Data 8 MIDTERM

INSTRUCTIONS

You have 1 hour and 50 minutes to complete the exam.

- The exam is closed book, closed notes, closed computer, closed calculator, except the provided midterm study guide.
- Mark your answers on the exam itself in the spaces provided. We will not grade answers written on scratch paper or outside the designated answer spaces.

• If yo	ou need to use the restroom, bring your phone and exam to the front of the room.
For questi	ons with circular bubbles , you should select exactly <i>one</i> choice.
O You	must choose either this option
Or o	this one, but not both!
For questi	ons with square checkboxes, you may select multiple choices.
☐ You	could select this choice.
☐ You	could select this one too!
\mathbf{Pre}	liminaries
You	can complete and submit these questions before the exam starts.
(a)	What is your full name?
(b)	What is your student ID number?
(c)	Who is your lab GSI? You may write <i>Unknown</i> if you don't know their name.
(d)	Sign here to confirm that all work on this exam is your own (or type your name if online).

1. (42.0 points) BeReal

BeReal is an app that prompts users to post one photo per day. Once prompted, users have 2 minutes to post a photo; after 2 minutes they are late. A user can only post one photo per day, but they can retake the photo before posting. Other users can comment on posts that day. Assume that all comments on a post are made on the same day as the post.

The posts table contains one row for each of 528 posts made by Data 8 students. Columns exist for the user (str) who posted, the date (str) of their post, the caption (str) of the posted photo, whether the photo was a retake (bool), and how many minutes the post was late (float). The first three rows are:

user	date	caption	retake	late
Wendy Wendy	$10/13 \\ 10/14$	sunny sun prof sahai	False True	0.0 90.2
Nicole	10/13	on the glade	False	35.5

The comments table contains one row for each of 1240 comments made on these posts. Columns exist for the author (str) of the comment, the comment (str), the date of the post (str), and the poster (str) who is the user that posted the photo being commented on. The first three rows are:

author	comment	post	poster
Will Wendy Will	midterm season cute dogs! prof sighting	10/13 $10/13$ $10/14$	Nicole Nicole Wendy

(a) (4.0 points)

This partially completed expression evaluates to the number of posts for which Wendy retook her photo before posting.

	(posts('retake')) a)
	(1.0 pt) Fill in blank (a).
ii.	(2.0 pt) Fill in blank (b).

iii. (1.0 pt) Which of these could fill in blank (c)?

column
 select
 group

take

(b) (9.0 points)

Complete this code to compute two quantities about pictures that aren't retakes:

- real_fractions is an array with one item for each user that contains the fraction (a float) of posts made by that user that are **not retakes**. The array may be in any order.
- good_post_fraction is the fraction (a float) of all posts that have a caption longer than 5 characters and a photo that is not a retake. Use the good_post function to compute it.

Hints: The average of an array of bool values is the fraction that are **True**. The sum of an array of bool values is the number that are **True**.

rea.	l_fractions = posts.sel (a)	.ect('user',	'retake') (b	column(_)	(c)
def	<pre>good_post(caption, retake): return len(caption) > 5 and</pre>	(d)			
good	d_post_fraction = sum(posts) /			
	(1.0 pt) Fill in blank (a). If you be			a blank write	"EMDTV"
1.	(1.0 pt) I'm m blank (a). If you be	neve no code n	s necessary in time	S Dialik, write	
ii.	(2.0 pt) Fill in blank (b). You may	not include a	ny . in your answ	ver.	
iii.	(1.0 pt) Fill in blank (c).				
iv.	(1.0 pt) Fill in blank (d).				
v.	(3.0 pt) Fill in blank (e). You may	not include ar	ny in vour answ	zer	
••	(Oto pt) I iii iii siaiii (e). Tou iiiay		ij i ili jodi dilow		
	(1.0. I) F:11: 11 1 (f)				
V1.	(1.0 pt) Fill in blank (f).				

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l C) (7	l) 1	DO.	${f ints}$. 1
· ·	, ,		•	P 0.	11100	•

This partially completed code assigns sahai_comments to the total number of comments (an integer) made on all of Wendy's posts for which the caption includes the string sahai within it.

Important: Assume all captions are lowercased already.

Reminder: The posts table has one row per post and columns user, date, caption, retake, and late. The comments table has one row per comment and columns author, comment, post, and poster.

ii.	(1.0 pt) Which of these could fill in blank (b)?
	<pre> apply</pre>

select
 join

O pivot

iii. (1.0 pt) Fill in blank (c).

iv. (2.0 pt) Fill in blank (d).

l		

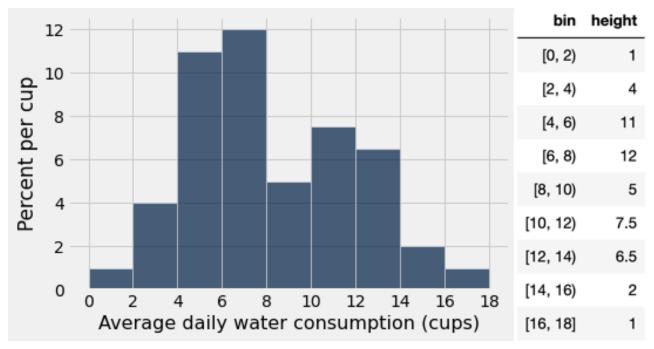
v. (1.0 pt) Fill in blank (e).

an expression that correctly computes each of the following results. You may abbreviate posts a comments as c. osts omments nder: The posts table has one row per post and columns user, date, caption, retake, and la comments table has one row per comment and columns author, comment, post, and poster. 2.0 pt) The largest number (a float) in the late column of the posts table.
omments nder: The posts table has one row per post and columns user, date, caption, retake, and la omments table has one row per comment and columns author, comment, post, and poster.
omments table has one row per comment and columns author, comment, post, and poster.
2.0 pt) The largest number (a float) in the late column of the posts table.
2.0 pt) The number (an integer) of different authors who commented on one or more post.
2.0 pt) An array of the captions of all posts with a positive (non-zero) late value. The array e in any order.
3.0 pt) A table with one row per user and three columns: the user, a column labeled Factorianing the average number of minutes that their non-retake posts were late, and a column labeled containing the average number of minutes that their retake posts were late.
3.0 pt) The largest number (an integer) of comments on any one post. A user can post at more per day, but there is no limit to the number of times that someone can comment on a post.
2. ee

(e)	(8.0	O points)
	i.	(2.0 pt) What is the best data visualization to compare the distribution of late values for posts that are retakes to the distribution of late values for posts that are not retakes.
		○ Scatter plot
		O Bar chart
		○ Line plot
		Overlaid histograms
	ii.	(2.0 pt) Suppose this dataset is a simple random sample of all BeReal posts made by Data 8 students What null hypothesis would help assess whether, among all Data 8 students' posts, the posts that are retakes have a different distribution of late values than the posts that are not retakes? (<i>Note</i> : A post is late if it has a non-zero late value.)
		O The average late value is different for posts that are retakes than posts that are not retakes.
		O The proportion of retake values that are True is different for posts that are late than for posts that are not late.
		O The distribution of late values among all Data 8 students is the same for posts that are retakes and posts that are not retakes.
		O The distribution of retake values among all Data 8 students is the same for posts that are late and posts that are not late.
	iii.	(2.0 pt) For a permutation test that shuffles the order of retake values many times to simulate data under this null hypothesis, what is the purpose of shuffling the order of the column?
		O Shuffling the retake values simulates drawing two samples of late values from the same distribution.
		○ Shuffling is a form of randomized controlled experiment.
		O Shuffling is equivalent to taking a random sample with replacement.
		O Shuffling randomly assigns retake conditions to users before they post.
	iv.	(2.0 pt) Suppose the absolute difference of means is used as the test statistic, 100,000 simulations are generated under the null hypothesis, and the resulting p-value is zero. What can we conclude from this test? Choose all that apply.
		☐ For all BeReal users, the distribution of late values is different for posts that are retakes and posts that are not retakes.
		☐ For all Data 8 students, the distribution of late values is different for posts that are retakes and posts that are not retakes.
		☐ For all Data 8 students, posts that are retakes have larger late values on average than posts that are not retakes.
		\square For all BeReal users, retaking photos causes a change in how late those photos are posted on average.
		☐ For all Data 8 students, retaking photos causes a change in how late those photos are posted on average.

2. (12.0 points) Histograms

The Mayo Clinic recommends drinking 13.5 cups of water per day. The histogram below describes the average daily water intake during September 2022 (measured in cups of water) for 400 Berkeley students. The exact heights of each bar appear in the adjacent table.



Choose the mathematical expression that evaluates to each quantity described below.

- (a) (2.0 pt) The number of students who drank an average of at least 8 but less than 10 cups per day.
 - \bigcirc 0.05
 - \bigcirc 0.05 * 2
 - \bigcirc 0.05 * 100
 - \bigcirc 0.05 * 2 * 100
 - \bigcirc 0.05 * 400
 - \bigcirc 0.05 * 2 * 400
 - O Not enough information provided
 - O None of these
- (b) (2.0 pt) The proportion of students who drank an average of at least 13.5 cups per day.
 - $\bigcirc 0.02 + 0.01$
 - $\bigcirc 0.065 + 0.02 + 0.01$
 - \bigcirc 0.065 / 2 + 0.02 + 0.01
 - \bigcirc 0.065 / 4 + 0.02 + 0.01
 - O Not enough information provided
 - O None of these

(c)	(2.0 pt) The proportion of students who drank an average of at least 4 cups per day.
	O 1 - (0.11)
	O 1 - (0.11) * 2
	\bigcirc 1 - (0.01 + 0.04)
	\bigcirc 1 - (0.01 + 0.04) * 2
	\bigcirc 1 - $(0.01 + 0.04 + 0.11)$
	\bigcirc 1 - $(0.01 + 0.04 + 0.11)$ * 2
	O Not enough information provided
	O None of these
(d)	(2.0 pt) The proportion of students who never drank more than 16 cups of water in any single day during September 2022.
	\bigcirc 1 - (0.01)
	O 1 - (0.01) * 2
	\bigcirc 1 - $(0.02 + 0.01)$
	\bigcirc 1 - $(0.02 + 0.01)$ * 2
	O Not enough information provided
	○ None of these
	(2.0 pt) The height (in percent per cup) of the bin from 4 to 8 if this histogram were drawn with bins=make_array(0, 2, 4, 8, 18).
	$\bigcirc \ (11+12) \ / \ 4 \ (ext{which equals } 5.75)$
	$\bigcirc \ (2*11+2*12) \ / \ 4 \ (\text{which equals } 11.5)$
	\bigcirc 11 + 12 (which equals 23)
	\bigcirc 2 * (11 + 12) (which equals 46)
	O Not enough information provided
	O None of these
(f)	(2.0 pt) The maximum possible height (in percent per cup) of the bin from 4 to 5 if this histogram were drawn with bins=np.arange(19).
	\bigcirc 11
	O 11 * 2
	O 11 / 2
	O 11 * 4
	O 11 / 4
	O None of these

3. (16.0 points) Chances

Some helpful students decide to pick up trash in a park near their dorm. Half the pieces of trash are bottles, one third are boxes, and one sixth are food.

(a) (8.0 points)

For each event below, choose the Python expression that evaluates to the probability of that event when **two** pieces of trash are chosen at random **with replacement**.

- i. (2.0 pt) The probability that they are both boxes.
 - \bigcirc (1 / 3)
 - \bigcirc (1 / 3) + (1 / 3)
 - O (1 / 3) ** 2
 - \bigcirc ((1 / 3) + (1 / 3)) ** 2
 - \bigcirc (1 / 3) ** 2 + (1 / 3) ** 2
- ii. (2.0 pt) The probability that the first one is a box.
 - \bigcirc (1 / 3)
 - \bigcirc (1 / 3) * (2 / 3)
 - O (1 / 3) ** 2
 - \bigcirc 1 (1 / 3)
 - \bigcirc 1 (1 / 3) * (2 / 3)
 - 0 1 (1 / 3) ** 2
- iii. (2.0 pt) The probability that one is a box and the other is food. (*Note:* Either the box or food can be chosen first for this event to occur.)
 - \bigcirc (1 / 3) + (1 / 6)
 - \bigcirc (1 / 3) * (1 / 6)
 - \bigcirc ((1 / 3) + (1 / 6)) ** 2
 - \bigcirc ((1 / 3) * (1 / 6)) ** 2
 - \bigcirc 2 * ((1 / 3) + (1 / 6))
 - \bigcirc 2 * ((1 / 3) * (1 / 6))
- iv. (2.0 pt) The probability that they are both the same kind of trash.
 - \bigcirc (1 / 2) * (1 / 3) * (1 / 6)
 - \bigcirc 1 ((1 / 2) * (1 / 3) * (1 / 6))
 - \bigcirc (1 / 2) ** 2 + (1 / 3) ** 2 + (1 / 6) ** 2
 - \bigcirc (1 / 2) ** 2 * (1 / 3) ** 2 * (1 / 6) ** 2

((b)) ((8.0	points)

There are $6{,}000$ pieces of trash in the park ($3{,}000$ bottles, $2{,}000$ boxes, $1{,}000$ pieces of food). Adrian collects 20 pieces at random and observes that A of them are bottles. Bala collects 100 pieces at random and observes that B of them are bottles.

i.	(3.0 pt) Which of the following are more probable than not? Choose all that apply.	
	☐ A is larger than B	
	☐ B is larger than A	
	\square (A / 20) is larger than (B / 100)	
	\square (B / 100) is larger than (A / 20)	
	\Box abs(A $/$ 20 - 0.5) is larger than abs(B $/$ 100 - 0.5)	
	\Box abs(B $/$ 100 - 0.5) is larger than abs(A $/$ 20 - 0.5)	
	☐ None of these	
ii.	(3.0 pt) Fill in the blank so that calling bottles(n) simulates collecting n pieces of trash at rando with replacement from the park and returns the number that are bottles. For credit, your answ must fit on one line.	
	<pre>trash = make_array('bottle', 'bottle', 'bottle', 'box', 'box', 'food')</pre>	
	<pre>def bottles(n): "Return the number of bottles in a random sample of n pieces of trash."</pre>	
	return	
iii.	(2.0 pt) Fill in the blank so that p is an empirical estimate of the probability that 20 pieces of trachosen at random with replacement from the park will contain at least 12 bottles.	sł
	results = make_array()	
	<pre>for i in np.arange(10000): results = np.append(results, bottles(20))</pre>	
	p =	

4. (30.0 points) Stars

You read online that the Milky Way galaxy contains 100 billion active stars, 10 billion white dwarf stars, and 1 billion neutron stars. You also find the following *near-Earth dataset* online: within 300 trillion kilometers (10 parsecs) of Earth, there are 392 active stars and 21 white dwarf stars, but 0 neutron stars.

(a)	(2.0 pt) Which of the following are true about the near-Earth dataset? Choose all that apply.					
	\square It describes a sample of the stars in the galaxy.					
	\square It describes a simple random sample of the stars in the galaxy.					
	\square It describes a randomly selected region of the galaxy.					
	\square It describes the population of all stars within 300 trillion kilometers of Earth.					
	☐ None of these.					
(b)	(8.0 points)					
	You decide to use these data to investigate whether the distribution of stars (active stars, white dwarf stars, and neutron stars) near Earth is the same as the distribution across the galaxy or whether it's unusual.					
	i. (2.0 pt) Complete this null hypothesis: The distribution of stars					
	O near Earth has exactly the same proportions as the galaxy's distribution.					
	O near Earth is like a random sample from the galaxy's distribution.					
	\bigcirc in a randomly selected region of the Milky Way is the same as the galaxy's distribution.					
	\bigcirc in every sample of stars is the same as the galaxy's distribution.					
	ii. (2.0 pt) Complete this alternative hypothesis: The distribution of stars near Earth					
	\bigcirc is the same as the galaxy's distribution.					
	○ is consistent with the galaxy's distribution.					
	is not like a random sample from the galaxy's distribution.					
	\bigcirc is not the same as the distribution from a randomly selected region of the galaxy.					
	iii. (2.0 pt) Which test statistic is best for choosing between these null and alternative hypotheses?					
	O Total variation distance from the galaxy's distribution					
	O Difference between the number of neutron stars in the sample and the galaxy					
	O Difference between the proportion of neutron stars in the sample and the galaxy					
	O Difference between the sizes of the samples					
	iv. (2.0 pt) Under the null hypothesis, what would best explain the fact that near Earth there are 0 neutron stars?					
	○ The number of stars near Earth is small.					
	O Neutron stars are dim and hard to observe.					
	O Neutron stars are mostly near the center of the galaxy and Earth is not.					
	\bigcirc Due to random chance, there happen to be 0 neutron stars near Earth.					

(c) (10.0 points)

Fill in the blanks of the simulation below to calculate a p-value for this hypothesis test by sampling 10000 times under the null hypothesis. (*Note*: 1e11 is a valid way to express 100 billion in Python.)

```
def half_abs_sum(a):
    "Return half the sum of the absolute values of a single array."
    return sum(np.abs(a)) / 2
obs = make_array(392, 21, 0)
                                                            # An array of counts
dist = make_array(1e11, 1e10, 1e9) / (1e11 + 1e10 + 1e9) # An array of proportions
observed_stat = half_abs_sum(_____)
stats = make_array()
for i in _____:
           (b)
    sample = sample_proportions(_____, dist)
    stats = np.append(stats, half_abs_sum(_____))
p_value = ____ / 10000
            (e)
 i. (2.0 pt) Fill in blank (a).
 ii. (2.0 pt) Fill in blank (b).
iii. (1.0 pt) Which of these could fill in blank (c)?
   Obs
    sum(obs)
    stats
    sum(stats)
iv. (2.0 pt) Fill in blank (d).
 v. (3.0 pt) Fill in blank (e).
```

apply.

(d) (10.0 points)

Interpret the hypothesis test you just implemented. i. (4.0 pt) What does the p-value represent in this hypothesis test? Choose all that apply. ☐ The theoretical probability that the alternative hypothesis is true. ☐ An emprical estimate of the probability that the alternative hypothesis is true. ☐ The theoretical probability that the null hypothesis is true. ☐ An empirical estimate of the probability that the null hypothesis is true. The theoretical probability under the null hypothesis that the test statistic would be at least as large as the observed test statistic. An empirical estimate of the probability under the null hypothesis that the test statistic would be at least as large as the observed test statistic. ☐ The fraction of all possible samples under the null hypothesis that have a test statistic at least as large as the observed test statistic. ☐ The fraction of simulated samples under the null hypothesis that had a test statistic at least as large as the observed test statistic. ☐ None of these ii. (2.0 pt) What does it mean to describe the p-value cutoff as an error probability? The p-value cutoff is the chance that the null hypothesis is true. The p-value cutoff is the chance that the null hypothesis is false. The p-value cutoff is the chance that the null hypothesis will be rejected if it were true. The p-value cutoff is the chance that the null hypothesis will not be rejected if it were false. (2.0 nt) Assuming everything that you read online is accurate and the computed n value from your

•	code is 0.0015. What can you conclude using a p-value cutoff of 1%? Choose all that
	\square The data are consistent with the null hypothesis.
	\square The data are not consistent with the null hypothesis.
	☐ The null hypothesis can be rejected.

iv. (2.0 pt) Which of the following facts, if true, should cause you to question the conclusions you drew from this hypothesis test? Choose all that apply.

	The total number of active stars in the Milky Way is unknown, but estimated to be between 10)()
	billion and 400 billion.	
\Box	White desired the second life of the change of city to be a second of the control	

☐ White dwarf stars are difficult to observe, so scientists believe there are some near Earth that have not yet been counted.

☐ Many of the active stars near Earth are much younger than the Sun.

☐ The null hypothesis **cannot** be rejected.

☐ The rotational speed of the Milky Way implies that 90% of the mass in the galaxy is dark martter.

☐ None of these