

Claim: For a wave heading towards a boundary between two media at an oblique angle, $\omega_I = \omega_R = \omega_T$.

A. True

B. False

ANNOUNCEMENTS

- Quiz 5 (this Friday)
 - Construct the expression for plane wave given a description
 - Both complex and real expressions
 - Combine two plane waves and describe the resulting superposed wave

Claim: For a wave heading towards a boundary between two media at an oblique angle, at the boundary,

$$\mathbf{k}_I \cdot \mathbf{r} = \mathbf{k}_R \cdot \mathbf{r} \neq \mathbf{k}_T \cdot \mathbf{r}.$$

A. True

B. False

An EM wave passes from air to metal, what does **your intuition** say happens to the wave in the metal?

- A. It will be amplified because of free electrons
- B. It will die out over some distance
- C. It will be blocked right at the interface because there's no E field in a metal
- D. Not sure

An EM wave passes from air to metal, which do you think is **most likely** the physics will give us?

- A. It will be amplified because of free electrons
- B. It will die out over some distance
- C. It will be blocked right at the interface because there's no E field in a metal
- D. Not sure

Suppose I stick some charge ρ_f down somewhere in a metal (with conductivity σ). What does $\rho(t)$ look like if we can invoke Ohm's law ($\mathbf{J} = \sigma \mathbf{E}$)? *Hint: Think about charge conservation.*

A. $\rho(t) = \rho_f \sin(\sigma t / \epsilon_0)$

B. $\rho(t) = \rho_f \cos(\sigma t / \epsilon_0)$

C. $\rho(t) = \rho_f e^{-\sigma t / \epsilon_0}$

D. $\rho(t) = \rho_f e^{-\epsilon_0 t / \sigma}$

E. Something else

Consider a good conductor ($\sigma \sim 10^8$ S/m), how long roughly does it take for free charge to dissipate ($t \sim \epsilon_0/\sigma$)?

A. 10^{-19} s

B. 10^{-12} s

C. 10^{-8} s

D. 10^{12} s

E. Something else

Given our estimates of collision times (10^{-14} s), for what kinds of light is our analysis not so great for?

- A. X-Rays ($\sim 10^{18}$ Hz)
- B. Visible light ($\sim 10^{15}$ Hz)
- C. IR ($\sim 10^{13}$ Hz)
- D. Radio ($\sim 10^8$ Hz)
- E. More than one of these

What does this ansatz attempt (i.e., using $\sim e^{(kz-i\omega t)}$) remind you for this?

- A. Solving the simple harmonic oscillator
- B. Solving the damped harmonic oscillator
- C. Solving the driven harmonic oscillator
- D. Some other set up

With the proposed solution, $\widetilde{\mathbf{E}} = \widetilde{\mathbf{E}}_0 e^{i(kz - \omega t)}$, what equation does k satisfy?

Think about the wave equation: $\nabla^2 \mathbf{E} = \mu\sigma \frac{\partial \mathbf{E}}{\partial t} + \mu\epsilon \frac{\partial^2 \mathbf{E}}{\partial t^2}$

A. $k^2 = i\omega\mu\sigma + \omega^2\sigma\epsilon$

B. $k^2 = \omega\mu\sigma + i\omega^2\sigma\epsilon$

C. $k = \omega\mu\sigma + i\omega^2\sigma\epsilon$

D. $k = i\omega\mu\sigma + \omega^2\sigma\epsilon$

E. Something else

What is the \sqrt{i} ?

A. $-i$

B. $\frac{1+i}{\sqrt{2}}$

C. -1

D. $e^{i\pi/4}$

E. None or more than one of these

An EM wave passes from air to metal, what happens to the wave in the metal?

- A. It will be amplified because of free electrons
- B. It will die out over some distance
- C. It will be blocked right at the interface because there's no E field in a metal
- D. Not sure

We found a traveling wave solution for the conductor situation,

$$\widetilde{\mathbf{E}}(\mathbf{r}, t) = \widetilde{\mathbf{E}}_0 e^{i(\widetilde{k}z - \omega t)}$$

$$\text{where } \widetilde{k} = \omega^2 \mu \epsilon + i(\omega \mu \sigma)$$

True (A) or False (B): This traveling wave is transverse.

(C) I'm not sure.

The magnetic field amplitude in a metal associated with a linearly polarized electric EM wave is:

$$\widetilde{B}_0 = \left(\frac{k_R + ik_I}{\omega} \right) \widetilde{E}_0$$

True (A) or False (B): The B field is in phase with the E field.

(C) It depends!

The magnetic field amplitude in a highly conductive metal ($\sigma \gg \epsilon\omega$) associated with a linearly polarized electric EM wave is

$$\widetilde{B}_0 = \sqrt{\frac{\mu\sigma}{\omega}} \frac{1+i}{\sqrt{2}} \widetilde{E}_0$$
$$\widetilde{B}_0 = \sqrt{\frac{\sigma}{\epsilon_0\omega}} \frac{1+i}{\sqrt{2}} \frac{\widetilde{E}_0}{c}$$

True (A) or False (B): The B field is in phase with the E field.

(C) It depends!