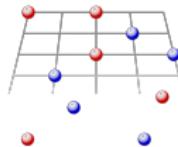


Individual molecule description of kappa-type organic charge transfer salts

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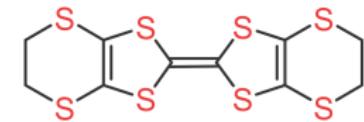
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Outline

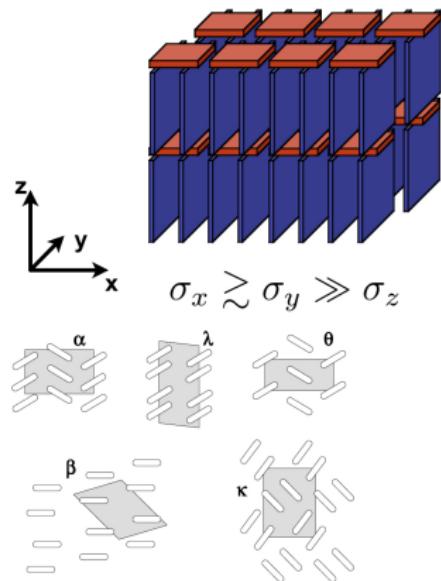
- 1 Crystal structure, Electronic structure, Phase diagram
- 2 Cooling-rate dependent metal-insulator transition
- 3 Superconducting state
- 4 Ab-initio calculations
- 5 Modelling
- 6 Explanation for the cooling-rate dependent MIT
- 7 RPA calculations for the superconducting state
- 8 Conclusion

Crystal structure of organic charge transfer salts

- ET = BEDT-TTF =
bis(ethylene-dithio)-tetrathiafulvalene is the electron donor
- X is the **electron acceptor** [e.g. Cu(NCS)₂]
- ET molecules can be packed in different patterns
- **κ -phase often superconducting**
- features (ET)₂ dimers that donate one electron to acceptor layer
- here we concentrate on κ -(ET)₂X

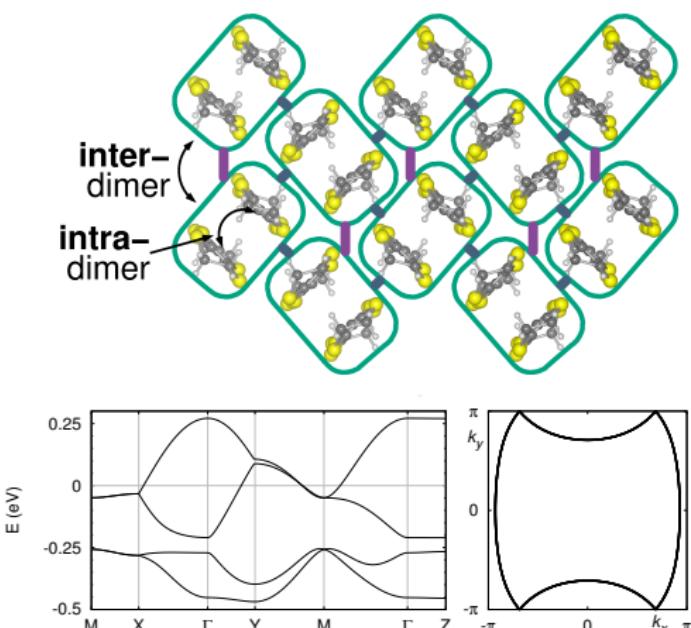


ET (BEDT-TTF)



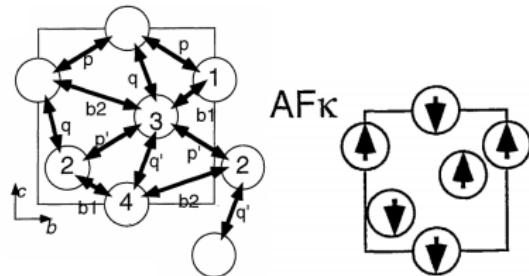
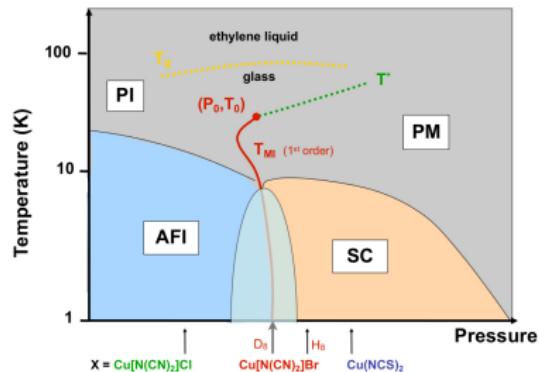
Electronic structure of κ -(ET)₂X

- two-dimensional electronic structure in the ET-plane
- anion layer has filled shells (e.g. Cu d¹⁰)
- bands at Fermi level only from organic molecules
- often modelled by 1/2-filled anisotropic triangular lattice of dimers
- alternative is 3/4-filled individual molecule model on complicated lattice
- Fermi surface is an ellipse larger than the first BZ



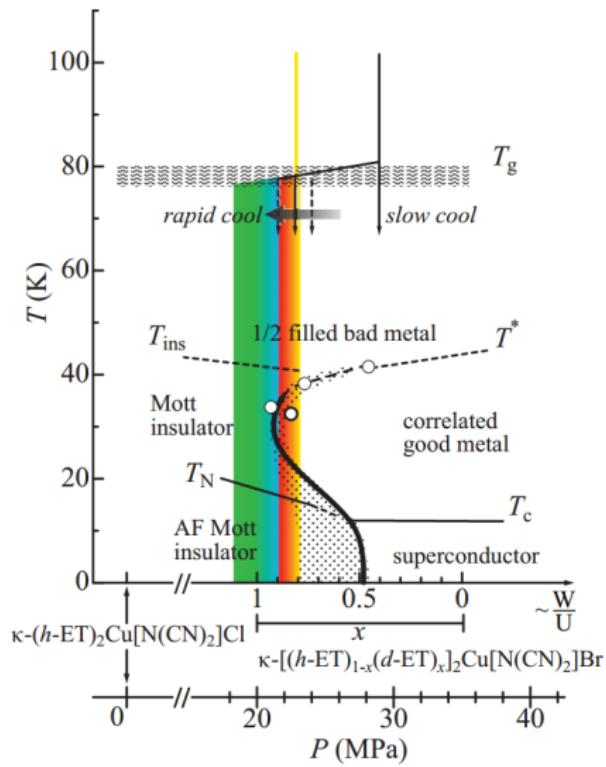
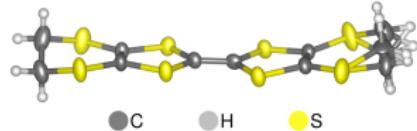
Properties of κ -(ET)₂X

- AFI to SC transition with pressure or variation of X ('chemical pressure')
- spin-1/2 smeared out over (ET)₂ dimer in AFI state
- almost perfect triangular lattice in κ -(ET)₂Cu₂(CN)₃, quantum spin-liquid
- nature of the superconducting state?
- no phase sensitive probes as in cuprates, problems with sample preparation
- critical endpoint of the MIT line
- freezing of intramolecular degrees of freedom around ~ 100 K



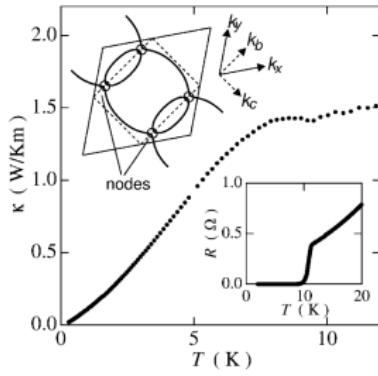
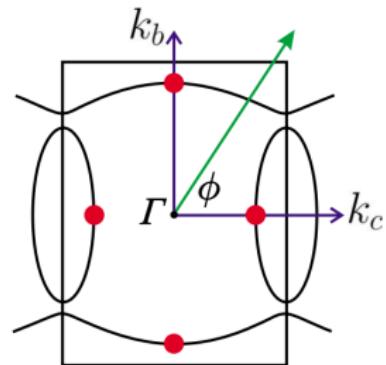
Cooling-rate dependent Metal-Insulator transition

- ground state can be tuned by deuteration
- ethylene end group orientations metastable: **parallel (eclipsed)** and **canted (staggered)**
- glass transition for ethylene endgroups
- metal-insulator transition can be studied in one sample without application of pressure



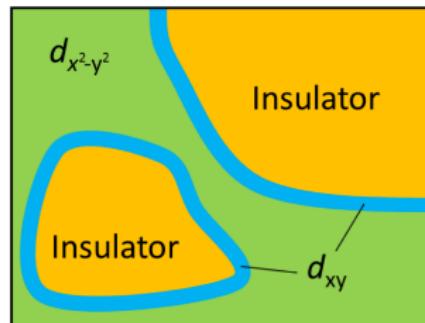
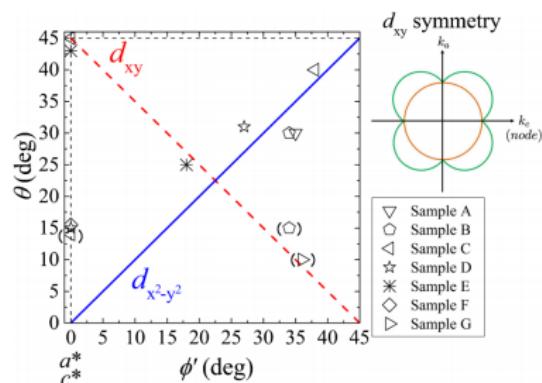
Experimental results for the SC order parameter

- experimentalists assume fourfold rotationally invariant order parameter
- all experiments subtract twofold rotationally invariant 'background'
- almost all experiments agree on presence of nodes, try to determine locations
- both d_{xy} and $d_{x^2-y^2}$ have been concluded to exist in experiment
- multitude of disagreeing experiments
- top panel result from magnetocalorimetry, bottom panel results from thermal conductivity



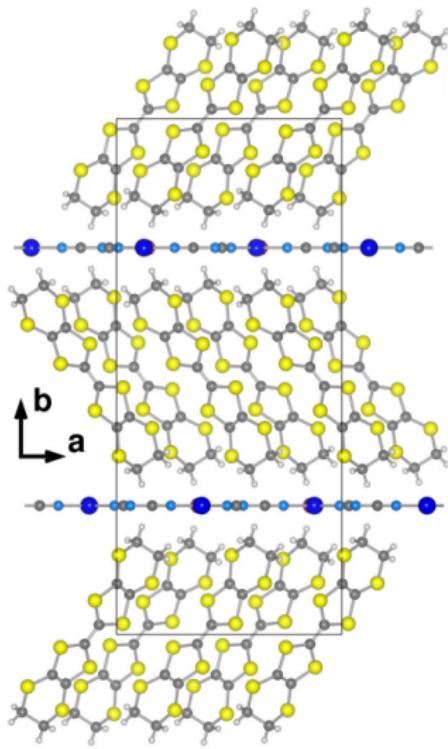
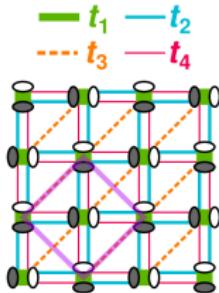
New results from scanning tunneling spectroscopy

- first time that clean surface was used
- more than one set of nodes in one sample
- consistent with both d_{xy} and $d_{x^2-y^2}$
- phase separation?
- insulating patches in SC matrix known for κ -(ET)₂X
- proximity of d_{xy} to AFI makes sense, square lattice physics
- how to explain $d_{x^2-y^2}$ phase?



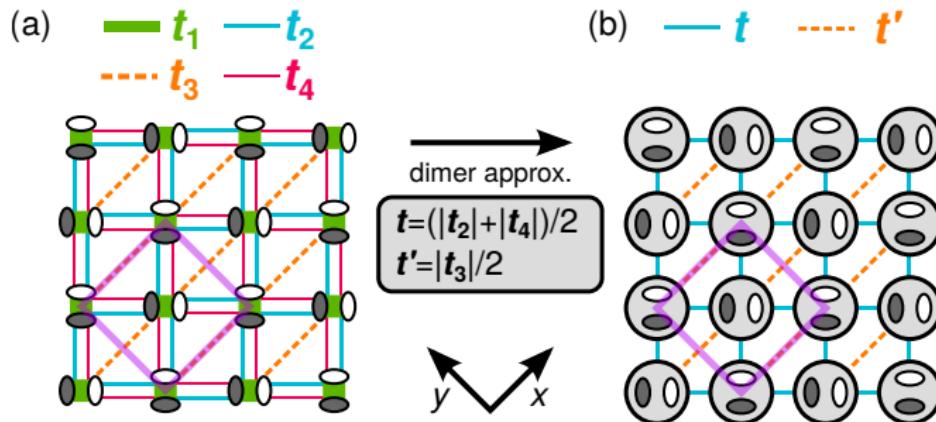
Ab-initio calculations for organic charge transfer salts

- all-electron full-potential DFT calculations (FPLO)
- more than 100 atoms per unit cell
- molecular orbital TB Hamiltonians from projective Wannier functions
- **four hopping parameters sufficient**
- $t_2/t_1 \in [0.538, 0.661]$, $t_3/t_1 \in [0.289, 0.404]$,
 $t_4/t_1 \in [0.099, 0.220]$



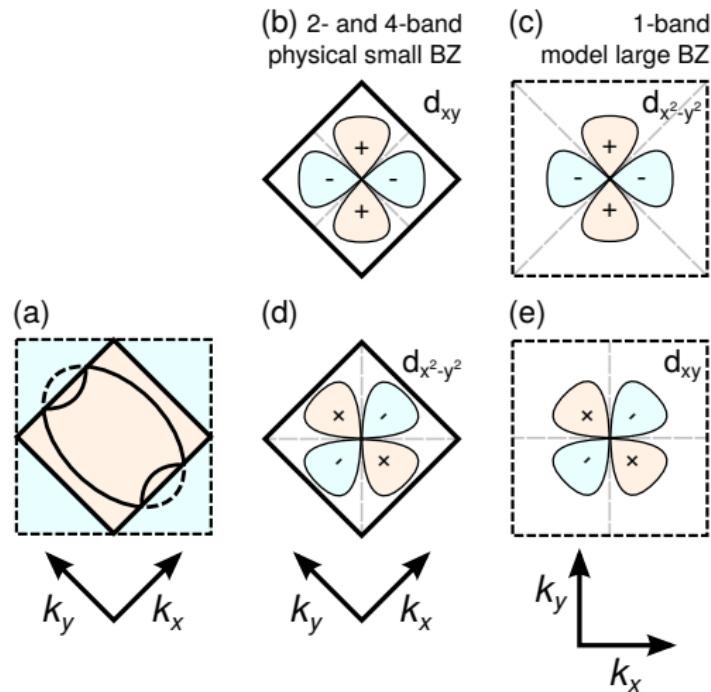
Relation between Dimer and Molecule model

- original lattice structure encoded in molecule model
- traditionally dimer-approximated **anisotropic triangular lattice** is used
- one-band instead of four-band model
- averaging of t_2 and t_4 introduces C_4 -symmetric hopping
- BZ can be unfolded from two- to one-band model



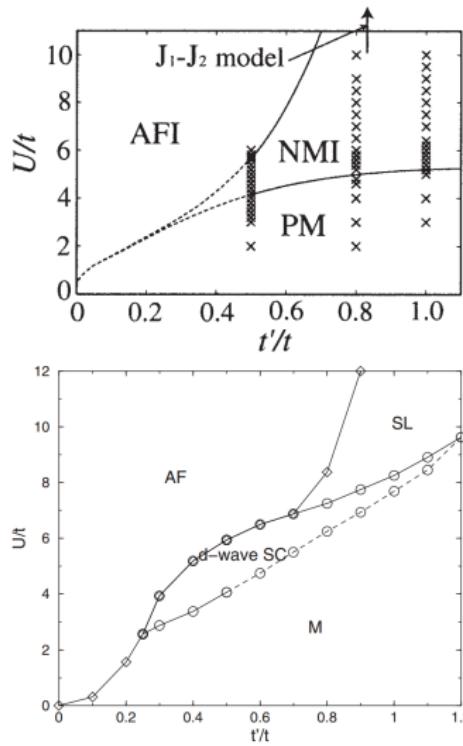
Brillouin zones and superconducting order parameters

- physical BZ is that of four- or two-band model
- larger unfolded BZ and 45 deg. rotation in one-band model
- natural SC order parameter of square lattice is $d_{x^2-y^2}$
- becomes d_{xy} in physical BZ
- we label SC states in physical BZ



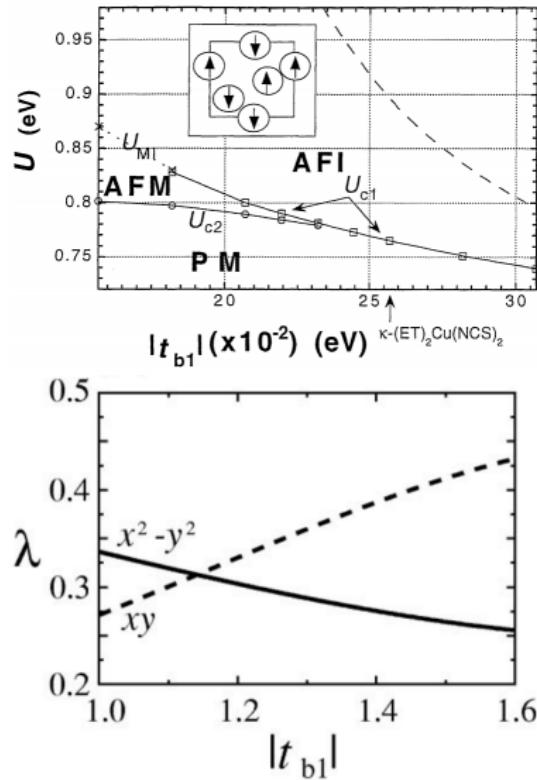
Phase diagram of the anisotropic triangular lattice model

- t'/t controls frustration
- on-site interaction term $H_{\text{int}} = U \sum_i n_{i\uparrow} n_{i\downarrow}$
- AFI, M, QSL and SC phases reproduced
- not all methods agree on phase boundaries and existence of SC
- top plot is PIRG, bottom plot is CDMFT (most extreme examples for disagreement)
- many studies find same SC order parameter as in cuprates (d_{xy})
- are $d_{x^2-y^2}$ experiments wrong?
- side note: intra-dimer charge ordering observed



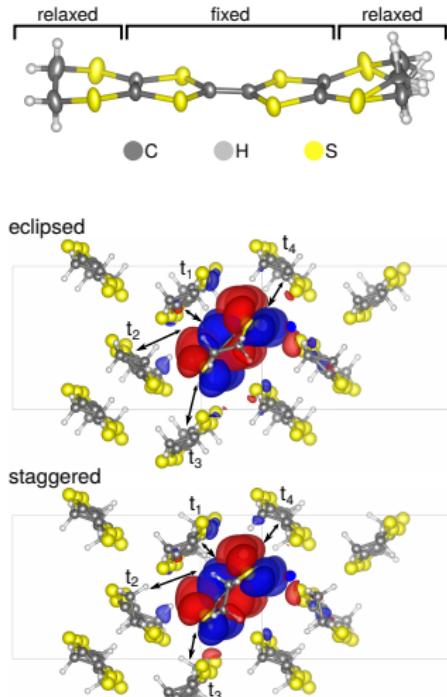
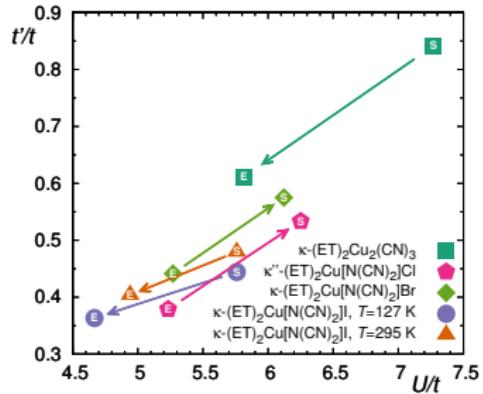
Phase diagram of the molecule model

- top panel HF, bottom panel FLEX
- HF reproduces important phases
- antiferromagnetic metal disappears for large dimerization
- SC order parameter changes as function of dimerization strength
- very few studies, no complete phase diagram
- influence of parameters aside from dimerization not studied



Influence of molecular conformations on the electronic structure

- relax ethylene endgroups and adjacent sulfur atoms in DFT
- endgroups influence hopping amplitudes and Hubbard repulsion
- analyze within dimer model
- staggered endgroups have larger t'/t , U/t



Tight binding+RPA formalism in a nutshell

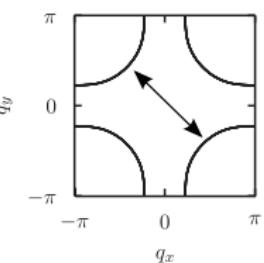
$$H = H_0 + H_{\text{int}} = \sum_{ij\sigma} t_{ij} (c_{i\sigma}^\dagger c_{j\sigma} + h.c.) + \frac{U}{2} \sum_{i\sigma} n_{i\sigma} n_{i\bar{\sigma}}$$

$$\chi_{st}^{pq}(\vec{q}) = -\frac{1}{N} \sum_{\vec{k}, \mu, \nu} a_\mu^s(\vec{k}) a_\mu^{p*}(\vec{k}) a_\nu^q(\vec{k} + \vec{q}) a_\nu^{t*}(\vec{k} + \vec{q}) \frac{f(E_\nu(\vec{k} + \vec{q})) - f(E_\mu(\vec{k}))}{E_\nu(\vec{k} + \vec{q}) - E_\mu(\vec{k})}$$

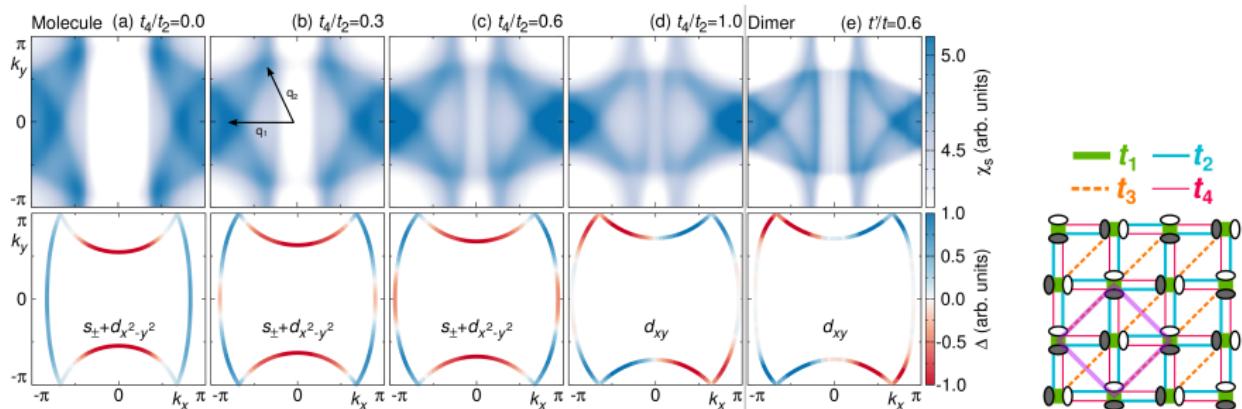
$$[(\chi_{\text{spin}}^{\text{RPA}})_{st}^{pq}]^{-1} = [\chi_{st}^{pq}]^{-1} - (U_{\text{spin}})_{st}^{pq}$$

$$\Gamma_{st}^{pq}(\vec{k}, \vec{k}') = \left[\frac{3}{2} U_s \chi_s^{\text{RPA}}(\vec{k} - \vec{k}') U_s + \frac{1}{2} U_s - \frac{1}{2} U_c \chi_c^{\text{RPA}}(\vec{k} - \vec{k}') U_c + \frac{1}{2} U_c \right]_{ps}^{tq}$$

$$\begin{aligned} \Gamma_{ij}(\vec{k}, \vec{k}') &= \sum_{stpq} a_i^{t*}(-\vec{k}) a_i^{s*}(\vec{k}) \text{Re} \left[\Gamma_{st}^{pq}(\vec{k}, \vec{k}') \right] a_j^p(\vec{k}') a_j^q(-\vec{k}') \\ &- \sum_j \oint_{C_j} \frac{dk'_\parallel}{2\pi} \frac{1}{4\pi v_F(\vec{k}')} \left[\Gamma_{ij}(\vec{k}, \vec{k}') + \Gamma_{ij}(\vec{k}, -\vec{k}') \right] g_j(\vec{k}') = \lambda_i g_i(\vec{k}) \end{aligned}$$



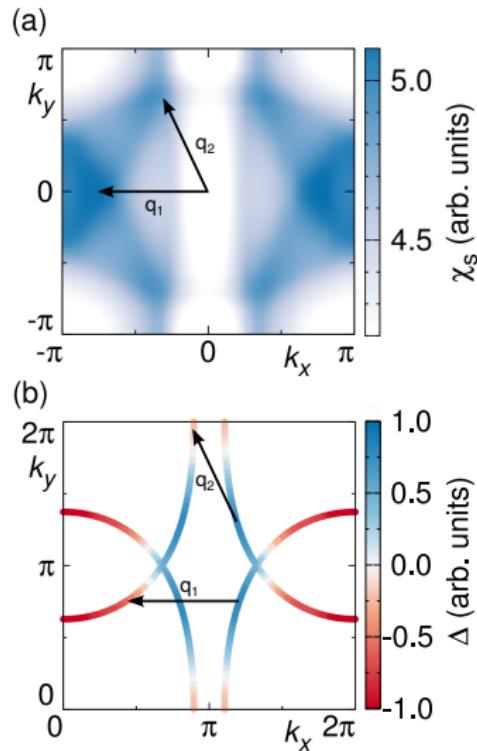
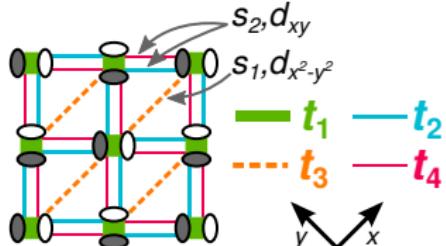
Susceptibility and order parameter: connecting the molecule and dimer models at finite dimerization



- dimer model physics is reproduced in molecule model for $t_4/t_2 \rightarrow 1$
- averaging of transfer integrals is crucial, not only dimerization strength
- additional set of nodes close to $k_y = 0$
- solution identified as $s_{\pm} + d_{x^2-y^2}$
- main features are q_1 and q_2

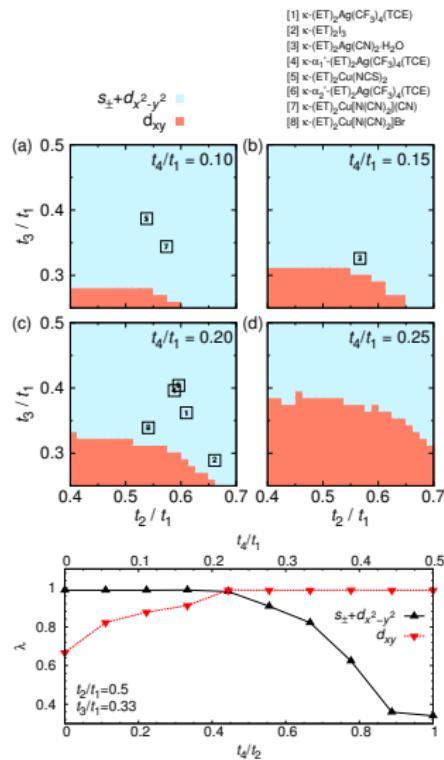
Connection between susceptibility features and hopping parameters

- $s_1: \cos k_x + \cos k_y$
- $s_2: \cos k_x \cdot \cos k_y$
- $d_{x^2-y^2}: \cos k_x - \cos k_y$
- $d_{xy}: \sin k_x \cdot \sin k_y$
- feature q_1 controlled by t_3
- feature q_2 controlled by t_2 and t_4
- increase of t_4/t_2 makes q_2 more square-like, drives d_{xy}



Pairing phase diagram of κ -(ET)₂X

- phase transition from d_{xy} to $s_{\pm} + d_{x^2-y^2}$
- dimerization plays only minor role
- competition between t_2 , t_4 and t_3 controls phases
- many materials close to phase transition
- additional set of nodes appears there
- some experimental reports of d_{xy} might have picked up those
- near-degeneracy of d_{xy} and $s_{\pm} + d_{x^2-y^2}$ in most materials



Connection to experiment: scanning tunneling spectroscopy

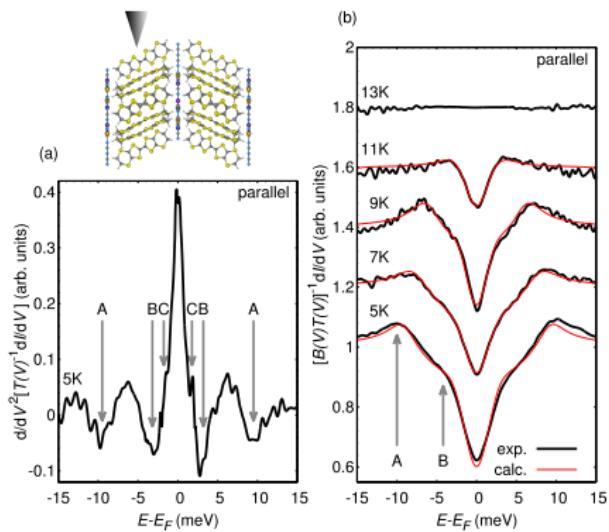
$$\Delta(\vec{k}) = \Delta_0 [c_{s_1}(\cos k_x + \cos k_y) + c_{d_1}(\cos k_x - \cos k_y) + c_{s_2}(\cos k_x \cdot \cos k_y)]$$

$$\rho_{qp}(E, \Gamma) \propto \sum_{\vec{k}} \text{Re} \frac{|E + i\Gamma|}{\sqrt{(E + i\Gamma)^2 - \Delta(\vec{k})^2}}$$

$$S(V) = \frac{1}{B(V)T(V)} \frac{dI(V)}{dV}$$

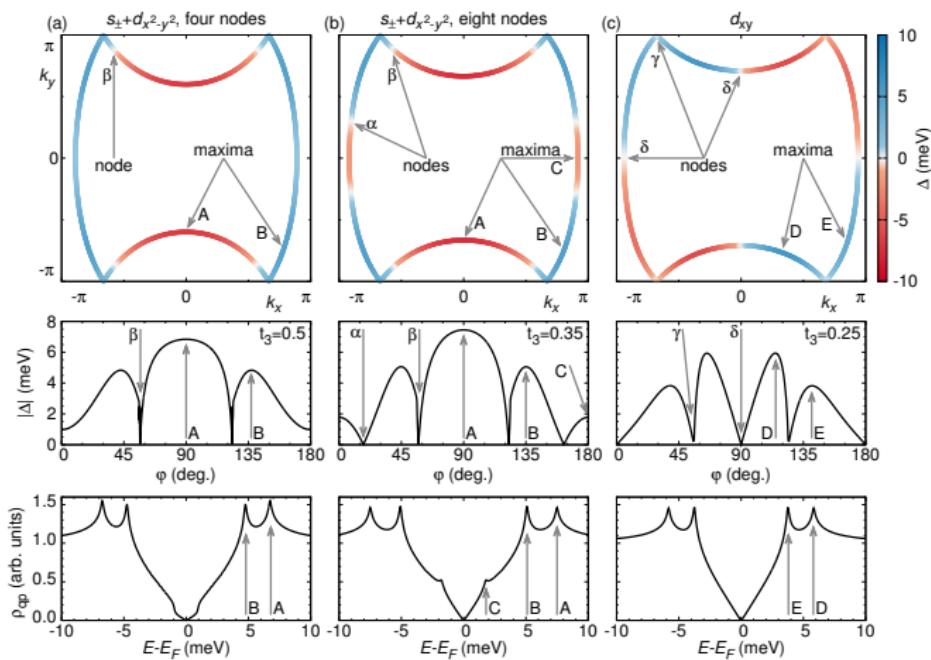
$$\propto \int_{-\infty}^{\infty} dE [\rho_{qp}(E)(1-x) + x] \frac{-df(E+eV)}{dV}$$

- simulate tunneling conductivity from quasiparticle DOS
- calculate QP DOS from Fermi surface approximation, FS not concentric circle
- introduce small broadening
- discriminates $d_{x^2-y^2}$ and d_{xy}



Simulation of STS for the different SC states

- three different nodal states
- $s_{\pm} + d_{x^2-y^2}$ with four nodes
- $s_{\pm} + d_{x^2-y^2}$ with eight nodes close to phase transition
- d_{xy} state in square-like regime
- QP DOS somewhat similar, but different slopes



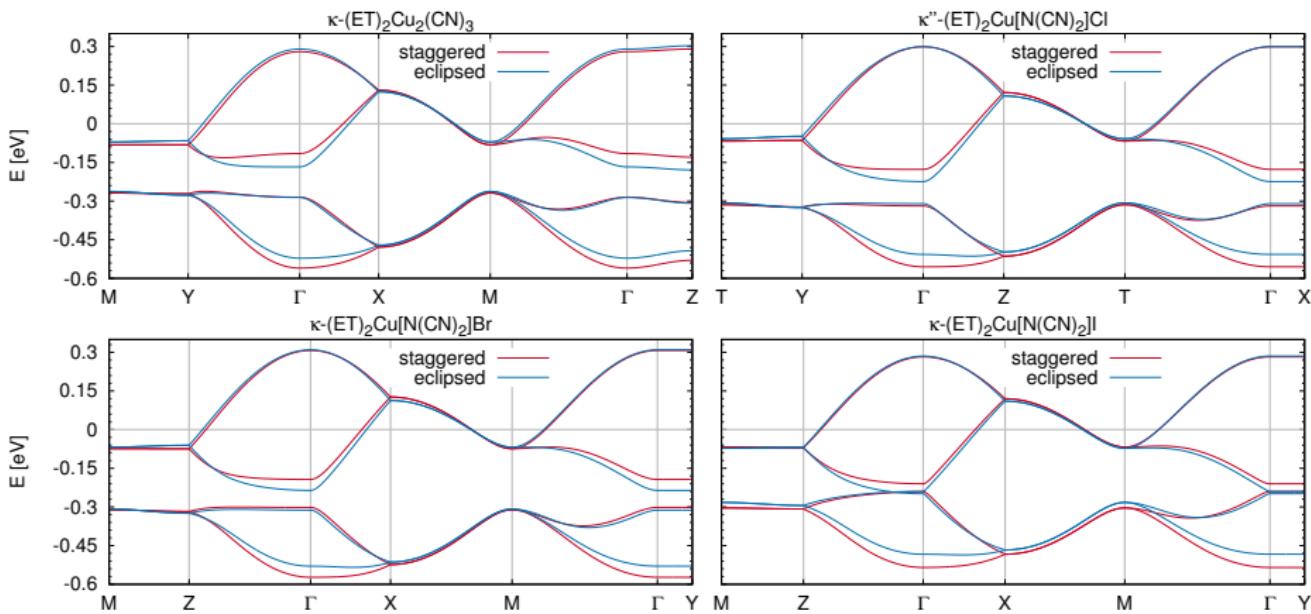
Summary

- κ -(ET)₂X materials offer extraordinary tunability
- we calculated kinetic part of models for many κ -type materials
- dimer model describes phase diagram to first approximation
- blocked further progress regarding SC state
- molecule model mostly unexplored
(spin-liquid, influence of V on phase boundaries)

References

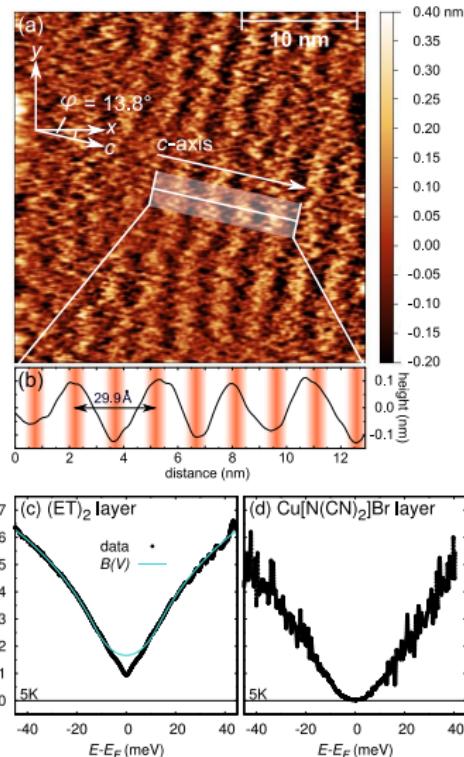
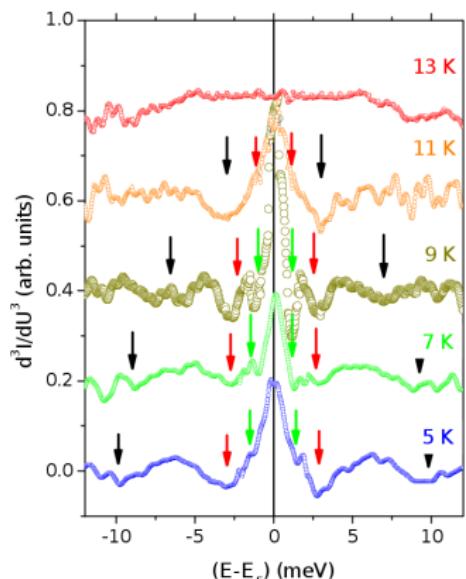
- Guterding, Valentí, Jeschke, PRB **92**, 081109(R) (2015)
- Guterding et al., PRL **116**, 237001 (2016)
- Guterding, Altmeyer, Jeschke, Valentí, arXiv:1605.07017

Electronic bandstructure for different ethylene endgroup configurations



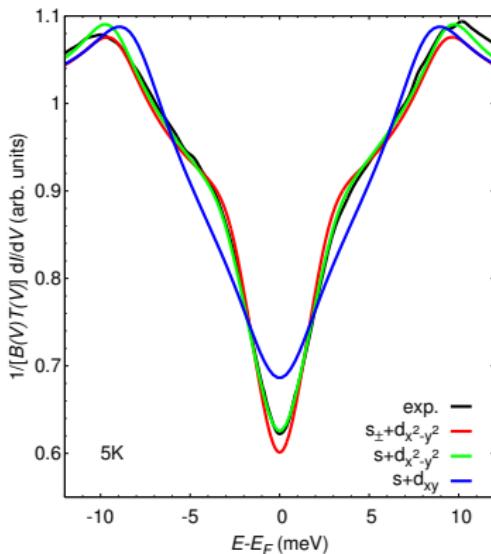
STS data for κ -(ET)₂[N(CN)₂]Br

- tunneling parallel to conducting layers
- background DOS is modelled by Anderson-Hubbard model



Alternative fits for STS data

- $s + d_{x^2-y^2}$ and $s_{\pm} + d_{x^2-y^2}$ equally good
- meaning of plain s-wave component?



Calculating the quasiparticle DOS

- use gap calculated from RPA and TB bands or Fermi surface
- full calculation uses bandstructure and tetrahedron method
- quasiparticle calculation uses Fermi surface only
- excellent agreement in relevant energy window

