# Introduction to Handling Data ECON20222 - Lecture 2 - GUN EXAMPLE version

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February 2024

## Aim for today

- Explore data
- Review hypothesis testing
- Review simple regression analysis
- Become more familiar with R

### Preparing your workfile

We add the basic libraries needed for this week's work:

```
library(tidyverse) # for almost all data handling tasks
library(readxl) # to import Excel data
library(ggplot2) # to produce nice graphics
library(stargazer) # to produce nice results tables
```

# New Dataset - US States Gun Policy

This is the example from the Siegel et al. (2019) paper which attempts to establish whether gun control laws have a causal impact on firearm deaths.

The data are from a variety of sources and some of them are collated in "US\_Gun\_example.csv". It comprises

- Data for each of the 51 US States and for years 2001 to 2021. This delivers 21\*51=1071 observations
- Data on age-adjusted death rates by firearm
- Data on when particular gun laws were in place in different states
- Data for a number of covariates (unemployment rate, number of officers, etc.)

```
merge_data <- read.csv("US_Gun_example.csv") # import data</pre>
```

This dataset was created with a significant amount of data handling and cleaning.

#### Gun Law Data

```
str(merge_data) # prints some basic info on variables
## 'data frame': 1071 obs. of 19 variables:
   $ X
                     : int 1 2 3 4 5 6 7 8 9 10 ...
##
##
   $ Year
                     $ State_code
                     : chr
                           "AK" "AL" "AR" "AZ" ...
##
##
   $ State
                     : chr "Alaska" "Alabama" "Arkansas" "Arizona" ...
##
   $ Population
                     : int 633687 4467634 2691571 5273477 34479458 4425687 34328
   $ Mechanism
                     : chr "Firearm" "Firearm" "Firearm" "Firearm" ...
##
##
   $ pol ubc
                    : int 0000101NA00...
   $ pol_vmisd
                     : int 0000101NA10...
##
   $ pol_mayissue
                     : int 0 1 0 0 1 1 1 NA 1 0 ...
##
##
   $ Age.Adjusted.Rate: num 14.83 16.41 15.27 15.92 9.32 ...
                           2.7 2.8 2.73 2.77 2.23 ...
##
   $ logy
                     : num
##
   $ ur
                           6.28 5.18 4.76 4.72 5.47 ...
                     : num
##
   $ law.officers
                     : int
                           1821 15303 7538 18548 106244 15172 9825 4716 2964 630
                           287 343 280 352 308 ...
##
   $ law.officers.pc
                     : num
##
   $ vcrime
                     : int
                           3696 19203 12042 28275 210661 15334 11387 4845 4845 1
                           583 430 447 536 611 ...
##
   $ vcrime.pc
                     : num
##
   $ alcc.pc
                     : num
                           2.67 1.86 1.74 2.5 2.2 ...
##
   $ incarc
                     : int 3033 24741 11489 27710 157142 14888 17507 NA 6841 724
##
   $ incarc.pc
                     : num
                           479 554 427 525 456 ...
```

## Data Description

Some of the names in merge\_data are obvious, but let us introduce a few in more detail.

- Age.Adjusted.rate Deaths by firearm for every 100,000 population in a State-Year.
   Here is a note on age adjustment.
- ur Average annual unemployment rate in a State-Year
- law.officers.pc number of law officers per 100,000 population in a State-Year
- vcrime.pc number of violent crimise (excl. homicides) per 100,000 population in a State-Year

These are the key variables we concentrate on in this data introduction.

```
summary(merge_data[c("Age.Adjusted.Rate","ur","law.officers.pc","vcrime.pc")])
```

```
##
   Age.Adjusted.Rate
                                      law.officers.pc
                                                        vcrime.pc
                           ur
   Min. : 2.14
##
                     Min.
                            : 2.100
                                      Min.
                                            : 37.08
                                                      Min.
                                                                76.94
   1st Qu.: 8.84
                     1st Qu.: 4.204
                                      1st Qu.:255.98
                                                      1st Qu.: 268.22
##
##
   Median :11.72
                     Median : 5.283
                                      Median: 296.35
                                                      Median: 358.09
   Mean :12.05
                     Mean : 5.648
                                     Mean :310.21
                                                      Mean : 393.14
##
##
   3rd Qu.:15.05
                     3rd Qu.: 6.737
                                      3rd Qu.:343.69
                                                      3rd Qu.: 493.70
##
   Max.
          :33.82
                     Max.
                            :13.733
                                      Max.
                                            :894.46
                                                      Max.
                                                             :1056.47
##
                                      NA's :23
```

#### Data - State-Years

#### To find the states and years in the sample:

```
unique (merge data$State) # unique finds all the different values in a variable
    [1] "Alaska"
                                "Alabama"
                                                        "Arkansas"
    [4] "Arizona"
                                "California"
                                                        "Colorado"
    [7] "Connecticut"
                                "District of Columbia" "Delaware"
## [10] "Florida"
                                "Georgia"
                                                        "Hawaii"
## [13] "Iowa"
                                "Idaho"
                                                        "Illinois"
## [16] "Indiana"
                                "Kansas"
                                                        "Kentucky"
## [19] "Louisiana"
                                "Massachusetts"
                                                        "Maryland"
## [22] "Maine"
                                "Michigan"
                                                        "Minnesota"
## [25] "Missouri"
                                "Mississippi"
                                                        "Montana"
## [28] "North Carolina"
                                "North Dakota"
                                                        "Nebraska"
## [31] "New Hampshire"
                                "New Jersev"
                                                        "New Mexico"
## [34] "Nevada"
                                "New York"
                                                        "Ohio"
## [37] "Oklahoma"
                                "Oregon"
                                                        "Pennsylvania"
## [40] "Rhode Island"
                                "South Carolina"
                                                        "South Dakota"
## [43] "Tennessee"
                                "Texas"
                                                        "IItah"
## [46] "Virginia"
                                "Vermont"
                                                        "Washington"
## [49] "Wisconsin"
                                "West Virginia"
                                                        "Wyoming"
unique(merge_data$Year)
```

```
## [1] 2001 2002 2003 2004 2005 2006 2007 2008 2009 2010 2011 2012 2013 2014 2015 ## [16] 2016 2017 2018 2019 2020 2021
```

#### Point out what unique does.

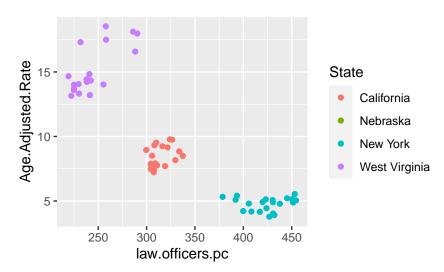
#### Data - State-Years

To find out how many observations we have for each state (State) and also calculate the mean of the above four variables. Use piping technique of the tidyverse

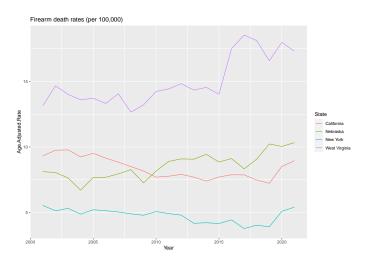
```
## # A tibble: 4 x 6
                  n avg.fds avg.ur avg.off avg.vcr
##
   State
    <chr>
              <int>
                     <dbl> <dbl> <dbl>
                                        <dbl>
##
                 21 8.40 7.32 314. 481.
## 1 California
                 21 8.57 3.54 NA 297.
## 2 Nebraska
## 3 New York
               21 4.76 6.21 424. 404.
## 4 West Virginia 21
                     15.0 6.24 NA 301.
```

For each state (j = 1, ..., 51) we have observations from 21 years (t = 1, ..., 21). We index observations with the subscript jt. This is what we call a panel.

Plotting the number of officers against firearm death rates



What about Nebraska? Is there a causal relation or unobserved heterogeneity?

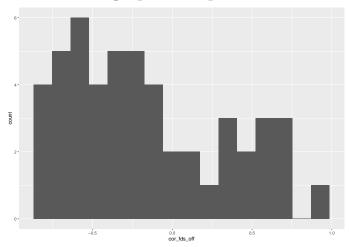


There seems to be a negative relationship between Firearm death rates (Age.Adjusted.Rate) and number of officers (Law.Officers.pc). This is variation across states and years.

Is there such a relationship inside states as well? **Time/year variation** only.

We calculate correlations for each state:

```
e.g. Arizona: Corr_{AZ}(fds_{AZ,t}, off_{AZ,t}) = \frac{Cov_{AZ}(fds_{AZ,t}, off_{AZ,t})}{s_{fds_{AZ,t}} s_{off_{AZ,t}}}
## # A tibble: 8 x 2
     State cor fds off
##
     <chr>
                          <dbl>
##
   1 Alabama
                        -0.120
   2 Alaska
                        -0.623
   3 Arizona
                        -0.265
## 4 Arkansas
                   0.596
## 5 California
                      0.403
## 6 Colorado
                      -0.646
## 7 Connecticut
                   -0.119
## 8 Delaware
                        -0.320
```



Point out that correlations are in [-1,1]. They are standardised covariances. Ensure you revise how to calculate sample s.d. and covariances!

## Data on Maps

Geographical relationships are sometimes best illustrated with maps.

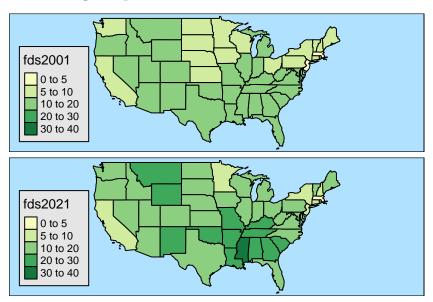
Sometimes these will reveal a pattern.

R can create great maps (but it requires a bit of setup - see the additional file on BB). You need the following

- A shape file for each country
- The statistics for each country
- a procedure to merge these bits of information in one data-frame (merge)

Let's look at the firearm death rates and how these vary by state.

## Data Using Maps: 2001 v 2021



Hypothesis testing is a core technique used in empirical analysis. Use sample data to infer something about the population mean (or correlation, or variance, etc). Hence *inference*.

It is crucial to understand that the particular sample we have is one of many different possible samples. Whatever conclusion we arrive at is not a conclusion with certainty.

#### Example

Are the average firearm death rates in 2001 and 2021 different from each other?

 $H_0$ :  $\mu_{fds,2001} = \mu_{fds,2021}$  $H_A$ :  $\mu_{fds,2001} \neq \mu_{fds,2021}$ 

The truth is either represented by  $H_0$  or  $H_A$ 

When performing a test we need to calibrate some level of uncertainty. We typically fix the Probability with which we reject a correct null hypothesis (Type I error). This is also called the significance level.

Depending on the type of hypothesis there will be a test statistic which will be used to come to a decision.

Assuming that  $H_0$  is true this test statistic has a random distribution (frequently t, N,  $\chi^2$  or F). We can then use this distribution to evaluate how likely it would have been to get the type of sample we have if the null hypothesis was true ( p-value ) or obtain critical values.

#### Decision Rule 1

If that probability, **p-value** < **significance level**, then we reject  $H_0$ . If, however, that **p-value** > **significance level** then we will not reject  $H_0$ 

#### Decision Rule 2

If the absolute value of the **test statistic** > the **critical value** (obtain from the Null distribution - see next slide), then we reject  $H_0$ .

If, however, the absolute value of the **test statistic** is < the **critical value**, then we will not reject  $H_0$ .

Example The test statistic

$$t = \frac{f\bar{d}s_{2021} - f\bar{d}s_{2001}}{\sqrt{\frac{s_{fds,2021}}{n} + \frac{s_{fds,2001}}{n}}}$$

How is this test statistic distributed (assuming  $H_0$  is true)? \*\*If\*\*

- The two samples are independent
- ② The random variables  $fds_{2021}$  and  $fds_{2001}$  are either normally distributed or we have sufficiently large samples
- **3** The variances in the two samples are identical

then  $t \sim t$  distributed with (n+n-2) degrees of freedom.

The above assumptions are crucial (and they differ from test to test). If they are not met then the resulting p-value (or critical values) are not correct. Other tests will have different distributions and require different assumptions!

## Hypothesis Testing - Example 1

#### Let's create a sample statistic:

```
## [1] "mean_2021 - mean_2001 = 370.23 - 424.34 = -54.11"
```

Is this different statistically and/or economically significant?

\textcolor{student}{Comment that the difference, 54, is about 13% of the 2001 mean.}

## Hypothesis Testing - Example 1

Formulate a null hypothesis: the difference in population means (mu) in vcrime.pc is equal to 0. We use the t.test function. We deliver the vcrime.pc series for both years to t.test.

```
t.test(test_data_2021$vcrime.pc,test_data_2001$vcrime.pc, mu=0) # testing that mu
```

```
##
## Welch Two Sample t-test
##
## data: test_data_2021$vcrime.pc and test_data_2001$vcrime.pc
## t = -1.5375, df = 94.887, p-value = 0.1275
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -123.98112 15.75956
## sample estimates:
## mean of x mean of y
```

The p-value then tells us how likely it is to get a result like the one we got (a difference of -54 or larger) if the null hypothesis was true (i.e. the true population means were the same).

The p-value is 0.1275 and hence it is possible but not very likely that this difference would have arisen by chance if the null hypothesis WAS correct.

## 370.2264 424.3372

## Hypothesis Testing - Example 2

What about the difference between 2011 and 2021 though?

```
test_data_2011 <- merge_data %>%
  filter(Year == 2011)
t.test(test data 2021$vcrime.pc,test data 2011$vcrime.pc, mu=0) # testing that mu
##
##
    Welch Two Sample t-test
##
## data: test data 2021$vcrime.pc and test data 2011$vcrime.pc
## t = 0.37061, df = 99.381, p-value = 0.7117
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -47.90612 69.91315
## sample estimates:
## mean of x mean of y
## 370.2264 359.2229
```

The p-value is 0.7117 and hence there is very likely that we would get a difference like the one we see or bigger if the null hypothesis was true.

## Hypothesis Testing - To reject or to not reject

When comparing between 2011 and 2021 the p-value was 0.71: Do not Reject  $H_0$ 

When comparing between 2001 and 2021 the p-value was app. 0.13: hmmm ...

- Conventional significance levels are 10%, 5%, 1% or 0.1%
- But what do they mean?

To illustrate we add a random variable (rvar) to all observations. The value comes from the identical distribution for all observations, the standard normal (N(0,1)) or rnorm in R):

```
merge_data$rvar <- rnorm(nrow(merge_data))  # add random variable

test_data <- merge_data
years <- unique(merge_data$Year)  # List of all years
n_years <- length(years)</pre>
```

By construction we know that the true underlying mean is identical in all countries.

But what happens if we calculate sample means of rvar in all years and then compare between years? (21\*21-21)/2=210 comparisons

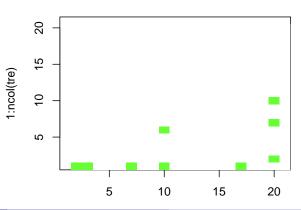
# Hypothesis Testing - To reject or to not reject

We have 210 hypothesis tests, all testing a correct null hypothesis. If a p-value is smaller than 10% we decide to reject  $H_0$ .

All null hypotheses we know to be true (population means are identical). Let's see how many of these hypothesis tests delivered p-values which are smaller than 10%.

```
## tre
## FALSE TRUE
## 201 9
```

Let's present a graphical representation of these results. Every green square representing a rejection of the null hypothesis.



## Regression Analysis - Introduction

Tool on which most of the work in this unit is based

- Allows to quantify relationships between 2 or more variables
- It can be used to implement hypothesis tests
- However it does not necessarily deliver causal relationships!

It is very easy to compute for everyone! Results will often have to be interpretated very carefully.

Your skill will be to interpret carefully and correctly!!!!

Let's start by creating a new dataset which only contains the 2001 data.

```
test_data <- merge_data %>%
filter(Year == 2001)
```

Now we run a regression of the violent crimes per 100,000 population variable (vcrime.pc) against a constant only.

```
vcrime.pc_i = \alpha + u_i
```

```
mod1 <- lm(vcrime.pc~1,data=test_data)</pre>
```

We use the stargazer function to display regression results

```
stargazer(mod1, type="text")
```

```
##
##
                            Dependent variable:
##
##
                                vcrime.pc
                                424.337***
  Constant
                                 (27.624)
##
##
                                    51
  Observations
## R2
                                   0.000
## Adjusted R2
                                   0.000
## Residual Std. Error 197.274 (df = 50)
## Note:
                        *p<0.1; **p<0.05; ***p<0.01
```

The estimate for the constant,  $\hat{\alpha}$ , is the sample mean.

Testing  $H_0: \mu_{vcrime.pc} = 0$  can be achieved by

```
##
## One Sample t-test
##
## data: test_data$vcrime.pc
## t = 15.361, df = 50, p-value < 2.2e-16
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## 368.8529 479.8216
## sample estimates:
## mean of x
## 424.3372</pre>
```

We can use the above regression to achieve the same:

$$t - test = \widehat{\alpha}/se_{\widehat{\alpha}} = (424.337 - 0)/27.624 = 15.36$$

That  $H_0$  makes no sense as all states show positive numbers of 'vcrime.pc'.

New dataset which contains the 2001 and 2021 data. Create a dummy variable (1 = if obs from 2021, 0 otherwise)

```
Dependent variable:
                              vcrime.pc
## Year2021
                               -54.111
                                (35.194)
                               424.337***
## Constant
                               (24.886)
## Observations
                                  102
## R2
                                  0.023
## Adjusted R2
                                  0.013
## Residual Std. Error 177.722 (df = 100)
## F Statistic
                          2.364 (df = 1; 100)
                       *p<0.1: **p<0.05: ***p<0.01
## Note:
```

```
##
##
                                                                                                                                                        Dependent variable:
##
##
                                                                                                                                                                                   vcrime.pc
                 Year2021
                                                                                                                                                                                    -54.111
                                                                                                                                                                                     (35.194)
##
##
                Constant
                                                                                                                                                                              424.337***
                                                                                                                                                                                     (24.886)
##
##
                Observations
                                                                                                                                                                                                     102
## R2
                                                                                                                                                                                               0.023
## Adjusted R2
                                                                                                                                                                                               0.013
## Residual Std. Error 177.722 (df = 100)
                                                                                                            2.364 (df = 1: 100)
## F Statistic
## Note:
                                                                                                                                  *p<0.1; **p<0.05; ***p<0.01
               • \hat{\alpha} = 424.337 = E(vcrime.pc|2001) = E(vcrime.pc|Year2021 = 0)
               \bullet \ \widehat{\beta} = -54.111 = E(vcrime.pc|2021) - E(vcrime.pc|2001) = E(vcrime.pc|Year2021 = 1) + E(vcrime.pc|2021) = E(vcrime.pc|20
                             1) - E(vcrime.pc|Year2021 = 0)
```

We now estimate a regression model which includes a constant and the number of law enforcement officers (per 100,000), law.officer.pc, as an explanatory variable (only 2021 data).

 $vcrime.pc_i = \alpha + \beta \ law.officer.pc_i + u_i$ 

##		
##		
##		Dependent variable:
##		
##		vcrime.pc
##		
##	law.officers.pc	0.204
##		(0.193)
##		
##	Constant	311.421***
##		(61.296)
##		
##		
##	Observations	50
##	R2	0.023
##	Adjusted R2	0.002
##	Residual Std. Error	156.747 (df = 48)
##	F Statistic	1.114 (df = 1; 48)
##		
##	Note:	*p<0.1; **p<0.05; ***p<0.01

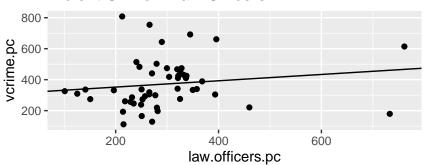
##		
##		Dependent variable:
##		
##		vcrime.pc
##	law.officers.pc	0.204
##		(0.193)
	Constant	311.421***
##		(61.296)
##		
##		
##	Observations	50
##	R2	0.023
##	Adjusted R2	0.002
##	Residual Std. Error	156.747 (df = 48)
##	F Statistic	1.114 (df = 1; 48)
##		
##	Note:	*p<0.1; **p<0.05; ***p<0.01

- $\hat{\beta} = 0.235$ . As the number of law officers increases by one unit (here that represents an increase of one officer per 100,000 population) we should expect that the number of violent crimes increases by 0.204 units (0.204 crimes per 100,000 population).
- $\widehat{\alpha} = 311.421$ . For a state with 0 law officers (per 100,000 population) we should expect there to be 311 violent crimes per 100,000 population.

Let's present a graphical representation.

```
ggplot(test_data, aes(x=law.officers.pc, y=vcrime.pc)) +
   geom_point() +
   geom_abline(intercept = mod1$coefficients[1], slope = mod1$coefficients[2])+
   ggtitle("Violent Crime v Law Officers")
```

#### Violent Crime v Law Officers



# Regression Analysis - What does it actually do?

Two interpretations (noye that here y is the dependent and x the explanatory variable)

- Finds the regression line (via  $\widehat{\alpha}$  and  $\widehat{\beta}$ ) that minimises the residual sum of squares  $\Sigma(y_i \widehat{\alpha} \widehat{\beta} x_i)^2$ .  $\rightarrow$  Ordinary Least Squares (OLS)
- ② Finds the regression line (via  $\hat{\alpha}$  and  $\hat{\beta}$ ) that ensures that the residuals ( $\hat{u}_i = y_i \hat{\alpha} \hat{\beta} x_i$ ) are uncorrelated with the explanatory variable(s).

In many ways 2) is the more insightful one.

# Regression Analysis - What does it actually do?

$$y = \alpha + \beta \ x + u$$

#### Assumptions

One of the regression assumptions is that the (unobserved) error terms u are uncorrelated with the explanatory variable(s), x. Then we call x exogenous.

This implies that Cov(x, u) = Corr(x, u) = 0

#### In sample

$$y_i = \widehat{\alpha} + \widehat{\beta} x_i + \widehat{u}$$

Where  $\hat{\alpha} + \hat{\beta} x_i$  is the regression-line.

In sample  $Corr(x_i, \widehat{u}_i) = 0$  (is ALWAYS TRUE BY CONSTRUCTION).

# Regression Analysis - Underneath the hood?

$$y = \alpha + \beta x + u$$

#### What happens if you call

mod1 <- lm(vcrime.pc~law.officers,data=test\_data)?</pre>

You will recall the following from Year 1 stats:

$$\hat{\beta} = \frac{\widehat{Cov}(y,x)}{\widehat{Var}(x)} = \frac{\widehat{Cov}(vcrime.pc, law.officers.pc)}{\widehat{Var}(law.officers.pc)}$$

$$\hat{\alpha} = \overline{y} - \hat{\beta} \ \overline{x} = \overline{vcrime.pc} - \hat{\beta} \ \overline{law.officers.pc}$$

The software will then replace  $\widehat{Cov}(y,x)$  and  $\widehat{Var}(x)$  with their sample estimates to obtain  $\hat{\beta}$  and then use that and the two sample means to get  $\hat{\alpha}$ .

# Regression Analysis - Underneath the hood?

Need to recognise that in a sample  $\hat{\beta}$  and  $\hat{\alpha}$  are really random variables.

$$\begin{split} \hat{\beta} &= \frac{\widehat{Cov}(y,x)}{\widehat{Var}(x)} \\ &= \frac{\widehat{Cov}(\alpha+\beta\ x+u,x)}{\widehat{Var}(x)} \\ &= \frac{\widehat{Cov}(\alpha,x) + \beta \widehat{Cov}(x,x) + \widehat{Cov}(u,x)}{\widehat{Var}(x)} \\ &= \beta \frac{\widehat{Var}(x)}{\widehat{Var}(x)} + \frac{\widehat{Cov}(u,x)}{\widehat{Var}(x)} = \beta + \frac{\widehat{Cov}(u,x)}{\widehat{Var}(x)} \end{split}$$

So  $\hat{\beta}$  is a function of the random term u and hence is itself a random variable. Once  $\widehat{Cov}(y,x)$  and  $\widehat{Var}(x)$  are replaced by sample estimates we get ONE value which is draw from a random distribution.

# Regression Analysis - The Exogeneity Assumption

Why is **assuming** Cov(x, u) = 0 important when, in sample, we are guaranteed  $Cov(x_i, \hat{u}_i) = 0$ ?

If  $Cov(x_i, u_i) = 0$  is **not true**, then

- Estimating the model by OLS imposes an incorrect relationship
- **②** The estimated coefficients  $\hat{\alpha}$  and  $\hat{\beta}$  are biased (on average incorrect if we had many samples)
- **1** The regression model has no causal interpretation

As we cannot observe  $u_i$ , the assumption of exogeneity cannot be tested and we need to make an argument using economic understanding.

# Regression Analysis - Outlook

$$y = \alpha + \beta x + u$$

Much of empirical econometric analysis is about making the exogeneity assumption (Corr(x,u)=0) more plausible/as plausible as possible. But this begins with thinking why an explanatory variable x is endogenous.

- Most models have more than one explanatory variable.
- Including more relevant explanatory variables can make the exogeneity assumption more plausible.
- **9** But fundamentally, if Cov(u, x) = 0 is implausible we need to find another variable z for which Cov(u, z) = 0 is plausible. A lot of the remainder of this unit is about elaborating on this issue.

#### Outlook

Over the next weeks you will learn

- Simple OLS regression with dummy
- Endogeneity
- Multiple regression
- Difference-in-Difference (DiD) estimator