# Introduction to Regression Analysis 1

#### Preparing your workfile

We add the basic libraries needed for this week's work:

```
library(tidyverse)  # for almost all data handling tasks
library(readxl)  # to import Excel data
library(ggplot2)  # to produce nice graphiscs
library(stargazer)  # to produce nice results tables
library(haven)  # to import stata file
library(AER)  # access to HS robust standard errors
```

#### Introduction

The data are an extract from the Understanding Society Survey (formerly the British Household Survey Panel).

#### Data Upload - and understanding data structure

Upload the data, which are saved in a STATA datafile (extension .dta). There is a function which loads STATA file. It is called read\_dta and is supplied by the haven package.

```
data_USoc <- read_dta("20222_USoc_extract.dta")</pre>
data_USoc <- as.data.frame(data_USoc)</pre>
                                             # ensure data frame structure
names(data_USoc)
    [1] "pidp"
                    "age"
                               "jbhrs"
                                          "paygu"
                                                     "wave"
                                                                "cpi"
                                                                            "vear"
                               "male"
                                          "race"
                                                     "educ"
                                                                           "mfsize9"
    [8] "region"
                    "urate"
                                                                "degree"
```

Let us ensure that categorical variables are stored as factor variables. It is easiest to work with these in R.

```
data_USoc$region <- as_factor(data_USoc$region)
data_USoc$male <- as_factor(data_USoc$male)
data_USoc$degree <- as_factor(data_USoc$degree)
data_USoc$race <- as_factor(data_USoc$race)</pre>
```

Click on the little table symbol in your environment tab to see the actual data table.

The variable pidp contains a unique person identifier and the variable wave indicates the wave and year the year of observation.

To explain the meaning of these let us just pick out all the observations that pertain to one particular individual (pidp == 272395767). The following command does the following in words: "Take data\_USoc filter/keep all observations which belong to individual pidp == 272395767, then select a list of variables (we don't need to see all 14 variables) and print the result":

```
paygu age educ
##
          pidp
                 male wave year
## 1 272395767 female
                          1 2009 774.8302
                                            40
                                                 11
## 2 272395767 female
                          2 2010 812.2778
                                            41
                                                 11
## 3 272395767 female
                          3 2011 772.1625
                                            42
                                                 11
```

The same person (female) was observed three years in a row (from 2009 to 2011). Their gross monthly income changed, as did, of course, their age, but not their education. This particular person was observed in three consequitive waves. Let's se whether this is a common pattern.

The code below figures out for how many individuals we have 1, 2 and 3 waves of observations. It is not important to understand that code.

```
## # A tibble: 3 x 2
##    n_wave n_pat
##    <int>    <int>
## 1    1 15099
## 2    2 12450
## 3    3 31091
```

##

As you can see only just over half of individuals have records for three waves. Let us look at the observations for an individual (pidp == 2670365) which only has observations for two waves.

```
## pidp male wave year paygu age educ
## 1 2670365 female 2 2010 230.0000 16 11
## 2 2670365 female 3 2011 346.6667 17 11
```

#### Some summary statistics

Let's use the stargazer function to produce a nice summary table

```
stargazer(data_USoc, type = "text")
```

##								
## ## ##	Statistic	 N 	Mean	St. Dev.	Min	Pct1(25)	Pct1(75)	Max
	pidp	133,272	839,218,358.000	467,699,610.000	280,165	410,528,927	1,225,328,047	1,639,568,724
	age	133,272	46.172	18.295	9	31	60	103
##	jbhrs	64,217	32.594	11.614	0.100	25.000	40.000	97.000
##	paygu	59,216	1,823.574	1,475.064	0.083	850.000	2,400.000	15,000.000
##	wave	133,272	1.912	0.818	1	1	3	3
##	cpi	133,272	116.790	4.199	110.800	114.500	119.600	126.100
##	year	133,272	2,010.453	0.991	2,009	2,010	2,011	2,013
##	urate	133,272	7.955	1.311	5.800	6.700	9.100	10.800

```
12.838
303.135

      12.838
      2.316
      11.000
      11.000

      303.135
      484.430
      1.000
      17.000

## educ 133,041
                                                                         15.000
                                                                                     17.000
## mfsize9 58,989
                                                                         350.000
                                                                                     1,500.000
## -----
Here are some frequency tables
data_USoc %>% count(wave)
## # A tibble: 3 x 2
   wave
            n
## <dbl> <int>
## 1
     1 50923
## 2
       2 43131
## 3 3 39218
data_USoc %>% count(region)
## # A tibble: 12 x 2
##
   region
                                 n
##
   <fct>
                             <int>
## 1 north east
                              5368
## 2 north west
                             14095
## 3 yorkshire and the humber 11139
## 4 east midlands 10257
## 5 west midlands
                            11747
                           11860
## 6 east of england
## 7 london
                            19994
## 8 south east
                            16461
## 9 south west
                             10554
## 10 wales
                              6676
## 11 scotland
                              9321
## 12 northern ireland
                              5800
data_USoc %>% count(male)
## # A tibble: 2 x 2
## male
## <fct> <int>
## 1 female 72072
## 2 male 61200
data_USoc %>% count(year)
## # A tibble: 5 x 2
## year
            n
##
    <dbl> <int>
## 1 2009 25363
## 2 2010 44495
## 3 2011 42213
## 4 2012 20048
## 5 2013 1153
data_USoc %>% count(race)
## # A tibble: 6 x 2
## race
## <fct> <int>
## 1 white 99593
```

```
## 2 mixed 2057
## 3 asian 12994
## 4 black 6167
## 5 other
            2078
## 6 <NA> 10383
data_USoc %>% count(educ)
## # A tibble: 7 x 2
##
      educ
     <dbl> <int>
##
## 1
        11 74150
## 2
        12 3673
## 3
        13 11628
## 4
        15 13193
## 5
        16 17509
## 6
        17 12888
## 7
        NA
             231
data_USoc %>% count(degree)
## # A tibble: 4 x 2
##
     degree
                         n
     <fct>
                     <int>
## 1 no degree
                    102644
## 2 first degree
                     17509
## 3 higher degree
                     12888
## 4 <NA>
                       231
data_USoc %>% count(mfsize9)
## # A tibble: 10 x 2
##
      mfsize9
##
        <dbl> <int>
               2269
##
    1
            1
##
    2
            6
               7722
##
    3
           17
               9599
##
    4
           37
               9095
##
    5
           75
               6766
##
    6
               5814
          150
   7
##
          350
               6788
##
    8
          750
               3768
##
    9
         1500
               7168
           NA 74283
```

The pay information (paygu) is provided as a measure of the (usual) gross pay per month. As workers work for dy we shall also adjust for increasing price levels (as measuredmutate function. We call this variable hrpay and also calculate the natural log of this variable (lnhrpay).

As we wanted to save these additional variables we assign the result of the operation to data\_USoc.

Let's check whether the log of the hourly pay differes if we analyse the data by certain criteria.

```
data_USoc %>% group_by(degree) %>%
              summarise(n = sum(!is.na(lnhrpay)),
                       mean = mean(lnhrpay,na.rm=TRUE),
                        sd = sd(lnhrpay,na.rm=TRUE))
## # A tibble: 4 x 4
##
     degree
                      n mean
                                  sd
##
     <fct>
                  <int> <dbl> <dbl>
                  40816 2.14 0.581
## 1 no degree
## 2 first degree 10601
                         2.57 0.602
## 3 higher degree 7525 2.67 0.637
## 4 <NA>
                      18 1.90 0.535
data_USoc %>% group_by(educ) %>%
              summarise(n = sum(!is.na(lnhrpay)),
                       mean = mean(lnhrpay,na.rm=TRUE),
                        sd = sd(lnhrpay,na.rm=TRUE))
## # A tibble: 7 x 4
##
      educ
              n mean
##
     <dbl> <int> <dbl> <dbl>
## 1
        11 26349 2.09 0.549
        12 1751 2.01 0.593
## 2
## 3
       13
           5651
                 2.18 0.631
## 4
       15 7065 2.33 0.604
       16 10601
                 2.57 0.602
## 6
       17 7525
                 2.67 0.637
       NA
              18 1.90 0.535
data_USoc %>% group_by(male) %>%
              summarise(n = sum(!is.na(lnhrpay)),
                       mean = mean(lnhrpay,na.rm=TRUE),
                        sd = sd(lnhrpay,na.rm=TRUE))
## # A tibble: 2 x 4
               n mean
##
     <fct> <int> <dbl> <dbl>
## 1 female 32609 2.20 0.598
## 2 male
           26351 2.38 0.656
```

You can see that difference in the averages for lnhrpay is about 0.183.

### Testing for differences

The first hypothesis test we may want to implement is to test whether the difference in the raw data is statistically significant (recall this is not the same economically significant difference).

We use the t.test function. We could create two subsets of data for lnhrpay, one for males and one for females and could then feed these two series into the t.test function (t.test(data\_male,data\_female, mu = 0)) but there is a more straightforward way to achieve this. We shall call t.test(lnhrpay~male, mu=0, data = data\_USoc). The lnhrpay~male is almost like a regression call, the variable we are interested in is lnhrpay but we want to know whether it differs according to male. The other inputs set the data farme (data = data\_USoc) and the null hypothesis (mu=0).

```
t.test(lnhrpay~male, mu=0, data = data_USoc) # testing that mu = 0

##

## Welch Two Sample t-test

##

## data: lnhrpay by male

## t = -35.022, df = 53923, p-value < 2.2e-16

## alternative hypothesis: true difference in means is not equal to 0

## 95 percent confidence interval:

## -0.1932469 -0.1727632

## sample estimates:

## mean in group female mean in group male

## 2.201202 2.384207</pre>
```

So here the p-value is extremely small indicating that the raw differential in log hourly wages between males and females is certainly statistically significant.

# A regression - Gender differences

Regression analysis is our bread-and-butter technique and we can obtain the same result with a regression model.

```
mod1 <- lm(lnhrpay~male,data = data_USoc)
cov1 <- vcovHC(mod1, type = "HC1")
robust_se <- sqrt(diag(cov1))
stargazer(mod1,type="text",se=list(NULL, robust_se))</pre>
```

```
##
##
  ______
                    Dependent variable:
##
                        lnhrpay
## malemale
                        0.183***
##
                         (0.005)
## Constant
                        2.201***
##
                         (0.003)
##
## Observations
                         58,960
## R2
                         0.021
## Adjusted R2
                         0.021
## Residual Std. Error 0.625 (df = 58958)
## F Statistic 1,251.147*** (df = 1; 58958)
## Note:
                  *p<0.1; **p<0.05; ***p<0.01
```

In the regression output you can see the variable male but it says malemale which is indication that basically a dummy variable has been included into your regression that takes the value 1 for every male respondent and 0 for everyone else.

The coefficient you can see for that is 0.183 which is exactly the difference between the male and female averages for lnhrpay.

If you were to merely calculate the regression model (mod1 <- lm(lnhrpay~male,data = data\_USoc)) and then show the results with stargazer) you would get a very similar regression output, but the standard errors for the parameter estimates would have been calculated on the basis of a homoskedasticity assumption. Without any further details, this is an assumption which on many occasions is breached. However, the consequences are not too worrysome as long as we change how we calculate the standard errors. And that is what the extra lines achieve.

We can actually write a little function which does add the HC robust standard errors to the usual output. It is not so important that you fully understand what is hapening here. Copy and paste the next code chunk into a new script file and save it as stargazer\_HC.r into your working directory.

```
stargazer_HC <- function(mod, type_in = "text") {
  cov1 <- vcovHC(mod, type = "HC1")
  robust_se <- sqrt(diag(cov1))
  stargazer(mod,type=type_in,se=list(NULL, robust_se))
}</pre>
```

Once you have saved stargazer\_HC.r into your working directory you need to make it accessible to your code by including

```
source("stargazer_HC.r")
```

into your script. It is possibly best to do that right at the top where you load the packages (library commands).

Then we call a regresison and if we want robust standard errors we merely call stargazer\_HC rather than stargazer). Added bonus is that you don't have to use the type = "text" option any longer as I used it as the default.

```
mod1 <- lm(lnhrpay~male,data = data_USoc)
stargazer_HC(mod1)</pre>
```

```
##
##
##
                        Dependent variable:
##
##
                              lnhrpay
##
  malemale
                              0.183***
##
##
                              (0.005)
##
                              2.201 ***
## Constant
                              (0.003)
##
##
## Observations
                               58,960
## R2
                               0.021
## Adjusted R2
                               0.021
## Residual Std. Error
                         0.625 \text{ (df = } 58958)
## F Statistic
                    1,251.147*** (df = 1; 58958)
*p<0.1; **p<0.05; ***p<0.01
## Note:
```

Sometimes it is useful to extract the actual estimated coefficient and use it for some subsequent calculation. On this occasion let us extract the estimated coefficient for male. When we estimated the regression model we saved the output in mod1. In fact mod1 contains a lot of information we may want to use, most notably the coefficient estimates, estimated residuals, fitted values etc. We access these as follows

#### mod1\$coefficients

```
## (Intercept) malemale
## 2.2012023 0.1830051

# mod1$residuals # uncomment if you want to see these
# mod1$fitted.values
```

And if want a particular coefficient we can get that as follows

```
mod1$coefficients["malemale"] # or

## malemale
## 0.1830051
# mod1$coefficients[1]
```

where we use the coefficient name we also saw in the regression output.

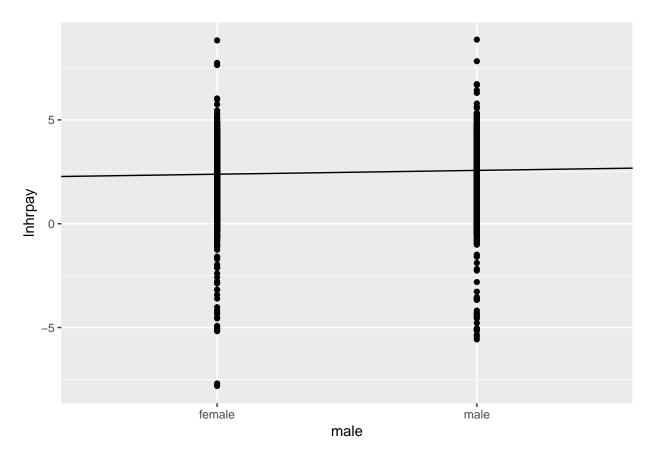
Let say we want to calculate the actual percentage points raw differential which is a function of this coefficient:

```
(exp(mod1$coefficients["malemale"])-1)*100
```

```
## malemale ## 20.08205
```

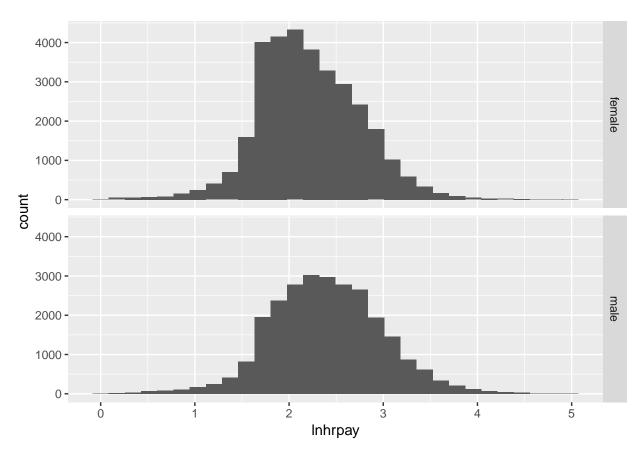
Let's produce a scatter plot of the data on which the above regression is based.

```
ggplot(data_USoc, aes(x = male, y = lnhrpay)) +
  geom_point() +
  geom_abline(intercept = mod1$coefficients[1], slope = mod1$coefficients[2])
```

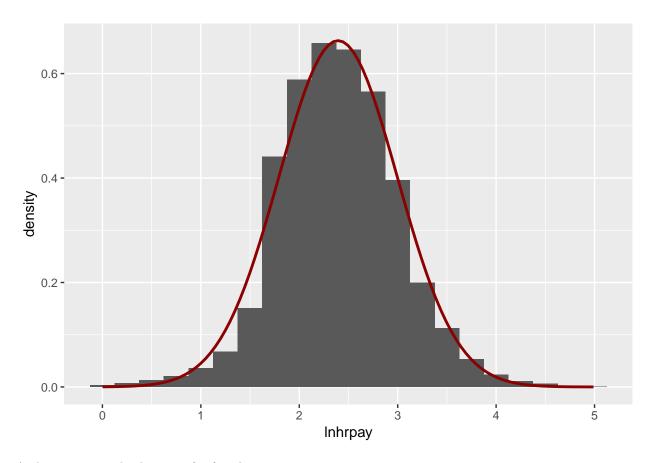


As you can see this plot has limited informative value as, on the horizontal axis, we only have two possible outcomes, female and male. On each of these we have a wide range of outcomes for lnhrpay. We want to find a way to illustrate the distribution of outcomes on the lnhrpay scale depending on the value for male.

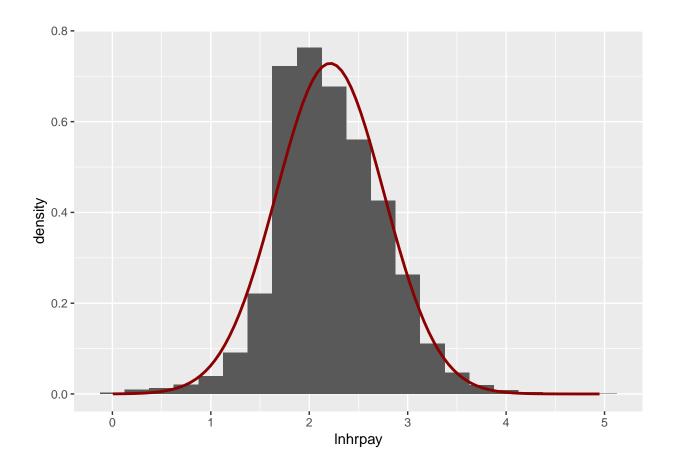
```
ggplot(subset(data_USoc, (lnhrpay>0) & (lnhrpay<5)), aes(x = lnhrpay)) +
geom_histogram() +
facet_grid(rows = vars(male))</pre>
```



You could, if you wanted to, fit a normal distribution to these (remember the variables are the log hourly pay rates). This is not super straightforward and it turns out that in this case you would want to generate the graphs seperately. I had to google "R ggplot add normal distribution fit to geom\_histogram" and came across https://stackoverflow.com/questions/1376967/using-stat-function-and-facet-wrap-together-inggplot2-in-r/1379074#1379074 which helped me to adopt a solution. The normal density is added with a stat\_function:



And now we can do the same for females.



### A regression - Education differences

After looking at gender differences we will now look at differences in earnings according to education differences.

Let's first look at the degree vari8able in our dataset.

```
data_USoc %>% count(degree)
```

```
## # A tibble: 4 x 2
## degree n
## <fct> <int>
## 1 no degree 102644
## 2 first degree 17509
## 3 higher degree 12888
## 4 <NA> 231
```

Let us create a new variable which merely differentiates between having any degree or no degree. So we essentially want to collapse the first degree and higher degree categories into a any degree category. Recall that this is a factor variable and there is a very convenient function (fct\_recode) which allows you to change the levels. The mutate(grad = ...) function creates a new variable with the definition of that variable following the equal sign.

```
"any degree" = "first degree",
"any degree" = "higher degree"))
```

And now let's look at the counts of this new variable.

```
data_USoc %>% count(grad)
```

```
## # A tibble: 3 x 2
## grad n
## <fct> <int>
## 1 no degree 102644
## 2 any degree 30397
## 3 <NA> 231
```

And now we run a regression just as we did for gender differences.

```
mod1 <- lm(lnhrpay~grad,data = data_USoc)
stargazer_HC(mod1)</pre>
```

```
##
##
                          Dependent variable:
##
                                lnhrpay
  gradany degree
                                0.472***
                                (0.005)
##
##
                                2.138***
## Constant
##
                                (0.003)
##
## Observations
                                 58,942
## R2
                                 0.119
## Adjusted R2
                                 0.119
## Residual Std. Error 0.592 (df = 58940)
## F Statistic 7,959.665*** (df = 1; 58940)
                       *p<0.1; **p<0.05; ***p<0.01
## Note:
```

And let's calculate the actual percentage points raw differential which is a function of the estimated coefficient to the grad variable:

```
(exp(mod1$coefficients["gradany degree"])-1)*100
```

```
## gradany degree
## 60.28478
```

Clearly there is a massive difference. Graduates, on average, earn more than 60% higher hourly wages.

## A regression - gender and education differences

We found that, individually, gender and degree status make significant differences to hourly pay. Let's use the full power of regression analysis and see how hourly pay changes as a function of both these factors.

```
mod1 <- lm(lnhrpay~grad+male,data = data_USoc)
stargazer_HC(mod1)</pre>
```

```
##
                       Dependent variable:
##
##
                            lnhrpay
## gradany degree
                            0.469***
##
                            (0.005)
##
## malemale
                            0.176***
##
                             (0.005)
##
## Constant
                            2.060***
##
                            (0.004)
## Observations
                            58,942
                             0.138
## R2
## Adjusted R2
                             0.138
## Residual Std. Error 0.586 (df = 58939)
## F Statistic 4,727.510*** (df = 2; 58939)
## -----
## Note:
                    *p<0.1; **p<0.05; ***p<0.01
```

Now with interaction terms. MARTYN this uses an interaction variable not like the "#" in stata!

```
mod2 <- lm(lnhrpay~grad*male,data = data_USoc)
stargazer_HC(mod2)</pre>
```

```
##
  ______
##
                      Dependent variable:
##
##
                           lnhrpay
  _____
## gradany degree
                            0.484***
##
                            (0.007)
##
## malemale
                            0.187***
##
                            (0.006)
##
## gradany degree:malemale
                           -0.034***
##
                            (0.011)
##
## Constant
                            2.056***
##
                            (0.004)
## Observations
                            58,942
                            0.138
## Adjusted R2
                            0.138
## Residual Std. Error 0.586 (df = 58938)
```