```
Order Parameters Calculated Using:
      COPL as found on:
      H.T.Stokes and D.M.Hatch, (2002). ISOTROPY, stokes.byu.edu/isotropy.html.
Sphere Packings:
ZNOXAC01
   Parent: 227 Oh-7, Fd-3m, F4_1/d-32/m, origin choice 2
   Subgroup: 227 Oh-7, Fd-3m, F4_1/d-32/m, origin choice 2
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 1
   origin: 0 0 0
   Irrep Dir Subgroup Size
   GM1+ (a) 227 Fd-3m 1
   GM1+ is the primary OP.
DEQPAQ, et al.
   Parent: 229 Oh-9, Im-3m, I4/m-32/m
   Subgroup: 217 Td-3, I-43m, I-43m
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 1
   origin: 0 0 0
   Irrep Dir Subgroup Size
   GM1+ (a) 229 Im-3m
GM2- (a) 217 I-43m
   GM2- is the primary OP.
FOHCUA, et al.
   Parent: 221 Oh-1, Pm-3m, P4/m-32/m
   Subgroup: 215 Td-1, P-43m, P-43m
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 1
   origin: 0 0 0
   Irrep Dir Subgroup Size
   GM1+ (a) 221 Pm-3m
   GM2- (a) 215 P-43m
   GM2- is the primary OP.
CUCZUV
   Parent: 194 D6h-4, P6_3/mmc, P6_3/m2/c
   Subgroup: 176 C6h-2, P6_3/m, P6_3/m
   Lattice vectors:
   1 -1 0
   1 2 0
   0 0 1
   origin: 0 0 1/2
   Irrep Dir
                Subgroup
                              Size
   GM1+ (a)
                194 P6_3/mmc
   GM2+ (a)
               176 P6_3/m
                                1
         (a,0) 193 P6_3/mcm
   K1
                                3
         (a,0) 176 P6_3/m
                                3
   K4 is the primary OP.
```

```
DILWIE01 & ZEYHIU
   Parent: 194 D6h-4, P6_3/mmc, P6_3/m2/c
   Subgroup: 165 D3d-4, P-3c1, P-32/c1
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 2
   origin: 0 0 0
   Irrep Dir
                Subgroup
                             Size
   GM1+(a)
               194 P6_3/mmc
                               1
   GM3+ (a)
               164 P-3m1
                               1
         (a,a) 165 P-3c1
                               2
   A2
   A2 is the primary OP.
TCYMET
   Parent: 229 Oh-9, Im-3m, I4/m-32/m
   Subgroup: 161 C3v-6, R3c, R3c, hexangonal axes
   Lattice vectors:
   0 1 -1
   -1 0 1
   1 1 1
   origin: 0 0 0
   Irrep Dir
                 Subgroup
                            Size
   GM1+ (a)
                 229 Im-3m
                            1
   GM5+
        (a,a,a) 166 R-3m
                              1
   GM2-
        (a)
                  217 I-43m
                              1
   GM4-
        (a,a,a) 160 R3m
                              1
                  223 Pm-3n
   H2+
         (a)
                              2
         (a,a,a) 167 R-3c
   H4+
                              2
   H1-
         (a)
                  222 Pn-3n
                              2
         (a,a,a) 167 R-3c
   H5-
                              2
   Coupled OP.
ZIZHIZ
   Parent: 194 D6h-4, P6_3/mmc, P6_3/m2/c
   Subgroup: 147 C3i-1, P-3, P-3
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 1
   origin: 0 0 0
   Irrep Dir Subgroup
                           Size
   GM1+
        (a)
             194 P6_3/mmc
                             1
             176 P6_3/m
                             1
   GM2+
        (a)
   GM3+ (a) 164 P-3m1
                             1
   GM4+ (a) 163 P-31c
                             1
   Coupled OP.
MTRETC10
   Parent: 225 Oh-5, Fm-3m, F4/m-32/m
   Subgroup: 152 D3-4, P3_121, P3_121
   Lattice vectors:
   0 - 1/2 - 1/2
   1/2 0 1/2
   -1 -1 1
   origin: -1/6 1/6 -1/2
   Irrep k params Dir
                                                                 Subgroup
                                                                              Size
   GM1+
                                                                 225 Fm-3m
                                                                                1
                     (a)
   GM5 +
                    (a, -a, -a)
                                                                 166 R-3m
                                                                                1
   GM1-
                                                                 209 F432
                                                                                1
                    (a)
   GM5-
                                                                 155 R32
                                                                                1
                    (a,-a,-a)
                                                                                3
   LD3
         2/3
                    (0,0,0,0,0,0,a,0,0,0,0,0,0,-1.732a,0) 152 P3_121
```

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FUZLUH & VAFWAA
```

Parent: 227 Oh-7, Fd-3m, F4\_1/d-32/m, origin choice 2

Subgroup: 141 D4h-19, I4\_1/amd, I4\_1/a2/m2/d, origin choice 2

Lattice vectors: 1/2 -1/2 0

1/2 1/2 0

0 0 1

origin: 1/4 1/4 0

Irrep Dir Subgroup Size GM1+ (a) 227 Fd-3m 1 GM3+ (a,0) 141 I4\_1/amd 1

GM3+ is the primary OP.

## ZZZKNW01

Parent: 225 Oh-5, Fm-3m, F4/m-32/m Subgroup: 121 D2d-11, I-42m, I-42m

Lattice vectors:

-1/2 0 1/2

1/2 0 1/2 0 1 0

origin: 0 0 0

Irrep Dir Subgroup Size
GM1+ (a) 225 Fm-3m 1
GM3+ (a,-1.732a) 139 I4/mmm 1
GM5- (0,0,a) 121 I-42m 1

 ${\tt GM5-}$  is the primary  ${\tt OP.}$ 

#### KUJSIR

Parent: 225 Oh-5, Fm-3m, F4/m-32/m

Subgroup: 142 D4h-20, I4\_1/acd, I4\_1/a2/c2/d, origin choice 2

Lattice vectors:

1 0 0 0 0 -1 0 2 0

origin: 0 1/4 1/4

Irrep Dir Size Subgroup 225 Fm-3m GM1+ (a)1 139 I4/mmm GM3+(a,-1.732a)1 134 P4\_2/nnm 2 X4-(a,0,0) 4 W3 (0,0,a,a,0,0) 142 I4\_1/acd

W3 is the primary OP.

## YEMRIR

Parent: 221 Oh-1, Pm-3m, P4/m-32/m

Subgroup: 120 D2d-10, I-4c2, I-4c2

Lattice vectors:

1 -1 0 1 1 0 0 0 2

origin: -1/2 -1/2 -1/2

Irrep Dir Subgroup Size GM1+ (a)221 Pm-3m GM3+ (a,0)123 P4/mmm 1 GM2- (a) 215 P-43m 1 GM3- (a,0) 111 P-42m 1 R4+ (a,0,0) 140 I4/mcm 2 R5-(a,0,0) 140 I4/mcm

Coupled OP.

```
ADAMAN08 & GERHOA
   Parent: 225 Oh-5, Fm-3m, F4/m-32/m
   Subgroup: 114 D2d-4, P-42_1c, P-42_1c
   Lattice vectors:
   -1/2 0 1/2
   1/2 0 1/2
   0 1 0
   origin: 0 0 0
   Irrep Dir
                      Subgroup
                                    Size
   GM1+ (a)
                      225 Fm-3m
   GM3+
         (a,-1.732a) 139 I4/mmm
                                      1
                  121 1 1
128 P4/mnc
        (0,0,a)
   GM5-
                                      1
   X3+
                                      2
         (a,0,0)
                    137 P4_2/nmc
                                      2
   X2-
         (a,0,0)
   Coupled OP.
KANGUB01
   Parent: 141 D4h-19, I4_1/amd, I4_1/a2/m2/d, origin choice 2
   Subgroup: 88 C4h-6, I4_1/a, I4_1/a, origin choice 2
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 1
   origin: 0 1/2 0
   Irrep Dir Subgroup
                            Size
   GM1+ (a) 141 I4_1/amd
                            1
   GM3+ (a)
              88 I4_1/a
                              1
   GM3+ is the primary OP.
(methane III)
   Parent: 225 Oh-5, Fm-3m, F4/m-32/m
   Subgroup: 64 D2h-18, Cmca, C2/m2/c2_1/a
   Lattice vectors:
   2 0 0
   0 1 1
   0 -1 1
   origin: 1/2 0 0
   Irrep k params Dir
                                                               Size
                                                Subgroup
                                                225 Fm-3m
   GM1+
                   (a)
                                                               1
   GM3+
                   (a,1.732a)
                                                139 I4/mmm
                                                                1
   GM5+
                  (0,a,0)
                                                 71 Immm
                                                                1
   SM2
                  (0,0,0,0,0,0,0,0,0,0,a,0)
                                                 51 Pmma
   L1-
                   (a,0,a,0)
                                                 67 Cmma
   L3-
                   (a, 0.268a, 0, 0, a, 0.268a, 0, 0)
                                                67 Cmma
                                                123 P4/mmm
   X1+
                   (0,0,a)
                                                131 P4_2/mmc
                                                                2
   X4+
                   (0,0,a)
                   (a,0,0,0,0,0)
   W2
                                                139 I4/mmm
                                                                4
                                                140 I4/mcm
   W3
                   (0,a,0,0,0,0)
   Coupled OP.
YIMWEW
   Parent: 229 Oh-9, Im-3m, I4/m-32/m
   Subgroup: 60 D2h-14, Pbcn, P2_1/b2/c2_1/n
   Lattice vectors:
   0 3 0
   -1 0 1
   1 0 1
   origin: -1/2 0 0
                                                            Size
   Irrep k params Dir
                                               Subgroup
            (a)
   GM1 +
                                               229 Im-3m
                                                             1
                   (a,-1.732a)
   GM3 +
                                               139 I4/mmm
                                                              1
```

GM5+

(0,0,a)

69 Fmmm

1

```
DT5
         5/6
                   (a,-a,a,a,0,0,0,0,0,0,0) 64 Cmca
                                              139 I4/mmm
   DT1
         1/3
                   (a,0,0,0,0,0)
                                                            3
   DT3
        1/3
                   (0,a,0,0,0,0)
                                               69 Fmmm
                                                            3
   H4 +
                   (a, -a, 0)
                                               64 Cmca
   H5+
                   (a,a,0)
                                               64 Cmca
   N1-
                   (0,0,a,0,0,0)
                                               68 Ccca
                                                           2
   N4-
                  (0,0,a,0,0,0)
                                               63 Cmcm
   D2
         1/6
                  (0,0,a,0,0,0,0,0,0,0,0,0)
                                             68 Ccca
                                                           6
   D3
         1/6
                  (0,0,0,0,0,0,0,0,0,a,0,0)
                                             63 Cmcm
                                                            6
   Coupled OP.
RASDOE & TFMETH02
   Parent: 70 D2h-24, Fddd, F2/d2/d2/d, origin choice 2
   Subgroup: 15 C2h-6, C2/c, C12/c1, unique axis b, cell choice 1
   Lattice vectors:
   0 -1 0
   -1 0 0
   0 1/2 -1/2
   origin: 1/4 0 1/4
   Irrep Dir Subgroup Size
   GM1+ (a) 70 Fddd
                       1
   GM3+ (a)
             15 C2/c
   GM3+ is the primary OP.
REKYUB
   Parent: 225 Oh-5, Fm-3m, F4/m-32/m
   Subgroup: 15 C2h-6, C2/c, C12/c1, unique axis b, cell choice 1
   Lattice vectors:
   -1/2 1 -1/2
   -1/2 0 1/2
   1 0 1
   origin: -1/4 0 -1/4
   Irrep Dir
                                Subgroup
                                            Size
                                225 Fm-3m
   GM1+ (a)
                                              1
                                139 I4/mmm
   GM3+ (a,-1.732a)
                                              1
   GM4+ (a,0,-a)
                                 12 C2/m
                                              1
   GM5+
        (a,a,b)
                                 12 C2/m
                                              1
                                 167 R-3c
   L1-
         (a,0,0,0)
                                              2
         (a,3.732a,0,0,0,0,0,0)
   L3-
                                15 C2/c
                                              2
   L3- is the primary OP.
```

# MECKOU

Parent: 225 Oh-5, Fm-3m, F4/m-32/m Subgroup: 12 C2h-3, C2/m, C12/m1, unique axis b, cell choice 1 Lattice vectors: 1/2 -1/2 -1 1/2 1/2 0 1/2 -1/2 1 origin: -1/4 1/4 0 Irrep Dir Subgroup Size GM1+(a)225 Fm-3m 1 139 I4/mmm GM3+ (a,0) 1 12 C2/m GM4+(a,a,0) 1 12 C2/m GM5+(a,b,-b)1

166 R-3m

L3- is the primary OP.

(0,0,0,a)

L3- (0,0,0,0,0,0,a,a) 12 C2/m

#### MECKUA

L2-

Parent: 225 Oh-5, Fm-3m, F4/m-32/m Subgroup: 14 C2h-5, P2\_1/c, P12\_1/c1, unique axis b, cell choice 1 Lattice vectors: 1/2 1 -1/2

2

```
1/2 0 1/2
   1 0 -1
   origin: -1/2 -1/4 1/4
   Irrep Dir
                                  Subgroup
                                                 Size
   GM1+ (a)
                                  225 Fm-3m
                                                   1
        (a, -1.732a)
   GM3+
                                  139 I4/mmm
                                                   1
                                  12 C2/m
                                                   1
   GM4+
         (a,0,a)
   GM5+
         (a,-a,b)
                                   12 C2/m
                                                   1
         (0,a,0,0)
   L2+
                                  167 R-3c
                                                   2
   L3+
         (0,0,a,3.732a,0,0,0,0)
                                  15 C2/c
                                                   2
   L1-
         (0,0,a,0)
                                  167 R-3c
   L3-
         (0,0,0,0,a,3.732a,0,0)
                                  15 C2/c
                                                   2
                                  137 P4_2/nmc
   X2-
         (a,0,0)
                                                   2
                                  129 P4/nmm
   X3-
         (a,0,0)
                                                   2
         (a,0,0,0,0,0)
                                  59 Pmmn
   X5-
                                                   2
   Coupled OP.
TOHSUE
   Parent: 225 Oh-5, Fm-3m, F4/m-32/m
   Subgroup: 14 C2h-5, P2_1/c, P12_1/c1, unique axis b, cell choice 1
   Lattice vectors:
   -1/2 0 1/2
   1/2 0 1/2
   origin: 0 - 1/4 - 1/4
   Irrep k params Dir
                                                 Subgroup
                                                               Size
                                                 225 Fm-3m
   GM1+
                    (a)
                                                                 1
                    (a,-1.732a)
                                                 139 I4/mmm
   GM3+
                                                                 1
   GM4+
                                                 12 C2/m
                                                                 1
                    (a,0,a)
   GM5+
                    (a,-a,b)
                                                 12 C2/m
                                                                 1
   DT2
         3/4
                    (a,-a,0,0,0,0)
                                                 138 P4_2/ncm
   DT4
         3/4
                    (a,a,0,0,0,0)
                                                130 P4/ncc
   DT5
         3/4
                    (0,a,-a,0,0,0,0,0,0,0,0,0)
                                                62 Pnma
                                                                 4
   X2-
                                                 137 P4_2/nmc
                                                                 2
                    (a,0,0)
                                                 129 P4/nmm
                    (a,0,0)
                                                                 2
   X3-
   X5-
                    (a,0,0,0,0,0)
                                                 59 Pmmn
                                                                 2
   Coupled OP.
CARBTC07 & CTBROM
   Parent: 225 Oh-5, Fm-3m, F4/m-32/m
   Subgroup: 15 C2h-6, C2/c, C12/c1, unique axis b, cell choice 1
   Lattice vectors:
   -2 -1 -1
   0 1 -1
   2 - 1 - 1
   origin: -1/2 1/2 1/2
   Irrep k params Dir
                                                                             Subgroup
                                                                                           Size
                                                                             225 Fm-3m
   GM1 +
                                                                                             1
                   (a)
   GM3 +
                    (a, 1.732a)
                                                                             139 I4/mmm
                                                                                             1
   GM4+
                   (0,a,-a)
                                                                             12 C2/m
                                                                                             1
   GM5+
                                                                              12 C2/m
                    (a,b,a)
   LD2
         3/4
                    (0,a,0,0,0,-a,0,0)
                                                                             167 R-3c
                    (0,0,a,0.268a,0,0,0,0,0,0.268a,a,0,0,0,0)
   LD3
         3/4
                                                                              15 C2/c
                                                                                             4
                                                                              67 Cmma
   L1-
                    (0,a,0,a)
   L2-
                                                                                             8
                                                                              12 C2/m
                    (a,b,c,-b)
   L3-
                    (a,-3.732a,b,c,d,-3.732d,0.866b+0.500c,0.500b-0.866c)
                                                                             12 C2/m
   X1+
                                                                             123 P4/mmm
                    (a,-a,b)
                                                                             123 P4/mmm
   X2+
                    (a,a,0)
   X3+
                    (a,a,0)
                                                                             134 P4_2/nnm
   X4+
                    (a,-a,b)
                                                                             134 P4_2/nnm
                                                                                             4
   X5+
                    (a,b,-b,a,0,c)
                                                                             12 C2/m
                                                                                             4
   C1
                    (0,0,a,0,0,0,a,0,0,0,0,0,0,a,0,0,0,a,0,0,0,0)
                                                                                             8
         1/2,1/4
                                                                             12 C2/m
   C2
         1/2,1/4
                   (0,0,a,0,0,0,0,-a,b,0,0,0,0,0,-a,0,0,0,0,a,-b,0,0,0)
                                                                             15 C2/c
                                                                                            16
```

C2 is the primary OP.

```
MEZDIE01 & MEZDOK01
```

Parent: 229 Oh-9, Im-3m, I4/m-32/mSubgroup: 2 Ci-1, P-1, P-1

Lattice vectors: 1/2 1/2 1/2 1 0 -1

-1/2 1/2 -1/2 origin: -1/4 -1/4 1/4

Irrep	Dir	Subgroup		Size
GM1+	(a)	229	Im-3m	1
GM2+	(a)	204	Im-3	1
GM3+	(a,b)	71	Immm	1
GM4+	(a,b,c)	2	P-1	1
GM5+	(a,b,c)	2	P-1	1
N1-	(0,0,a,0,0,0)	68	Ccca	2
N2-	(0,0,0,a,0,0)	63	Cmcm	2
N3-	(0,0,a,0,0,0)	67	Cmma	2
N4-	(0,0,0,a,0,0)	63	Cmcm	2

Coupled OP.

## OHABEE

Parent: 229 Oh-9, Im-3m, I4/m-32/m Subgroup: 2 Ci-1, P-1, P-1

Lattice vectors: 1/2 1/2 1/2 1 -1 0

1 1 -2

origin: -1 -1/2 1

Irrep	k params	Dir	Sub	group	Size
GM1+		(a)	229	Im-3m	1
GM2+		(a)	204	Im-3	1
GM3+		(a,b)	71	Immm	1
GM4+		(a,b,c)	2	P-1	1
GM5+		(a,b,c)	2	P-1	1
LD1	1/3	(a,0,0,0,-1.732a,0,0,0)	164	P-3m1	3
LD2	1/3	(a,0,0,0.577a,0,0,0)	147	P-3	3
LD3	1/3	(a,b,0,0,0,0,0,0,0,-0.577a-1.155b,-1.155a-0.577b,0,0,0,0,0,0)	2	P-1	3
N1-		(0,0,0,0,a,0)	68	Ccca	2
N2-		(0,0,0,0,a)	63	Cmcm	2
N3-		(0,0,0,0,a,0)	67	Cmma	2
N4-		(0,0,0,0,a)	63	Cmcm	2
C1	1/6,2/3	(a,0,0,0,0,0,0,0,0,0,0,0,0,0.577a,0,0,0,0,0,0,0,0,0,0,0)	11	P2_1/m	6
C2	1/6,2/3	(a,0,0,0,0,0,0,0,0,0,0,1.732a,0,0,0,0,0,0,0,0,0,0,0)	13	P2/c	6

Coupled OP.

# Dimer Packings:

```
FOJBUB & VADRAU
   Parent: 225 Oh-5, Fm-3m, F4/m-32/m
   Subgroup: 205 Th-6, Pa-3, P2_1/a-3
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 1
   origin: 0 0 0
   Irrep Dir
                       Subgroup
                                  Size
   GM1+ (a)
GM2+ (a)
                       225 Fm-3m
202 Fm-3
                                  1
                                    1
        (a,a,a,a,a,a) 205 Pa-3
   X5+
   X5+ is the primary OP.
LUFYEQ
   Parent: 141 D4h-19, I4_1/amd, I4_1/a2/m2/d, origin choice 2
   Subgroup: 88 C4h-6, I4_1/a, I4_1/a, origin choice 2
   Lattice vectors:
   1 0 0
   0 1 0
   0 0 1
   origin: 0 1/2 0
   Irrep Dir Subgroup
                           Size
   GM1+ (a) 141 I4_1/amd 1
   GM3+ (a) 88 I4_1/a
                            1
   GM3+ is the primary OP.
CARBTC
   Parent: 166 D3d-5, R-3m, R-32/m, hexangonal axes
   Subgroup: 14 C2h-5, P2_1/c, P12_1/c1, unique axis b, cell choice 1
   Lattice vectors:
   -2/3 -1/3 -1/3
   0 1 0
   2 1 0
   origin: 0 0 0
   Irrep Dir
                   Subgroup
                               Size
   GM1+ (a)
                   166 R-3m
                                  1
   GM3+ (a,0)
                   12 C2/m
                                  1
                    14 P2 1/c
                                  2
   F2+
        (0,a,0)
   F2+ is the primary OP.
```

## Mixed

```
ROXKOX, RUQMEV, & SENLAY
    Parent: 223 Oh-3, Pm-3n, P4_2/m-32/n
    Subgroup: 218 Td-4, P-43n, P-43n
    Lattice vectors:
    1 0 0
    0 1 0
    0 0 1
    origin: 0 0 0

Irrep Dir Subgroup Size
    GM1+ (a) 223 Pm-3n 1
    GM2- (a) 218 P-43n 1
GM2- is the primary OP.
```