

> Geographic Data Science  
with  
**PySAL**

and the  
**pydata stack**

Sergio J. Rey

Dani Arribas-Bel

---

# Table of Contents

Introduction	1.1
Distribution	1.2
About the authors	1.3
Outline	1.4
Data	1.5
Part I	1.6
Software and Tools Installation	1.6.1
Spatial data processing with PySAL	1.6.2
Geovisualization	1.6.3
Spatial weights in PySAL	1.6.4
ESDA with PySAL	1.6.5
Space-time analysis	1.6.6
Part II	1.7
Points	1.7.1
Spatial clustering	1.7.2
Spatial Regression	1.7.3

# Geographic Data Science with PySAL and the pydata stack

This two-part tutorial will first provide participants with a gentle introduction to Python for geospatial analysis, and an introduction to version `PySAL` 1.11 and the related eco-system of libraries to facilitate common tasks for Geographic Data Scientists. The first part will cover munging geo-data and exploring relations over space. This includes importing data in different formats (e.g. shapefile, GeoJSON), visualizing, combining and tidying them up for analysis, and will use libraries such as `pandas`, `geopandas`, `PySAL`, or `rasterio`. The second part will provide a gentle overview to demonstrate several techniques that allow to extract geospatial insight from the data. This includes spatial clustering and regression and point pattern analysis, and will use libraries such as `PySAL`, `scikit-learn`, or `clusterpy`. A particular emphasis will be set on presenting concepts through visualization, for which libraries such as `matplotlib`, `seaborn`, and `folium` will be used.





# Distribution

[URL] [PDF] [EPUB] [MOBI] [IPYNB]

## License



Geographic Data Science with PySAL and the pydata stack by Sergio J. Rey and Dani Arribas-Bel is licensed under a [Creative Commons Attribution-NonCommercial-ShareAlike 4.0 International License](#).

## About the authors



[Sergio Rey](#) is professor of geographical sciences and core faculty member of the GeoDa Center for Geospatial Analysis and Computation at the Arizona State University. His research interests include open science, spatial and spatio-temporal data analysis, spatial econometrics, visualization, high performance geocomputation, spatial inequality dynamics, integrated multiregional modeling, and regional science. He co-founded the Python Spatial Analysis Library (PySAL) in 2007 and continues to direct the PySAL project. Rey is a fellow of the spatial econometrics association and editor of the journal Geographical Analysis.



[Dani Arribas-Bel](#) is Lecturer in Geographic Data Science and member of the Geographic Data Science Lab at the University of Liverpool (UK). Dani is interested in understanding cities as well as in the quantitative and computational methods required to leverage the power of the large amount of urban data increasingly becoming available. He is also part of the team of core developers of PySAL, the open-source library written in Python for spatial analysis. Dani regularly teaches Geographic Data Science and Python courses at the University of Liverpool and has designed and developed several workshops at different levels on spatial analysis and econometrics, Python and open source scientific computing.

# Outline

## Part I

1. Software and Tools Installation (10 min)
2. Spatial data processing with PySAL (45 min)
  - a. Input-output
  - b. Visualization and Mapping
  - c. Spatial weights
3. Exercise (10 min.)
4. ESDA with PySAL (45 min)
  - a. Global Autocorrelation
  - b. Local Autocorrelation
  - c. Space-Time exploratory analysis
5. Exercise (10 min)

## Part II

1. Point Patterns (30 min)
  - a. Point visualization
  - b. Centrography and distance based statistics
2. Exercise (10 min)
3. Spatial clustering a (30 min)
  - a. Geodemographic analysis
  - b. Regionalization
4. Exercise (30 min)
5. Spatial Regression (30 min)
  - a. Baseline (nonspatial) regression
  - b. Exogenous and endogenous spatially lagged regressors
  - c. Prediction performance of spatial models
6. Exercise (10 min)

# Data

This tutorial makes use of a variety of data sources. Below is a brief description of each dataset as well as the links to the original source where the data was downloaded from. For convenience, we have repackaged the data and included them in the compressed file with the notebooks. You can download it [here](#).

## AirBnb listing for Austin (TX)

This dataset contains information for [AirBnb](#) properties for the area of Austin (TX). It is originally provided by [Inside AirBnb](#). Same as the source, the dataset is released under a [CC0 1.0 Universal License](#). You can see a summary of the dataset [here](#).

**Source:** [Inside AirBnb](#)'s extract of AirBnb locations in Austin (TX).

**Path:** `data/listings.csv.gz`

## Austin Zipcodes

Boundaries for Zipcodes in Austin. The original source is provided by the City of Austin GIS Division.

**Source:** open data from the city of Austin [\[url\]](#)

**Path:** `data/Zipcodes.geojson`

## **Part I**

# Software and Tools Installation

## Dependencies

Participants should have installed the following dependencies:

- [Anaconda](#) or [MiniConda](#) Python distributions for Python 2.7. See installation instructions on the links.
- `git`
- A `conda` environment loaded with all the dependencies can be installed by running the `pydata.sh` script available as part of the `envs` repository ([Github link](#)). To install it, follow these instructions:
  - Clone the repository on your machine:  
`> git clone https://github.com/darrrias/envs.git`
  - Navigate into the folder:  
`> cd envs`
  - Run the script:  
`> bash pydata.sh`

Once installed, you need to activate the environment to run the notebooks. In Windows, open up [PowerShell](#) and type:

```
> activate pydata
```

And if you are on GNU/Linux or OSX:

```
> source activate pydata
```

## Get started

Instructions to fire up a notebook here.

```
#by convention, we use these shorter two-letter names
import pysal as ps
import pandas as pd
import numpy as np
```

## Spatial Data Processing with PySAL & Pandas

PySAL has two simple ways to read in data. But, first, you need to get the path from where your notebook is running on your computer to the place the data is. For example, to find where the notebook is running:

```
!pwd
```

```
/home/serge/Dropbox/p/pysal/workshops/scipy16/gds_scipy16/content/part1
```

PySAL has a command that it uses to get the paths of its example datasets. Let's work with a commonly-used dataset first.

```
dbf_path = '../data/texas.dbf'
print(dbf_path)
```

```
../data/texas.dbf
```

For the purposes of this part of the workshop, we'll use the `texas.dbf` example data, and the `usjoin.csv` data.

```
csv_path = ps.examples.get_path('usjoin.csv')
```

## Working with shapefiles

To read in a shapefile, we will need the path to the file.

```
shp_path = '../data/texas.shp'
print(shp_path)
```

```
../data/texas.shp
```

Then, we open the file using the `ps.open` command:

```
f = ps.open(shp_path)
```

`f` is what we call a "file handle." That means that it only *points* to the data and provides ways to work with it. By itself, it does not read the whole dataset into memory. To see basic information about the file, we can use a few different methods.

For instance, the header of the file, which contains most of the metadata about the file:

```
f.header
```

```
{
'BBOX Mmax': 0.0,
'BBOX Mmin': 0.0,
'BBOX Xmax': -93.50721740722656,
'BBOX Xmin': -106.6495132446289,
'BBOX Ymax': 36.49387741088867,
'BBOX Ymin': 25.845197677612305,
'BBOX Zmax': 0.0,
'BBOX Zmin': 0.0,
'File Code': 9994,
'File Length': 49902,
'Shape Type': 5,
'Unused0': 0,
'Unused1': 0,
'Unused2': 0,
'Unused3': 0,
'Unused4': 0,
'Version': 1000}
```

To actually read in the shapes from memory, you can use the following commands:

```
f.by_row(14) #gets the 14th shape from the file
```

```
<pysal.cg.shapes.Polygon at 0x7f1e5423c550>
```

```
all_polygons = f.read() #reads in all polygons from memory
```

```
len(all_polygons)
```

```
254
```

So, all 254 polygons have been read in from file. These are stored in PySAL shape objects, which can be used by PySAL and can be converted to other Python shape objects. ]

They typically have a few methods. So, since we've read in polygonal data, we can get some properties about the polygons. Let's just have a look at the first polygon:

```
all_polygons
```

```
[<pysal.cg.shapes.Polygon at 0x7f1e23a751d0>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75190>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75410>,
<pysal.cg.shapes.Polygon at 0x7f1e56420490>,
<pysal.cg.shapes.Polygon at 0x7f1e23a56ed0>,
<pysal.cg.shapes.Polygon at 0x7f1e23a754d0>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75550>,
<pysal.cg.shapes.Polygon at 0x7f1e23a755d0>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75650>,
<pysal.cg.shapes.Polygon at 0x7f1e23a756d0>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75750>,
<pysal.cg.shapes.Polygon at 0x7f1e23a757d0>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75890>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75910>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75990>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75a10>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75a90>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75b10>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75b90>,
<pysal.cg.shapes.Polygon at 0x7f1e23a56c90>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75bd0>,
<pysal.cg.shapes.Polygon at 0x7f1e23a75c50>,
```







```
<pysal.cg.shapes.Polygon at 0x7f1e23151b10>,
<pysal.cg.shapes.Polygon at 0x7f1e23151c90>,
<pysal.cg.shapes.Polygon at 0x7f1e23151d10>,
<pysal.cg.shapes.Polygon at 0x7f1e54229d90>,
<pysal.cg.shapes.Polygon at 0x7f1e23151e50>,
<pysal.cg.shapes.Polygon at 0x7f1e23151ed0>,
<pysal.cg.shapes.Polygon at 0x7f1e23151f50>,
<pysal.cg.shapes.Polygon at 0x7f1e23151f10>,
<pysal.cg.shapes.Polygon at 0x7f1e23169110>,
<pysal.cg.shapes.Polygon at 0x7f1e23169190>,
<pysal.cg.shapes.Polygon at 0x7f1e23169210>,
<pysal.cg.shapes.Polygon at 0x7f1e23169290>,
<pysal.cg.shapes.Polygon at 0x7f1e23169390>,
<pysal.cg.shapes.Polygon at 0x7f1e23169410>,
<pysal.cg.shapes.Polygon at 0x7f1e23169490>,
<pysal.cg.shapes.Polygon at 0x7f1e23169550>]
```

```
all_polygons[0].centroid #the centroid of the first polygon
```

```
(-100.27156110567945, 36.27508640938005)
```

```
all_polygons[0].area
```

```
0.23682222998468205
```

```
all_polygons[0].perimeter
```

```
1.9582821721538344
```

While in the Jupyter Notebook, you can examine what properties an object has by using the tab key.

```
polygon = all_polygons[0]
```

```
polygon. #press tab when the cursor is right after the dot
```

```
File "<ipython-input-16-aa03438a2fa8>", line 1
    polygon. #press tab when the cursor is right after the dot
          ^
SyntaxError: invalid syntax
```

## Working with Data Tables

When you're working with tables of data, like a `csv` or `dbf`, you can extract your data in the following way. Let's open the `dbf` file we got the path for above.

```
f = ps.open(dbf_path)
```

Just like with the shapefile, we can examine the header of the `dbf` file

```
f.header
```

```
[u'NAME',
 u'STATE_NAME',
 u'STATE_FIPS',
 u'CTY_FIPS',
 u'FIPS',
 u'STFIPS',
 u'COFIPS',
 u'FIPSNO',
 u'SOUTH',
 u'HR60',
 u'HR70',
 u'HR80',
 u'HR90',
 u'HC60',
 u'HC70',
 u'HC80',
 u'HC90',
 u'PO60',
 u'PO70',
 u'PO80',
 u'PO90',
 u'RD60',
 u'RD70',
 u'RD80',
 u'RD90',
 u'PS60',
 u'PS70',
 u'PS80',
 u'PS90',
 u'UE60',
 u'UE70',
 u'UE80',
 u'UE90',
 u'DV60',
 u'DV70',
 u'DV80',
 u'DV90',
 u'MA60',
 u'MA70',
 u'MA80',
 u'MA90',
 u'POL60',
 u'POL70',
 u'POL80',
 u'POL90',
 u'DNL60',
 u'DNL70',
 u'DNL80',
 u'DNL90',
 u'MFIL59',
 u'MFIL69',
 u'MFIL79',
 u'MFIL89',
 u'FP59',
 u'FP69',
 u'FP79',
 u'FP89',
 u'BLK60',
 u'BLK70',
 u'BLK80',
 u'BLK90',
 u'GI59',
 u'GI69',
 u'GI79',
 u'GI89',
 u'FH60',
 u'FH70',
 u'FH80',
 u'FH90']
```

So, the header is a list containing the names of all of the fields we can read. If we were interested in getting the `['NAME', 'STATE_NAME', 'HR90', 'HR80']` fields.

If we just wanted to grab the data of interest, `HR90`, we can use either `by_col` or `by_col_array`, depending on the format we want the resulting data in:

```
HR90 = f.by_col('HR90')
print(type(HR90).__name__, HR90[0:5])
HR90 = f.by_col_array('HR90')
print(type(HR90).__name__, HR90[0:5])
```

```
('list', [0.0, 0.0, 18.31166453, 0.0, 3.6517674554])
('ndarray', array([[ 0.      ],
   [ 0.      ],
   [ 18.31166453],
   [ 0.      ],
   [ 3.65176746]]))
```

As you can see, the `by_col` function returns a list of data, with no shape. It can only return one column at a time:

```
HRs = f.by_col('HR90', 'HR80')
```

```
-----
TypeError                                 Traceback (most recent call last)
<ipython-input-20-1fef6a3c3a50> in <module>()
----> 1 HRs = f.by_col('HR90', 'HR80')

TypeError: __call__() takes exactly 2 arguments (3 given)
```

This error message is called a "traceback," as you see in the top right, and it usually provides feedback on why the previous command did not execute correctly. Here, you see that one-too-many arguments was provided to `_call_`, which tells us we cannot pass as many arguments as we did to `by_col`.

If you want to read in many columns at once and store them to an array, use `by_col_array`:

```
HRs = f.by_col_array('HR90', 'HR80')
```

```
HRs
```

```
array([[ 0.      ,  0.      ],
   [ 0.      , 10.50199538],
   [18.31166453,  5.10386362],
   [ 0.      ,  0.      ],
   [ 3.65176746, 10.4297038 ],
   [ 0.      ,  0.      ],
   [ 0.      , 18.85369532],
   [ 2.59514448,  6.33617194],
   [ 0.      ,  0.      ],
   [ 5.59753708,  6.0331825 ],
   [17.3692707 , 14.53139626],
   [ 5.06893755,  4.9960032 ],
   [ 9.73560868,  8.84307335],
   [ 5.66989851,  4.67049647],
   [ 0.      ,  0.      ],
   [ 4.08893052,  4.44077341],
   [16.49348507,  0.      ]])
```

```
[ 0.     ,  7.17154332],
[ 0.     ,  8.1799591 ],
[ 3.48074279,  7.8746358 ],
[ 0.     ,  6.0397415 ],
[ 3.67511944, 12.63104711],
[ 8.19705726, 17.14148582],
[ 0.     ,  0.     ],
[ 11.19883532,  4.79616307],
[ 8.53606487,  5.95876534],
[ 6.30954634,  5.23450586],
[ 19.83995768,  8.36942649],
[ 43.51610096,  0.     ],
[ 14.83459427,  0.     ],
[ 7.8459064 ,  6.77920141],
[ 5.76850971, 12.41398879],
[ 2.21160651,  5.3564733 ],
[ 4.7187618 , 16.32386549],
[ 0.     ,  0.     ],
[ 13.6190056 ,  9.08475248],
[ 0.     ,  0.     ],
[ 5.78904712,  5.74382539],
[ 11.6411725 , 10.35132393],
[ 11.57638838,  5.93938854],
[ 8.66447889,  7.23170379],
[ 7.58454876, 11.06999399],
[ 16.12643122,  4.11776817],
[ 0.     ,  0.     ],
[ 0.     ,  9.41885655],
[ 0.     , 11.28795575],
[ 8.68383071, 18.26906873],
[ 4.18077679,  0.     ],
[ 5.50986955,  7.17463051],
[ 20.67397147, 18.76524676],
[ 0.     ,  0.     ],
[ 0.     , 13.81692573],
[ 7.75526031,  8.85335741],
[ 13.7258939 , 20.66542674],
[ 9.54973022,  4.49964003],
[ 4.80598249,  5.01724679],
[ 5.24022789,  4.89079552],
[ 9.3250237 , 9.65344145],
[ 3.15613527,  6.68621809],
[ 15.27205076, 15.54581351],
[ 0.     ,  4.31499461],
[ 0.     ,  0.     ],
[ 3.677958 ,  3.4935108 ],
[ 0.     ,  0.     ],
[ 16.55903295, 13.85425326],
[ 4.27240878, 24.17911891],
[ 12.96260289,  6.24687656],
[ 0.     ,  0.     ],
[ 5.04362738,  6.85824018],
[ 0.     ,  4.01654818],
[ 5.78041365,  7.92173328],
[ 0.     , 29.62152801],
[ 11.11778178,  7.92841771],
[ 16.82821755, 10.78167116],
[ 4.53823463,  8.09814957],
[ 5.32162576, 13.85310171],
[ 5.14522395,  3.73616684],
[ 15.7535989 , 15.99138866],
[ 24.88112651, 22.42368558],
[ 7.81127949,  4.58883994],
[ 14.89203276, 13.77695116],
[ 0.     ,  8.51426139],
[ 6.06428138,  9.65176434],
[ 0.     ,  5.65834889],
[ 7.15537906, 10.99384345],
[ 0.     ,  0.     ],
[ 16.26129579,  6.17894217],
[ 3.69959304,  6.71636779],
[ 0.     , 10.13941698],
```

```
[ 4.25034534, 12.82275456],
[ 13.35470086, 35.39253539],
[ 22.97970126, 16.23307275],
[ 7.02790077, 6.36415707],
[ 8.69822382, 15.94438598],
[ 10.13378803, 16.35947213],
[ 15.88088069, 17.42271184],
[ 5.83200398, 7.39109226],
[ 4.60071541, 7.52700312],
[ 9.78469752, 12.27479928],
[ 10.30741159, 11.11792209],
[ 11.33681683, 23.13278217],
[ 8.31669993, 11.00352113],
[ 9.01485648, 5.13347023],
[ 5.62160947, 3.03250849],
[ 0.      , 7.11642471],
[ 6.97447343, 5.00387801],
[ 6.02627456, 5.7607005 ],
[ 2.38171793, 4.43262411],
[ 9.14599291, 17.72107035],
[ 0.      , 12.86752879],
[ 9.67949484, 14.86488601],
[ 12.52316786, 15.0987553 ],
[ 6.21890547, 16.04878832],
[ 9.82342395, 13.32054561],
[ 7.47328301, 5.28387625],
[ 6.61157025, 12.43688282],
[ 9.74445175, 6.11989754],
[ 0.      , 0.      ],
[ 0.      , 25.56237219],
[ 7.50391611, 12.90801426],
[ 0.      , 0.      ],
[ 3.86428627, 23.46473585],
[ 11.77123447, 21.66866018],
[ 0.      , 8.42318059],
[ 3.43288706, 6.38630776],
[ 3.87923928, 9.07523369],
[ 12.49375312, 15.63273495],
[ 4.31053063, 0.      ],
[ 12.64382349, 2.24769611],
[ 39.13511398, 0.      ],
[ 6.30835226, 12.65742675],
[ 0.      , 0.      ],
[ 11.43510578, 0.      ],
[ 7.66270572, 8.82130059],
[ 21.17938943, 20.21602264],
[ 16.56770109, 10.15099607],
[ 10.95830365, 15.67420453],
[ 7.95696871, 16.48206751],
[ 0.      , 0.      ],
[ 4.67195116, 2.34878245],
[ 8.125292 , 7.86311883],
[ 5.08323802, 11.92520511],
[ 8.33437513, 11.38303927],
[ 0.      , 7.24637681],
[ 7.49568998, 14.43313849],
[ 0.      , 0.      ],
[ 7.89577576, 17.37196859],
[ 6.95458655, 7.66107408],
[ 21.83235867, 14.94835344],
[ 10.95050372, 0.      ],
[ 0.      , 24.05002405],
[ 15.26338885, 7.27212284],
[ 7.52785306, 11.14454474],
[ 0.      , 15.26426254],
[ 6.1716966 , 10.74575543],
[ 4.93060178, 8.32986256],
[ 8.73743993, 7.05467372],
[ 13.6286201 , 4.5605874 ],
[ 6.44703759, 15.92392912],
[ 12.21077898, 13.08936447],
[ 17.19605965, 7.54489211],
```

```
[ 7.50219707,  9.74627205],
[ 9.7761267 , 16.38874094],
[ 7.26343008, 17.59633996],
[ 17.12915382,  0.    ],
[ 0.    , 18.78110621],
[ 11.14827202,  0.    ],
[ 0.    ,  0.    ],
[ 24.52182442,  7.2337963 ],
[ 10.01241539,  4.10939202],
[ 7.20126218, 10.36955499],
[ 5.8796725 ,  3.74468722],
[ 4.37653521,  7.4795914 ],
[ 19.4760931 ,  9.05059281],
[ 2.86590434,  9.85804416],
[ 4.06064211,  3.92049241],
[ 12.2159785 ,  8.74584572],
[ 5.31123858, 17.18213058],
[ 2.44648318, 18.95016108],
[ 24.26006793,  8.20411847],
[ 24.18379686,  0.    ],
[ 15.35921361,  4.40160218],
[ 0.    ,  0.    ],
[ 10.04469891,  6.42508353],
[ 8.15396066, 12.39355249],
[ 11.52573257, 12.19319205],
[ 12.96613246,  9.13075237],
[ 4.03355921,  9.82294148],
[ 0.    ,  0.    ],
[ 16.74480911,  7.12098554],
[ 11.37958502, 22.65262204],
[ 10.45396336, 14.82919464],
[ 6.37251153, 12.12231415],
[ 5.08021662, 12.3170912 ],
[ 0.    ,  0.    ],
[ 6.88687448,  3.71298617],
[ 7.34537976,  5.79105861],
[ 14.25110446, 13.46937401],
[ 10.35080964,  8.34943582],
[ 15.03778243, 14.47900809],
[ 9.95272456, 10.6202209 ],
[ 23.54931879, 32.62023941],
[ 4.56965293,  0.    ],
[ 8.40392631, 15.04381511],
[ 27.63957988,  0.    ],
[ 3.78902698,  8.46131066],
[ 4.50172352,  6.40216576],
[ 5.43980852, 10.62529884],
[ 6.31193587,  4.70543949],
[ 13.27492367,  8.99054195],
[ 9.24884004,  9.27749707],
[ 8.13293053, 15.03039196],
[ 23.24905551, 15.79498114],
[ 18.39050982, 19.38376483],
[ 8.54325327,  4.31704369],
[ 12.48439451,  0.    ],
[ 7.508447 ,  8.28321985],
[ 11.42530705, 11.88301175],
[ 0.    ,  0.    ],
[ 5.91179943, 10.22090923],
[ 15.17946265, 18.03273111],
[ 10.30169242, 13.92536007],
[ 8.84642604,  7.05355411],
[ 5.11286653, 12.48252447],
[ 5.45857488, 10.64325151],
[ 10.83188908, 21.14835572],
[ 5.3526027 ,  9.8089703 ],
[ 7.17221841,  8.72004302],
[ 24.66699556,  8.5719184 ],
[ 12.37133808, 12.09043646],
[ 8.24674254,  0.    ],
[ 0.    ,  6.41889723],
[ 0.    ,  3.47005344],
```

```
[ 5.30468802, 16.64745806],
[ 31.72186271, 18.1356547 ],
[ 40.7996736 , 0.      ],
[ 9.58497077, 11.72986129],
[ 4.17920428, 3.58847382],
[ 5.24851729, 11.92057491],
[ 9.25654901, 11.08223015],
[ 6.80862653, 10.9170933 ],
[ 5.5890901 , 2.33754091],
[ 18.0626516 , 26.63044926],
[ 5.3079965 , 10.95950463],
[ 10.30414398, 17.39897719],
[ 5.50527405, 13.98964766],
[ 13.04886801, 6.4499484 ],
[ 10.77702339, 0.      ],
[ 8.12611734, 27.6854928 ],
[ 0.      , 0.      ],
[ 14.80823338, 17.11533289],
[ 7.30031678, 8.23832776],
[ 5.648122 , 7.62122511],
[ 12.30201446, 11.76132146]])
```

It is best to use `by_col_array` on data of a single type. That is, if you read in a lot of columns, some of them numbers and some of them strings, all columns will get converted to the same datatype:

```
allcolumns = f.by_col_array(['NAME', 'STATE_NAME', 'HR90', 'HR80'])
```

```
allcolumns
```

```
array([[u'Lipscomb', u'Texas', u'0.0', u'0.0'],
       [u'Sherman', u'Texas', u'0.0', u'10.501995379'],
       [u'Dallam', u'Texas', u'18.31166453', u'5.1038636248'],
       ...,
       [u'Hidalgo', u'Texas', u'7.3003167816', u'8.2383277607'],
       [u'Willacy', u'Texas', u'5.6481219994', u'7.6212251119'],
       [u'Cameron', u'Texas', u'12.302014455', u'11.761321464']],
      dtype='|<U13')
```

Note that the numerical columns, `HR90` & `HR80` are now considered strings, since they show up with the single tickmarks around them, like `'0.0'`.

These methods work similarly for `.csv` files as well

## Using Pandas with PySAL

A new functionality added to PySAL recently allows you to work with shapefile/dbf pairs using Pandas. This *optional* extension is only turned on if you have Pandas installed. The extension is the `ps.pdio` module:

```
ps.pdio
```

```
<module 'pysal.contrib.pdutilities' from '/home/serge/anaconda2/envs/pydata/lib/python2.7/site-packages/pysal/contrib/pdutilities/__init__.pyc'>
```

To use it, you can read in shapefile/dbf pairs using the `ps.pdio.read_files` command.

```
shp_path = ps.examples.get_path('NAT.shp')
data_table = ps.pdio.read_files(shp_path)
```

This reads in *the entire database table* and adds a column to the end, called `geometry`, that stores the geometries read in from the shapefile.

Now, you can work with it like a standard pandas dataframe.

```
data_table.head()
```

	<b>NAME</b>	<b>STATE_NAME</b>	<b>STATE_FIPS</b>	<b>CNTY_FIPS</b>	<b>FIPS</b>	<b>STFIPS</b>	<b>COFIP</b>
<b>0</b>	Lake of the Woods	Minnesota	27	077	27077	27	77
<b>1</b>	Ferry	Washington	53	019	53019	53	19
<b>2</b>	Stevens	Washington	53	065	53065	53	65
<b>3</b>	Okanogan	Washington	53	047	53047	53	47
<b>4</b>	Pend Oreille	Washington	53	051	53051	53	51

5 rows × 70 columns

The `read_files` function only works on shapefile/dbf pairs. If you need to read in data using CSVs, use pandas directly:

```
usjoin = pd.read_csv(csv_path)
#usjoin = ps.pdio.read_files(csv_path) #will not work, not a shp/dbf pair
```

```
usjoin.head()
```

	<b>Name</b>	<b>STATE_FIPS</b>	<b>1929</b>	<b>1930</b>	<b>1931</b>	<b>1932</b>	<b>1933</b>	<b>1934</b>	<b>1935</b>
<b>0</b>	Alabama	1	323	267	224	162	166	211	217
<b>1</b>	Arizona	4	600	520	429	321	308	362	416
<b>2</b>	Arkansas	5	310	228	215	157	157	187	207
<b>3</b>	California	6	991	887	749	580	546	603	660
<b>4</b>	Colorado	8	634	578	471	354	353	368	444

5 rows × 83 columns

The nice thing about working with pandas dataframes is that they have very powerful baked-in support for relational-style queries. By this, I mean that it is very easy to find things like:

The number of counties in each state:

```
data_table.groupby("STATE_NAME").size()
```

```

STATE_NAME
Alabama      67
Arizona       14
Arkansas      75
California    58
Colorado      63
Connecticut    8
Delaware       3
District of Columbia 1
Florida       67
Georgia      159
Idaho        44
Illinois     102
Indiana      92
Iowa         99
Kansas        105
Kentucky      120
Louisiana    64
Maine         16
Maryland      24
Massachusetts 12
Michigan      83
Minnesota    87
Mississippi   82
Missouri     115
Montana       55
Nebraska      93
Nevada        17
New Hampshire 10
New Jersey    21
New Mexico    32
New York      58
North Carolina 100
North Dakota   53
Ohio          88
Oklahoma      77
Oregon        36
Pennsylvania   67
Rhode Island   5
South Carolina 46
South Dakota   66
Tennessee     95
Texas         254
Utah          29
Vermont        14
Virginia      123
Washington     38
West Virginia   55
Wisconsin     70
Wyoming       23
dtype: int64

```

Or, to get the rows of the table that are in Arizona, we can use the `query` function of the dataframe:

```
data_table.query('STATE_NAME == "Arizona"')
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	CO
<b>1707</b>	Navajo	Arizona	04	017	04017	4	17
<b>1708</b>	Coconino	Arizona	04	005	04005	4	5
<b>1722</b>	Mohave	Arizona	04	015	04015	4	15
<b>1726</b>	Apache	Arizona	04	001	04001	4	1
<b>2002</b>	Yavapai	Arizona	04	025	04025	4	25
<b>2182</b>	Gila	Arizona	04	007	04007	4	7
<b>2262</b>	Maricopa	Arizona	04	013	04013	4	13
<b>2311</b>	Greenlee	Arizona	04	011	04011	4	11
<b>2326</b>	Graham	Arizona	04	009	04009	4	9
<b>2353</b>	Pinal	Arizona	04	021	04021	4	21
<b>2499</b>	Pima	Arizona	04	019	04019	4	19
<b>2514</b>	Cochise	Arizona	04	003	04003	4	3
<b>2615</b>	Santa Cruz	Arizona	04	023	04023	4	23
<b>3080</b>	La Paz	Arizona	04	012	04012	4	12

14 rows × 70 columns

Behind the scenes, this uses a fast vectorized library, `numexpr`, to essentially do the following.

First, compare each row's `STATE_NAME` column to '`Arizona`' and return `True` if the row matches:

```
data_table.STATE_NAME == 'Arizona'
```

```
0    False
1    False
2    False
3    False
4    False
5    False
6    False
7    False
8    False
9    False
10   False
11   False
12   False
13   False
14   False
15   False
16   False
17   False
18   False
19   False
20   False
21   False
22   False
23   False
24   False
25   False
26   False
27   False
28   False
29   False
...
3055  False
3056  False
3057  False
3058  False
3059  False
3060  False
3061  False
3062  False
3063  False
3064  False
3065  False
3066  False
3067  False
3068  False
3069  False
3070  False
3071  False
3072  False
3073  False
3074  False
3075  False
3076  False
3077  False
3078  False
3079  False
3080  True
3081  False
3082  False
3083  False
3084  False
Name: STATE_NAME, dtype: bool
```

Then, use that to filter out rows where the condition is true:

```
data_table[data_table.STATE_NAME == 'Arizona']
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	CO
<b>1707</b>	Navajo	Arizona	04	017	04017	4	17
<b>1708</b>	Coconino	Arizona	04	005	04005	4	5
<b>1722</b>	Mohave	Arizona	04	015	04015	4	15
<b>1726</b>	Apache	Arizona	04	001	04001	4	1
<b>2002</b>	Yavapai	Arizona	04	025	04025	4	25
<b>2182</b>	Gila	Arizona	04	007	04007	4	7
<b>2262</b>	Maricopa	Arizona	04	013	04013	4	13
<b>2311</b>	Greenlee	Arizona	04	011	04011	4	11
<b>2326</b>	Graham	Arizona	04	009	04009	4	9
<b>2353</b>	Pinal	Arizona	04	021	04021	4	21
<b>2499</b>	Pima	Arizona	04	019	04019	4	19
<b>2514</b>	Cochise	Arizona	04	003	04003	4	3
<b>2615</b>	Santa Cruz	Arizona	04	023	04023	4	23
<b>3080</b>	La Paz	Arizona	04	012	04012	4	12

14 rows × 70 columns

We might need this behind the scenes knowledge when we want to chain together conditions, or when we need to do spatial queries.

This is because spatial queries are somewhat more complex. Let's say, for example, we want all of the counties in the US to the West of -121 longitude. We need a way to express that question. Ideally, we want something like:

```
SELECT
  *
FROM
  data_table
WHERE
  x_centroid < -121
```

So, let's refer to an arbitrary polygon in the the dataframe's geometry column as `poly`. The centroid of a PySAL polygon is stored as an `(x,Y)` pair, so the longitude is the first element of the pair, `poly.centroid[0]`.

Then, applying this condition to each geometry, we get the same kind of filter we used above to grab only counties in Arizona:

```
data_table.geometry.apply(lambda x: x.centroid[0] < -121)
```

```

0    False
1    False
2    False
3    False
4    False
5    False
6    False
7    False
8    False
9    False
10   False
11   False
12   False
13   False
14   False
15   False
16   False
17   False
18   False
19   False
20   False
21   False
22   False
23   False
24   False
25   False
26   False
27   True
28   False
29   False
...
3055  False
3056  False
3057  False
3058  False
3059  False
3060  False
3061  False
3062  False
3063  False
3064  False
3065  False
3066  False
3067  False
3068  False
3069  False
3070  False
3071  False
3072  False
3073  False
3074  False
3075  False
3076  False
3077  False
3078  False
3079  False
3080  False
3081  False
3082  False
3083  False
3084  False
Name: geometry, dtype: bool

```

If we use this as a filter on the table, we can get only the rows that match that condition, just like we did for the `STATE_NAME` query:

```
data_table[data_table.geometry.apply(lambda x: x.centroid[0] < -121)]
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	C
<b>27</b>	Whatcom	Washington	53	073	53073	53	7
<b>31</b>	Skagit	Washington	53	057	53057	53	5
<b>44</b>	Clallam	Washington	53	009	53009	53	9
<b>47</b>	Snohomish	Washington	53	061	53061	53	6
<b>48</b>	Island	Washington	53	029	53029	53	2
<b>57</b>	Jefferson	Washington	53	031	53031	53	3
<b>71</b>	Kitsap	Washington	53	035	53035	53	5
<b>80</b>	King	Washington	53	033	53033	53	3
<b>85</b>	Mason	Washington	53	045	53045	53	4
<b>92</b>	Grays Harbor	Washington	53	027	53027	53	2
<b>107</b>	Pierce	Washington	53	053	53053	53	5
<b>116</b>	Thurston	Washington	53	067	53067	53	6
<b>130</b>	Pacific	Washington	53	049	53049	53	4
<b>131</b>	Lewis	Washington	53	041	53041	53	4
<b>169</b>	Skamania	Washington	53	059	53059	53	5
<b>170</b>	Cowlitz	Washington	53	015	53015	53	1
<b>171</b>	Wahkiakum	Washington	53	069	53069	53	6
<b>181</b>	Clatsop	Oregon	41	007	41007	41	7
<b>183</b>	Columbia	Oregon	41	009	41009	41	9
<b>193</b>	Clark	Washington	53	011	53011	53	1
<b>216</b>	Tillamook	Oregon	41	057	41057	41	5
<b>217</b>	Washington	Oregon	41	067	41067	41	6
<b>224</b>	Multnomah	Oregon	41	051	41051	41	5
<b>225</b>	Hood River	Oregon	41	027	41027	41	2

226	Wasco	Oregon	41	065	41065	41	€
240	Clackamas	Oregon	41	005	41005	41	£
242	Yamhill	Oregon	41	071	41071	41	£
253	Marion	Oregon	41	047	41047	41	£
269	Polk	Oregon	41	053	41053	41	£
272	Lincoln	Oregon	41	041	41041	41	£
...	...	...	...	...	...	...	.
493	Curry	Oregon	41	015	41015	41	£
517	Josephine	Oregon	41	033	41033	41	£
594	Siskiyou	California	06	093	06093	6	¤
601	Del Norte	California	06	015	06015	6	£
687	Humboldt	California	06	023	06023	6	£
709	Trinity	California	06	105	06105	6	£
735	Shasta	California	06	089	06089	6	£
907	Tehama	California	06	103	06103	6	£
974	Butte	California	06	007	06007	6	£
1005	Mendocino	California	06	045	06045	6	£
1047	Glenn	California	06	021	06021	6	£
1090	Yuba	California	06	115	06115	6	£
1101	Lake	California	06	033	06033	6	£
1141	Colusa	California	06	011	06011	6	£
1172	Sutter	California	06	101	06101	6	£
1262	Yolo	California	06	113	06113	6	£
1281	Napa	California	06	055	06055	6	£
1282	Sonoma	California	06	097	06097	6	¤

<b>1301</b>	Sacramento	California	06	067	06067	6	€
<b>1401</b>	Marin	California	06	041	06041	6	€
<b>1404</b>	San Joaquin	California	06	077	06077	6	€
<b>1447</b>	Solano	California	06	095	06095	6	€
<b>1462</b>	Contra Costa	California	06	013	06013	6	€
<b>1514</b>	Alameda	California	06	001	06001	6	€
<b>1530</b>	San Francisco	California	06	075	06075	6	€
<b>1559</b>	San Mateo	California	06	081	06081	6	€
<b>1609</b>	Santa Clara	California	06	085	06085	6	€
<b>1664</b>	Santa Cruz	California	06	087	06087	6	€
<b>1731</b>	San Benito	California	06	069	06069	6	€
<b>1745</b>	Monterey	California	06	053	06053	6	€

69 rows × 70 columns

This works on any type of spatial query.

For instance, if we wanted to find all of the counties that are within a threshold distance from an observation's centroid, we can do it in the following way.

First, specify the observation. Here, we'll use Cook County, IL:

```
data_table.query('(NAME == "Cook") & (STATE_NAME == "Illinois")')
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	COFI
<b>3044</b>	Cook	Illinois	17	031	17031	17	31

1 rows × 70 columns

```
geom = data_table.query('(NAME == "Cook") & (STATE_NAME == "Illinois")).geometry
```

```
geom.values[0].centroid
```

```
(-87.82107391263027, 41.84346628270174)
```

```
cook_county_centroid = geom.values[0].centroid
```

```
import scipy.spatial.distance as d
def near_target_point(polygon, target=cook_county_centroid, threshold=1):
    return d.euclidean(polygon.centroid, target) < threshold
```

```
data_table[data_table.geometry.apply(near_target_point)]
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	CO
<b>631</b>	Will	Illinois	17	197	17197	17	197
<b>633</b>	Kendall	Illinois	17	093	17093	17	93
<b>634</b>	Lake	Indiana	18	089	18089	18	89
<b>635</b>	Porter	Indiana	18	127	18127	18	127
<b>686</b>	Grundy	Illinois	17	063	17063	17	63
<b>718</b>	Kankakee	Illinois	17	091	17091	17	91
<b>731</b>	Newton	Indiana	18	111	18111	18	111
<b>3010</b>	Racine	Wisconsin	55	101	55101	55	101
<b>3019</b>	Kenosha	Wisconsin	55	059	55059	55	59
<b>3028</b>	McHenry	Illinois	17	111	17111	17	111
<b>3030</b>	Lake	Illinois	17	097	17097	17	97
<b>3044</b>	Cook	Illinois	17	031	17031	17	31
<b>3045</b>	Kane	Illinois	17	089	17089	17	89
<b>3046</b>	De Kalb	Illinois	17	037	17037	17	37
<b>3059</b>	Du Page	Illinois	17	043	17043	17	43

15 rows × 70 columns

## Moving in and out of the dataframe

Most things in PySAL will be explicit about what type their input should be. Most of the time, PySAL functions require either lists or arrays. This is why the file-handler methods are the default IO method in PySAL: the rest of the computational tools are built around their datatypes.

However, it is very easy to get the correct datatype from Pandas using the `values` and `tolist` commands.

`tolist()` will convert its entries to a list. But, it can only be called on individual columns (called `Series` in pandas documentation)

So, to turn the `NAME` column into a list:

```
data_table.NAME.tolist()
```

```
[u'Lake of the Woods',
 u'Ferry',
 u'Stevens',
 u'Okanogan',
 u'Pend Oreille',
 u'Boundary',
 u'Lincoln',
 u'Flathead',
 u'Glacier',
 u'Toole',
 u'Liberty',
 u'Hill',
 u'Sheridan',
 u'Divide',
 u'Burke',
 u'Renville',
 u'Bottineau',
 u'Rolette',
 u'Towner',
 u'Cavalier',
 u'Pembina',
 u'Kittson',
 u'Roseau',
 u'Blaine',
 u'Phillips',
 u'Valley',
 u'Daniels',
 u'Whatcom',
 u'Bonner',
 u'Ward',
 u'Koochiching',
 u'Skagit',
 u'Williams',
 u'McHenry',
 u'St. Louis',
 u'Roosevelt',
 u'Mountrial',
 u'Marshall',
 u'Ramsey',
 u'Walsh',
 u'Beltrami',
 u'Pierce',
 u'Chelan',
 u'Pondera',
 u'Clallam',
 u'Benson',
 u'Chouteau',
 u'Snohomish',
 u'Island',
 u'Sanders',
 u'Lake',
 u'Nelson',
 u'Grand Forks',
 u'Polk',
 u'Pennington',
 u'Douglas',
 u'McKenzie',
 u'Jefferson',
 u'Richland',
 u'Teton',
 u'McCone',
 u'Shoshone',
 u'Spokane',
 u'Lake',
 u'Clearwater',
 u'Kootenai',
 u'Garfield',
 u'Red Lake',
```

```
u'Grant',
u'Lincoln',
u'Lewis and Clark',
u'Kitsap',
u'Itasca',
u'Sheridan',
u'Wells',
u'McLean',
u'Eddy',
u'Dunn',
u'Fergus',
u'Dawson',
u'King',
u'Cascade',
u'Griggs',
u'Steele',
u'Traill',
u'Mason',
u'Missoula',
u'Petroleum',
u'Powell',
u'Kittitas',
u'Foster',
u'Mercer',
u'Grays Harbor',
u'Norman',
u'Mahnomen',
u'Mineral',
u'Cass',
u'Aroostook',
u'Judith Basin',
u'Hubbard',
u'Benewah',
u'Wibaux',
u'Golden Valley',
u'Billings',
u'Stutsman',
u'Kidder',
u'Burleigh',
u'Pierce',
u'Oliver',
u'Adams',
u'Whitman',
u'Barnes',
u'Cass',
u'Prairie',
u'Becker',
u'Clay',
u'Thurston',
u'Latah',
u'Meagher',
u'Yakima',
u'Aitkin',
u'Stark',
u'Morton',
u'Bayfield',
u'Clearwater',
u'Custer',
u'Rosebud',
u'Granite',
u'Wadena',
u'Crow Wing',
u'Pacific',
u'Lewis',
u'Broadwater',
u'Carlton',
u'Golden Valley',
u'Douglas',
u'Musselshell',
u'Wheatland',
u'Franklin',
u'Benton',
```

```
u'Grant',
u'Otter Tail',
u'Garfield',
u'Fallon',
u'Idaho',
u'Ravalli',
u'Ashland',
u'Logan',
u'Emmons',
u'La Moure',
u'Slope',
u'Hettinger',
u'Ransom',
u'Richland',
u'Wilkin',
u'Nez Perce',
u'Columbia',
u'Walla Walla',
u'Iron',
u'Somerset',
u'Piscataquis',
u'Jefferson',
u'Yellowstone',
u'Treasure',
u'Lewis',
u'Asotin',
u'Sioux',
u'Pine',
u'Penobscot',
u'Skamania',
u'Cowlitz',
u'Wahkiakum',
u'Todd',
u'Morrison',
u'McIntosh',
u'Dickey',
u'Sargent',
u'Bowman',
u'Adams',
u'Deer Lodge',
u'Mille Lacs',
u'Clatsop',
u'Sweet Grass',
u'Columbia',
u'Silver Bow',
u'Washburn',
u'Sawyer',
u'Burnett',
u'Kanabec',
u'Carter',
u'Stillwater',
u'Grant',
u'Douglas',
u'Clark',
u'Klickitat',
u'Big Horn',
u'Traverse',
u'Umatilla',
u'Wallowa',
u'Price',
u'Campbell',
u'Harding',
u'McPherson',
u'Perkins',
u'Corson',
u'Brown',
u'Beaverhead',
u'Marshall',
u'Roberts',
u'Morrow',
u'Union',
u'Madison',
```

```
u'Benton',
u'Gilliam',
u'Powder River',
u'Stearns',
u'Tillamook',
u'Washington',
u'Pope',
u'Stevens',
u'Isanti',
u'Chisago',
u'Sherman',
u'Polk',
u'Multnomah',
u'Hood River',
u'Wasco',
u'Lemhi',
u'Washington',
u'Franklin',
u'Barron',
u'Rusk',
u'Carbon',
u'Walworth',
u'Edmunds',
u'Day',
u'Big Stone',
u'Sherburne',
u'Ziebach',
u'Dewey',
u'Clackamas',
u'Wright',
u'Yamhill',
u'Anoka',
u'Kandiyohi',
u'Swift',
u'Taylor',
u'Oxford',
u'Grant',
u'Meeker',
u'Coos',
u'Washington',
u'Chippewa',
u'Marion',
u'Lac Qui Parle',
u'Adams',
u'Potter',
u'Faulk',
u'Hennepin',
u'Spink',
u'St. Croix',
u'Dunn',
u'Butte',
u'Valley',
u'Clark',
u'Codington',
u'Chippewa',
u'Ramsey',
u'Baker',
u'Polk',
u'Wheeler',
u'Meade',
u'Lincoln',
u'Clark',
u'Essex',
u'Grand Isle',
u'Franklin',
u'Orleans',
u'Clinton',
u'Park',
u'Crook',
u'Big Horn',
u'Campbell',
u'Sheridan',
```

```
u'Franklin',
u'Grant',
u'McLeod',
u'Carver',
u'Deuel',
u'Dakota',
u'Yellow Medicine',
u'Sully',
u'Hyde',
u'Hand',
u'Renville',
u'Pierce',
u'Custer',
u'Eau Claire',
u'Washington',
u'Jefferson',
u'Scott',
u'Hamlin',
u'Lamoille',
u'Linn',
u'Stanley',
u'Caledonia',
u'Waldo',
u'Haakon',
u'Fremont',
u'Sibley',
u'Chittenden',
u'Kennebec',
u'Goodhue',
u'Benton',
u'Redwood',
u'Wood',
u'Pepin',
u'Teton',
u'Beadle',
u'Lyon',
u'Lincoln',
u'Lawrence',
u'Buffalo',
u'Trempealeau',
u'Jackson',
u'Clark',
u'Crook',
u'Johnson',
u'Hughes',
u'Essex',
u'Le Sueur',
u'Rice',
u'Kingsbury',
u'Brookings',
u'Pennington',
u'Gem',
u'Brown',
u'Washington',
u'Androscoggin',
u'Nicollet',
u'Wabasha',
u'Malheur',
u'Hancock',
u'Grafton',
u'Deschutes',
u'Knox',
u'Boise',
u'Lincoln',
u'Addison',
u'Carroll',
u'Lane',
u'Blue Earth',
u'Juneau',
u'Butte',
u'Lyman',
u'Orange',
```

```
u'Waseca',
u'Buffalo',
u'Jerauld',
u'Moody',
u'Pipestone',
u'Dodge',
u'Sanborn',
u'Murray',
u'Cottonwood',
u'Steele',
u'Olmsted',
u'Miner',
u'Lake',
u'Winona',
u'Weston',
u'Jones',
u'Cumberland',
u'Washakie',
u'Monroe',
u'Payette',
u'Hamilton',
u'Watowwan',
u'Herkimer',
u'La Crosse',
u'Elmore',
u'Hot Springs',
u'Jefferson',
u'Harney',
u'Sagadahoc',
u'Fremont',
u'Jackson',
u'Blaine',
u'Teton',
u'Windsor',
u'Douglas',
u'Aurora',
u'Brule',
u'Madison',
u'Canyon',
u'Mellette',
u'Camas',
u'Custer',
u'Rutland',
u'Faribault',
u'Minnehaha',
u'Rock',
u'Freeborn',
u'Nobles',
u'Jackson',
u'Martin',
u'Houston',
u'Mower',
u'Fillmore',
u'Davison',
u'Hanson',
u'McCook',
u'York',
u'Washington',
u'Ada',
u'Warren',
u'Tripp',
u'Belknap',
u'Vernon',
u'Shannon',
u'Owyhee',
u'Bonneville',
u'Bingham',
u'Klamath',
u'Lake',
u'Coos',
u'Merrimack',
u'Sullivan',
```

```
u'Strafford',
u'Richland',
u'Natrona',
u'Gregory',
u'Niobrara',
u'Charles Mix',
u'Turner',
u'Lincoln',
u'Worth',
u'Mitchell',
u'Allamakee',
u'Winnebago',
u'Winneshiek',
u'Converse',
u'Osceola',
u'Dickinson',
u'Kossuth',
u'Howard',
u'Emmet',
u'Lyon',
u'Douglas',
u'Hutchinson',
u'Fall River',
u'Sublette',
u'Crawford',
u'Saratoga',
u'Bennett',
u'Todd',
u'Bennington',
u'Lincoln',
u'Fulton',
u'Rockingham',
u'Sioux',
u'Windham',
u"O'Brien",
u'Cerro Gordo',
u'Clay',
u'Hancock',
u'Palo Alto',
u'Floyd',
u'Chickasaw',
u'Iowa',
u'Grant',
u'Hillsborough',
u'Lincoln',
u'Gooding',
u'Minidoka',
u'Cheshire',
u'Yankton',
u'Bon Homme',
u'Power',
u'Union',
u'Clay',
u'Fayette',
u'Clayton',
u'Montgomery',
u'Caribou',
u'Bannock',
u'Sioux',
u'Dawes',
u'Sheridan',
u'Jackson',
u'Keya Paha',
u'Boyd',
u'Cherry',
u'Curry',
u'Rensselaer',
u'Schenectady',
u'Plymouth',
u'Cherokee',
u'Bremer',
u'Butler',
```

```
u'Buena Vista',
u'Twin Falls',
u'Pocahontas',
u'Humboldt',
u'Wright',
u'Franklin',
u'Otsego',
u'Holt',
u'Essex',
u'Knox',
u'Cedar',
u'Jerome',
u'Schoharie',
u'Brown',
u'Lafayette',
u'Albany',
u'Rock',
u'Josephine',
u'Dixon',
u'Berkshire',
u'Franklin',
u'Middlesex',
u'Worcester',
u'Dubuque',
u'Cassia',
u'Webster',
u'Delaware',
u'Buchanan',
u'Black Hawk',
u'Goshen',
u'Platte',
u'Bear Lake',
u'Woodbury',
u'Ida',
u'Sac',
u'Calhoun',
u'Hamilton',
u'Hampshire',
u'Hardin',
u'Grundy',
u'Dakota',
u'Delaware',
u'Jo Daviess',
u'Columbia',
u'Oneida',
u'Greene',
u'Suffolk',
u'Carbon',
u'Pierce',
u'Box Butte',
u'Antelope',
u'Albany',
u'Franklin',
u'Jackson',
u'Wayne',
u'Hampden',
u'Jones',
u'Benton',
u'Linn',
u'Tama',
u'Thurston',
u'Sweetwater',
u'Plymouth',
u'Norfolk',
u'Monona',
u'Crawford',
u'Carroll',
u'Greene',
u'Boone',
u'Marshall',
u'Story',
u'Ulster',
```

```
u'Cuming',
u'Bristol',
u'Stanton',
u'Madison',
u'Grant',
u'Loup',
u'Hooker',
u'Garfield',
u'Thomas',
u'Wheeler',
u'Blaine',
u'Dutchess',
u'Barnstable',
u'Burt',
u'Litchfield',
u'Hartford',
u'Clinton',
u'Tolland',
u'Windham',
u'Sullivan',
u'Providence',
u'Cache',
u'Siskiyou',
u'Garden',
u'Box Elder',
u'Rich',
u'Scotts Bluff',
u'Morrill',
u'Wayne',
u'Del Norte',
u'Humboldt',
u'Elko',
u'Modoc',
u'Washoe',
u'Cedar',
u'Boone',
u'Jasper',
u'Polk',
u'Poweshiek',
u'Harrison',
u'Guthrie',
u'Shelby',
u'Audubon',
u'Iowa',
u'Dallas',
u'Johnson',
u'Rock Island',
u'Scott',
u'Bristol',
u'Kent',
u'Colfax',
u'Dodge',
u'Platte',
u'Arthur',
u'Greeley',
u'McPherson',
u'Logan',
u'Custer',
u'Valley',
u'Will',
u'Lucas',
u'Kendall',
u'Lake',
u'Porter',
u'Fulton',
u'Geauga',
u'New London',
u'Williams',
u'Banner',
u'Washington',
u'Newport',
u'Fairfield',
```

```
u'Laramie',
u'Wyoming',
u'Washington',
u'Middlesex',
u'New Haven',
u'Lackawanna',
u'La Salle',
u'Orange',
u'Elk',
u'Cuyahoga',
u'Venango',
u'Forest',
u'Ottawa',
u'Cameron',
u'Wood',
u'Pike',
u'Lycoming',
u'Muscatine',
u'Sullivan',
u'Bureau',
u'Henry',
u'Uinta',
u'Noble',
u'De Kalb',
u'Putnam',
u'Nance',
u'Lorain',
u'Mahaska',
u'Pottawattamie',
u'Washington',
u'Marion',
u'Madison',
u'Warren',
u'Keokuk',
u'Cass',
u'Adair',
u'Sandusky',
u'Trumbull',
u'Mercer',
u'Marshall',
u'Henry',
u'Clinton',
u'Grundy',
u'Humboldt',
u'Butler',
u'Saunders',
u'Erie',
u'Kosciusko',
u'Starke',
u'Clarion',
u'Cheyenne',
u'Defiance',
u'Weber',
u'Louisa',
u'Luzerne',
u'Polk',
u'Douglas',
u'Sherman',
u'Howard',
u'Lincoln',
u'Merrick',
u'Keith',
u'Kimball',
u'Jefferson',
u'Morgan',
u'Trinity',
u'Westchester',
u'Sussex',
u'Summit',
u'Portage',
u'Mercer',
u'Rockland',
```

```
u'Putnam',
u'Columbia',
u'Kankakee',
u'Whitley',
u'Jasper',
u'Huron',
u'Allen',
u'Medina',
u'Summit',
u'Centre',
u'Clearfield',
u'Monroe',
u'Seneca',
u'Paulding',
u'Stark',
u'Newton',
u'Deuel',
u'Passaic',
u'Sarpy',
u'Shasta',
u'Lassen',
u'Northumberland',
u'Fulton',
u'Butler',
u'Armstrong',
u'Pulaski',
u'Montour',
u'Hancock',
u'Mills',
u'Putnam',
u'Montgomery',
u'Adams',
u'Clarke',
u'Wapello',
u'Jefferson',
u'Union',
u'Henry',
u'Hamilton',
u'Lucas',
u'Monroe',
u'Davis',
u'Knox',
u'Marshall',
u'Union',
u'Carbon',
u'Mahoning',
u'Lawrence',
u'Bergen',
u'Livingston',
u'Warren',
u'Tooele',
u'Morris',
u'Des Moines',
u'Henderson',
u'Warren',
u'Cass',
u'Ashland',
u'Wabash',
u'Seward',
u'Lancaster',
u'Buffalo',
u'Dawson',
u'York',
u'Hall',
u'Huntington',
u'Iroquois',
u'Miami',
u'Ford',
u'Moffat',
u'Weld',
u'Jackson',
u'Perkins',
```

```
u'Logan',
u'Sedgwick',
u'Routt',
u'Larimer',
u'Daggett',
u'Crawford',
u'Lander',
u'Eureka',
u'Richland',
u'Wayne',
u'Van Wert',
u'Wyandot',
u'Stark',
u'Peoria',
u'Northampton',
u'Pershing',
u'Schuylkill',
u'Adams',
u'Wells',
u'Woodford',
u'Columbiana',
u'Cass',
u'White',
u'Salt Lake',
u'Allen',
u'Indiana',
u'Fremont',
u'Page',
u'Taylor',
u'Ringgold',
u'Nassau',
u'Davis',
u'Van Buren',
u'Decatur',
u'Wayne',
u'Essex',
u'Appanoose',
u'Snyder',
u'Uintah',
u'Beaver',
u'Mifflin',
u'Duchesne',
u'Hudson',
u'Lee',
u'Hardin',
u'Otoe',
u'Lehigh',
u'Hunterdon',
u'Suffolk',
u'McLean',
u'Somerset',
u'Carroll',
u'Tazewell',
u'Blair',
u'Benton',
u'Phillips',
u'Huntingdon',
u'Cambria',
u'Union',
u'Mercer',
u'Carroll',
u'Fulton',
u'Morrow',
u'Marion',
u'Saline',
u'Adams',
u'Clay',
u'Fillmore',
u'Juniata',
u'Hayes',
u'Chase',
u'Frontier',
```

```
u'Gosper',
u'Auglaize',
u'Kearney',
u'Wasatch',
u'Phelps',
u'Berks',
u'Westmoreland',
u'Allegheny',
u'Grant',
u'Holmes',
u'Dauphin',
u'Tuscarawas',
u'Hancock',
u'McDonough',
u'Perry',
u'Hancock',
u'Bucks',
u'Clark',
u'Scotland',
u'Schuylerville',
u'Middlesex',
u'Jefferson',
u'Blackford',
u'Putnam',
u'Atchison',
u'Jay',
u'Utah',
u'Nodaway',
u'Mercer',
u'Howard',
u'Harrison',
u'Tippecanoe',
u'Worth',
u'Knox',
u'Nemaha',
u'Lebanon',
u'Logan',
u'Gage',
u'Johnson',
u'Morgan',
u'Union',
u'Vermilion',
u'Warren',
u'Shelby',
u'Washington',
u'Grand',
u'Coshocoton',
u'Tehama',
u'Monmouth',
u'Plumas',
u'Delaware',
u'Montgomery',
u'Mason',
u'Clinton',
u'Yuma',
u'Washington',
u'Harrison',
u'Mercer',
u'Tipton',
u'Champaign',
u'Brooke',
u'Madison',
u'Delaware',
u'Gentry',
u'Sullivan',
u'Fountain',
u'Darke',
u'Thayer',
u'Jefferson',
u'Adair',
u'Dundy',
u'Franklin',
```

```
u'Webster',
u'Nuckolls',
u'Hitchcock',
u'Harlan',
u'Furnas',
u'Red Willow',
u'Logan',
u'Bedford',
u'Cumberland',
u'Randolph',
u'Lancaster',
u'Knox',
u'Franklin',
u'Piatt',
u'De Witt',
u'Somerset',
u'Schuylerville',
u'Licking',
u'Champaign',
u'Holt',
u'Richardson',
u'Pawnee',
u'Grundy',
u'Boulder',
u'Lewis',
u'Chester',
u'Hamilton',
u'York',
u'Montgomery',
u'Rio Blanco',
u'Guernsey',
u'Adams',
u'Miami',
u'Ohio',
u'Boone',
u'Burlington',
u'Vermillion',
u'Menard',
u'Belmont',
u'Ocean',
u'Fulton',
u'Muskingum',
u'Butte',
u'Daviess',
u'Franklin',
u'Fayette',
u'Philadelphia',
u'Andrew',
u'Cass',
u'White Pine',
u'Madison',
u'Brown',
u'Garfield',
u'Henry',
u'Adams',
u'Delaware',
u'Macon',
u'De Kalb',
u'Macon',
u'Clark',
u'Linn',
u'Marshall',
u'Greene',
u'Wayne',
u'Juab',
u'Churchill',
u'Norton',
u'Phillips',
...]
```

To extract many columns, you must select the columns you want and call their `.values` attribute.

If we were interested in grabbing all of the `HR` variables in the dataframe, we could first select those column names:

```
HRs = [col for col in data_table.columns if col.startswith('HR')]
```

We can use this to focus only on the columns we want:

```
data_table[HRs]
```

	<b>HR60</b>	<b>HR70</b>	<b>HR80</b>	<b>HR90</b>
<b>0</b>	0.000000	0.000000	8.855827	0.000000
<b>1</b>	0.000000	0.000000	17.208742	15.885624
<b>2</b>	1.863863	1.915158	3.450775	6.462453
<b>3</b>	2.612330	1.288643	3.263814	6.996502
<b>4</b>	0.000000	0.000000	7.770008	7.478033
<b>5</b>	0.000000	0.000000	4.573101	4.000640
<b>6</b>	7.976390	5.536179	5.633168	5.720497
<b>7</b>	1.011173	1.689475	4.490115	2.814460
<b>8</b>	11.529039	9.273857	28.227324	5.500096
<b>9</b>	0.000000	5.708740	0.000000	6.605892
<b>10</b>	0.000000	0.000000	0.000000	0.000000
<b>11</b>	3.574045	3.840688	7.413585	1.888146
<b>12</b>	0.000000	0.000000	0.000000	0.000000
<b>13</b>	0.000000	0.000000	0.000000	0.000000
<b>14</b>	0.000000	0.000000	0.000000	0.000000
<b>15</b>	0.000000	0.000000	0.000000	0.000000
<b>16</b>	2.945942	0.000000	0.000000	0.000000
<b>17</b>	0.000000	0.000000	19.161808	5.219752
<b>18</b>	0.000000	0.000000	0.000000	0.000000
<b>19</b>	0.000000	8.117213	0.000000	0.000000
<b>20</b>	0.000000	0.000000	0.000000	0.000000
<b>21</b>	0.000000	4.864050	0.000000	0.000000
<b>22</b>	0.000000	0.000000	0.000000	2.218377
<b>23</b>	4.119804	9.910312	14.287755	14.863258
<b>24</b>	5.530668	0.000000	12.421589	0.000000
<b>25</b>	5.854801	5.811757	6.504065	4.045798
<b>26</b>	0.000000	10.811980	0.000000	0.000000
<b>27</b>	1.422131	2.439530	4.061193	2.086920
<b>28</b>	2.138534	2.142245	5.518079	3.756292
<b>29</b>	0.708135	1.138434	0.570854	1.150993

...	...	...	...	...
<b>3055</b>	0.000000	0.000000	2.107526	0.739919
<b>3056</b>	0.000000	0.970572	4.400324	0.825491
<b>3057</b>	0.611430	2.568301	1.974919	2.828994
<b>3058</b>	2.022286	2.033140	0.000000	3.987956
<b>3059</b>	0.850723	1.981012	2.782690	2.260130
<b>3060</b>	1.790825	3.732470	5.757329	4.007173
<b>3061</b>	0.556604	1.060271	1.010560	2.769193
<b>3062</b>	0.000000	1.756836	5.505395	2.907653
<b>3063</b>	0.427592	3.688132	2.625587	0.000000
<b>3064</b>	0.896660	2.704530	4.229303	2.938915
<b>3065</b>	1.051403	5.379304	7.057466	3.424679
<b>3066</b>	2.095434	6.671377	9.243279	7.285916
<b>3067</b>	1.872835	3.951663	5.339935	3.201065
<b>3068</b>	1.917913	6.382639	1.304631	0.000000
<b>3069</b>	1.939789	4.960564	0.000000	6.072530
<b>3070</b>	5.452765	15.156192	24.841012	28.268787
<b>3071</b>	7.520089	9.163383	10.590286	6.443839
<b>3072</b>	7.202448	9.746302	11.850014	12.561604
<b>3073</b>	8.253379	15.655752	21.173432	16.479507
<b>3074</b>	2.181802	3.074760	3.191133	3.300700
<b>3075</b>	4.902862	11.782264	7.680787	18.362582
<b>3076</b>	18.513376	17.133324	15.034136	12.027015
<b>3077</b>	4.159907	4.126434	3.967782	6.585273
<b>3078</b>	5.403098	5.970974	4.127839	2.586787
<b>3079</b>	1.121183	1.096311	2.442074	2.806112
<b>3080</b>	5.046682	13.152054	13.251761	5.521552
<b>3081</b>	3.411368	7.393533	11.453817	8.691999
<b>3082</b>	1.544425	6.023552	5.280349	4.367330
<b>3083</b>	9.302820	1.800148	3.000030	3.727712
<b>3084</b>	3.396162	2.284879	1.194743	2.048855

3085 rows × 4 columns

With this, calling `.values` gives an array containing all of the entries in this subset of the table:

```
data_table[['HR90', 'HR80']].values
```

```
array([[ 0.      ,  8.85582713],
       [ 15.88562351, 17.20874204],
       [ 6.46245315,  3.4507747 ],
       ...,
       [ 4.36732988,  5.2803488 ],
       [ 3.72771194,  3.00003  ],
       [ 2.04885495,  1.19474313]])
```

Using the PySAL pdio tools means that if you're comfortable with working in Pandas, you can continue to do so.

If you're more comfortable using Numpy or raw Python to do your data processing, PySAL's IO tools naturally support this.

# Exploratory Geovisualization with PySAL

## Introduction

When PySAL was originally planned, the intention was to focus on the computational aspects of exploratory spatial data analysis and spatial econometric methods, while relying on existing GIS packages and visualization libraries for visualization of computations. Indeed, we have partnered with [esri](#) and [QGIS](#) towards this end.

However, over time we have received many requests for supporting basic geovisualization within PySAL so that the step of having to interoperate with an external package can be avoided, thereby increasing the efficiency of the spatial analytical workflow.

In this notebook, we demonstrate several approaches towards geovisualization within a self-contained exploratory workflow. The idea here is the support quick generation of different views of your data to complement the statistical and econometric work in PySAL. Once your work has progressed to the publication stage, we point you to resources that can be used for publication quality output.

## PySAL Viz Module

### Contributors:

- Dani Arribas-Bel [daniel.arribas.bel@gmail.com](mailto:daniel.arribas.bel@gmail.com)
- Serge Rey [sjsrey@gmail.com](mailto:sjsrey@gmail.com)

This document describes the main structure, components and usage of the mapping module in PySAL. The is organized around three main layers:

- A lower-level layer that reads polygon, line and point shapefiles and returns a Matplotlib collection.
- A medium-level layer that performs some usual transformations on a Matplotlib object (e.g. color code polygons according to a vector of values).
- A higher-level layer intended for end-users for particularly useful cases and style preferences pre-defined (e.g. Create a choropleth).

```
%matplotlib inline
import numpy as np
import pysal as ps
import random as rdm
from pysal.contrib.viz import mapping as maps

from pylab import *
```

## Lower-level component

This includes basic functionality to read spatial data from a file (currently only shapefiles supported) and produce rudimentary Matplotlib objects. The main methods are:

- `map_poly_shape`: to read in polygon shapefiles
- `map_line_shape`: to read in line shapefiles
- `map_point_shape`: to read in point shapefiles

These methods all support an option to subset the observations to be plotted (very useful when missing values are present). They can also be overlaid and combined by using the `setup_ax` function. the resulting object is very basic but also very flexible so, for minds used to matplotlib this should be good news as it

allows to modify pretty much any property and attribute.

## Example

```

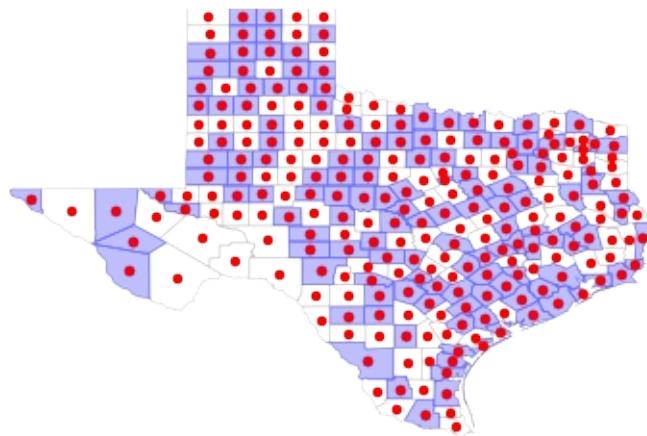
shp_link = './data/texas.shp'
shp = ps.open(shp_link)
some = [bool(rdm.getrandbits(1)) for i in ps.open(shp_link)]


fig = figure()

base = maps.map_poly_shp(shp)
base.set_facecolor('none')
base.set_linenwidth(0.75)
base.set_edgecolor('0.8')
some = maps.map_poly_shp(shp, which=some)
some.set_alpha(0.5)
some.set_linenwidth(0.)
cents = np.array([poly.centroid for poly in ps.open(shp_link)])
pts = scatter(cents[:, 0], cents[:, 1])
pts.set_color('red')

ax = maps.setup_ax([base, some, pts], [shp.bbox, shp.bbox, shp.bbox])
fig.add_axes(ax)
show()

```



## Medium-level component

This layer comprises functions that perform usual transformations on matplotlib objects, such as color coding objects (points, polygons, etc.) according to a series of values. This includes the following methods:

- base\_choropleth\_classless
- base\_choropleth\_unique

## Example

```

net_link = ps.examples.get_path('eberly_net.shp')
net = ps.open(net_link)
values = np.array(ps.open(net_link.replace('.shp', '.dbf')).by_col('TNODE'))

pts_link = ps.examples.get_path('eberly_net_pts_onnetwork.shp')
pts = ps.open(pts_link)

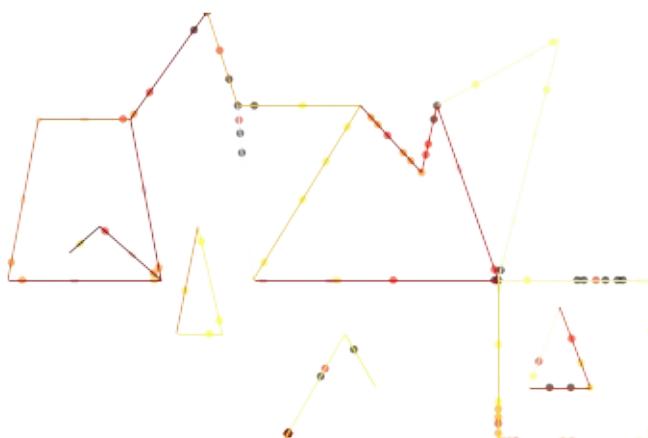
fig = figure()

netm = maps.map_line_shp(net)
netc = maps.base_choropleth_unique(netm, values)

ptsm = maps.map_point_shp(pts)
ptsm = maps.base_choropleth_classif(ptsm, values)
ptsm.set_alpha(0.5)
ptsm.set_linewidth(0.)

ax = maps.setup_ax([netc, ptsm], [net.bbox, net.bbox])
fig.add_axes(ax)
show()

```



```
maps.plot_poly_lines('../data/texas.shp')
```

```
calling plt.show()
```



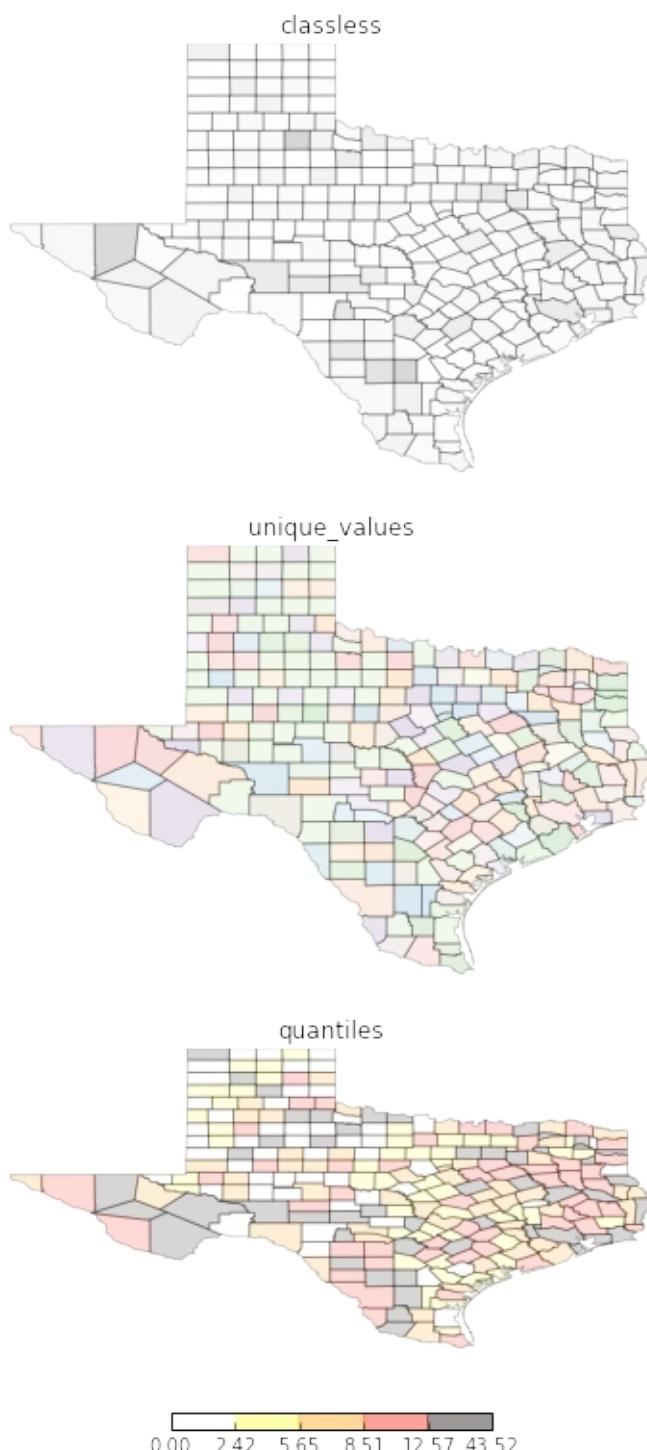
## Higher-level component

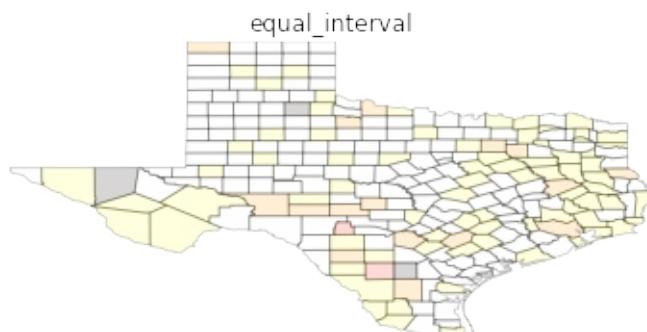
This currently includes the following end-user functions:

- `plot_poly_lines`: very quick shapfile plotting

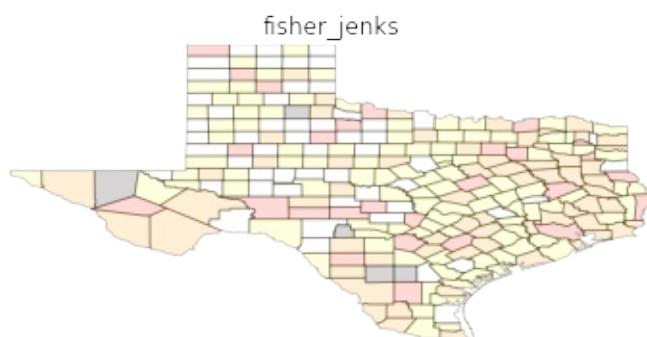
```
shp_link = './data/texas.shp'
values = np.array(ps.open('./data/texas.dbf').by_col('HR90'))

types = ['classless', 'unique_values', 'quantiles', 'equal_interval', 'fisher_jenks']
for typ in types:
    maps.plot_choropleth(shp_link, values, typ, title=typ)
```





0.00 8.70 17.41 26.11 34.81 43.52



0.00 3.16 8.85 15.88 27.64 43.52

## Folium

### Contributors:

- Levi Wolf [levi.john.wolf@gmail.com](mailto:levi.john.wolf@gmail.com)
- Serge Rey [sjsrey@gmail.com](mailto:sjsrey@gmail.com)

In addition to using matplotlib, the viz module includes components that interface with the [folium](#) library which provides a Pythonic way to generate [Leaflet](#) maps.

```
import pysal as ps
import geojson as gj
from pysal.contrib.viz import folium_mapping as fm
```

```
-----
ImportError           Traceback (most recent call last)
```

```
<ipython-input-6-677ccf6438e5> in <module>()
      1 import pysal as ps
----> 2 import geojson as gj
      3 from pysal.contrib.viz import folium_mapping as fm
```

```
ImportError: No module named geojson
```

First, we need to convert the data into a JSON format. JSON, short for "Javascript Serialized Object Notation," is a simple and effective way to represent objects in a digital environment. For geographic information, the [GeoJSON](#) standard defines how to represent geographic information in JSON format.

Python programmers may be more comfortable thinking of JSON data as something akin to a standard Python dictionary.

```
filepath = '../data/texas.shp'[:-4]
shp = ps.open(filepath + '.shp')
dbf = ps.open(filepath + '.dbf')
```

```
js = fm.build_features(shp, dbf)
```

Just to show, this constructs a dictionary with the following keys:

```
js.keys()
```

```
[u'type', 'bbox', 'features']
```

```
js.type
```

```
'FeatureCollection'
```

```
js.bbox
```

```
[-106.6495132446289, 25.845197677612305, -93.50721740722656, 36.49387741088867]
```

```
js.features[0]
```

```
{"bbox": [-100.5494155883789, 36.05754852294922, -99.99715423583984, 36.49387741088867], "geometry": {"coordinates": 686645507812, 36.49387741088867}, [-100.00114440917969, 36.49251937866211], [-99.99715423583984, 36.0575485229454059600830078, 36.058135986328125], [-100.5494155883789, 36.48944854736328], [-100.00686645507812, 36.49387741088867], "type": "Polygon"}, "properties": {"BLK60": 0.029359953, "BLK70": 0.0286861733, "BLK80": 0.0265533723, "BLK90": 0.031816, "TY_FIPS": "295", "COFIPS": 295, "DNL60": 1.293817423, "DNL70": 1.3170337879, "DNL80": 1.3953635084, "DNL90": 1.2153856, "DV70": 2.2709475333, "DV80": 3.5164835165, "DV90": 6.1016949153, "FH60": 6.7245119306, "FH70": 4.5, "353601497, "FH90": 6.0935799782, "FIPS": "48295", "FIPSNO": 48295, "FP59": 22.4, "FP69": 12.1, "FP79": 10.851262862, "FP89": 99674, "GI59": 0.2869290401, "GI69": 0.378218563, "GI79": 0.4070049836, "GI89": 0.3730049522, "HC60": 0.0, "HC70": 0.0, "HC90": 0.0, "HR60": 0.0, "HR70": 0.0, "HR80": 0.0, "HR90": 0.0, "MA60": 32.4, "MA70": 34.3, "MA80": 31.0, "MA90": 35.8, "MFIL59": 8.5318847402, "MFIL69": 8.9704320743, "MFIL79": 9.8020637224, "MFIL89": 10.252241206, "NAME": "Lipscomb", "PO60": 3406, "PO70": 3486, "PO80": 3766, "PO90": 3143, "POL60": 8.1332938612, "POL70": 8.1565102261, "POL80": 8.2337687092, "POL90": 8.0529330368, "PS60": -1.514026445, "PS70": -1.449058083, "PS80": -1.476411495, "PS90": -1.571799202, "RD60": -0.917851658, "RD70": -0.602337681, "RD80": -0.355503211, "RD90": -0.605606852, "SOUTH": 1, "STATE_FIPS": "48", "STATE_NAME": "Texas", "STFIPS": 48, "UE60": 2.0, "UE70": 1.9411764706, "UE90": 1.7328519856}, "type": "Feature"}
```



Then, we write the json to a file:

```
with open('./example.json', 'w') as out:
    gj.dump(js, out)
```

## Mapping

Let's look at the columns that we are going to map.

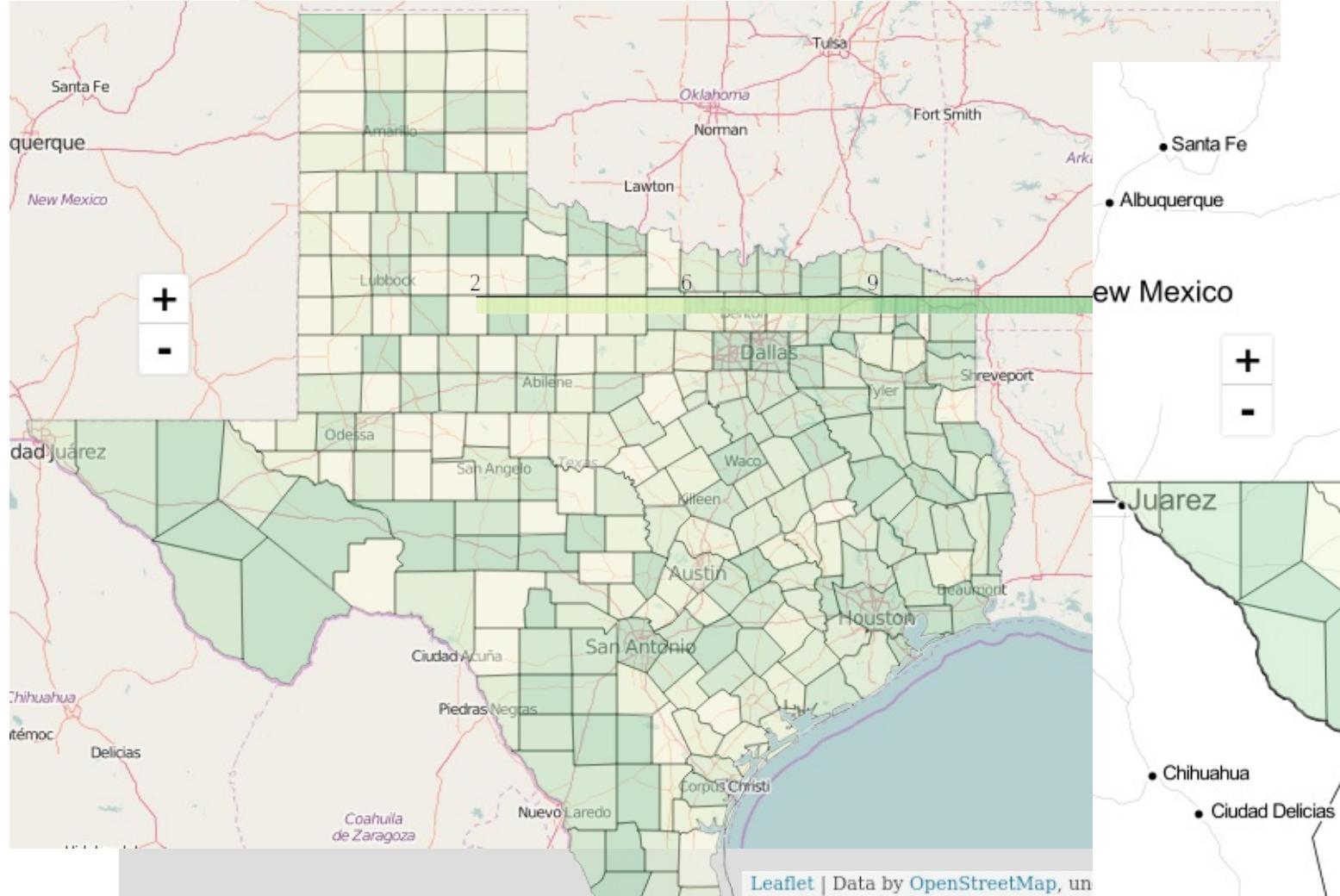
```
list(js.features[0].properties.keys())[5]
```

```
[u'HR90', u'PS90', u'FH80', u'HC60', u'FP79']
```

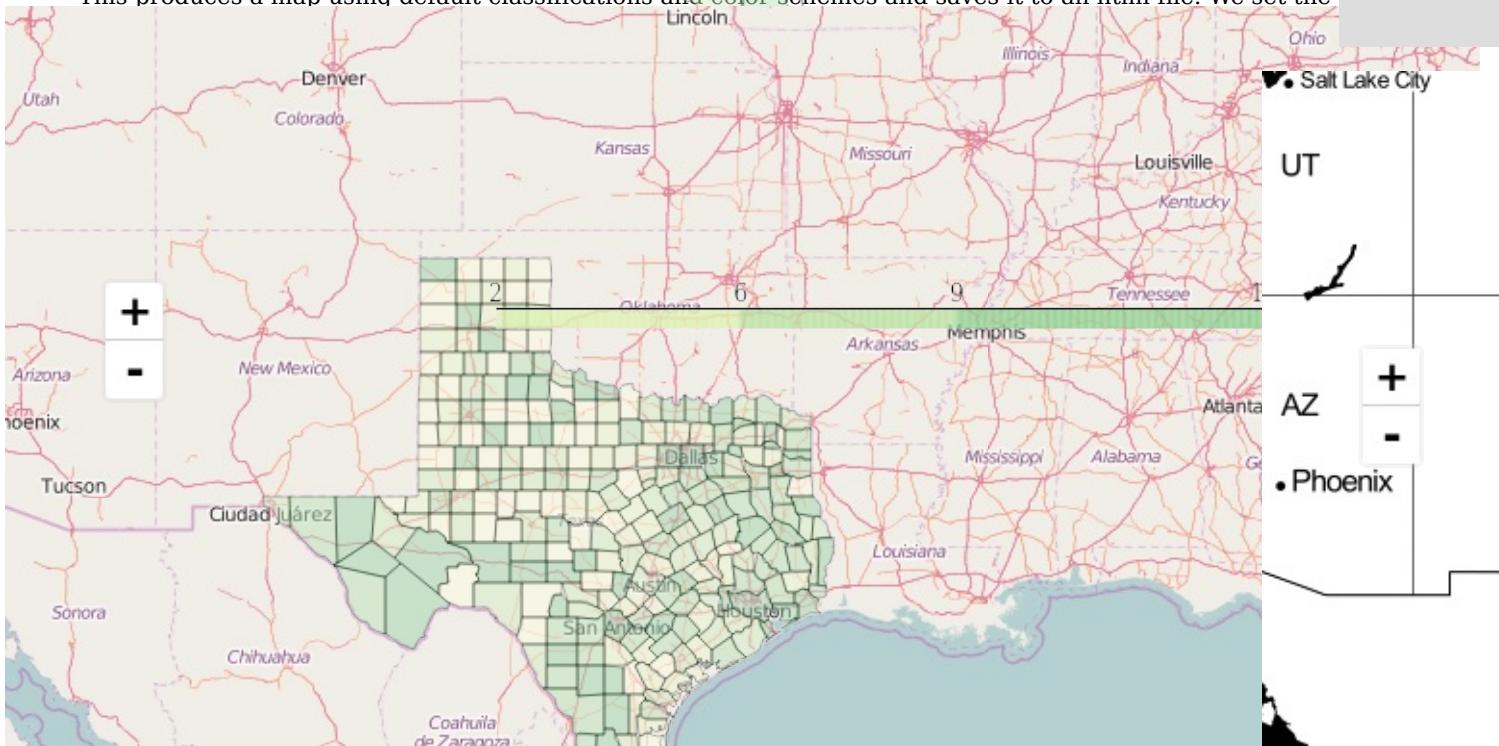
We can map these attributes by calling them as arguments to the choropleth mapping function:

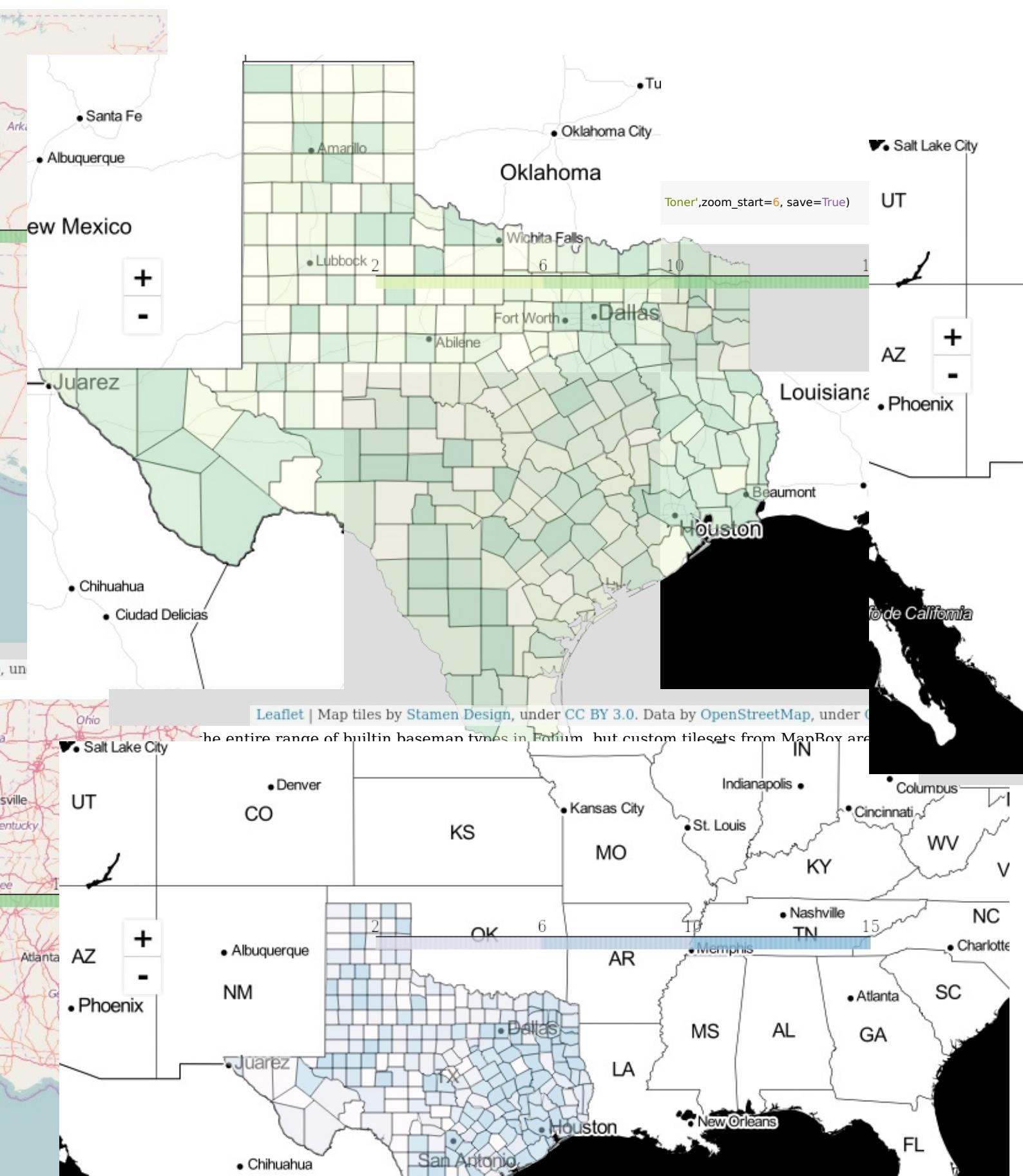
```
import folium as fol
```

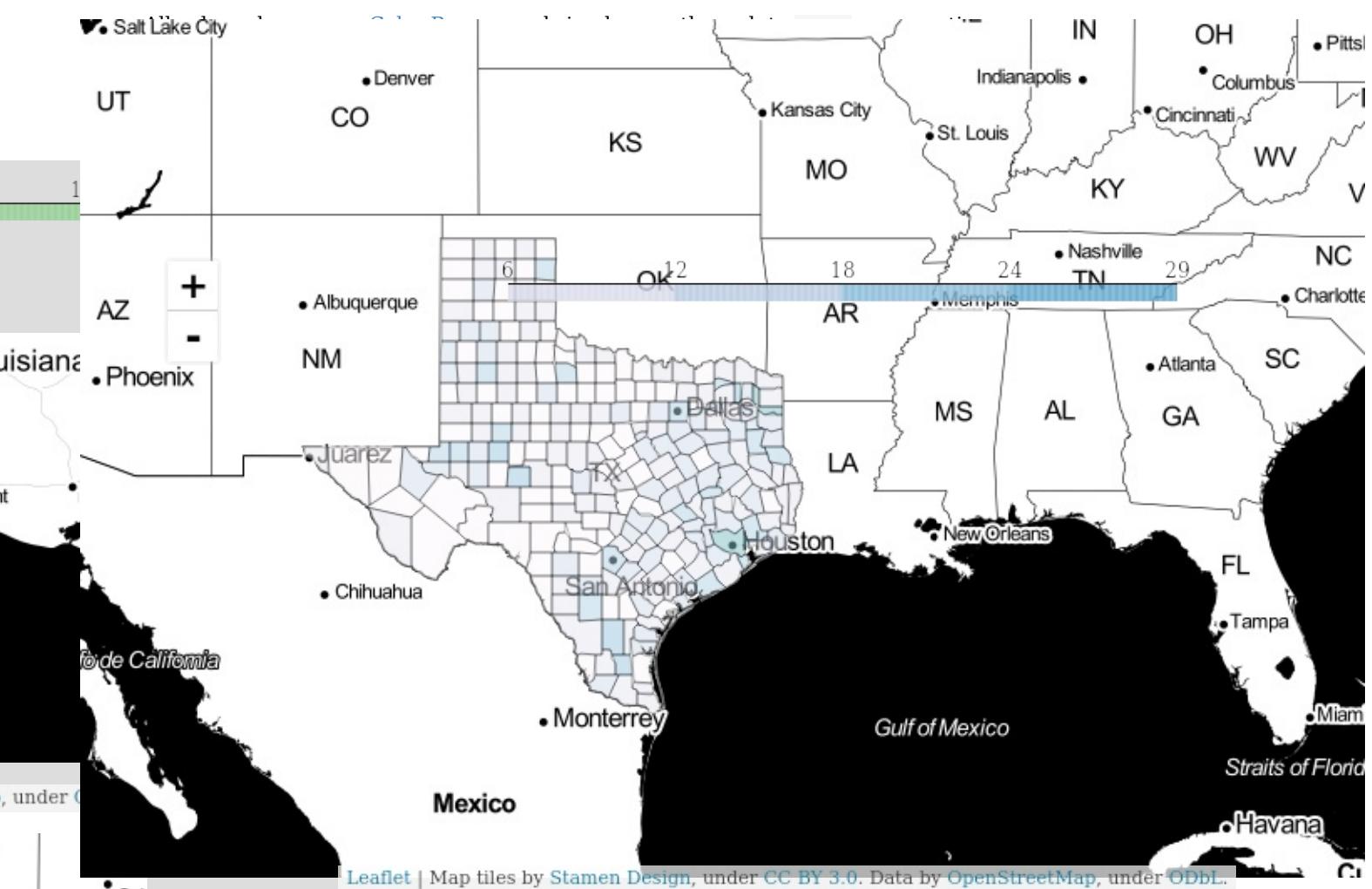
```
fm.choropleth_map?
```



This produces a map using default classifications and color schemes and saves it to an html file. We set the







Leaflet | Map tiles by Stamen Design, under CC BY 3.0. Data by OpenStreetMap, under ODbL.

We don't have time to go into the details here today, we note that for publication ready maps you can turn to Cartopy. For an example of a recent publication and code see Rey (2016).



# Spatial Weights

Spatial weights are mathematical structures used to represent spatial relationships. They characterize the relationship of each observation to every other observation using some concept of proximity or closeness that depends on the weight type.

They can be build in PySAL from shapefiles, as well as some types of files.

```
import pysal as ps
import numpy as np
```

There are functions to construct weights directly from a file path.

```
shp_path = "../data/texas.shp"
```

## Weight Types

### Contiguity:

#### Queen Weights

A commonly-used type of weight is a queen contiguity weight, which reflects adjacency relationships as a binary indicator variable denoting whether or not a polygon shares an edge or a vertex with another polygon. These weights are symmetric, in that when polygon \$A\$ neighbors polygon \$B\$, both  $w\{AB\} = 1$  and  $w\{BA\} = 1$ .

To construct queen weights from a shapefile, use the `queen_from_shapefile` function:

```
qW = ps.queen_from_shapefile(shp_path)
dataframe = ps.pdio.read_files(shp_path)
```

```
qW
```

```
<pysal.weights.weights.W at 0x7fac6769e590>
```

All weights objects have a few traits that you can use to work with the weights object, as well as to get information about the weights object.

To get the neighbors & weights around an observation, use the observation's index on the weights object, like a dictionary:

```
qW[4] #neighbors & weights of the 5th observation
```

```
{0: 1.0, 3: 1.0, 5: 1.0, 6: 1.0, 7: 1.0}
```

By default, the weights and the pandas dataframe will use the same index. So, we can view the observation and its neighbors in the dataframe by putting the observation's index and its neighbors' indexes together in one list:

```
self_and_neighbors = [4]
self_and_neighbors.extend(qW.neighbors[4])
print(self_and_neighbors)
```

```
[4, 0, 3, 5, 6, 7]
```

and grabbing those elements from the dataframe:

```
dataframe.loc[self_and_neighbors]
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	COFI
<b>4</b>	Ochiltree	Texas	48	357	48357	48	357
<b>0</b>	Lipscomb	Texas	48	295	48295	48	295
<b>3</b>	Hansford	Texas	48	195	48195	48	195
<b>5</b>	Roberts	Texas	48	393	48393	48	393
<b>6</b>	Hemphill	Texas	48	211	48211	48	211
<b>7</b>	Hutchinson	Texas	48	233	48233	48	233

6 rows × 70 columns

A full, dense matrix describing all of the pairwise relationships is constructed using the `.full` method, or when `pysal.full` is called on a weights object:

```
Wmatrix, ids = qW.full()
#Wmatrix, ids = ps.full(qW)
```

```
Wmatrix
```

```
array([[ 0.,  0.,  0., ...,  0.,  0.,  0.],
       [ 0.,  0.,  1., ...,  0.,  0.,  0.],
       [ 0.,  1.,  0., ...,  0.,  0.,  0.],
       ...,
       [ 0.,  0.,  0., ...,  0.,  1.,  1.],
       [ 0.,  0.,  0., ...,  1.,  0.,  1.],
       [ 0.,  0.,  0., ...,  1.,  1.,  0.]])
```

Note that this matrix is binary, in that its elements are either zero or one, since an observation is either a neighbor or it is not a neighbor.

However, many common use cases of spatial weights require that the matrix is row-standardized. This is done simply in PySAL using the `.transform` attribute

```
qW.transform = 'r'
```

Now, if we build a new full matrix, its rows should sum to one:

```
Wmatrix, ids = qW.full()
```

```
Wmatrix.sum(axis=1) #numpy axes are 0:column, 1:row, 2:facet, into higher dimensions
```

Since weight matrices are typically very sparse, there is also a sparse weights matrix constructor:

qW.sparse

```
<254x254 sparse matrix of type '<type 'numpy.float64'>'  
with 1460 stored elements in Compressed Sparse Row format>
```

By default, PySAL assigns each observation an index according to the order in which the observation was read in. This means that, by default, all of the observations in the weights object are indexed by table order. If you have an alternative ID variable, you can pass that into the weights constructor.

For example, the `texas.shp` dataset has a possible alternative ID Variable, a `FIPS` code.

```
dataframe.head()
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	COFIPS
0	Lipscomb	Texas	48	295	48295	48	295
1	Sherman	Texas	48	421	48421	48	421
2	Dallam	Texas	48	111	48111	48	111
3	Hansford	Texas	48	195	48195	48	195
4	Ochiltree	Texas	48	357	48357	48	357

5 rows × 70 columns

The observation we were discussing above is in the fifth row: Pend Oreille county, Washington. Note that its FIPS code is 53051.

Then, instead of indexing the weights and the dataframe just based on read-order, use the `FIPS` code as an index:

```
qW = ps.queen_from_shapefile(shp_path, idVariable='FIPS')
```

```
ps.knnW_from_shapefile??
```

Now, Pend Oreille county has a different index:

```
qW[4] #fails, since no FIPS is 4.
```

```
-----
KeyError          Traceback (most recent call last)

<ipython-input-17-1d8a3009bc1e> in <module>()
      1 qW[4] #fails, since no FIPS is 4.

/home/serge/anaconda2/envs/pydata/lib/python2.7/site-packages/pysal/weights/weights.pyc in __getitem__(self, key)
  504     {1: 1.0, 4: 1.0, 101: 1.0, 85: 1.0, 5: 1.0}
  505     """
--> 506     return dict(zip(self.neighbors[key], self.weights[key]))
  507
  508 def __iter__(self):
```

KeyError: 4

Note that a `KeyError` in Python usually means that some index, here `4`, was not found in the collection being searched, the IDs in the queen weights object. This makes sense, since we explicitly passed an `idVariable` argument, and nothing has a `FIPS` code of `4`.

Instead, if we use the observation's `FIPS` code:

```
qW['48111']
```

```
{u'48205': 1.0, u'48341': 1.0, u'48421': 1.0}
```

We get what we need.

In addition, we have to now query the dataframe using the `FIPS` code to find our neighbors. But, this is relatively easy to do, since pandas will parse the query by looking into python objects, if told to.

First, let us store the neighbors of our target county:

```
self_and_neighbors = ['48111']
self_and_neighbors.extend(qW.neighbors['48111'])
```

Then, we can use this list in `.query`:

```
dataframe.query('FIPS in @self_and_neighbors')
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	COFIPS
<b>1</b>	Sherman	Texas	48	421	48421	48	421
<b>2</b>	Dallam	Texas	48	111	48111	48	111
<b>8</b>	Hartley	Texas	48	205	48205	48	205
<b>9</b>	Moore	Texas	48	341	48341	48	341

4 rows × 70 columns

Note that we have to use `@` before the name in order to show that we're referring to a python object and not a column in the dataframe.

```
#dataframe.query('FIPS in neights') will fail because there is no column called 'neights'
```

Of course, we could also reindex the dataframe to use the same index as our weights:

```
fips_frame = dataframe.set_index(dataframe.FIPS)
fips_frame.head()
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	COFIPS
FIPS							
<b>48295</b>	Lipscomb	Texas	48	295	48295	48	295
<b>48421</b>	Sherman	Texas	48	421	48421	48	421
<b>48111</b>	Dallam	Texas	48	111	48111	48	111
<b>48195</b>	Hansford	Texas	48	195	48195	48	195
<b>48357</b>	Ochiltree	Texas	48	357	48357	48	357

5 rows × 70 columns

Now that both are using the same weights, we can use the `.loc` indexer again:

```
fips_frame.loc[self_and_neighbors]
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	CC
FIPS							
<b>48111</b>	Dallam	Texas	48	111	48111	48	11
<b>48205</b>	Hartley	Texas	48	205	48205	48	20
<b>48421</b>	Sherman	Texas	48	421	48421	48	42
<b>48341</b>	Moore	Texas	48	341	48341	48	34

4 rows × 70 columns

## Rook Weights

Rook weights are another type of contiguity weight, but consider observations as neighboring only when they share an edge. The rook neighbors of an observation may be different than its queen neighbors, depending on how the observation and its nearby polygons are configured.

We can construct this in the same way as the queen weights, using the special `rook_from_shapefile` function

```
rW = ps.rook_from_shapefile(shp_path, idVariable='FIPS')
```

```
rW['48111']
```

```
{u'48205': 1.0, u'48421': 1.0}
```

These weights function exactly like the Queen weights, and are only distinguished by what they consider "neighbors."

## Bishop Weights

In theory, a "Bishop" weighting scheme is one that arises when only polygons that share vertexes are considered to be neighboring. But, since Queen contiguity requires either an edge or a vertex and Rook contiguity requires only shared edges, the following relationship is true:

$$\mathcal{Q} = \mathcal{R} \cup \mathcal{B}$$

where  $\mathcal{Q}$  is the set of neighbor pairs via queen contiguity,  $\mathcal{R}$  is the set of neighbor pairs via Rook contiguity, and  $\mathcal{B}$  via Bishop contiguity. Thus:

$$\mathcal{Q} \setminus \mathcal{R} = \mathcal{B}$$

Bishop weights entail all Queen neighbor pairs that are not also Rook neighbors.

PySAL does not have a dedicated bishop weights constructor, but you can construct very easily using the `w_difference` function. This function is one of a family of tools to work with weights, all defined in `ps.weights`, that conduct these types of set operations between weight objects.

```
bW = ps.w_difference(qW, rW, constrained=False, silent_island_warning=True) #silence because there will be a lot of warnings
```

```
bW.histogram
```

```
[(0, 161), (1, 48), (2, 33), (3, 8), (4, 4)]
```

Thus, the vast majority of counties have no bishop neighbors. But, a few do. A simple way to see these observations in the dataframe is to find all elements of the dataframe that are not "islands," the term for an observation with no neighbors:

```
islands = bW.islands
```

```
dataframe.query('FIPS not in @islands')
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS
<b>0</b>	Lipscomb	Texas	48	295	48295	48
<b>1</b>	Sherman	Texas	48	421	48421	48
<b>2</b>	Dallam	Texas	48	111	48111	48
<b>3</b>	Hansford	Texas	48	195	48195	48
<b>4</b>	Ochiltree	Texas	48	357	48357	48
<b>5</b>	Roberts	Texas	48	393	48393	48
<b>6</b>	Hemphill	Texas	48	211	48211	48
<b>7</b>	Hutchinson	Texas	48	233	48233	48
<b>8</b>	Hartley	Texas	48	205	48205	48
<b>9</b>	Moore	Texas	48	341	48341	48
<b>10</b>	Potter	Texas	48	375	48375	48
<b>11</b>	Carson	Texas	48	065	48065	48
<b>12</b>	Gray	Texas	48	179	48179	48
<b>13</b>	Wheeler	Texas	48	483	48483	48
<b>14</b>	Oldham	Texas	48	359	48359	48
<b>15</b>	Randall	Texas	48	381	48381	48
<b>16</b>	Armstrong	Texas	48	011	48011	48
<b>17</b>	Collingsworth	Texas	48	087	48087	48
<b>18</b>	Donley	Texas	48	129	48129	48

<b>27</b>	Wilbarger	Texas	48	487	48487	48
<b>28</b>	Motley	Texas	48	345	48345	48
<b>29</b>	Cottle	Texas	48	101	48101	48
<b>30</b>	Floyd	Texas	48	153	48153	48
<b>31</b>	Hale	Texas	48	189	48189	48
<b>32</b>	Lamb	Texas	48	279	48279	48
<b>33</b>	Bailey	Texas	48	017	48017	48
<b>35</b>	Wichita	Texas	48	485	48485	48
<b>38</b>	Red River	Texas	48	387	48387	48
<b>41</b>	Lamar	Texas	48	277	48277	48
<b>43</b>	King	Texas	48	269	48269	48
...	...	...	...	...	...	...
<b>119</b>	Midland	Texas	48	329	48329	48
<b>126</b>	Anderson	Texas	48	001	48001	48
<b>128</b>	Freestone	Texas	48	161	48161	48
<b>132</b>	Hudspeth	Texas	48	229	48229	48
<b>140</b>	Tom Green	Texas	48	451	48451	48
<b>144</b>	Upton	Texas	48	461	48461	48
<b>145</b>	Reagan	Texas	48	383	48383	48
<b>146</b>	Leon	Texas	48	289	48289	48
<b>149</b>	Concho	Texas	48	095	48095	48
<b>158</b>	Robertson	Texas	48	395	48395	48
<b>165</b>	Madison	Texas	48	313	48313	48
<b>166</b>	Schleicher	Texas	48	413	48413	48
<b>167</b>	Menard	Texas	48	327	48327	48

<b>172</b>	Brazos	Texas	48	041	48041	48
<b>183</b>	Presidio	Texas	48	377	48377	48
<b>191</b>	Bastrop	Texas	48	021	48021	48
<b>200</b>	Fayette	Texas	48	149	48149	48
<b>205</b>	Caldwell	Texas	48	055	48055	48
<b>212</b>	Gonzales	Texas	48	177	48177	48
<b>214</b>	Medina	Texas	48	325	48325	48
<b>217</b>	Uvalde	Texas	48	463	48463	48
<b>218</b>	Kinney	Texas	48	271	48271	48
<b>224</b>	Atascosa	Texas	48	013	48013	48
<b>228</b>	Zavala	Texas	48	507	48507	48
<b>229</b>	Frio	Texas	48	163	48163	48
<b>230</b>	Maverick	Texas	48	323	48323	48
<b>234</b>	La Salle	Texas	48	283	48283	48
<b>235</b>	McMullen	Texas	48	311	48311	48
<b>239</b>	Webb	Texas	48	479	48479	48
<b>242</b>	Duval	Texas	48	131	48131	48

93 rows × 70 columns

## Distance

There are many other kinds of weighting functions in PySAL. Another separate type use a continuous measure of distance to define neighborhoods. To use these measures, we first must extract the polygons' centroids.

For each polygon `poly` in `dataframe.geometry`, we want `poly.centroid`. So, one way to do this is to make a list of all of the centroids:

```
>>> ps.min_threshold_dist_from_shapefile(ps.examples.get_path("stl_hom.shp"), ps.cg.sphere.RADIUS_EARTH_MILES)
```

```
31.846942936393717
```

```
centroids = [list(poly.centroid) for poly in dataframe.geometry]
```

```
radius = ps.cg.sphere.RADIUS_EARTH_MILES  
radius
```

```
3958.755865744055
```

```
threshold = ps.min_threshold_dist_from_shapefile('../data/texas.shp')
```

```
threshold
```

```
1.0040319244447573
```

```
threshold = ps.min_threshold_dist_from_shapefile('../data/texas.shp',radius)
```

```
threshold
```

```
60.47758554135752
```

```
knn4_bad = ps.knnW_from_shapefile('../data/texas.shp', k=4)
```

```
knn4 = ps.knnW_from_shapefile?
```

```
knn4 = ps.knnW_from_shapefile
```

```
knn4 = ps.knnW_from_shapefile
```

```
knn4 = ps.knnW_from_shapefile
```

```
knn4 = ps.knnW_from_shapefile('../data/texas.shp', k=4, radius=radius)
```

```
knn4.histogram
```

```
[(4, 254)]
```

```
knn4_bad.histogram
```

```
[(4, 254)]
```

```
knn4[0]
```

```
{3: 1.0, 4: 1.0, 5: 1.0, 6: 1.0}
```

```
knn4_bad[0]
```

```
{4: 1.0, 5: 1.0, 6: 1.0, 13: 1.0}
```

If we were working with point data, this step would be unnecessary.

## KnnW

If we wanted to consider only the  $k$ -nearest neighbors to an observation's centroid, we could use the `knnW` function in PySAL.

This specific type of distance weights requires that we first build a `KDTree`, a special representation for spatial point data. Fortunately, this is built in to PySAL:

```
kdtree = ps.cg.KDTree(centroids)
```

Then, we can use this to build a spatial weights object where only the closest  $k$  observations are considered "neighbors." In this example, let's do the closest 5:

```
nn5 = ps.knnW(kdtree, k=5)
```

```
nn5.histogram
```

```
[(5, 254)]
```

So, all observations have exactly 5 neighbors. Sometimes, these neighbors are actually different observations than the ones identified by contiguity neighbors.

For example, Pend Oreille gets a new neighbor, Kootenai county:

```
nn5[4]
```

```
{0: 1.0, 3: 1.0, 5: 1.0, 6: 1.0, 7: 1.0}
```

```
dataframe.loc[nn5.neighbors[4] + [4]]
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	COFI
5	Roberts	Texas	48	393	48393	48	393
3	Hansford	Texas	48	195	48195	48	195
0	Lipscomb	Texas	48	295	48295	48	295
7	Hutchinson	Texas	48	233	48233	48	233
6	Hemphill	Texas	48	211	48211	48	211
4	Ochiltree	Texas	48	357	48357	48	357

6 rows × 70 columns

## Kernel W

Kernel Weights are continuous distance-based weights that use kernel densities to provide an indication of neighborliness.

Typically, they estimate a `bandwidth`, which is a parameter governing how far out observations should be considered neighboring. Then, using this bandwidth, they evaluate a continuous kernel function to provide a weight between 0 and 1.

Many different choices of kernel functions are supported, and bandwidth can be estimated at each point or over the entire map.

For example, if we wanted to use a single estimated bandwidth for the entire map and weight according to a gaussian kernel:

```
kernelW = ps.Kernel(centroids, fixed=True, function='gaussian')
#ps.Kernel(centroids, fixed=False, function='gaussian') #same kernel, but bandwidth changes at each observation
```

```
dataframe.loc[kernelW.neighbors[4] + [4]]
```

	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	C
<b>15</b>	Randall	Texas	48	381	48381	48	381
<b>16</b>	Armstrong	Texas	48	011	48011	48	11
<b>11</b>	Carson	Texas	48	065	48065	48	65
<b>10</b>	Potter	Texas	48	375	48375	48	375
<b>9</b>	Moore	Texas	48	341	48341	48	341
<b>3</b>	Hansford	Texas	48	195	48195	48	195
<b>7</b>	Hutchinson	Texas	48	233	48233	48	233
<b>1</b>	Sherman	Texas	48	421	48421	48	421
<b>25</b>	Hall	Texas	48	191	48191	48	191
<b>17</b>	Collingsworth	Texas	48	087	48087	48	87
<b>18</b>	Donley	Texas	48	129	48129	48	129
<b>13</b>	Wheeler	Texas	48	483	48483	48	483
<b>12</b>	Gray	Texas	48	179	48179	48	179
<b>6</b>	Hemphill	Texas	48	211	48211	48	211
<b>5</b>	Roberts	Texas	48	393	48393	48	393
<b>4</b>	Ochiltree	Texas	48	357	48357	48	357
<b>0</b>	Lipscomb	Texas	48	295	48295	48	295
<b>4</b>	Ochiltree	Texas	48	357	48357	48	357

18 rows × 70 columns

As you can see, this provides our target observation, Pend Oreille, with many new neighbors. \

```
mind = ps.threshold_binaryW_from_shapefile('../data/texas.shp', radius=radius, threshold=50)
```

WARNING: there are 5 disconnected observations  
Island ids: [132, 133, 181, 182, 195]

```
mind = ps.threshold_binaryW_from_shapefile('../data/texas.shp', radius=radius, threshold=threshold)
```

```
mind.histogram
```

```
[(1, 2),  
(2, 3),  
(3, 4),  
(4, 8),  
(5, 5),  
(6, 20),  
(7, 26),  
(8, 9),  
(9, 32),  
(10, 31),  
(11, 37),  
(12, 33),  
(13, 23),  
(14, 6),  
(15, 7),  
(16, 2),  
(17, 4),  
(18, 2)]
```

```
centroids = np.array([list(poly.centroid) for poly in dataframe.geometry])
```

```
centroids[0:10]
```

```
array([[-100.27156111, 36.27508641],  
       [-101.8930971 , 36.27325425],  
       [-102.59590795, 36.27354996],  
       [-101.35351324, 36.27230422],  
       [-100.81561379, 36.27317803],  
       [-100.81482387, 35.8405153 ],  
       [-100.2694824 , 35.83996075],  
       [-101.35420366, 35.8408377 ],  
       [-102.59375964, 35.83958662],  
       [-101.89248229, 35.84058246]])
```

```
mind[0]
```

```
{3: 1, 4: 1, 5: 1, 6: 1, 13: 1}
```

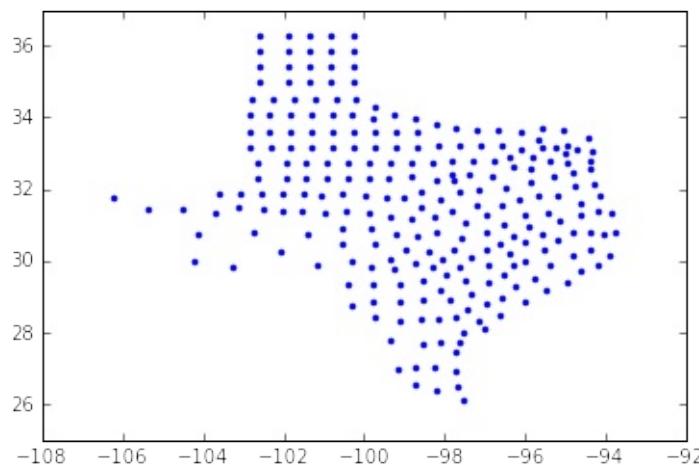
```
knn4[0]
```

```
{3: 1.0, 4: 1.0, 5: 1.0, 6: 1.0}
```

```
%matplotlib inline  
import matplotlib.pyplot as plt
```

```
plt.plot(centroids[:,0], centroids[:,1],'.')  
plt.ylim([25,37])
```

```
(25, 37)
```



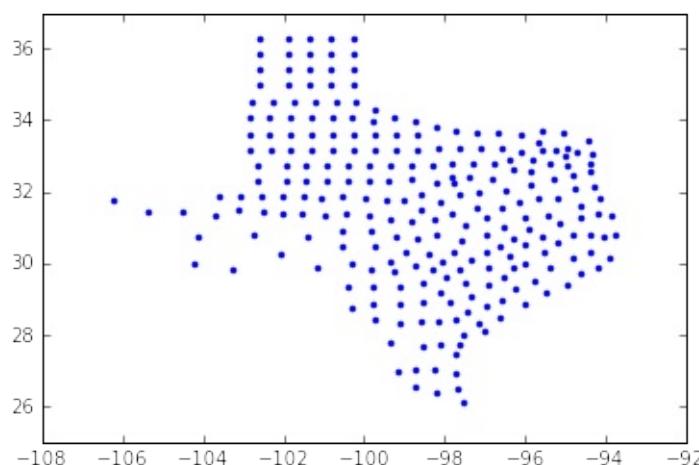
```
wq = ps.queen_from_shapefile('../data/texas.shp')
```

```
wq[0]
```

```
{4: 1.0, 5: 1.0, 6: 1.0}
```

```
plt.plot(centroids[:,0], centroids[:,1],'.')
plt.ylim([25,37])
```

```
(25, 37)
```



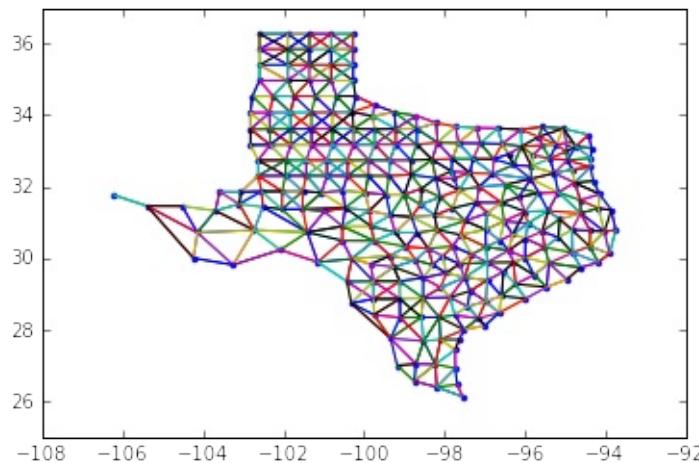
```
wq.neighbors[0]
```

```
[4, 5, 6]
```

```

plt.plot(centroids[:,0], centroids[:,1],'')
#plt.plot(s04[:,0], s04[:,1], '-')
plt.ylim([25,37])
for k,neighs in wq.neighbors.items():
    #print(k,neighs)
    origin = centroids[k]
    for neigh in neighs:
        segment = centroids[[k,neigh]]
        plt.plot(segment[:,0], segment[:,1], '-')

```

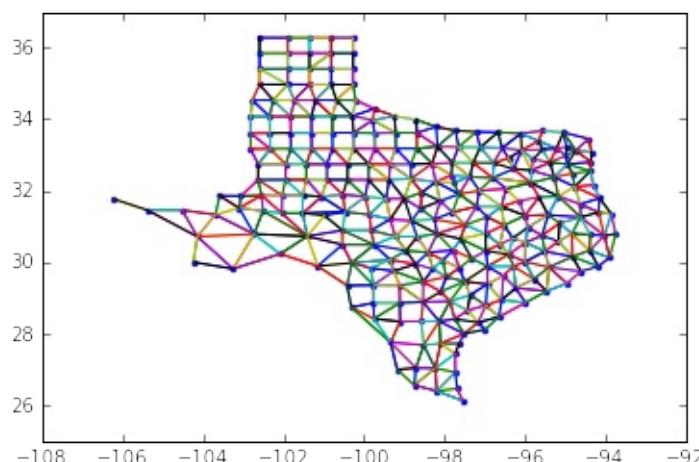


```
wr = ps.rook_from_shapefile('../data/texas.shp')
```

```

plt.plot(centroids[:,0], centroids[:,1],'')
#plt.plot(s04[:,0], s04[:,1], '-')
plt.ylim([25,37])
for k,neighs in wr.neighbors.items():
    #print(k,neighs)
    origin = centroids[k]
    for neigh in neighs:
        segment = centroids[[k,neigh]]
        plt.plot(segment[:,0], segment[:,1], '-')

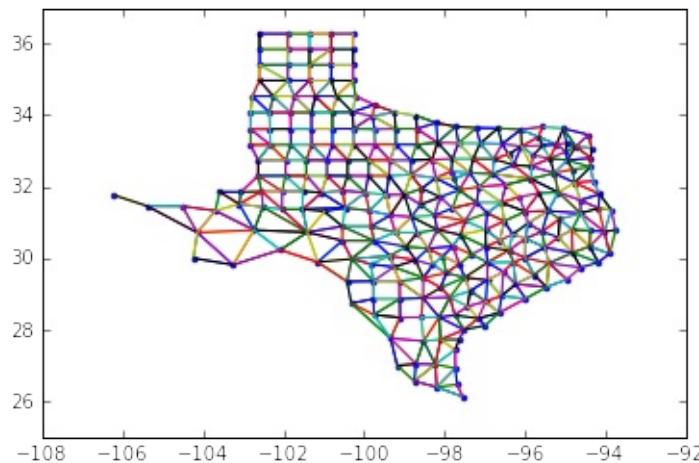
```



```

plt.plot(centroids[:,0], centroids[:,1],'')
#plt.plot(s04[:,0], s04[:,1], '-')
plt.ylim([25,37])
for k,neighs in wr.neighbors.items():
    #print(k,neighs)
    origin = centroids[k]
    for neigh in neighs:
        segment = centroids[[k,neigh]]
        plt.plot(segment[:,0], segment[:,1], '-')

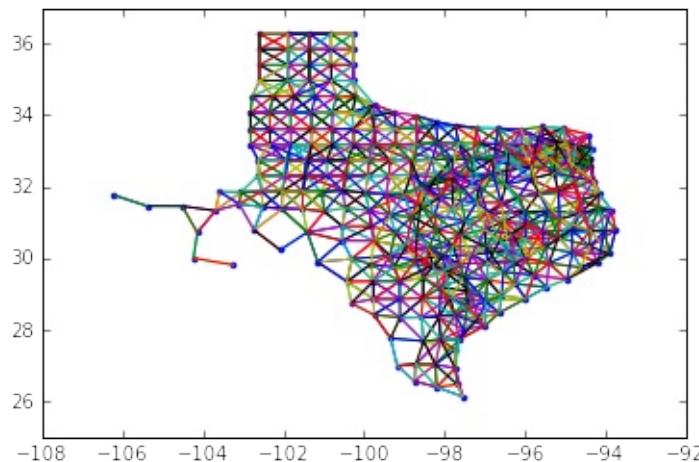
```



```

plt.plot(centroids[:,0], centroids[:,1],'')
#plt.plot(s04[:,0], s04[:,1], '-')
plt.ylim([25,37])
for k,neighs in mind.neighbors.items():
    #print(k,neighs)
    origin = centroids[k]
    for neigh in neighs:
        segment = centroids[[k,neigh]]
        plt.plot(segment[:,0], segment[:,1], '-')

```





```
%matplotlib inline
import pysal as ps
import pandas as pd
import numpy as np
from pysal.contrib.viz import mapping as maps
```

A well-used functionality in PySAL is the use of PySAL to conduct exploratory spatial data analysis. This notebook will provide an overview of ways to conduct exploratory spatial analysis in Python.

First, let's read in some data:

```
data = ps.pdio.read_files("../data/texas.shp")
W = ps.queen_from_shapefile("../data/texas.shp")
W.transform = 'r'
```

```
data.head()
```

	<b>NAME</b>	<b>STATE_NAME</b>	<b>STATE_FIPS</b>	<b>CNTY_FIPS</b>	<b>FIPS</b>	<b>STFIPS</b>	<b>COFIP</b>
<b>0</b>	Lipscomb	Texas	48	295	48295	48	295
<b>1</b>	Sherman	Texas	48	421	48421	48	421
<b>2</b>	Dallam	Texas	48	111	48111	48	111
<b>3</b>	Hansford	Texas	48	195	48195	48	195
<b>4</b>	Ochiltree	Texas	48	357	48357	48	357

5 rows × 70 columns

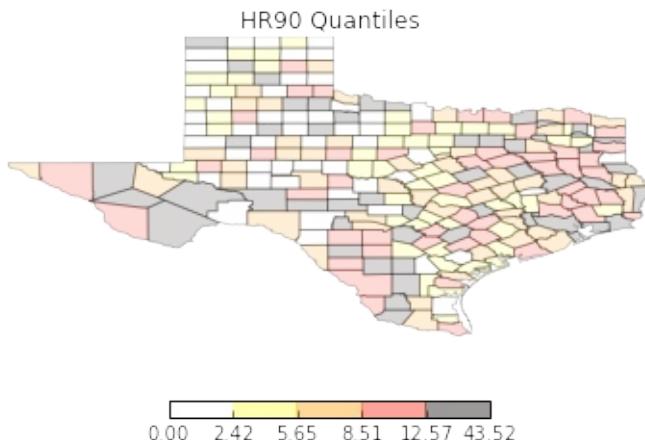
```
data.head()
```

	<b>NAME</b>	<b>STATE_NAME</b>	<b>STATE_FIPS</b>	<b>CNTY_FIPS</b>	<b>FIPS</b>	<b>STFIPS</b>	<b>COFIP</b>
<b>0</b>	Lipscomb	Texas	48	295	48295	48	295
<b>1</b>	Sherman	Texas	48	421	48421	48	421
<b>2</b>	Dallam	Texas	48	111	48111	48	111
<b>3</b>	Hansford	Texas	48	195	48195	48	195
<b>4</b>	Ochiltree	Texas	48	357	48357	48	357

5 rows × 70 columns

```
data = ps.pdio.read_files("../data/texas.shp")
W = ps.queen_from_shapefile("../data/texas.shp")
W.transform = 'r'
```

```
shp_link = "../data/texas.shp"
maps.plot_choropleth(shp_link, data.HR90, 'quantiles', title='HR90 Quantiles')
```



In PySAL, commonly-used analysis methods are very easy to access. For example, if we were interested in examining the spatial dependence in `HR90` we could quickly compute a Moran's  $I\$$  statistic:

```
I_HR90 = ps.Moran(data.HR90.values, W)
```

```
I_HR90.I, I_HR90.p_sim
```

```
(0.085976640313889768, 0.014)
```

Thus, the  $I\$$  statistic is  $0.859\$$  for this data, and has a very small  $p\$$  value.

We can visualize the distribution of simulated  $I\$$  statistics using the stored collection of simulated statistics:

```
I_HR90.sim[0:5]
```

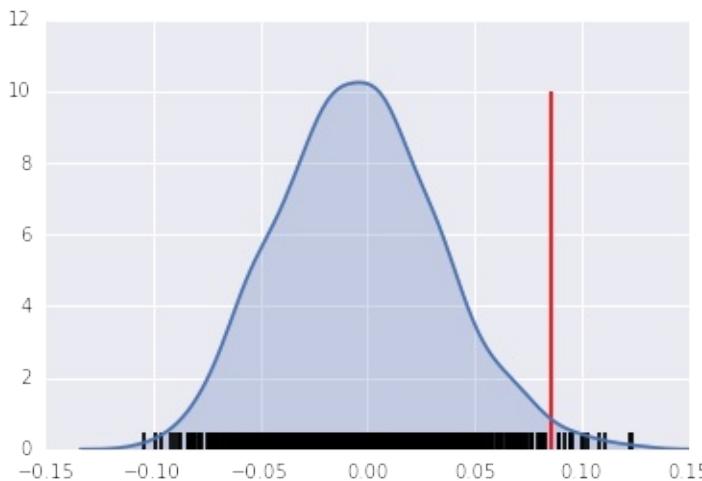
```
array([-0.04389574,  0.01129696,  0.02567161,  0.01608838, -0.04648693])
```

A simple way to visualize this distribution is to make a KDEplot (like we've done before), and add a rug showing all of the simulated points, and a vertical line denoting the observed value of the statistic:

```
import matplotlib.pyplot as plt
import seaborn as sns
%matplotlib inline
```

```
sns.kdeplot(I_HR90.sim, shade=True)
plt.vlines(I_HR90.sim, 0, 0.5)
plt.vlines(I_HR90.I, 0, 10, 'r')
plt.xlim([-0.15, 0.15])
```

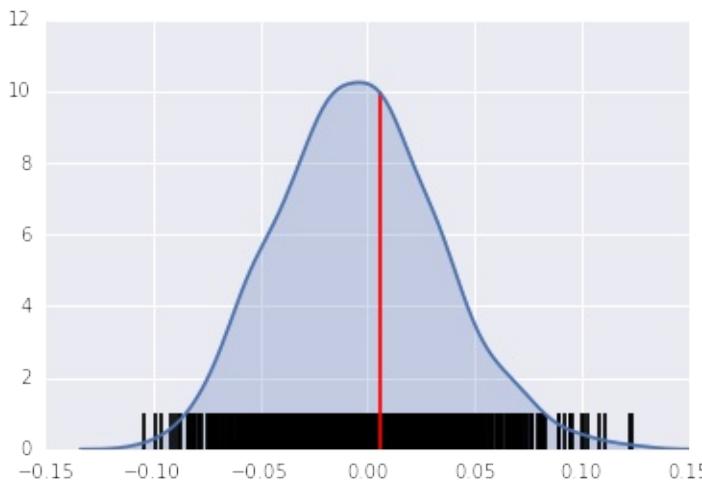
```
(-0.15, 0.15)
```



Instead, if our  $I^*$  statistic were close to our expected value,  $I_{HR90.EI}$ , our plot might look like this:

```
sns.kdeplot(I_HR90.sim, shade=True)
plt.vlines(I_HR90.sim, 0, 1)
plt.vlines(I_HR90.EI+.01, 0, 10, 'r')
plt.xlim([-0.15, 0.15])
```

(-0.15, 0.15)



In addition, we can compute a global Bivariate Moran statistic, which relates an observation to the spatial lag of another observation:

```
bv_HRBLK = ps.Moran_BV(data.HR90.values, data.BLK90.values, W)
```

bv\_HRBLK.I, bv\_HRBLK.p\_sim

(0.080041444794258343, 0.005000000000000001)

## Local Autocorrelation Statistics

In addition to the Global autocorrelation statistics, PySAL has many local autocorrelation statistics. Let's compute a local Moran statistic for the same data shown above:

```
LMo_HR90 = ps.Moran_Local(data.HR90.values, W)
```

Now, instead of a single \$I\$ statistic, we have an *array* of local \$I\_i\$ statistics, stored in the `.ls` attribute, and p-values from the simulation are in `p_sim`.

```
LMo_HR90.ls, LMo_HR90.p_sim
```

```
(array([-1.12087323e+00, 4.74852232e-01, -1.22758423e+00,
       9.38686608e-01, 6.89742960e-01, 7.85031726e-01,
       7.10475151e-01, 4.10606860e-01, 7.40368367e-03,
       1.48663520e-01, -5.99072474e-01, 8.11752611e-02,
      -1.20482997e-01, 3.18800252e-01, 3.47276792e-01,
       4.39609038e-02, -3.04514513e-01, 2.01610062e-01,
       2.85061414e-01, 5.84462378e-01, 7.56336432e-01,
       3.83077442e-01, 3.99898754e-03, -9.16855756e-01,
      -4.87000938e-02, 1.46381951e-02, -1.20220927e-01,
      -7.65176192e-01, -2.57853261e+00, 2.03465774e-01,
     -1.00025313e-02, 1.51706786e-01, 4.93433817e-01,
       4.35124305e-01, -3.12259940e-01, -2.32723324e-01,
       2.82455741e-03, 1.22002377e-01, -1.27741850e-02,
      -3.54088100e-04, -9.99830522e-03, -4.29411693e-02,
       1.14955949e-01, -5.76707109e-01, -5.79367567e-01,
      -2.44357064e-01, -2.45937883e-02, 1.28248005e-01,
       2.40904907e-01, -1.30657056e+00, 8.75684587e-02,
       7.60257313e-01, 7.46769544e-03, 8.46525604e-02,
      -9.91242446e-02, -3.63476666e-03, -1.84994288e-01,
       6.10806717e-02, -4.10962997e-01, -1.55435599e-02,
       3.34932522e-01, 5.84998647e-01, 3.97457030e-01,
       4.84549106e-01, -7.05237462e-01, -1.89267505e-01,
      -5.36300770e-01, 2.18228666e-01, 2.45387767e-01,
       1.04747657e+00, -5.03740235e-02, -4.99501600e-01,
      -6.79039774e-02, -4.28204631e-01, -5.19255631e-02,
       1.62667971e-01, 3.96182300e-02, 1.39001221e-01,
       7.85033384e-01, -6.34873174e-02, -2.05239166e-01,
       6.70092095e-01, 1.19432435e-01, 8.33565709e-02,
       6.08109031e-02, 4.71129836e-02, -7.53103370e-01,
       4.12179684e-01, 4.18690212e-01, -1.24823445e-01,
      -2.20055897e-01, 8.71366261e-01, -8.79710509e-02,
       1.68820593e-03, 1.07166595e-02, -3.54370029e-02,
       1.20592772e-03, 2.34359115e-01, 1.74921357e-01,
      -1.82542919e-01, -2.17921039e-01, -1.29920391e-03,
      -5.76690555e-02, 1.45723641e-01, 3.62521949e-01,
       4.39212267e-02, 1.62791100e-01, 2.34754317e-01,
       4.24252755e-02, -7.44382557e-01, 1.01380671e-01,
       1.68446607e-01, 1.36810620e-01, 4.56977527e-02,
       6.92868233e-02, 3.82546883e-02, 1.23206557e-01,
       5.81014061e-01, 6.19044577e-01, 5.97840100e-02,
       6.02552478e-01, 1.98331508e-01, -2.08124490e-01,
       2.89307856e-01, 2.94694807e-01, 3.17901639e-01,
       3.26156089e-01, 3.01034558e-01, 1.49504893e-01,
       1.95148623e+00, -2.54303828e-01, 5.08956169e-01,
       6.08264082e-01, -3.81888449e-02, -3.00282633e-01,
      -2.65739969e-02, 2.24230408e-01, -1.44008615e-02,
       4.66594113e-01, -4.31489357e-02, 1.87061533e-02,
       1.45607307e-01, 2.47182058e-03, -6.64057756e-01,
       1.54192078e-02, 2.36636263e-01, -8.45056351e-03,
      -1.34851321e-01, 1.18537899e-01, -2.27964598e-01,
      -4.18648686e-01, 3.39507930e-01, -2.63719989e-02,
       1.55681623e-01, 1.22301226e-01, 1.77438253e-01,
       4.10677287e-02, 1.49101636e-01, 1.04297773e-01,
      -7.67634652e-02, -5.64248729e-03, -3.05586580e-02,
       5.53503759e-02, 1.37140043e-02, 1.29212068e+00,
      -8.56707799e-02, 2.62786886e-01, -6.36623531e-01,
      -3.90746796e-01, 2.74114791e-02, -3.42998234e-02,
       1.96470454e-02, 2.66085647e-01, -5.86103398e-01,
      -1.40050219e-01, -9.58183688e-02, 1.06002105e-01,
       5.78305864e-02, 9.12034797e-02, 1.75316202e-01,
      1.53146979e+00, 2.55223569e-01, -1.07521719e+00,
```

```

2.10421553e-01, 1.79559685e-03, 2.46623711e-01,
-1.37221563e-01, -1.93104397e-01, -6.70944099e-01,
-6.21994147e-01, 2.62134357e-01, 8.44258361e-02,
2.15034457e-03, -1.13695914e-02, -9.85881978e-01,
-3.88051312e-02, -3.94113412e-02, 2.54665339e-01,
1.03033517e-01, 1.87014888e-01, 6.57921237e-02,
8.93885114e-01, -4.12463002e-02, 5.93523798e-04,
-7.48641130e-01, -2.33977229e-01, -1.81364976e-01,
-2.12719096e-02, -1.77624803e-01, 7.56458111e-01,
4.65743492e-02, -1.17037830e-02, 1.42744115e-01,
-2.52132245e-01, 2.20273885e-02, 1.32249407e-01,
1.50840035e-02, 1.58872364e-01, -3.07330315e-01,
-2.15826555e-01, 7.78727321e-01, 1.53798953e-01,
1.39830232e-02, 1.14430614e-02, -4.13603775e-01,
-1.13601903e-01, 3.98036147e-02, 5.00495648e-02,
1.85345062e-02, 8.20513963e-01, -2.85154006e-03,
3.37194545e-01, -6.54881438e-01, 2.87571205e-01,
3.40025967e+00, 2.79223250e+00, 2.18713536e-01,
2.57852929e-01, 1.00405907e-01, 1.92499398e-01,
9.07540052e-02, 1.49438551e-01, 1.33219486e+00,
9.58722126e-03, -9.26242513e-02, 1.26208606e-01,
3.53039195e-01, 1.91842139e-01, -2.84025227e-03,
2.62219645e-01, 1.87256013e-01, 2.39837728e-03,
8.94400168e-02, -1.39329420e-01]),

array([ 0.009, 0.173, 0.029, 0.009, 0.001, 0.008, 0.064, 0.057,
       0.434, 0.135, 0.074, 0.315, 0.043, 0.009, 0.254, 0.45 ,
       0.238, 0.393, 0.262, 0.015, 0.055, 0.051, 0.263, 0.035,
       0.444, 0.129, 0.169, 0.124, 0.061, 0.242, 0.319, 0.092,
       0.031, 0.009, 0.22 , 0.283, 0.431, 0.247, 0.497, 0.424,
       0.364, 0.172, 0.377, 0.097, 0.082, 0.238, 0.074, 0.271,
       0.038, 0.009, 0.466, 0.04 , 0.479, 0.374, 0.034, 0.465,
       0.149, 0.108, 0.079, 0.467, 0.21 , 0.068, 0.037, 0.107,
       0.035, 0.188, 0.003, 0.308, 0.053, 0.016, 0.302, 0.126,
       0.42 , 0.209, 0.371, 0.134, 0.426, 0.325, 0.191, 0.045,
       0.359, 0.06 , 0.139, 0.443, 0.143, 0.483, 0.014, 0.041,
       0.207, 0.264, 0.279, 0.145, 0.133, 0.432, 0.435, 0.457,
       0.463, 0.144, 0.027, 0.028, 0.069, 0.02 , 0.041, 0.149,
       0.204, 0.289, 0.067, 0.256, 0.156, 0.124, 0.072, 0.2 ,
       0.141, 0.28 , 0.061, 0.371, 0.07 , 0.073, 0.061, 0.071,
       0.081, 0.273, 0.142, 0.273, 0.125, 0.058, 0.11 , 0.05 ,
       0.256, 0.168, 0.033, 0.226, 0.016, 0.251, 0.414, 0.476,
       0.1 , 0.209, 0.167, 0.383, 0.005, 0.201, 0.115, 0.108,
       0.397, 0.289, 0.301, 0.094, 0.404, 0.044, 0.227, 0.146,
       0.262, 0.4 , 0.139, 0.17 , 0.077, 0.27 , 0.127, 0.379,
       0.438, 0.234, 0.238, 0.427, 0.011, 0.384, 0.052, 0.102,
       0.322, 0.347, 0.263, 0.483, 0.08 , 0.174, 0.299, 0.329,
       0.299, 0.413, 0.442, 0.352, 0.065, 0.265, 0.045, 0.073,
       0.45 , 0.096, 0.319, 0.184, 0.099, 0.06 , 0.059, 0.221,
       0.466, 0.441, 0.026, 0.305, 0.222, 0.201, 0.203, 0.285,
       0.173, 0.116, 0.373, 0.379, 0.323, 0.174, 0.213, 0.399,
       0.07 , 0.023, 0.165, 0.141, 0.358, 0.331, 0.079, 0.246,
       0.41 , 0.165, 0.257, 0.102, 0.099, 0.12 , 0.307, 0.488,
       0.005, 0.287, 0.418, 0.203, 0.434, 0.002, 0.192, 0.242,
       0.063, 0.039, 0.013, 0.059, 0.012, 0.108, 0.331, 0.001,
       0.119, 0.241, 0.012, 0.489, 0.314, 0.245, 0.117, 0.152,
       0.36 , 0.354, 0.251, 0.485, 0.378, 0.41 ]))

```

We can adjust the number of permutations used to derive every *pseudo-\$p\$* value by passing a different `permutations` argument:

```
LMo_HR90 = ps.Moran_Local(data.HR90.values, W, permutations=9999)
```

In addition to the typical clustermap, a helpful visualization for LISA statistics is a Moran scatterplot with statistically significant LISA values highlighted.

This is very simple, if we use the same strategy we used before:

First, construct the spatial lag of the covariate:

```
Lag_HR90 = ps.lag_spatial(W, data.HR90.values)
HR90 = data.HR90.values
```

Then, we want to plot the statistically-significant LISA values in a different color than the others. To do this, first find all of the statistically significant LISAs. Since the `$p$`-values are in the same order as the `$I_i$` statistics, we can do this in the following way

```
sigs = HR90[LMo_HR90.p_sim <= .001]
W_sigs = Lag_HR90[LMo_HR90.p_sim <= .001]
insigs = HR90[LMo_HR90.p_sim > .001]
W_insigs = Lag_HR90[LMo_HR90.p_sim > .001]
```

Then, since we have a lot of points, we can plot the points with a statistically insignificant LISA value lighter using the `alpha` keyword. In addition, we would like to plot the statistically significant points in a dark red color.

```
b,a = np.polyfit(HR90, Lag_HR90, 1)
```

Matplotlib has a list of [named colors](#) and will interpret colors that are provided in hexadecimal strings:

```
plt.plot(sigs, W_sigs, '^', color='firebrick')
plt.plot(insigs, W_insigs, '.', alpha=.2)
# dashed vert at mean of the last year's PCI
plt.vlines(HR90.mean(), Lag_HR90.min(), Lag_HR90.max(), linestyle='--')
# dashed horizontal at mean of lagged PCI
plt.hlines(Lag_HR90.mean(), HR90.min(), HR90.max(), linestyle='--')

# red line of best fit using global I as slope
plt.plot(HR90, a + b*HR90, 'r')
plt.text(s='I = %.3f' % I_HR90.I, x=50, y=15, fontsize=18)
plt.title('Moran Scatterplot')
plt.ylabel('Spatial Lag of HR90')
plt.xlabel('HR90')
```

```
<matplotlib.text.Text at 0x7f5a57011e10>
```



We can also make a LISA map of the data.

```
sig = LM0_HR90.p_sim < 0.05
```

```
sig.sum()
```

```
42
```

```
hotspots = LMo_HR90.q==1 * sig
```

```
hotspots.sum()
```

```
9
```

```
coldspots = LMo_HR90.q==3 * sig
```

```
coldspots.sum()
```

```
16
```

```
data.HR90[hotspots]
```

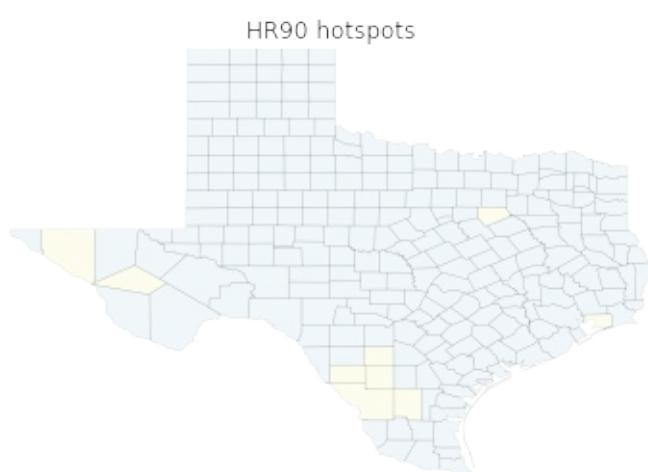
```
98    9.784698
132   11.435106
164   17.129154
209   13.274924
229   12.371338
234   31.721863
236   9.584971
239   9.256549
242   18.062652
Name: HR90, dtype: float64
```

```
data[hotspots]
```

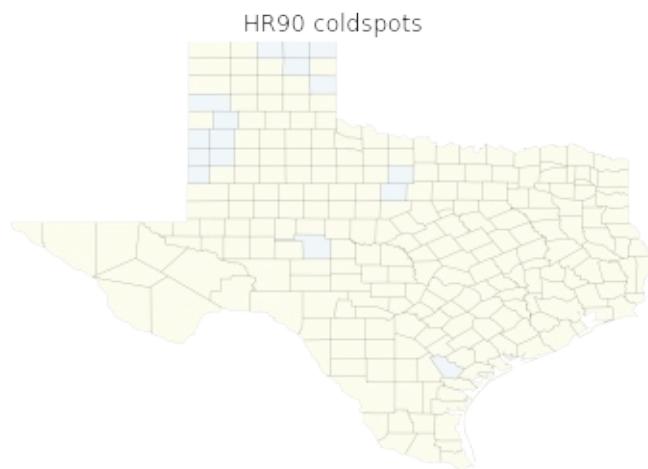
	NAME	STATE_NAME	STATE_FIPS	CNTY_FIPS	FIPS	STFIPS	COI
<b>98</b>	Ellis	Texas	48	139	48139	48	139
<b>132</b>	Hudspeth	Texas	48	229	48229	48	229
<b>164</b>	Jeff Davis	Texas	48	243	48243	48	243
<b>209</b>	Chambers	Texas	48	071	48071	48	71
<b>229</b>	Frio	Texas	48	163	48163	48	163
<b>234</b>	La Salle	Texas	48	283	48283	48	283
<b>236</b>	Dimmit	Texas	48	127	48127	48	127
<b>239</b>	Webb	Texas	48	479	48479	48	479
<b>242</b>	Duval	Texas	48	131	48131	48	131

9 rows × 70 columns

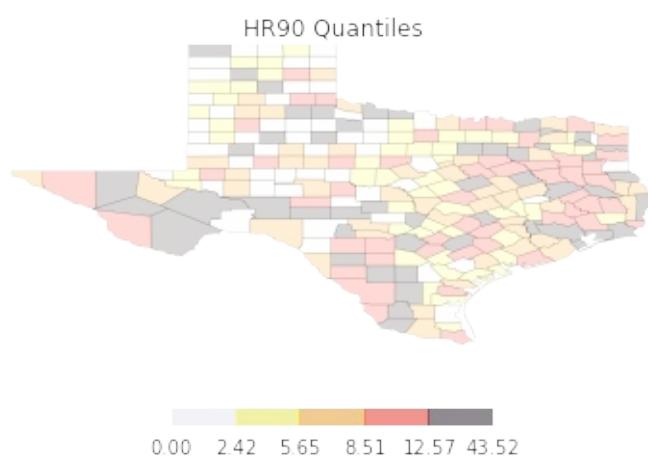
```
maps.plot_choropleth(shp_link, hotspots*1., 'unique_values', title='HR90 hotspots')
```



```
maps.plot_choropleth(shp_link, coldspots*1., 'unique_values', title='HR90 coldspots')
```

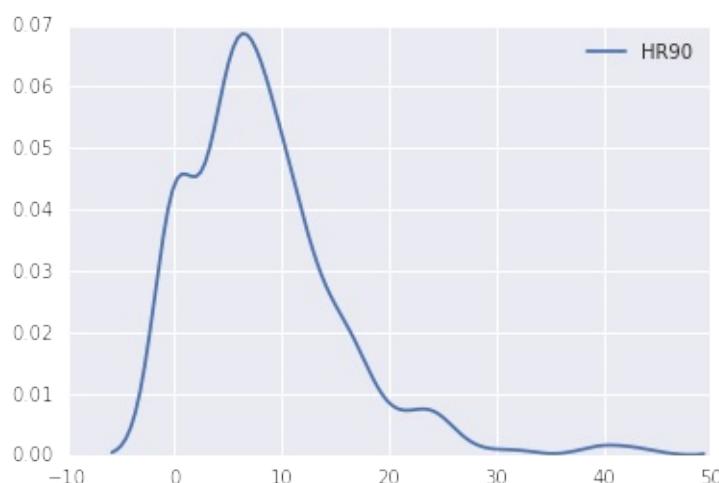


```
maps.plot_choropleth(shp_link, data.HR90, 'quantiles', title='HR90 Quantiles')
```



```
sns.kdeplot(data.HR90)
```

```
<matplotlib.axes._subplots.AxesSubplot at 0x7f5a5a448e90>
```



```
data.HR90.mean()
```

```
8.302494460285041
```

```
data.HR90.median()
```

```
7.23234613355
```

```
import pysal as ps
import numpy as np
%pylab inline
```

Populating the interactive namespace from numpy and matplotlib

```
f = ps.open(ps.examples.get_path('usjoin.csv'), 'r')
```

To determine what is in the file, check the `header` attribute on the file object:

```
f.header
```

```
['Name',
 'STATE_FIPS',
 '1929',
 '1930',
 '1931',
 '1932',
 '1933',
 '1934',
 '1935',
 '1936',
 '1937',
 '1938',
 '1939',
 '1940',
 '1941',
 '1942',
 '1943',
 '1944',
 '1945',
 '1946',
 '1947',
 '1948',
 '1949',
 '1950',
 '1951',
 '1952',
 '1953',
 '1954',
 '1955',
 '1956',
 '1957',
 '1958',
 '1959',
 '1960',
 '1961',
 '1962',
 '1963',
 '1964',
 '1965',
 '1966',
 '1967',
 '1968',
 '1969',
 '1970',
 '1971',
 '1972',
 '1973',
 '1974',
 '1975',
 '1976',
 '1977',
 '1978',
 '1979',
```

```
'1980',
'1981',
'1982',
'1983',
'1984',
'1985',
'1986',
'1987',
'1988',
'1989',
'1990',
'1991',
'1992',
'1993',
'1994',
'1995',
'1996',
'1997',
'1998',
'1999',
'2000',
'2001',
'2002',
'2003',
'2004',
'2005',
'2006',
'2007',
'2008',
'2009']
```

Ok, lets pull in the name variable to see what we have

```
name = f.by_col('Name')
```

```
name
```

```
[ 'Alabama',
  'Arizona',
  'Arkansas',
  'California',
  'Colorado',
  'Connecticut',
  'Delaware',
  'Florida',
  'Georgia',
  'Idaho',
  'Illinois',
  'Indiana',
  'Iowa',
  'Kansas',
  'Kentucky',
  'Louisiana',
  'Maine',
  'Maryland',
  'Massachusetts',
  'Michigan',
  'Minnesota',
  'Mississippi',
  'Missouri',
  'Montana',
  'Nebraska',
  'Nevada',
  'New Hampshire',
  'New Jersey',
  'New Mexico',
  'New York',
  'North Carolina',
  'North Dakota',
  'Ohio',
  'Oklahoma',
  'Oregon',
  'Pennsylvania',
  'Rhode Island',
  'South Carolina',
  'South Dakota',
  'Tennessee',
  'Texas',
  'Utah',
  'Vermont',
  'Virginia',
  'Washington',
  'West Virginia',
  'Wisconsin',
  'Wyoming' ]
```

Now obtain per capital incomes in 1929 which is in the column associated with 1929

```
y1929 = f.by_col('1929')
```

```
y1929
```

```
[323,  
 600,  
 310,  
 991,  
 634,  
 1024,  
 1032,  
 518,  
 347,  
 507,  
 948,  
 607,  
 581,  
 532,  
 393,  
 414,  
 601,  
 768,  
 906,  
 790,  
 599,  
 286,  
 621,  
 592,  
 596,  
 868,  
 686,  
 918,  
 410,  
 1152,  
 332,  
 382,  
 771,  
 455,  
 668,  
 772,  
 874,  
 271,  
 426,  
 378,  
 479,  
 551,  
 634,  
 434,  
 741,  
 460,  
 673,  
 675]
```

And now 2009

```
y2009 = f.by_col("2009")
```

```
y2009
```

```
[32274,  
 32077,  
 31493,  
 40902,  
 40093,  
 52736,  
 40135,  
 36565,  
 33086,  
 30987,  
 40933,  
 33174,  
 35983,  
 37036,  
 31250,  
 35151,  
 35268,  
 47159,  
 49590,  
 34280,  
 40920,  
 29318,  
 35106,  
 32699,  
 37057,  
 38009,  
 41882,  
 48123,  
 32197,  
 46844,  
 33564,  
 38672,  
 35018,  
 33708,  
 35210,  
 38827,  
 41283,  
 30835,  
 36499,  
 33512,  
 35674,  
 30107,  
 36752,  
 43211,  
 40619,  
 31843,  
 35676,  
 42504]
```

These are read into regular Python lists which are not particularly well suited to efficient data analysis. So let's convert them to numpy arrays

```
y2009 = np.array(y2009)
```

```
y2009
```

```
array([32274, 32077, 31493, 40902, 40093, 52736, 40135, 36565, 33086,  
 30987, 40933, 33174, 35983, 37036, 31250, 35151, 35268, 47159,  
 49590, 34280, 40920, 29318, 35106, 32699, 37057, 38009, 41882,  
 48123, 32197, 46844, 33564, 38672, 35018, 33708, 35210, 38827,  
 41283, 30835, 36499, 33512, 35674, 30107, 36752, 43211, 40619,  
 31843, 35676, 42504])
```

Much better. But pulling these in and converting them a column at a time is tedious and error prone. So we will do all of this in a list comprehension.

```
Y = np.array( [ f.by_col(str(year)) for year in range(1929,2010) ] ) * 1.0
```

```
Y.shape
```

```
(81, 48)
```

```
Y = Y.transpose()
```

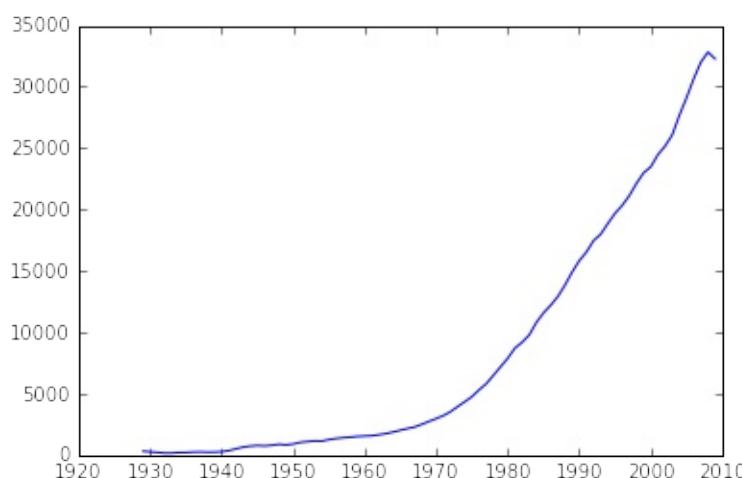
```
Y.shape
```

```
(48, 81)
```

```
years = np.arange(1929,2010)
```

```
plot(years,Y[0])
```

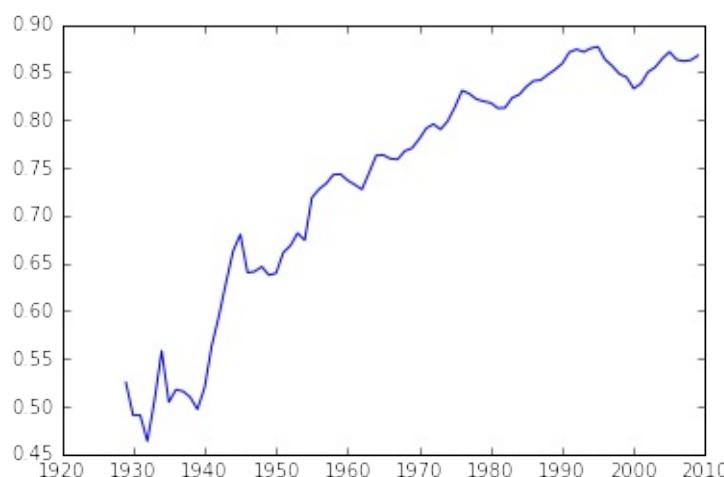
```
[<matplotlib.lines.Line2D at 0x7fcee352a1d0>]
```



```
RY = Y / Y.mean(axis=0)
```

```
plot(years,RY[0])
```

```
[<matplotlib.lines.Line2D at 0x7fcee342d690>]
```



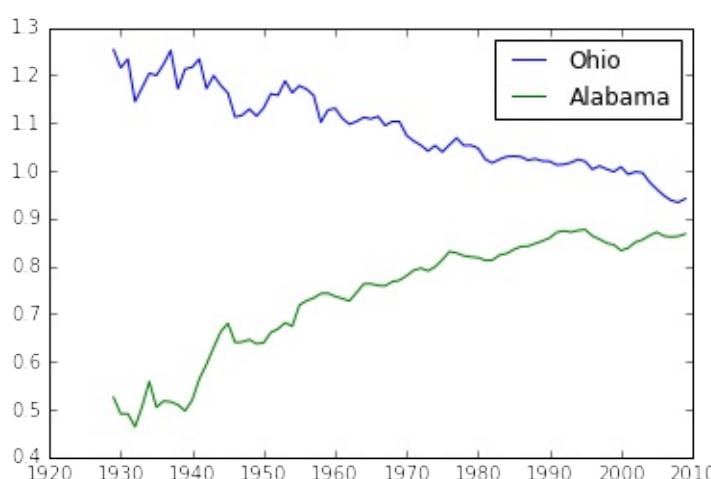
```
name = np.array(name)
```

```
np.nonzero(name=='Ohio')
```

```
(array([32]),)
```

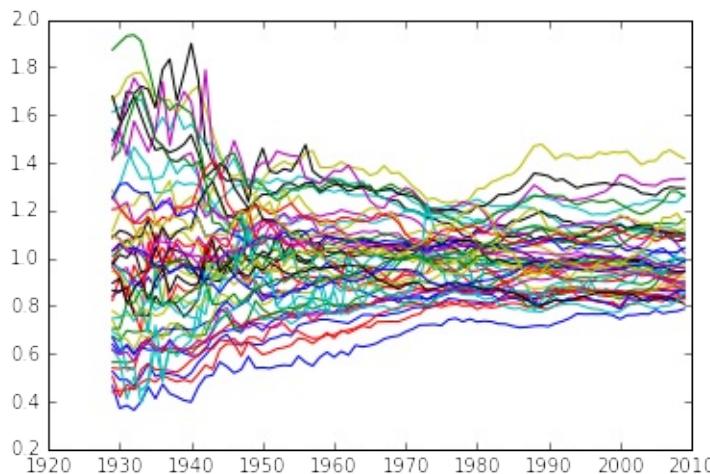
```
plot(years, RY[32], label='Ohio')
plot(years, RY[0], label='Alabama')
legend()
```

```
<matplotlib.legend.Legend at 0x7fcee3436890>
```



## Spaghetti Plot

```
for row in RY:
    plot(years, row)
```



## Kernel Density (univariate, aspatial)

```
from scipy.stats.kde import gaussian_kde
```

```
density = gaussian_kde(Y[:,0])
```

```
Y[:,0]
```

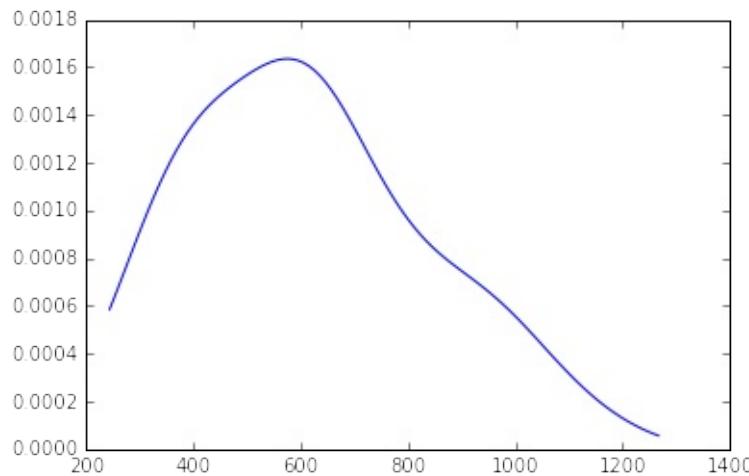
```
array([ 323.,  600.,  310.,  991.,  634., 1024., 1032.,  518.,
       347.,  507.,  948.,  607.,  581.,  532.,  393.,  414.,
      601.,  768.,  906.,  790.,  599.,  286.,  621.,  592.,
      596.,  868.,  686.,  918.,  410., 1152.,  332.,  382.,
      771.,  455.,  668.,  772.,  874.,  271.,  426.,  378.,
      479.,  551.,  634.,  434.,  741.,  460.,  673.,  675.])
```

```
density = gaussian_kde(Y[:,0])
```

```
minY0 = Y[:,0].min()*.90
maxY0 = Y[:,0].max()*1.10
x = np.linspace(minY0, maxY0, 100)
```

```
plot(x,density(x))
```

```
[<matplotlib.lines.Line2D at 0x7fcee3050350>]
```

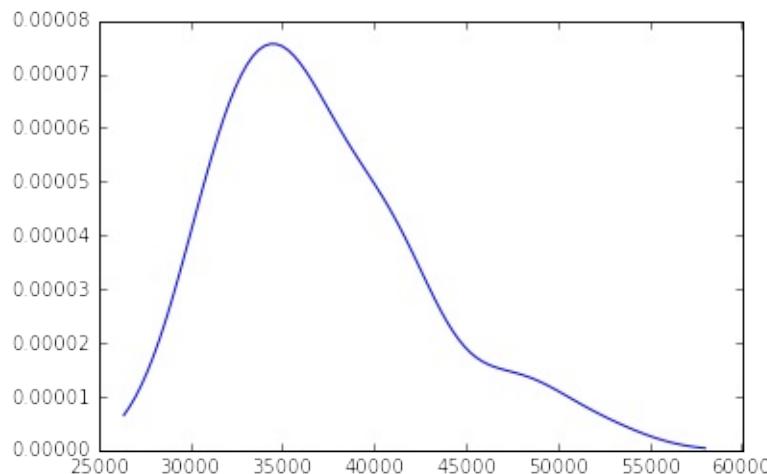


```
d2009 = gaussian_kde(Y[:, -1])
```

```
minY0 = Y[:, -1].min()*.90
maxY0 = Y[:, -1].max()*1.10
x = np.linspace(minY0, maxY0, 100)
```

```
plot(x,d2009(x))
```

```
[<matplotlib.lines.Line2D at 0x7fce178a5d0>]
```



```
minR0 = RY.min()
```

```
maxR0 = RY.max()
```

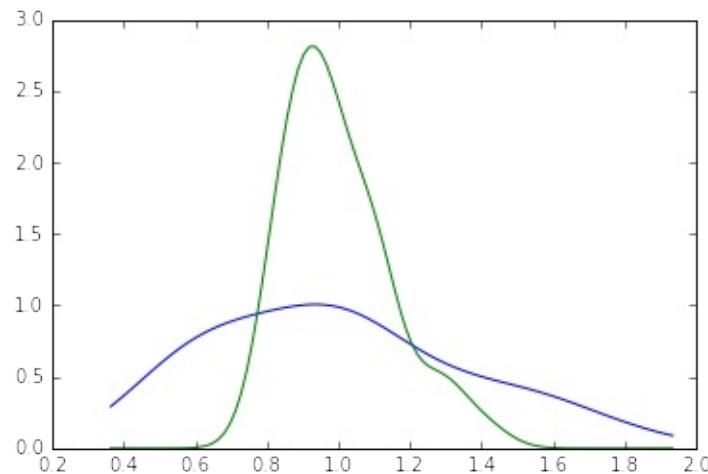
```
x = np.linspace(minR0, maxR0, 100)
```

```
d1929 = gaussian_kde(RY[:, 0])
```

```
d2009 = gaussian_kde(RY[:, -1])
```

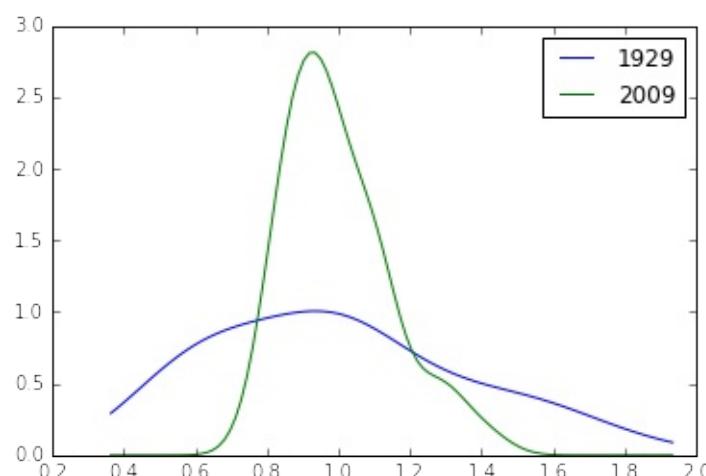
```
plot(x, d1929(x))
plot(x, d2009(x))
```

```
[<matplotlib.lines.Line2D at 0x7fce17c3c50>]
```

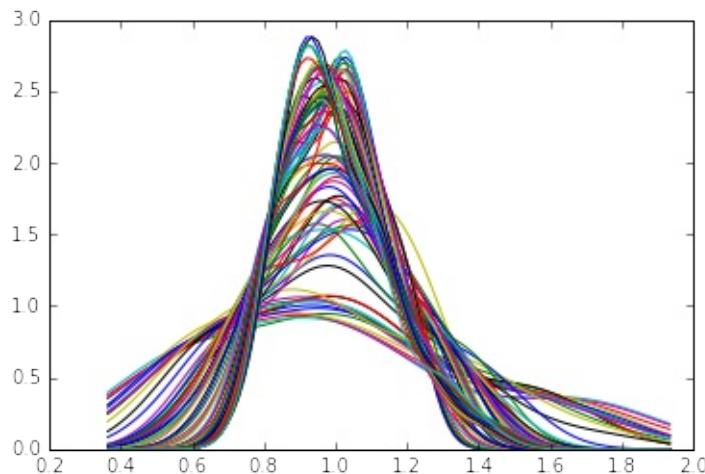


```
plot(x, d1929(x), label='1929')
plot(x, d2009(x), label='2009')
legend()
```

```
<matplotlib.legend.Legend at 0x7fce3161b50>
```

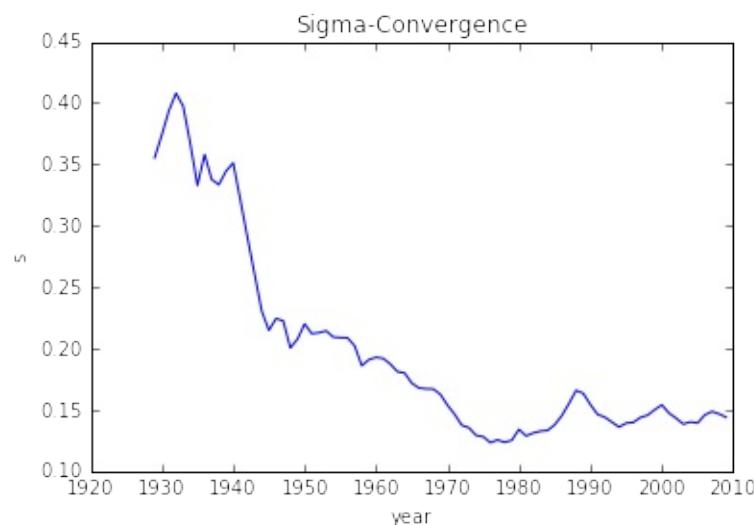


```
for cs in RY.T: # take cross sections
    plot(x, gaussian_kde(cs)(x))
```



```
sigma = RY.std(axis=0)
plot(years, sigma)
ylabel('s')
xlabel('year')
title("Sigma-Convergence")
```

<matplotlib.text.Text at 0x7fce14d13d0>



So the distribution is becoming less dispersed over time.

But what about internal mixing? Do poor (rich) states remain poor (rich), or is there movement within the distribution over time?

## Markov Chains

```
c = np.array([[b,a,c],
[c,c,a],
[c,b,c],
[a,a,b],
[a,b,c]])
```

c

```
array([['b', 'a', 'c'],
       ['c', 'c', 'a'],
       ['c', 'b', 'c'],
       ['a', 'a', 'b'],
       ['a', 'b', 'c']],
      dtype='|S1')
```

```
m = ps.Markov(c)
```

```
m.classes
```

```
array(['a', 'b', 'c'],
      dtype='|S1')
```

```
m.transitions
```

```
array([[ 1.,  2.,  1.],
       [ 1.,  0.,  2.],
       [ 1.,  1.,  1.]])
```

```
m.p
```

```
matrix([[ 0.25    ,  0.5     ,  0.25    ],
       [ 0.33333333,  0.        ,  0.66666667],
       [ 0.33333333,  0.33333333,  0.33333333]])
```

## State Per Capita Incomes

```
f = ps.open(ps.examples.get_path("usjoin.csv"))
pci = np.array([f.by_col[str(y)] for y in range(1929,2010)])
pci.shape
```

```
(81, 48)
```

Put series into cross-sectional quintiles (i.e., quintiles for each year)

```
q5 = np.array([ps.Quantiles(y).yb for y in pci]).transpose()
```

```
q5.shape
```

```
(48, 81)
```

```
q5[:,0]
```

```
array([0, 2, 0, 4, 2, 4, 4, 1, 0, 1, 4, 2, 2, 1, 0, 1, 2, 3, 4, 4, 2, 0, 2,
       2, 2, 4, 3, 4, 0, 4, 0, 0, 3, 1, 3, 3, 4, 0, 1, 0, 1, 2, 2, 1, 3, 1,
       3, 3])
```

```
pci.shape
```

```
(81, 48)
```

```
pci[0]
```

```
array([ 323, 600, 310, 991, 634, 1024, 1032, 518, 347, 507, 948,
       607, 581, 532, 393, 414, 601, 768, 906, 790, 599, 286,
       621, 592, 596, 868, 686, 918, 410, 1152, 332, 382, 771,
       455, 668, 772, 874, 271, 426, 378, 479, 551, 634, 434,
       741, 460, 673, 675])
```

we are looping over the rows of y which is ordered Txn (rows are cross sections, row 0 is the cross-section for period 0

```
m5 = ps.Markov(q5)
```

```
m5.classes
```

```
array([0, 1, 2, 3, 4])
```

```
m5.transitions
```

```
array([[ 729.,  71.,  1.,  0.,  0.],
       [ 72.,  567.,  80.,  3.,  0.],
       [ 0.,  81.,  631.,  86.,  2.],
       [ 0.,  3.,  86.,  573.,  56.],
       [ 0.,  0.,  1.,  57.,  741.]])
```

```
m5.p
```

```
matrix([[ 0.91011236,  0.0886392 ,  0.00124844,  0.      ,  0.      ],
       [ 0.09972299,  0.78531856,  0.11080332,  0.00415512,  0.      ],
       [ 0.      ,  0.10125 ,  0.78875 ,  0.1075 ,  0.0025 ],
       [ 0.      ,  0.00417827,  0.11977716,  0.79805014,  0.07799443],
       [ 0.      ,  0.      ,  0.00125156,  0.07133917,  0.92740926]])
```

```
m5.steady_state
```

```
matrix([[ 0.20774716],
       [ 0.18725774],
       [ 0.20740537],
       [ 0.18821787],
       [ 0.20937187]])
```

```
fmpt = ps.ergodic.fmpt(m5.p)
```

```
fmpt
```

```
matrix([[ 4.81354357, 11.50292712, 29.60921231, 53.38594954,
       103.59816743],
       [ 42.04774505, 5.34023324, 18.74455332, 42.50023268,
       92.71316899],
       [ 69.25849753, 27.21075248, 4.82147603, 25.27184624,
       75.43305672],
       [ 84.90689329, 42.85914824, 17.18082642, 5.31299186,
       51.60953369],
       [ 98.41295543, 56.36521038, 30.66046735, 14.21158356,
       4.77619083]])
```

For a state with income in the first quintile, it takes on average 11.5 years for it to first enter the second quintile, 29.6 to get to the third quintile, 53.4 years to enter the fourth, and 103.6 years to reach the richest quintile.

But, this approach assumes the movement of a state in the income distribution is independent of the movement of its neighbors or the position of the neighbors in the distribution. Does spatial context matter?

## Dynamics of Spatial Dependence

Read in a GAL file to construct our W

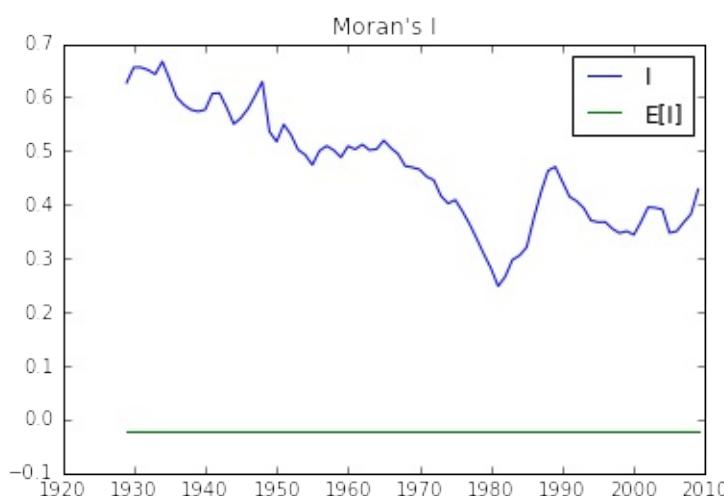
```
w = ps.open(ps.examples.get_path("states48.gal")).read()
w.n
w.transform = 'R'
```

```
mits = [ps.Moran(cs, w) for cs in RY.T]
```

```
res = np.array([(m.I, m.EI, m.p_sim, m.z_sim) for m in mits])
```

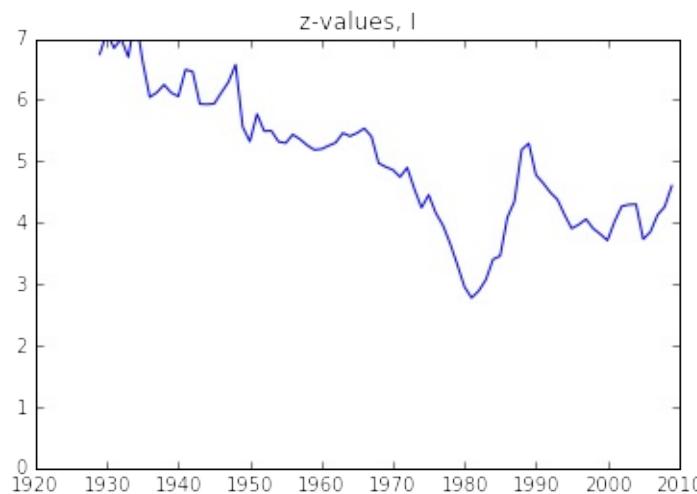
```
plot(years, res[:,0], label='I')
plot(years, res[:,1], label='E[I]')
title("Moran's I")
legend()
```

```
<matplotlib.legend.Legend at 0x7fce13b3c90>
```



```
plot(years, res[:, -1])
ylim(0, 7.0)
title('z-values, l')
```

<matplotlib.text.Text at 0x7fce12e2a90>



## Spatial Markov

```
pci.shape
```

(81, 48)

```
pci = pci.T
```

```
pci.shape
```

(48, 81)

```
rpci = pci / pci.mean(axis=0)
```

```
rpci[:, 0]
```

```
array([ 0.5250254 ,  0.97527938,  0.50389434,  1.61083644,  1.03054521,
       1.6644768 ,  1.67748053,  0.8419912 ,  0.56403657,  0.82411107,
       1.54094142,  0.98665764,  0.94439553,  0.86474771,  0.63880799,
       0.67294277,  0.97690484,  1.2483576 ,  1.47267186,  1.28411785,
       0.97365391,  0.46488317,  1.00941416,  0.96227565,  0.96877751,
       1.41090417,  1.11506942,  1.49217745,  0.66644091,  1.8725364 ,
       0.53965459,  0.62092787,  1.253234 ,  0.73958686,  1.08581104,
       1.25485946,  1.42065696,  0.44050119,  0.69244836,  0.61442601,
       0.77859804,  0.89563156,  1.03054521,  0.70545208,  1.20447003,
       0.74771419,  1.09393837,  1.0971893 ])
```

```
rpci[:, 0].mean()
```

```
0.9999999999999998
```

```
sm = ps.Spatial_Markov(rpc1, w, fixed=True, k=5)
```

```
sm.p
```

```
matrix([[ 0.91461837,  0.07503234,  0.00905563,  0.00129366,  0.      ],
       [ 0.06570302,  0.82654402,  0.10512484,  0.00131406,  0.00131406],
       [ 0.00520833,  0.10286458,  0.79427083,  0.09505208,  0.00260417],
       [ 0.      ,  0.00913838,  0.09399478,  0.84856397,  0.04830287],
       [ 0.      ,  0.      ,  0.      ,  0.06217617,  0.93782383]])
```

```
for p in sm.P:
    print(p)
```

```
[[ 0.96341463  0.0304878  0.00609756  0.      0.      ]
 [ 0.06040268  0.83221477  0.10738255  0.      0.      ]
 [ 0.      0.14      0.74      0.12      0.      ]
 [ 0.      0.03571429  0.32142857  0.57142857  0.07142857]
 [ 0.      0.      0.      0.16666667  0.83333333]]
 [[ 0.79831933  0.16806723  0.03361345  0.      0.      ]
 [ 0.0754717  0.88207547  0.04245283  0.      0.      ]
 [ 0.00537634  0.06989247  0.8655914  0.05913978  0.      ]
 [ 0.      0.      0.06372549  0.90196078  0.03431373]
 [ 0.      0.      0.      0.19444444  0.80555556]]
 [[ 0.84693878  0.15306122  0.      0.      0.      ]
 [ 0.08133971  0.78947368  0.1291866  0.      0.      ]
 [ 0.00518135  0.0984456  0.79274611  0.0984456  0.00518135]
 [ 0.      0.      0.09411765  0.87058824  0.03529412]
 [ 0.      0.      0.      0.10204082  0.89795918]]
 [[ 0.8852459  0.09836066  0.      0.01639344  0.      ]
 [ 0.03875969  0.81395349  0.13953488  0.      0.00775194]
 [ 0.0049505  0.09405941  0.77722772  0.11881188  0.0049505 ]
 [ 0.      0.02339181  0.12865497  0.75438596  0.09356725]
 [ 0.      0.      0.09661836  0.90338164]]
 [[ 0.33333333  0.66666667  0.      0.      0.      ]
 [ 0.0483871  0.77419355  0.16129032  0.01612903  0.      ]
 [ 0.01149425  0.16091954  0.74712644  0.08045977  0.      ]
 [ 0.      0.01036269  0.06217617  0.89637306  0.03108808]
 [ 0.      0.      0.02352941  0.97647059]]]
```

```
sm.S
```

```
array([[ 0.43509425,  0.2635327 ,  0.20363044,  0.06841983,  0.02932278],
       [ 0.13391287,  0.33993305,  0.25153036,  0.23343016,  0.04119356],
       [ 0.12124869,  0.21137444,  0.2635101 ,  0.29013417,  0.1137326 ],
       [ 0.0776413 ,  0.19748806,  0.25352636,  0.22480415,  0.24654013],
       [ 0.01776781,  0.19964349,  0.19009833,  0.25524697,  0.3372434 ]])
```

```
for f in sm.F:
    print(f)
```

```
[[ 2.29835259 28.95614035 46.14285714 80.80952381 279.42857143]
 [ 33.86549708 3.79459555 22.57142857 57.23809524 255.85714286]
 [ 43.60233918 9.73684211 4.91085714 34.66666667 233.28571429]
 [ 46.62865497 12.76315789 6.25714286 14.61564626 198.61904762]
 [ 52.62865497 18.76315789 12.25714286 6. 34.1031746 ]]
[[ 7.46754205 9.70574606 25.76785714 74.53116883 194.23446197]
 [ 27.76691978 2.94175577 24.97142857 73.73474026 193.4380334 ]
 [ 53.57477715 28.48447637 3.97566318 48.76331169 168.46660482]
 [ 72.03631562 46.94601483 18.46153846 4.28393653 119.70329314]
 [ 77.17917276 52.08887197 23.6043956 5.14285714 24.27564033]]
[[ 8.24751154 6.53333333 18.38765432 40.70864198 112.76732026]
 [ 47.35040872 4.73094099 11.85432099 34.17530864 106.23398693]
 [ 69.42288828 24.76666667 3.794921 22.32098765 94.37966594]
 [ 83.72288828 39.06666667 14.3 3.44668119 76.36702977]
 [ 93.52288828 48.86666667 24.1 9.8 8.79255406]]
[[ 12.87974382 13.34847151 19.83446328 28.47257282 55.82395142]
 [ 99.46114206 5.06359731 10.54545198 23.05133495 49.68944423]
 [ 117.76777159 23.03735526 3.94436301 15.0843986 43.57927247]
 [ 127.89752089 32.4393006 14.56853107 4.44831643 31.63099455]
 [ 138.24752089 42.7893006 24.91853107 10.35 4.05613474]]
[[ 56.2815534 1.5 10.57236842 27.02173913 110.54347826]
 [ 82.9223301 5.00892857 9.07236842 25.52173913 109.04347826]
 [ 97.17718447 19.53125 5.26043557 21.42391304 104.94565217]
 [ 127.1407767 48.74107143 33.29605263 3.91777427 83.52173913]
 [ 169.6407767 91.24107143 75.79605263 42.5 2.96521739]]

```

## LISA Markov

```
lm = ps.LISA_Markov(pci,w)
```

```
lm.classes
```

```
array([1, 2, 3, 4])
```

```
lm.transitions
```

```
array([[ 1.08700000e+03, 4.40000000e+01, 4.00000000e+00,
       3.40000000e+01],
       [ 4.10000000e+01, 4.70000000e+02, 3.60000000e+01,
       1.00000000e+00],
       [ 5.00000000e+00, 3.40000000e+01, 1.42200000e+03,
       3.90000000e+01],
       [ 3.00000000e+01, 1.00000000e+00, 4.00000000e+01,
       5.52000000e+02]])
```

```
np.set_printoptions(3, suppress=True)
```

```
lm.transitions
```

```
array([[ 1087., 44., 4., 34.],
       [ 41., 470., 36., 1.],
       [ 5., 34., 1422., 39.],
       [ 30., 1., 40., 552.]])
```

```
lm.p
```

```
matrix([[ 0.93 ,  0.038,  0.003,  0.029],
       [ 0.075,  0.858,  0.066,  0.002],
       [ 0.003,  0.023,  0.948,  0.026],
       [ 0.048,  0.002,  0.064,  0.886]])
```

```
lm.steady_state
```

```
matrix([[ 0.286],
       [ 0.142],
       [ 0.405],
       [ 0.168]])
```

```
ps.ergodic.fmpt(lm.p)
```

```
matrix([[ 3.501, 37.93 , 40.558, 43.174],
       [ 31.728, 7.047, 28.682, 49.915],
       [ 52.445, 47.421, 2.47 , 43.756],
       [ 38.768, 51.518, 26.316, 5.969]])
```

## Test of independence of own chains and lag chains

```
lm.transitions
```

```
array([[ 1087.,   44.,    4.,   34.],
       [  41.,  470.,   36.,    1.],
       [  5.,   34., 1422.,   39.],
       [ 30.,    1.,   40.,  552.]])
```

```
lm.expected_t
```

```
array([[ 1123.281,   11.538,   0.348,   33.834],
       [  3.503,  528.474,  15.918,   0.106],
       [  0.154,  23.216, 1466.907,   9.723],
       [  9.608,   0.099,   6.235,  607.058]])
```

```
lm.chi_2
```

```
(1058.2079036003051, 0.0, 9)
```



## **Part II**

# Point Patterns

IPYNB

This notebook covers a brief introduction on how to visualize and analyze point patterns. To demonstrate this, we will use a dataset of all the AirBnb listings in the city of Austin (check the Data section for more information about the dataset).

Before anything, let us load up the libraries we will use:

```
%matplotlib inline

import numpy as np
import pandas as pd
import geopandas as gpd
import seaborn as sns
import matplotlib.pyplot as plt
import folium
```

```
/home/dani/anaconda/envs/pydata/lib/python2.7/site-packages/matplotlib/font_manager.py:273: UserWarning: Matplotlib is building the font cache using fc-list. This may take a moment.
```

```
warnings.warn('Matplotlib is building the font cache using fc-list. This may take a moment.'
```

## Data preparation

Let us first set the paths to the datasets we will be using:

```
# Adjust this to point to the right file in your computer
listings_link = '../data/listings.csv.gz'
```

The core dataset we will use is `listings.csv`, which contains a lot of information about each individual location listed at AirBnb within Austin:

```
lst = pd.read_csv(listings_link)
lst.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 5835 entries, 0 to 5834
Data columns (total 92 columns):
id              5835 non-null int64
listing_url     5835 non-null object
scrape_id       5835 non-null int64
last_scraped    5835 non-null object
name            5835 non-null object
summary         5373 non-null object
space           4475 non-null object
description     5832 non-null object
experiences_offered 5835 non-null object
neighborhood_overview 3572 non-null object
notes           2413 non-null object
transit          3492 non-null object
thumbnail_url   5542 non-null object
medium_url      5542 non-null object
picture_url     5835 non-null object
xl_picture_url 5542 non-null object
host_id          5835 non-null int64
host_url         5835 non-null object
host_name        5820 non-null object
host_since       5820 non-null object
```

host_location	5810 non-null object
host_about	3975 non-null object
host_response_time	4177 non-null object
host_response_rate	4177 non-null object
host_acceptance_rate	3850 non-null object
host_is_superhost	5820 non-null object
host_thumbnail_url	5820 non-null object
host_picture_url	5820 non-null object
host_neighbourhood	4977 non-null object
host_listings_count	5820 non-null float64
host_total_listings_count	5820 non-null float64
host_verifications	5835 non-null object
host_has_profile_pic	5820 non-null object
host_identity_verified	5820 non-null object
street	5835 non-null object
neighbourhood	4800 non-null object
neighbourhood_cleansed	5835 non-null int64
neighbourhood_group_cleansed	0 non-null float64
city	5835 non-null object
state	5835 non-null object
zipcode	5810 non-null float64
market	5835 non-null object
smart_location	5835 non-null object
country_code	5835 non-null object
country	5835 non-null object
latitude	5835 non-null float64
longitude	5835 non-null float64
is_location_exact	5835 non-null object
property_type	5835 non-null object
room_type	5835 non-null object
accommodates	5835 non-null int64
bathrooms	5789 non-null float64
bedrooms	5829 non-null float64
beds	5812 non-null float64
bed_type	5835 non-null object
amenities	5835 non-null object
square_feet	302 non-null float64
price	5835 non-null object
weekly_price	2227 non-null object
monthly_price	1717 non-null object
security_deposit	2770 non-null object
cleaning_fee	3587 non-null object
guests_included	5835 non-null int64
extra_people	5835 non-null object
minimum_nights	5835 non-null int64
maximum_nights	5835 non-null int64
calendar_updated	5835 non-null object
has_availability	5835 non-null object
availability_30	5835 non-null int64
availability_60	5835 non-null int64
availability_90	5835 non-null int64
availability_365	5835 non-null int64
calendar_last_scraped	5835 non-null object
number_of_reviews	5835 non-null int64
first_review	3827 non-null object
last_review	3829 non-null object
review_scores_rating	3789 non-null float64
review_scores_accuracy	3776 non-null float64
review_scores_cleanliness	3778 non-null float64
review_scores_checkin	3778 non-null float64
review_scores_communication	3778 non-null float64
review_scores_location	3779 non-null float64
review_scores_value	3778 non-null float64
requires_license	5835 non-null object
license	1 non-null float64
jurisdiction_names	0 non-null float64
instant_bookable	5835 non-null object
cancellation_policy	5835 non-null object
require_guest_profile_picture	5835 non-null object
require_guest_phone_verification	5835 non-null object
calculated_host_listings_count	5835 non-null int64
reviews_per_month	3827 non-null float64

```
dtypes: float64(20), int64(14), object(58)
memory usage: 4.1+ MB
```

It turns out that one record displays a very odd location and, for the sake of the illustration, we will remove it:

```
odd = lst.loc[lst.longitude>-80, ['longitude', 'latitude']]
odd
```

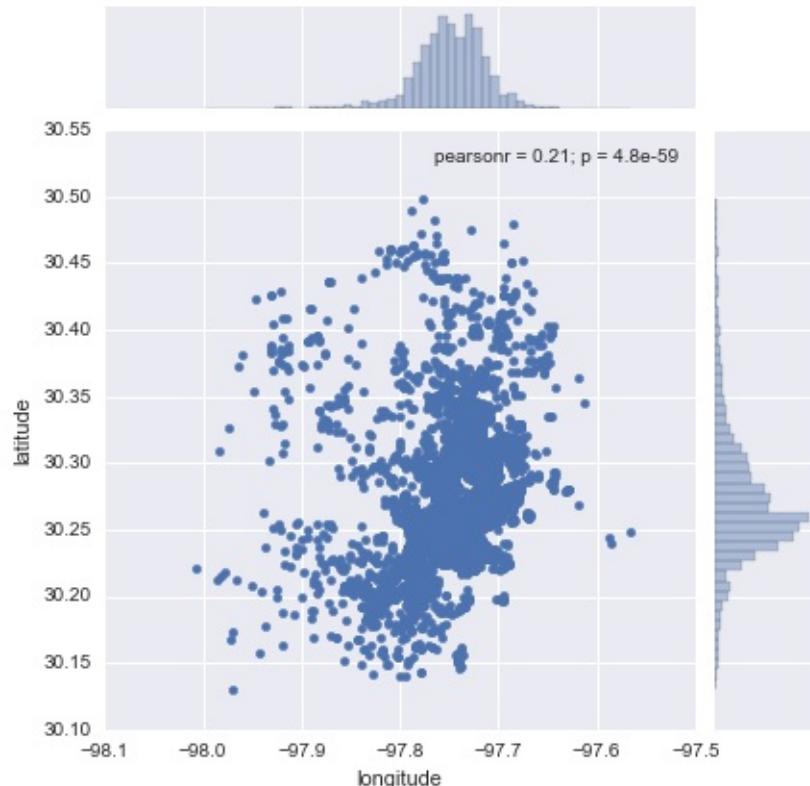
	<b>longitude</b>	<b>latitude</b>
<b>5832</b>	-5.093682	43.214991

```
lst = lst.drop(odd.index)
```

## Point Visualization

The most straightforward way to get a first glimpse of the distribution of the data is to plot their latitude and longitude:

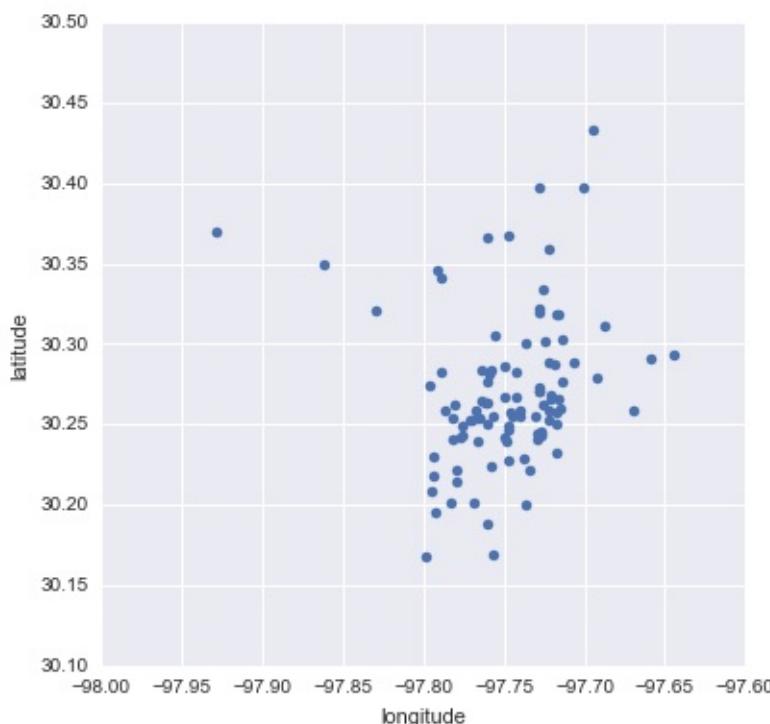
```
sns.jointplot(x="longitude", y="latitude", data=lst);
```



Now this does not necessarily tell us much about the dataset or the distribution of locations within Austin. There are two main challenges in interpreting the plot: one, there is lack of context, which means the points are not identifiable over space (unless you are so familiar with lon/lat pairs that they have a clear meaning to you); and two, in the center of the plot, there are so many points that it is hard to tell any pattern other than a big blurb of blue.

Let us first focus on the first problem, geographical context. The quickest and easiest way to provide context to this set of points is to overlay a general map. If we had an image with the map or a set of several data sources that we could aggregate to create a map, we could build it from scratch. But in the XXI Century, the easiest is to overlay our point dataset on top of a web map. In this case, we will use [Leaflet](#), and we will convert our underlying `matplotlib` points with `mplleaflet`. The full dataset (+5k observations) is a bit too much for leaflet to plot it directly on screen, so we will obtain a random sample of 100 points:

```
# NOTE: `mplleaflet.display` turned off to be able to compile the website,
#       comment out the last line of this cell for rendering Leaflet map.
rids = np.arange(lst.shape[0])
np.random.shuffle(rids)
f, ax = plt.subplots(1, figsize=(6, 6))
lst.iloc[rids[:100], :].plot(kind='scatter', x='longitude', y='latitude', \
    s=30, linewidth=0, ax=ax);
#mplleaflet.display(fig=f,)
```



This map allows us to get a much better sense of where the points are and what type of location they might be in. For example, now we can see that the big blue blurb has to do with the urbanized core of Austin.

## bokeh alternative

Leaflet is not the only technology to display data on maps, although it is probably the default option in many cases. When the data is larger than "acceptable", we need to resort to more technically sophisticated alternatives. One option is provided by `bokeh` and its `datashaded` submodule (see [here](#) for a very nice introduction to the library, from where this example has been adapted).

Before we delve into `bokeh`, let us reproject our original data (lon/lat coordinates) into Web Mercator, as `bokeh` will expect them. To do that, we turn the coordinates into a `GeoSeries`:

```
from shapely.geometry import Point
xys_wb = gpd.GeoSeries(lst[['longitude', 'latitude']].apply(Point, axis=1), \
    crs="+init=epsg:4326")
xys_wb = xys_wb.to_crs(epsg=3857)
x_wb = xys_wb.apply(lambda i: i.x)
y_wb = xys_wb.apply(lambda i: i.y)
```

Now we are ready to setup the plot in `bokeh`:

```
from bokeh.plotting import figure, output_notebook, show
from bokeh.tile_providers import STAMEN_TERRAIN
output_notebook()

minx, miny, maxx, maxy = xys_wb.total_bounds
y_range = miny, maxy
x_range = minx, maxx

def base_plot(tools='pan,wheel_zoom,reset', plot_width=600, plot_height=400, **plot_args):
    p = figure(tools=tools, plot_width=plot_width, plot_height=plot_height,
        x_range=x_range, y_range=y_range, outline_line_color=None,
        min_border=0, min_border_left=0, min_border_right=0,
        min_border_top=0, min_border_bottom=0, **plot_args)

    p.axis.visible = False
    p.xgrid.grid_line_color = None
    p.ygrid.grid_line_color = None
    return p

options = dict(line_color=None, fill_color="#800080", size=4)
```

```
<div class="bk-banner">
    <a href="http://bokeh.pydata.org" target="_blank" class="bk-logo bk-logo-small bk-logo-notebook"></a>
    <span id="a0125a61-aa40-4d88-9db2-d2b800c39acb">Loading BokehJS ...</span>
</div>
```

And good to go for mapping!

```
# NOTE: `show` turned off to be able to compile the website,
#       comment out the last line of this cell for rendering.
p = base_plot()
p.add_tile(STAMEN_TERRAIN)
p.circle(x=x_wb, y=y_wb, **options)
#show(p)
```

```
<bokeh.models.renderers.GlyphRenderer at 0x7f6c701fa7d0>
```

As you can quickly see, `bokeh` is substantially faster at rendering larger amounts of data.

The second problem we have spotted with the first scatter is that, when the number of points grows, at some point it becomes impossible to discern anything other than a big blur of color. To some extent, interactivity gets at that problem by allowing the user to zoom in until every point is an entity on its own. However, there exist techniques that allow to summarize the data to be able to capture the overall pattern at once. Traditionally, kernel density estimation (KDE) has been one of the most common solutions by approximating a continuous surface of point intensity. In this context, however, we will explore a more recent alternative suggested by the `datashader` library (see the [paper](#) if interested in more details).

Arguably, our dataset is not large enough to justify the use of a reduction technique like `datashader`, but we will create the plot for the sake of the illustration. Keep in mind, the usefulness of this approach increases the more points you need to be plotting.

```
# NOTE: `show` turned off to be able to compile the website,
#       comment out the last line of this cell for rendering.

import datashader as ds
from datashader.callbacks import InteractiveImage
from datashader.colors import viridis
from datashader import transfer_functions as tf
from bokeh.tile_providers import STAMEN_TONER

p = base_plot()
p.add_tile(STAMEN_TONER)

pts = pd.DataFrame({'x': x_wb, 'y': y_wb})
pts['count'] = 1

def create_image90(x_range, y_range, w, h):
    cvs = ds.Canvas(plot_width=w, plot_height=h, x_range=x_range, y_range=y_range)
    agg = cvs.points(pts, 'x', 'y', ds.count('count'))
    img = tf.interpolate(agg.where(agg > np.percentile(agg, 90)), \
        cmap=viridis, how='eq_hist')
    return tf.dynspread(img, threshold=0.1, max_px=4)

#InteractiveImage(p, create_image90)
```

The key advantage of `datashader` is that it decouples the point processing from the plotting. That is the bit that allows it to be scalable to truly large datasets (e.g. millions of points). Essentially, the approach is based on generating a very fine grid, counting points within pixels, and encoding the count into a color scheme. In our map, this is not particularly effective because we do not have too many points (the previous plot is probably a more effective one) and essentially there is a pixel per location of every point. However, hopefully this example shows how to create this kind of scalable maps.

## Centrography and distance based statistics

### Exercise

*Split the dataset by type of property and create a map for the five most common types.*

Consider the following sorting of property types:

```
lst.property_type.groupby(lst.property_type)\n    .count()\n    .sort_values(ascending=False)
```

property_type	
House	3549
Apartment	1855
Condominium	106
Loft	83
Townhouse	57
Other	47
Bed & Breakfast	37
Camper/RV	34
Bungalow	18
Cabin	17
Tent	11
Villa	7
Treehouse	7
Earth House	2
Chalet	1
Hut	1
Boat	1
Tipi	1

Name: property\_type, dtype: int64



# Spatial Clustering

IPYNB

**NOTE:** much of this material has been ported and adapted from "Lab 8" in [Arribas-Bel \(2016\)](#).

This notebook covers a brief introduction to spatial regression. To demonstrate this, we will use a dataset of all the AirBnb listings in the city of Austin (check the Data section for more information about the dataset).

Many questions and topics are complex phenomena that involve several dimensions and are hard to summarize into a single variable. In statistical terms, we call this family of problems *multivariate*, as opposed to *univariate* cases where only a single variable is considered in the analysis. Clustering tackles this kind of questions by reducing their dimensionality -the number of relevant variables the analyst needs to look at- and converting it into a more intuitive set of classes that even non-technical audiences can look at and make sense of. For this reason, it is widely used in applied contexts such as policymaking or marketing. In addition, since these methods do not require many preliminary assumptions about the structure of the data, it is a commonly used exploratory tool, as it can quickly give clues about the shape, form and content of a dataset.

The core idea of statistical clustering is to summarize the information contained in several variables by creating a relatively small number of categories. Each observation in the dataset is then assigned to one, and only one, category depending on its values for the variables originally considered in the classification. If done correctly, the exercise reduces the complexity of a multi-dimensional problem while retaining all the meaningful information contained in the original dataset. This is because, once classified, the analyst only needs to look at in which category every observation falls into, instead of considering the multiple values associated with each of the variables and trying to figure out how to put them together in a coherent sense. When the clustering is performed on observations that represent areas, the technique is often called geodemographic analysis.

The basic premise of the exercises we will be doing in this notebook is that, through the characteristics of the houses listed in AirBnb, we can learn about the geography of Austin. In particular, we will try to classify the city's zipcodes into a small number of groups that will allow us to extract some patterns about the main kinds of houses and areas in the city.

## Data

Before anything, let us load up the libraries we will use:

```
%matplotlib inline

import seaborn as sns
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import pysal as ps
import geopandas as gpd
from sklearn import cluster
from sklearn.preprocessing import scale

sns.set(style="whitegrid")
```

Let us also set the paths to all the files we will need throughout the tutorial:

```
# Adjust this to point to the right file in your computer
abb_link = './data/listings.csv.gz'
zc_link = './data/Zipcodes.geojson'
```

Before anything, let us load the main dataset:

```
lst = pd.read_csv(link)
```

Originally, this is provided at the individual level. Since we will be working in terms of neighborhoods and areas, we will need to aggregate them to that level. For this illustration, we will be using the following subset of variables:

```
varis = ['bedrooms', 'bathrooms', 'beds']
```

This will allow us to capture the main elements that describe the "look and feel" of a property and, by aggregation, of an area or neighborhood. All of the variables above are numerical values, so a sensible way to aggregate them is by obtaining the average (of bedrooms, etc.) per zipcode.

```
aves = lst.groupby('zipcode')[varis].mean()
aves.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Float64Index: 47 entries, 33558.0 to 78759.0
Data columns (total 3 columns):
bedrooms    47 non-null float64
bathrooms   47 non-null float64
beds        47 non-null float64
dtypes: float64(3)
memory usage: 1.5 KB
```

In addition to these variables, it would be good to include also a sense of what proportions of different types of houses each zipcode has. For example, one can imagine that neighborhoods with a higher proportion of condos than single-family homes will probably look and feel more urban. To do this, we need to do some data munging:

```
types = pd.get_dummies(lst['property_type'])
prop_types = types.join(lst['zipcode'])\
    .groupby('zipcode')\
    .sum()
prop_types_pct = (prop_types * 100.).div(prop_types.sum(axis=1), axis=0)
prop_types_pct.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Float64Index: 47 entries, 33558.0 to 78759.0
Data columns (total 18 columns):
Apartment      47 non-null float64
Bed & Breakfast 47 non-null float64
Boat           47 non-null float64
Bungalow       47 non-null float64
Cabin          47 non-null float64
Camper/RV      47 non-null float64
Chalet         47 non-null float64
Condominium    47 non-null float64
Earth House    47 non-null float64
House          47 non-null float64
Hut            47 non-null float64
Loft           47 non-null float64
Other          47 non-null float64
Tent           47 non-null float64
Tipi           47 non-null float64
Townhouse      47 non-null float64
Treehouse      47 non-null float64
Villa          47 non-null float64
dtypes: float64(18)
memory usage: 7.0 KB
```

Now we bring both sets of variables together:

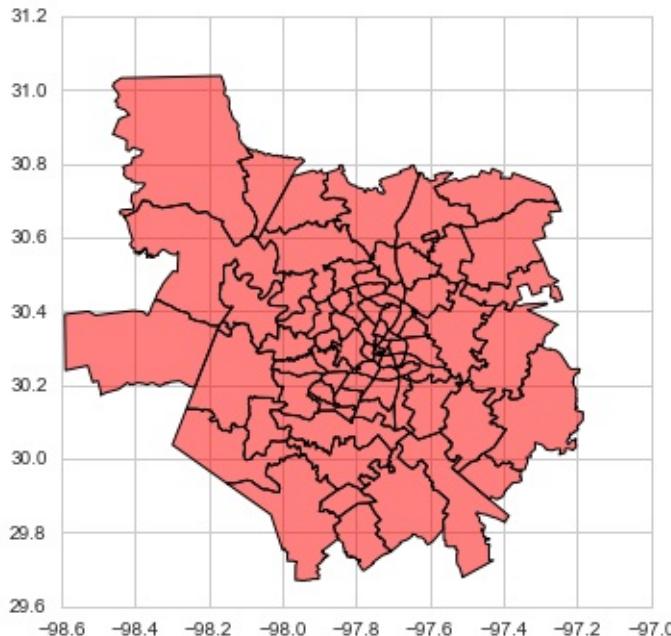
```
aves_props = aves.join(prop_types_pct)
```

And since we will be feeding this into the clustering algorithm, we will first standardize the columns:

```
db = pd.DataFrame(\n    scale(aves_props), \\ \n    index=aves_props.index, \\ \n    columns=aves_props.columns)\\ \n    .rename(lambda x: str(int(x)))
```

Now let us bring geography in:

```
zc = gpd.read_file(zc_link)\nzc.plot(color='red');
```



And combine the two:

```
zdb = zc[['geometry', 'zipcode', 'name']].join(db, on='zipcode')\
    .dropna()
```

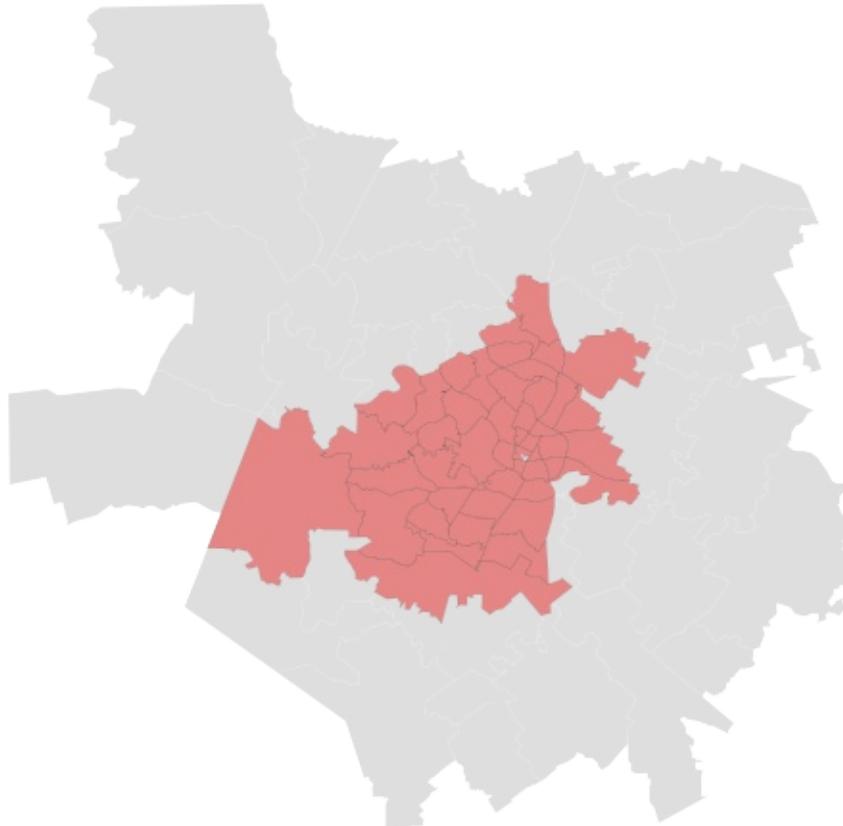
To get a sense of which areas we have lost:

```
f, ax = plt.subplots(1, figsize=(9, 9))

zc.plot(color='grey', linewidth=0, ax=ax)
zdb.plot(color='red', linewidth=0.1, ax=ax)

ax.set_axis_off()

plt.show()
```



## Geodemographic analysis

The main intuition behind geodemographic analysis is to group disparate areas of a city or region into a small set of classes that capture several characteristics shared by those in the same group. By doing this, we can get a new perspective not only on the types of areas in a city, but on how they are distributed over space. In the context of our AirBnb data analysis, the idea is that we can group different zipcodes of Austin based on the type of houses listed on the website. This will give us a hint into the geography of AirBnb in the Texan tech capital.

Although there exist many techniques to statistically group observations in a dataset, all of them are based on the premise of using a set of attributes to define classes or categories of observations that are similar *within* each of them, but differ *between* groups. How similarity within groups and dissimilarity between them is defined and how the classification algorithm is operationalized is what makes techniques differ and also what makes each of them particularly well suited for specific problems or types of data. As an illustration, we will only dip our toes into one of these methods, K-means, which is probably the most commonly used technique for statistical clustering.

Technically speaking, we describe the method and the parameters on the following line of code, where we specifically ask for five groups:

```
km5 = cluster.KMeans(n_clusters=5)
```

Following the `sklearn` pipeline approach, all the heavy-lifting of the clustering happens when we `fit` the model to the data:

```
km5cls = km5.fit(zdb.drop(['geometry', 'name'], axis=1).values)
```

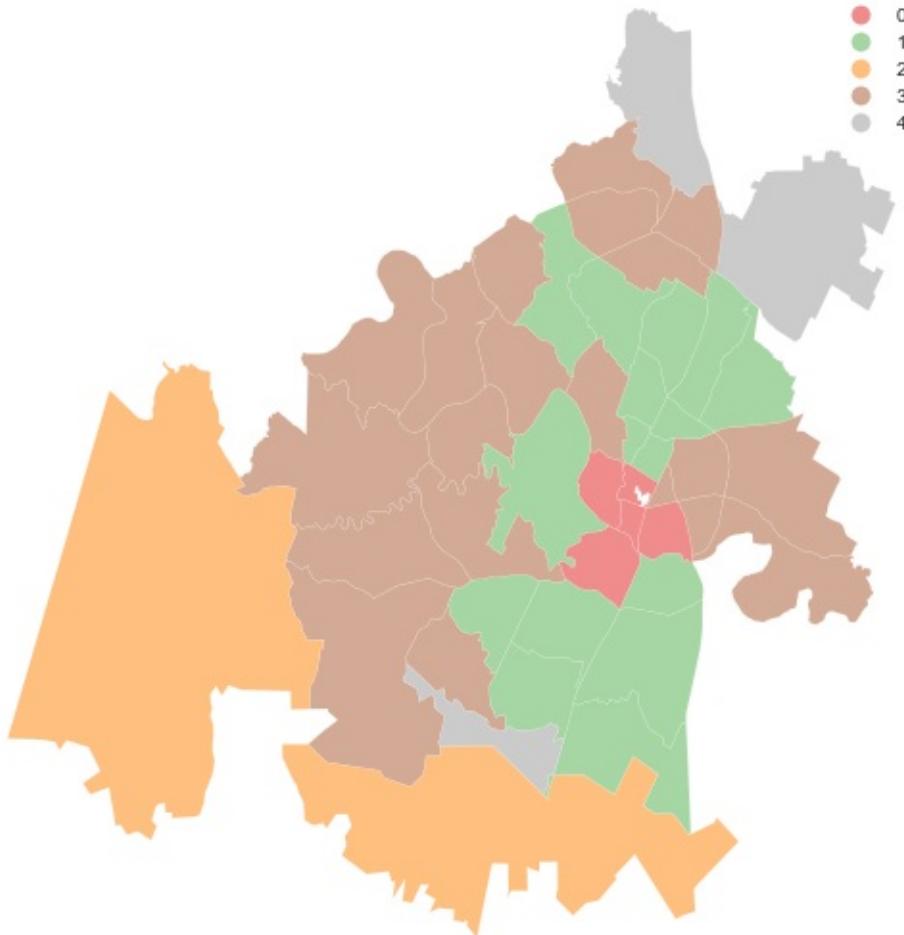
Now we can extract the classes and put them on a map:

```
f, ax = plt.subplots(1, figsize=(9, 9))

zdb.assign(cl=km5cls.labels_)\n    .plot(column='cl', categorical=True, legend=True,\n          linewidth=0.1, edgecolor='white', ax=ax)

ax.set_axis_off()

plt.show()
```

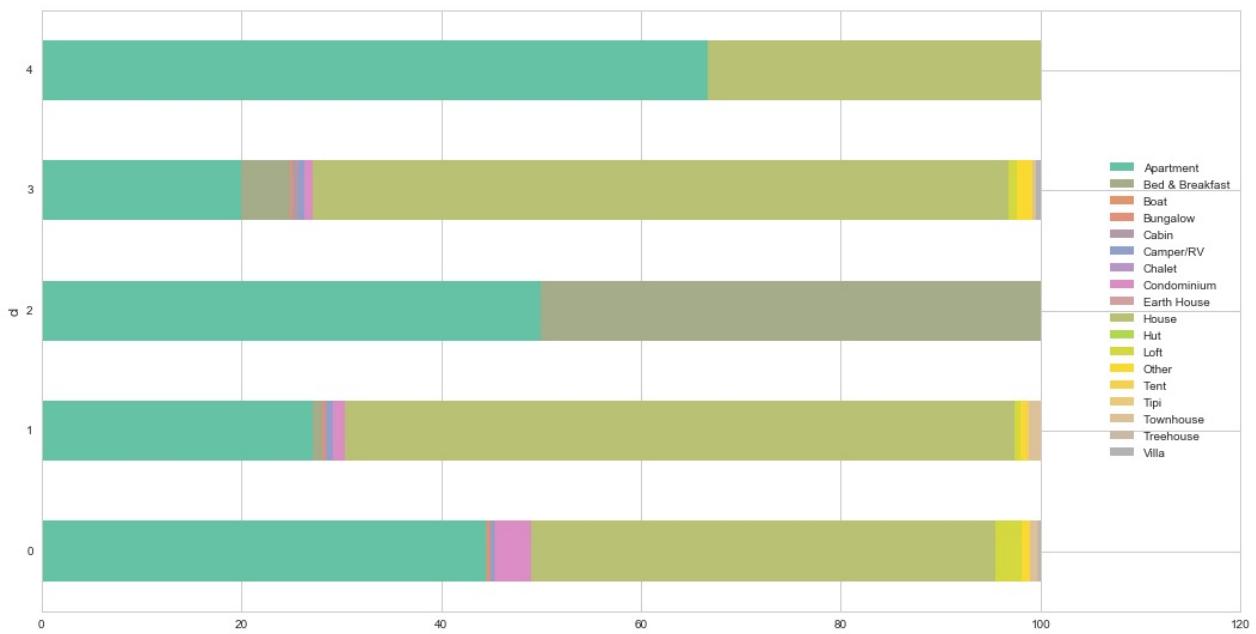


The map above shows a clear pattern: there is a class at the core of the city (number 0, in red), then two other ones in a sort of "urban ring" (number 1 and 3, in green and brown, respectively), and two peripheral sets of areas (number 2 and 4, yellow and green).

This gives us a good insight into the geographical structure, but does not tell us much about what are the defining elements of these groups. To do that, we can have a peak into the characteristics of the classes. For example, let us look at how the proportion of different types of properties are distributed across clusters:

```
cl_pcts = prop_types_pct.rename(lambda x: str(int(x)))\
    .reindex(zdb['zipcode'])\
    .assign(cl=km5cls.labels_)\
    .groupby('cl')\
    .mean()
```

```
f, ax = plt.subplots(1, figsize=(18, 9))
cl_pcts.plot(kind='barh', stacked=True, ax=ax, \
    cmap='Set2', linewidth=0)
ax.legend(ncol=1, loc="right");
```



A few interesting, albeit maybe not completely unsurprising, characteristics stand out. First, most of the locations we have in the dataset are either apartments or houses. However, how they are distributed is interesting. The urban core -cluster 0- distinctively has the highest proportion of condos and lofts. The suburban ring -clusters 1 and 3- is very consistent, with a large share of houses and less apartments, particularly so in the case of cluster 3. Class 4 has only two types of properties, houses and apartments, suggesting there are not that many places listed at Airbnb. Finally, class 3 arises as a more rural and leisure one: beyond apartmentes, it has a large share of bed & breakfasts.

#### Mini Exercise

*What are the average number of beds, bedrooms and bathrooms for every class?*

## Regionalization analysis: building (meaningful) regions

In the case of analysing spatial data, there is a subset of methods that are of particular interest for many common cases in Geographic Data Science. These are the so-called regionalization techniques.

Regionalization methods can take also many forms and faces but, at their core, they all involve statistical clustering of observations with the additional constraint that observations need to be geographical neighbors to be in the same category. Because of this, rather than category, we will use the term area for each observation and region for each class or cluster -hence regionalization, the construction of regions from smaller areas.

As in the non-spatial case, there are many different algorithms to perform regionalization, and they all differ on details relating to the way they measure (dis)similarity, the process to regionalize, etc. However, same as above too, they all share a few common aspects. In particular, they all take a set of input attributes *and* a representation of space in the form of a binary spatial weights matrix. Depending on the algorithm, they also require the desired number of output regions into which the areas are aggregated.

In this example, we are going to create aggregations of zipcodes into groups that have areas where the Airbnb listed location have similar ratings. In other words, we will create delineations for the "quality" or "satisfaction" of Airbnb users. In other words, we will explore what are the boundaries that separate areas where Airbnb users tend to be satisfied about their experience versus those where the ratings are not as high. To do this, we will focus on the `review_scores_X` set of variables in the original dataset:

```
ratings = [i for i in lst if 'review_scores_' in i]
ratings
```

```
['review_scores_rating',
 'review_scores_accuracy',
 'review_scores_cleanliness',
 'review_scores_checkin',
 'review_scores_communication',
 'review_scores_location',
 'review_scores_value']
```

Similarly to the case above, we now bring this at the zipcode level. Note that, since they are all scores that range from 0 to 100, we can use averages and we do not need to standardize.

```
rt_av = lst.groupby('zipcode')[ratings]\n    .mean()\n    .rename(lambda x: str(int(x)))
```

And we link these to the geometries of zipcodes:

```
zrt = zc[['geometry', 'zipcode']].join(rt_av, on='zipcode')\n    .dropna()\n\nzrt.info()
```

```
<class 'geopandas.geodataframe.GeoDataFrame'>\nInt64Index: 43 entries, 0 to 78\nData columns (total 9 columns):\ngeometry          43 non-null object\nzipcode           43 non-null object\nreview_scores_rating      43 non-null float64\nreview_scores_accuracy     43 non-null float64\nreview_scores_cleanliness   43 non-null float64\nreview_scores_checkin       43 non-null float64\nreview_scores_communication 43 non-null float64\nreview_scores_location      43 non-null float64\nreview_scores_value         43 non-null float64\ndtypes: float64(7), object(2)\nmemory usage: 3.4+ KB
```

In contrast to the standard clustering techniques, regionalization requires a formal representation of topology. This is so the algorithm can impose spatial constraints during the process of clustering the observations. We will use exactly the same approach as in the previous sections of this tutorial for this and build spatial weights objects `w` with `PySAL`. For the sake of this illustration, we will consider queen contiguity, but any other rule should work fine as long as there is a rational behind it. Weights constructors currently only work from shapefiles on disk, so we will write our `GeoDataFrame` first, then create the `w` object, and remove the files.

```
zrt.to_file('tmp')
w = ps.queen_from_shapefile('tmp/tmp.shp', idVariable='zipcode')
# NOTE: this might not work on Windows
! rm -r tmp
w
```

```
<pysal.weights.weights.W at 0x7f0cc9b433d0>
```

Now we are ready to run the regionalization algorithm. In this case we will use the `max-p` ([Duque, Anselin & Rey, 2012](#)), which does not require a predefined number of output regions but instead it takes a target variable that you want to make sure a minimum threshold is met. In our case, since it is based on ratings,

we will impose that every resulting region has at least 10% of the total number of reviews. Let us work through what that would mean:

```
n_rev = lst.groupby('zipcode')\
    .sum()\n    ['number_of_reviews']\
    .rename(lambda x: str(int(x)))\
    .reindex(zrt['zipcode'])\nthr = np.round(0.1 * n_rev.sum())\nthr
```

```
6271.0
```

This means we want every resulting region to be based on at least 6,271 reviews. Now we have all the pieces, let us glue them together through the algorithm:

```
# Set the seed for reproducibility\nnp.random.seed(1234)\n\nz = zrt.drop(['geometry', 'zipcode'], axis=1).values\nmaxp = ps.region.Maxp(w, z, thr, n_rev.values[:, None], initial=1000)
```

We can check whether the solution is better (lower within sum of squares) than we would have gotten from a purely random regionalization process using the `c inference` method:

```
%%time\nnp.random.seed(1234)\nmaxp.cinference(nperm=999)
```

```
CPU times: user 27.4 s, sys: 0 ns, total: 27.4 s\nWall time: 27.4 s
```

Which allows us to obtain an empirical p-value:

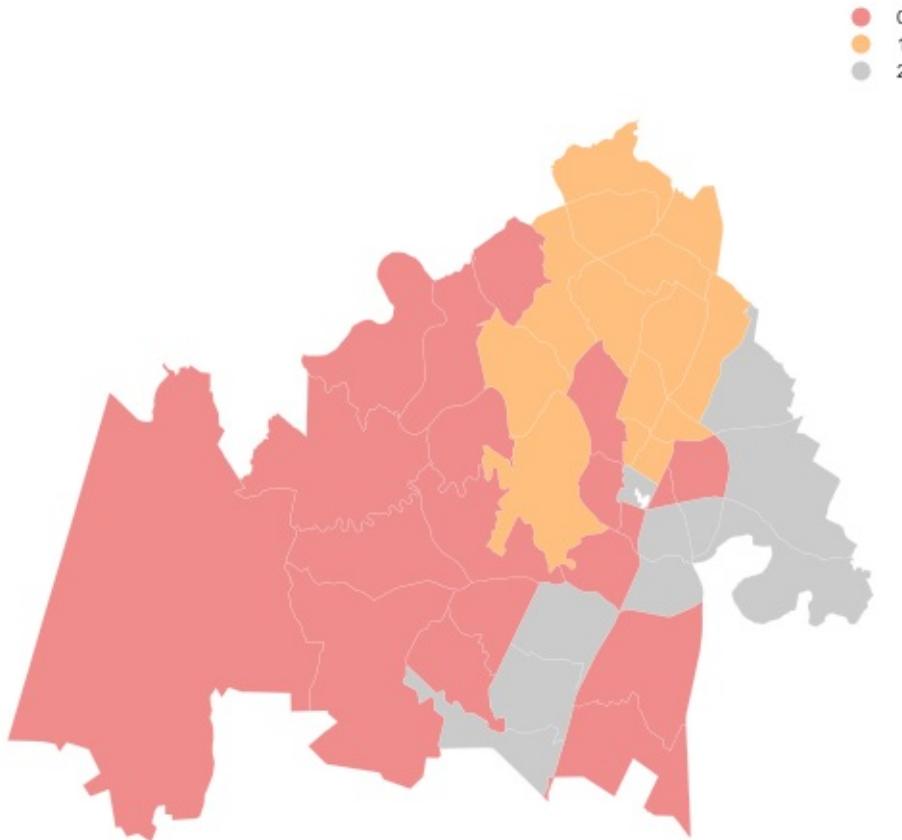
```
maxp.cpvalue
```

```
0.001
```

Which gives us reasonably good confidence that the solution we obtain is more meaningful than pure chance.

With that out of the way, let us see what the result looks like on a map! First we extract the labels:

```
lbls = pd.Series(maxp.area2region).reindex(zrt['zipcode'])\n\nf, ax = plt.subplots(1, figsize=(9, 9))\n\nzrt.assign(cl=lbls.values)\\
    .plot(column='cl', categorical=True, legend=True, \\
          linewidth=0.1, edgecolor='white', ax=ax)\n\nax.set_axis_off()\nplt.show()
```



The map shows a clear geographical pattern with a western area, another in the North and a smaller one in the East. Let us unpack what each of them is made of:

```
zrt[ratings].groupby(lbls.values).mean().T
```

	0	1	2
<b>review_scores_rating</b>	96.425334	95.264603	92.111148
<b>review_scores_accuracy</b>	9.703800	9.561277	9.548701
<b>review_scores_cleanliness</b>	9.597942	9.610098	8.965437
<b>review_scores_checkin</b>	9.876563	9.821887	9.764887
<b>review_scores_communication</b>	9.909209	9.821964	9.775652
<b>review_scores_location</b>	9.609283	9.483582	8.893100
<b>review_scores_value</b>	9.618152	9.543733	9.441086

Although very similar, there are some patterns to be extracted. For example, the East area seems to have lower overall scores.

## Exercise

*Obtain a geodemographic classification with eight classes instead of five and replicate the analysis above*

*Re-run the regionalization exercise imposing a minimum of 5% reviews per area*

# Spatial Regression

[IPYNB](#)

**NOTE:** much of this material has been ported and adapted from the Spatial Econometrics note in [Arribas-Bel \(2016b\)](#).

This notebook covers a brief and gentle introduction to spatial econometrics in Python. To do that, we will use a set of Austin properties listed in AirBnb.

The core idea of spatial econometrics is to introduce a formal representation of space into the statistical framework for regression. This can be done in many ways: by including predictors based on space (e.g. distance to relevant features), by splitting the datasets into subsets that map into different geographical regions (e.g. [spatial regimes](#)), by exploiting close distance to other observations to borrow information in the estimation (e.g. [kriging](#)), or by introducing variables that put in relation their value at a given location with those in nearby locations, to give a few examples. Some of these approaches can be implemented with standard non-spatial techniques, while others require bespoke models that can deal with the issues introduced. In this short tutorial, we will focus on the latter group. In particular, we will introduce some of the most commonly used methods in the field of spatial econometrics.

The example we will use to demonstrate this draws on hedonic house price modelling. This a well-established methodology that was developed by [Rosen \(1974\)](#) that is capable of recovering the marginal willingness to pay for goods or services that are not traded in the market. In other words, this allows us to put an implicit price on things such as living close to a park or in a neighborhood with good quality of air. In addition, since hedonic models are based on linear regression, the technique can also be used to obtain predictions of house prices.

## Data

Before anything, let us load up the libraries we will use:

```
%matplotlib inline

import seaborn as sns
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import pysal as ps
import geopandas as gpd

sns.set(style="whitegrid")
```

```
/home/dani/anaconda/envs/pydata/lib/python2.7/site-packages/matplotlib/font_manager.py:273: UserWarning: Matplotlib is building the font cache using fc-list. This may take a moment.
  warnings.warn('Matplotlib is building the font cache using fc-list. This may take a moment.')
```

Let us also set the paths to all the files we will need throughout the tutorial, which is only the original table of listings:

```
# Adjust this to point to the right file in your computer
abb_link = './data/listings.csv.gz'
```

And go ahead and load it up too:

```
lst = pd.read_csv(abb_link)
```

## Baseline (nonspatial) regression

Before introducing explicitly spatial methods, we will run a simple linear regression model. This will allow us, on the one hand, set the main principles of hedonic modeling and how to interpret the coefficients, which is good because the spatial models will build on this; and, on the other hand, it will provide a baseline model that we can use to evaluate how meaningful the spatial extensions are.

Essentially, the core of a linear regression is to explain a given variable -the price of a listing \$i\$ on AirBnb (\$P\_i\$)- as a linear function of a set of other characteristics we will collectively call  $\mathbf{X}_i$ :

$$\ln(P_i) = \alpha + \beta X_i + \epsilon_i$$

For several reasons, it is common practice to introduce the price in logarithms, so we will do so here. Additionally, since this is a probabilistic model, we add an error term  $\epsilon_i$  that is assumed to be well-behaved (i.i.d. as a normal).

For our example, we will consider the following set of explanatory features of each listed property:

```
x = ['host_listings_count', 'bathrooms', 'bedrooms', 'beds', 'guests_included']
```

Additionally, we are going to derive a new feature of a listing from the `amenities` variable. Let us construct a variable that takes 1 if the listed property has a pool and 0 otherwise:

```
def has_pool(a):
    if 'Pool' in a:
        return 1
    else:
        return 0

lst['pool'] = lst['amenities'].apply(has_pool)
```

For convenience, we will re-package the variables:

```
yxs = lst.loc[:, x + ['pool', 'price']].dropna()
y = np.log(
    yxs['price'].apply(lambda x: float(x.strip('$').replace(',', ''))) +
    0.000001
)
```

To run the model, we can use the `sprep` module in `Pysal`, which implements a standard OLS routine, but is particularly well suited for regressions on spatial data. Also, although for the initial model we do not need it, let us build a spatial weights matrix that connects every observation to its 8 nearest neighbors. This will allow us to get extra diagnostics from the baseline model.

```
w = ps.knnW_from_array(lst.loc[
    yxs.index, [
        'longitude', 'latitude'
    ].values)
w.transform = 'T'
w
```

unsupported weights transformation

```
<pysal.weights.weights.W at 0x7f3c066107d0>
```

At this point, we are ready to fit the regression:

```
m1 = ps.spreg.OLS(y.values[:, None], yxs.drop('price', axis=1).values, \
    w=w, spat_diag=True, \
    name_x=yxs.drop('price', axis=1).columns.tolist(), name_y='ln(price)')
```

To get a quick glimpse of the results, we can print its summary:

```
print(m1.summary)
```

```
REGRESSION
-----
SUMMARY OF OUTPUT: ORDINARY LEAST SQUARES
-----
Data set      : unknown
Weights matrix : unknown
Dependent Variable : ln(price)      Number of Observations: 5767
Mean dependent var : 5.1952        Number of Variables : 7
S.D. dependent var : 0.9455        Degrees of Freedom : 5760
R-squared       : 0.4042
Adjusted R-squared : 0.4036
Sum squared residual: 3071.189      F-statistic       : 651.3958
Sigma-square   : 0.533          Prob(F-statistic) : 0
S.E. of regression : 0.730        Log likelihood   : -6366.162
Sigma-square ML  : 0.533          Akaike info criterion: 12746.325
S.E. of regression ML: 0.7298      Schwarz criterion : 12792.944
-----
Variable      Coefficient    Std.Error     t-Statistic   Probability
-----
CONSTANT      4.0976886    0.0223530   183.3171506  0.0000000
host_listings_count -0.0000130  0.0001790  -0.0726772  0.9420655
bathrooms      0.2947079    0.0194817   15.1273879  0.0000000
bedrooms       0.3274226    0.0159666   20.5067654  0.0000000
beds           0.0245741    0.0097379   2.5235601   0.0116440
guests_included 0.0075119  0.0060551   1.2406028   0.2148030
pool           0.0888039    0.0221903   4.0019209   0.0000636
-----
REGRESSION DIAGNOSTICS
MULTICOLLINEARITY CONDITION NUMBER      9.260
TEST ON NORMALITY OF ERRORS
TEST          DF      VALUE      PROB
Jarque-Bera    2  1358479.047  0.0000
DIAGNOSTICS FOR HETEROSKEDASTICITY
RANDOM COEFFICIENTS
TEST          DF      VALUE      PROB
Breusch-Pagan test    6  1414.297  0.0000
Koenker-Bassett test  6   36.756  0.0000
DIAGNOSTICS FOR SPATIAL DEPENDENCE
TEST          MI/DF     VALUE      PROB
Lagrange Multiplier (lag)  1   255.796  0.0000
Robust LM (lag)        1   13.039  0.0003
Lagrange Multiplier (error) 1   278.752  0.0000
Robust LM (error)      1   35.995  0.0000
Lagrange Multiplier (SARMA) 2   291.791  0.0000
=====
===== END OF REPORT ======
```

Results are largely unsurprising, but nonetheless reassuring. Both an extra bedroom and an extra bathroom increase the final price around 30%. Accounting for those, an extra bed pushes the price about 2%. Neither the number of guests included nor the number of listings the host has in total have a significant effect on the final price.

Including a spatial weights object in the regression buys you an extra bit: the summary provides results on the diagnostics for spatial dependence. These are a series of statistics that test whether the residuals of the regression are spatially correlated, against the null of a random distribution over space. If the latter is rejected a key assumption of OLS, independently distributed error terms, is violated. Depending on the structure of the spatial pattern, different strategies have been defined within the spatial econometrics literature to deal with them. If you are interested in this, a very recent and good resource to check out is [Anselin & Rey \(2015\)](#). The main summary from the diagnostics for spatial dependence is that there is clear evidence to reject the null of spatial randomness in the residuals, hence an explicitly spatial approach is warranted.

## Spatially lagged exogenous regressors ( wx )

The first and most straightforward way to introduce space is by "spatially lagging" one of the explanatory variables.

```
yxs_w = yxs.assign(w_pool=ps.lag_spatial(w, yxs['pool'].values))

m2 = ps.spreg.OLS(y.values[:, None], \
                   yxs_w.drop('price', axis=1).values, \
                   w=w, spat_diag=True, \
                   name_x=yxs_w.drop('price', axis=1).columns.tolist(), name_y='ln(price)')

print(m2.summary)
```

## REGRESSION

## SUMMARY OF OUTPUT: ORDINARY LEAST SQUARES

Data set : unknown  
 Weights matrix : unknown  
 Dependent Variable : ln(price) Number of Observations: 5767  
 Mean dependent var : 5.1952 Number of Variables : 8  
 S.D. dependent var : 0.9455 Degrees of Freedom : 5759  
 R-squared : 0.4044  
 Adjusted R-squared : 0.4037  
 Sum squared residual: 3070.363 F-statistic : 558.6139  
 Sigma-square : 0.533 Prob(F-statistic) : 0  
 S.E. of regression : 0.730 Log likelihood : -6365.387  
 Sigma-square ML : 0.532 Akaike info criterion : 12746.773  
 S.E. of regression ML: 0.7297 Schwarz criterion : 12800.053

Variable	Coefficient	Std.Error	t-Statistic	Probability
CONSTANT	4.0906444	0.0230571	177.4134022	0.0000000
host_listings_count	-0.0000108	0.0001790	-0.0603617	0.9518697
bathrooms	0.2948787	0.0194813	15.1365024	0.0000000
bedrooms	0.3277450	0.0159679	20.5252404	0.0000000
beds	0.0246650	0.0097377	2.5329419	0.0113373
guests_included	0.0076894	0.0060564	1.2696250	0.2042695
pool	0.0725756	0.0257356	2.8200486	0.0048181
w_pool	0.0188875	0.0151729	1.2448141	0.2132508

## REGRESSION DIAGNOSTICS

MULTICOLLINEARITY CONDITION NUMBER 9.605

## TEST ON NORMALITY OF ERRORS

TEST	DF	VALUE	PROB
Jarque-Bera	2	1368880.320	0.0000

## DIAGNOSTICS FOR HETROSKEDEASTICITY

## RANDOM COEFFICIENTS

TEST	DF	VALUE	PROB
Breusch-Pagan test	7	1565.566	0.0000
Koenker-Bassett test	7	40.537	0.0000

## DIAGNOSTICS FOR SPATIAL DEPENDENCE

TEST	MI/DF	VALUE	PROB
Lagrange Multiplier (lag)	1	255.124	0.0000
Robust LM (lag)	1	13.448	0.0002
Lagrange Multiplier (error)	1	276.862	0.0000
Robust LM (error)	1	35.187	0.0000
Lagrange Multiplier (SARMA)	2	290.310	0.0000

===== END OF REPORT =====

**Spatially lagged endogenous regressors (wy)**

```
m3 = ps.spreg.GM_Lag(y.values[:, None], yxs.drop('price', axis=1).values, \
w=w, spat_diag=True, \
name_x=yxs.drop('price', axis=1).columns.tolist(), name_y='ln(price)')
```

```
print(m3.summary)
```

```

REGRESSION
-----
SUMMARY OF OUTPUT: SPATIAL TWO STAGE LEAST SQUARES
-----
Data set      : unknown
Weights matrix : unknown
Dependent Variable : ln(price)      Number of Observations: 5767
Mean dependent var : 5.1952        Number of Variables : 8
S.D. dependent var : 0.9455       Degrees of Freedom : 5759
Pseudo R-squared   : 0.4224
Spatial Pseudo R-squared: 0.4056

-----
Variable    Coefficient   Std.Error   z-Statistic   Probability
-----
CONSTANT    3.7085715   0.1075621   34.4784213   0.0000000
host_listings_count -0.0000587  0.0001765  -0.3324585  0.7395430
    bathrooms    0.2857932   0.0193237   14.7897969   0.0000000
    bedrooms     0.3272598   0.0157132   20.8270544   0.0000000
    beds         0.0239548   0.0095848   2.4992528    0.0124455
    guests_included  0.0065147  0.0059651   1.0921407   0.2747713
    pool          0.0891100  0.0218383   4.0804521   0.0000449
    W_ln(price)   0.0392530  0.0106212   3.6957202   0.0002193
-----
Instrumented: W_ln(price)
Instruments: W_bathrooms, W_bedrooms, W_beds, W_guests_included,
             W_host_listings_count, W_pool

DIAGNOSTICS FOR SPATIAL DEPENDENCE
TEST           MI/DF   VALUE      PROB
Anselin-Kelejian Test   1    31.545   0.0000
=====
===== END OF REPORT =====

```

## Prediction performance of spatial models

```

from sklearn.metrics import mean_squared_error as mse

mses = pd.Series({'OLS': mse(y, m1.predy.flatten()), \
                  'OLS+W': mse(y, m2.predy.flatten()), \
                  'Lag': mse(y, m3.predy_e)})
mses.sort_values()

```

```

Lag    0.531327
OLS+W  0.532402
OLS    0.532545
dtype: float64

```

## Exercise

*Run a regression including both the spatial lag of pools and of the price. How does its predictive performance compare?*