spam one?
- Experience tells us that presence of excessive exclamation marks in an email makes it more likely to be a spam. Explore that relationship for this dataset.
- How is the number of images attached with the email relate to spam emails?
- Returning to the length of an email, how do non-spam emails characterize wrt the number of recipients?

#### **EDA**

- Data Analysis is not always about providing answers to the specific questions asked.
- More than often, asking the right questions are more than important.
- Many industries/institutions generate huge volume of data, but have no clue what to do with them.



#### **Measuring variability**

- Variation is the tendency of the values of a variable to change from measurement to measurement.
- You can see variation easily in real life; if you measure any continuous variable twice, you will get two different results. This is true even if you measure quantities that are constant, like the speed of light.
- Each of your measurements will include a small amount of error that varies from measurement to measurement.
- Categorical variables can also vary if you measure across different subjects (e.g. the eye colors of different people), or different times (e.g. fluctuation [up/down] of a stock over different time periods).
- Every variable has its own pattern of variation, which can reveal interesting information.
- The best way to understand that pattern is to visualize the distribution of the variable's values.



#### Exploring number of characters in spam vs non-spam emails

- Let us first explore how the number of characters vary from spam to non-spam emails.
- In this quest, we can first look into summaries of central tendencies and variability for the *num\_char* variable grouped by the *spam* status.
- A good way to visualize and compare the location and spread is to create side-byside boxplots.
- Note that spam is of numeric type. We have to change it to factor type.
- We also rename os as "Not\_spam" and 1s as "Spam".

```
# Exploring number of characters in spam vs non-spam emails
email <- email %>%
  mutate(spam = as.factor(spam)) %>%
  mutate(spam = recode(spam, "o" = "Not_spam", "ı" = "Spam"))
email
```

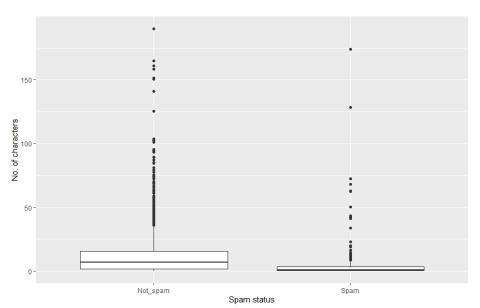
What change do you notice?



```
# Visualize
```

```
email %>%
  ggplot(aes(x = spam, y = num_char)) +
  geom_boxplot() +
  labs(x = "Spam status",
      y = "No. of characters")
```

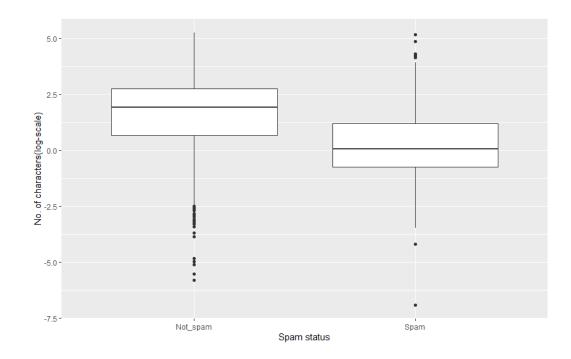
What can you infer from the plot? Any suggestions on how to improve the plot?





# It might be a good idea to change the scale of the y-axis.

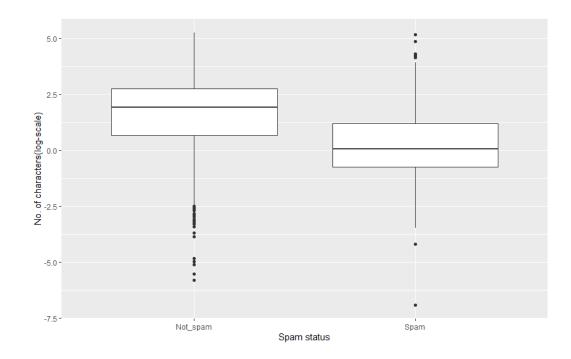
```
email %>%
  mutate(log_num_char = log(num_char)) %>%
  ggplot(aes(x = spam, y = log_num_char)) +
  geom_boxplot()+
  labs(x = "Spam status", y = "No. of characters(log-scale)")
```





# It might be a good idea to change the scale of the y-axis.

```
email %>%
  mutate(log_num_char = log(num_char)) %>%
  ggplot(aes(x = spam, y = log_num_char)) +
  geom_boxplot()+
  labs(x = "Spam status", y = "No. of characters(log-scale)")
```





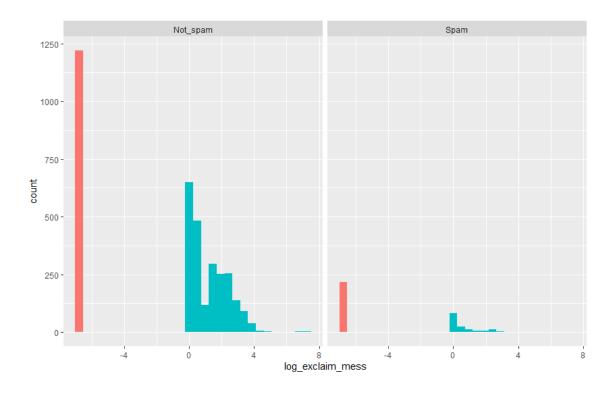
#### exclaim\_mess vs spam

- We now explore another variable exclaim\_mess, the number of exclamation marks in the emails.
- We deploy summary statistics and visualizations to explore the differences.
- Note that many of the emails do not have any exclamation mark, hence log-transformation of the scale will return -Inf, corresponding to log(0).
- A way-around is to add a small quantity, say 0.001 to the values to prevent returning  $-Inf(-\infty)$ .



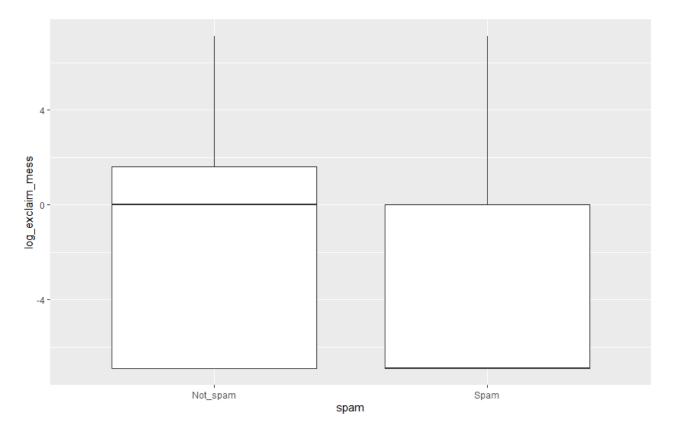
#### # Visualize

```
email %>%
  mutate(log_exclaim_mess = log(exclaim_mess + o.oo1)) %>%
  mutate(custom_fill = as.factor(exclaim_mess > o)) %>%
  ggplot(aes(x = log_exclaim_mess, fill = custom_fill)) +
  geom_histogram() + theme(legend.position = "none") + facet_wrap(~ spam)
```





```
# Visualize: Box-plots
email %>%
  mutate(log_exclaim_mess = log(exclaim_mess + o.oo1)) %>%
  ggplot(aes(x = spam, y = log_exclaim_mess)) +
  geom_boxplot()
```





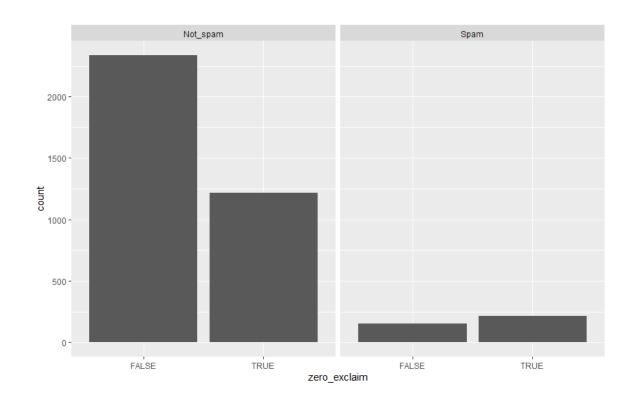
#### **Tackling inflated Zeroes**

- We can see that both the non-spam and spam groups have the maximum counts for zeroes (no exclamation marks). This 'inflation' of zeroes affects the summary of data.
- Zero Inflation is common in many data applications.
- Suppose you are monitoring the sales of a new chocolate recently launched in the market.
- Data is collected from every customer entering a store, and number of the new chocolate bought by that customer is stored in a variable.
- A zero might not mean that a customer is choosing an alternate product; it may also mean that the customer is not interested in buying chocolates.
- One strategy is to categorize the variable into levels; for example, we can have two groups, one with zero exclamation marks, and the other with positive number of exclamation marks.
- Next, we can summarize and visualize the data for the two groups separately.



### **# Tackling inflated Zeroes**

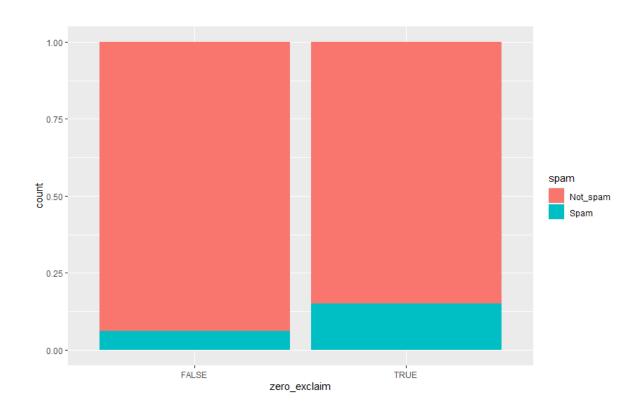
```
email %>%
mutate(zero_exclaim = (exclaim_mess == 0)) %>%
ggplot(aes(x = zero_exclaim)) +
geom_bar() +
facet_wrap(~spam)
```





### **# Tackling inflated Zeroes**

```
email %>%
mutate(zero_exclaim = (exclaim_mess == 0)) %>%
ggplot(aes(x = zero_exclaim, fill = spam)) +
geom_bar(position = "fill")
```



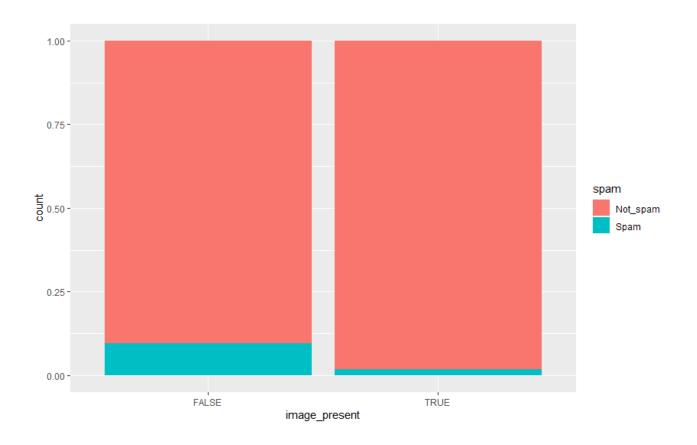


```
# Tackling inflated zeroes: example with the image variable
email %>%
count(image)
## A tibble: 8 \times 2
## image n
## <dbl> <int>
## 1 0 3811
## 2 1 76
## 3 2 17
## 4 3 11
## 5 4 2
## 6 5 2
## 7 9 1
## 8 20 1
```

- There are 3811 images with no images attached.
- This poses a zero inflation problem.

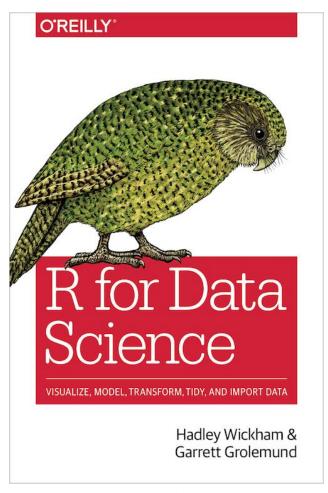


```
email %>%
  mutate(image_present = (image > o)) %>%
  ggplot(aes(x = image_present, fill = spam)) +
  geom_bar(position = "fill")
```





# Reference



https://r4ds.had.co.nz/