

Velocity is a defined quantity:

$$\mathbf{u} = \frac{\Delta \mathbf{r}}{\Delta t} = \left\langle \frac{\Delta x}{\Delta t}, \frac{\Delta y}{\Delta t}, \frac{\Delta z}{\Delta t} \right\rangle$$

In another inertial frame, seen to be moving to the right,  
parallel to x, observers see:

$$\mathbf{u}' = \frac{\Delta \mathbf{r}'}{\Delta t'} = \left\langle \frac{\Delta x'}{\Delta t'}, \frac{\Delta y'}{\Delta t'}, \frac{\Delta z'}{\Delta t'} \right\rangle$$

Is velocity a 4-vector?

A. Yes

B. No

Which of the following equations is the correct way to write out the Lorentz scalar product?

A.  $a \cdot b = -a^0 b^0 + a^1 b^1 + a^2 b^2 + a^3 b^3$

B.  $a \cdot b = a_0 b^0 + a_1 b^1 + a_2 b^2 + a_3 b^3$

C.  $a \cdot b = a_\nu b^\nu$

D. None of these

E. All three are correct

Imagine this quantity:

$$u^\mu \equiv \begin{pmatrix} c \\ \frac{\Delta x}{\Delta t} \\ \frac{\Delta y}{\Delta t} \\ \frac{\Delta z}{\Delta t} \end{pmatrix}$$

Is this quantity a 4-vector?

- A. Yes, and I can say why.
- B. No, and I can say why.
- C. None of the above.

Imagine this quantity:

$$\eta^\mu \equiv \frac{1}{\Delta\tau} \begin{pmatrix} ct \\ \Delta x \\ \Delta y \\ \Delta z \end{pmatrix}$$

Is this quantity a 4-vector?

- A. Yes, and I can say why.
- B. No, and I can say why.
- C. None of the above.

In my frame ( $S$ ) I measure two events which occur at the same place, but different times  $t_1$  and  $t_2$  (they are NOT simultaneous)

Might you (in frame  $S'$ ) measure those SAME two events to occur simultaneously in your frame?

- A. Possibly, if he's in the right frame!
- B. Not a chance
- C. Definitely need more info!
- D. ???

Two events have a timelike separation. In a "1+1"-dimensional spacetime (Minkowski) diagram (x horizontal, ct vertical), the magnitude of the slope of a line connecting the two events is

- A. Greater than 1
- B. Equal to 1
- C. Less than 1

Consider the world line of an object drawn on a Minkowski (space-time) diagram. At any point in that space, the slope of that line is:

- A. larger than 1
- B. less than 1
- C. able to take on any value

Points that lie outside the light cone for a given event are:

- A. accessible no matter where they are
- B. accessible for given world lines (trajectories)
- C. always inaccessible



The space time interval is defined by:

$$I \equiv x^2 + c^2 t^2$$

Events with common space time intervals lie on a hyperbole of constant  $I$ .

**True or False:** A Lorentz boost can allow you to shift between different hyperboles.

- A. True
- B. False

Consider the product of the speed of light and the proper time:  $c d\tau$ .

Is this quantity invariant?

A. Yes

B. No

C. I don't know how to tell

Is this "4-velocity" a contravariant 4-vector?

$$\eta^\mu \equiv \frac{dx^\mu}{d\tau}$$

- A. Yes
- B. No
- C. I don't know how to tell

What is  $\frac{dt}{d\tau}$ ?

- A.  $\gamma$
- B.  $1/\gamma$
- C.  $\gamma^2$
- D.  $1/\gamma^2$
- E. Something else

With  $\eta^0 = c\gamma$  and  $\vec{\eta} = \gamma\vec{u}$ , what is the square of  $\eta$ ?

$$\eta^2 \equiv \eta \cdot \eta = \eta_\mu \eta^\mu$$

A.  $c^2$

B.  $u^2$

C.  $-c^2$

D.  $-u^2$

E. Something else

The momentum vector  $\vec{p}$  is given by,

$$\vec{p} = \frac{m\vec{u}}{\sqrt{1 - u^2/c^2}}$$

What is  $|\vec{p}|$  as  $u$  approaches zero?

- A. zero
- B.  $m u$
- C.  $m c$
- D. Something else