Introduction to Panel Data Models

Preparing your workfile

We add the basic libraries needed for this week's work:

```
library(tidyverse)    # for almost all data handling tasks
library(ggplot2)      # to produce nice graphiscs
library(stargazer)    # to produce nice results tables
library(haven)        # to import stata file
library(AER)          # access to HS robust standard errors
source("stargazer_HC.r")  # includes the robust regression display
```

As we are using panel methods we also require an additional package `plm`.

```
# install.packages("plm") # only exwcute this if plm is not installed yet
library(plm)
```

Introduction

The data are an extract from the Understanding Society Survey (formerly the British Household Survey Panel).

Data Upload - and understanding data structure

Upload the data, which are saved in a STATA datafile (extension `.dta`). There is a function which loads STATA file. It is called `read_dta` and is supplied by the `haven` package.

```
data_USoc <- read_dta("20222_USoc_extract.dta")
data_USoc <- as.data.frame(data_USoc)    # ensure data frame structure
names(data_USoc)
```

```
##  [1] "pidp"    "age"     "jbhrs"   "paygu"   "wave"    "cpi"     "year"
##  [8] "region"  "urate"   "male"    "race"    "educ"    "degree"  "mfsize9"
```

Let us ensure that categorical variables are stored as `factor` variables. It is easiest to work with these in R.

```
data_USoc$region <- as_factor(data_USoc$region)
data_USoc$male <- as_factor(data_USoc$male)
data_USoc$degree <- as_factor(data_USoc$degree)
data_USoc$race <- as_factor(data_USoc$race)
```

The pay information (`paygu`) is provided as a measure of the (usual) gross pay per month. As workers work for varying numbers of hours per week (`jbhrs`) we divide the monthly pay by the approximate monthly hours (`4*jbhrs`). We shall also adjust for increasing price levels (as measured by `cpi`). These two adjustments leave us with an inflation adjusted hourly wage. We call this variable `hrpay` and also calculate the natural log of this variable (`lnhrpay`).

```r
data_USoc <- data_USoc %>%
             mutate(hrpay = paygu/(jbhrs*4)/(cpi/100)) %>%
             mutate(lnhrpay = log(hrpay))
```

As we wanted to save these additional variables we assign the result of the operation to `data_USoc`.

We will also use the logarithm of the unemployment rate

```r
data_USoc <- data_USoc %>%
             mutate(lnurate=log(urate))
```

Understanding the Panel Structure

To explain the meaning of these let us just pick out all the observations that pertain to one particular individual (`pidp == 272395767`). The following command does the following in words: "Take `data_USoc` filter/keep all observations which belong to individual pidp == 272395767, then select a list of variables (we don't need to see all 14 variables) and print the result":

```r
data_USoc %>% filter(pidp == 272395767) %>%
             select(c("pidp","male","wave","year","paygu","age","educ")) %>%
             print()
```

```
##        pidp   male wave year    paygu age educ
## 1 272395767 female    1 2009 774.8302  40   11
## 2 272395767 female    2 2010 812.2778  41   11
## 3 272395767 female    3 2011 772.1625  42   11
```

The same person (female) was observed three years in a row (from 2009 to 2011). Their gross monthly income changed, as did, of course, their age, but not their education. This particular person was observed in three consequitive waves. Let's se whether this is a commom pattern.

In the context of this exercise we will ignore the second wave and only look at waves 1 and 3.

```r
data_USoc <- data_USoc %>%
  filter(wave != 2) %>%
  filter(!is.na(lnhrpay))
```

The code below figures how many waves we have for each individual (1 or 2) and then saves this in a new variable ('n_wave). This information will be used later as we may want to know whether only using observations for which we have both waves makes a difference to the analysis.

```r
data_USoc <- data_USoc %>%
               group_by(pidp) %>%
               mutate(n_wave = n())
```

Now we need to let R know that we are dealing with panel data. This is why we loaded up the `plm` library which contains the `plm.data` function. Using the `index = c("pidp","wave")` we let the function know what identifies the individuals and what identifies the wave.

```r
pdata_USoc <- pdata.frame(data_USoc, index = c("pidp","wave")) # defines the panel dimensions
```

We saved the output in `pdata_USoc` and we will use this for any panel data estimations.

When dealing with panel data it is super useful to understand in how many and in which wave individuals are prepresented. We already calculated the `n_wave` variable which tells us in how many of our remaining two waves observations are represented. We also have information (`wave`) on which wave someone is represented in. To disentagle this we merely need a contingency `table` of the `n_wave` and `waves` variables.

```r
table(pdata_USoc$n_wave,pdata_USoc$wave, dnn = c("n_waves","waves"))
```

```
##          waves
## n_waves      1     3
##        1  9666  4112
##        2 13078 13078
```

Naturally the 13078 respondents which have two observations (`n_wave == 2`) are represented in waves 1 and 3. Then we have (`n_wave == 1`) 9666 respondents which are represented in wave 1 and the 4112 which are represented in wave 3.

For the respondents for which we have 2 waves of observations we can actually calculate a difference, or change in variables. This will become important in a later model estimation (althoough for that we could let R do the work in the background) and hence we will calculate these variables explicitely, here for `lnhrpay` and `lnurate`.

```r
# the lag function below will recognise the panel nature of the data and
# will only calculate lags for individuals
# we also need to specify that we are calculating k=2 step lag as
# we calculate the difference between wave 3 and 1

Dlnhrpay <- pdata_USoc$lnhrpay-lag(pdata_USoc$lnhrpay,k=2)
Dlnurate <- pdata_USoc$lnurate-lag(pdata_USoc$lnurate,k=2)
#Dregion <- ifelse(pdata_USoc$region==lag(pdata_USoc$region,k=2),"no move","move")
pdata_USoc$Dlnhrpay <- Dlnhrpay   # add the new series to the dataframe
pdata_USoc$Dlnurate <- Dlnurate
```

For a later purpose we will also identify all individuals who moved from one region to another between waves 1 and 3. It is not so important to understand the code of how the `move` variable is generated and hence we do not show it here.

```
## # A tibble: 3 x 2
##   move        n
##   <fct>   <int>
## 1 no move 25804
## 2 move      352
## 3 <NA>    13778
```

So ther are 352 observations associated with movers. That means that there are 176 movers.

Some data descriptions

We will use the `lnhrpay` and the `urate` variables below. We therefore will have a look at these variables.

```r
stargazer(pdata_USoc[,c("lnhrpay","urate","year","Dlnhrpay","Dlnurate")],type = "text")
```

```
##
## ======================================================================
## Statistic   N      Mean    St. Dev.   Min   Pctl(25) Pctl(75)  Max
## ----------------------------------------------------------------------
## lnhrpay   39,934   2.284    0.635   -7.816   1.888    2.678   8.868
## urate     39,934   7.877    1.303    5.800   6.400    9.000   10.800
## year      39,934 2,010.393  1.146    2,009   2,009    2,011   2,013
## Dlnhrpay  13,078  -0.009    0.524   -10.381  -0.145   0.123   9.522
## Dlnurate  13,078   0.037    0.065   -0.464   -0.011   0.083   0.547
## ----------------------------------------------------------------------
```

Note the following. For `Dlnhrpay` and `Dlnurate` we only have one observation for each respondednt for which we have observations from wave 1 and 3 (i.e. 13,078). For the other variables we have two observations for those represented in both waves and one observation for those only represented in one wave.

You should also note that there is variation in both of the change variables. In the case of the change in the unemployment rate that is as people reside in different regions and the unemployment change varies between different regions and years. In addition there is a small number of respondents who move from one region to another. This is not visible from the code above.

Let us look at some summary statistics grouped by region

```
pdata_USoc %>% group_by(region) %>%
              summarise(n = n(), mean_lnhrpay = mean(lnhrpay),mean_urate = mean(urate))
```

```
## # A tibble: 12 x 4
##    region                        n mean_lnhrpay mean_urate
##    <fct>                     <int>        <dbl>      <dbl>
##  1 north east                 1576         2.21       9.88
##  2 north west                 4280         2.24       8.44
##  3 yorkshire and the humber   3247         2.20       9.00
##  4 east midlands              3107         2.20       9.15
##  5 west midlands              3454         2.23       7.67
##  6 east of england            3724         2.32       6.58
##  7 london                     5736         2.42       9.30
##  8 south east                 5125         2.39       6.10
##  9 south west                 3119         2.25       6.11
## 10 wales                      1831         2.14       8.45
## 11 scotland                   3020         2.27       7.76
## 12 northern ireland           1715         2.24       6.78
```

Below we will want to use the mean `lnhrpay` and mean `lnurate` as calculated for every region-year. The following will group the data by region-year (as we have 12 regions and 5 years we will have potentially up to 60 such groups). This is similar to the above command but note that we start with `pdata_USoc <-` to ensure that the calculated average wage and unemployment rate values are added as variables to the data frame. Also, instead of `summarise` (which displays the calculated statistics) we use the `mutate` function as we want the calculated series to be saved in the data frame.

```
pdata_USoc <- pdata_USoc %>%
              group_by(region,year) %>%
              mutate(mean_lnhrpay = mean(lnhrpay),mean_urate = mean(urate))
```

Estimating Models

We start by estimating a model which does not use the panel nature of the data.

```
POLS0 <- lm(lnhrpay~lnurate, data = pdata_USoc)
stargazer_HC(POLS0)
```

```
##
## ===========================================================
##                              Dependent variable:
##                     ---------------------------------------
##                                    lnhrpay
## -----------------------------------------------------------
## lnurate                           -0.102***
##                                    (0.019)
```

```
##
## Constant                          2.493***
##                                    (0.038)
##
## -----------------------------------------------------------
## Observations                      39,934
## R2                                 0.001
## Adjusted R2                        0.001
## Residual Std. Error          0.634 (df = 39932)
## F Statistic               30.049*** (df = 1; 39932)
## ===========================================================
## Note:                          *p<0.1; **p<0.05; ***p<0.01
##                        Robust standard errors in parenthesis
```

Let's add the predicted model values to the data frame.

```
pdata_USoc$pred_POLS0 <- POLS0$fitted.values
```

Here we basically used all observations available, whether they were from wave 1 or 3. We **pooled** the observations and hence we could use our normal `lm` function to estimate this model. The `plm` package we imported earlier has a few panel specific tricks up its sleeve and we could estimate this model with the `plm` function.

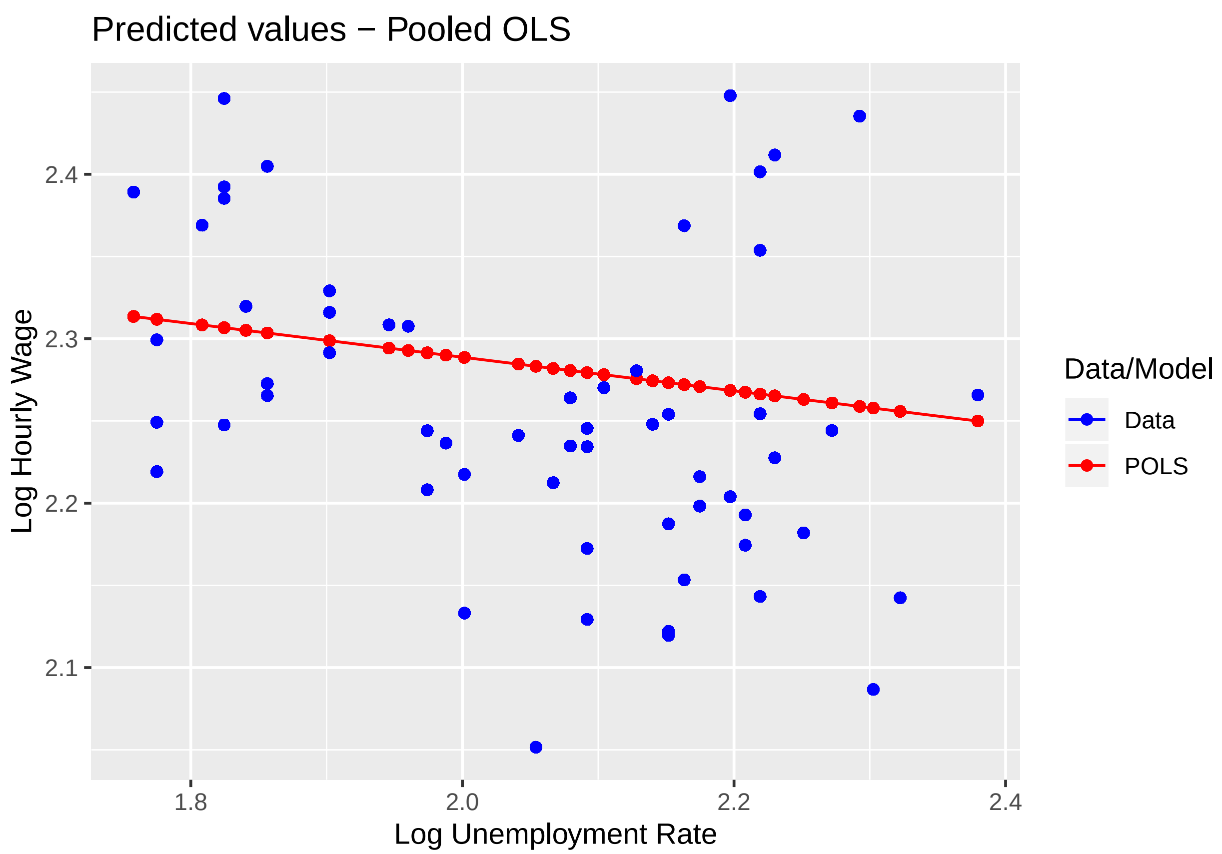
```
POLS0a <- plm(lnhrpay~lnurate, data = pdata_USoc, model = "pooling")
stargazer_HC(POLS0a)
```

```
##
## ===================================================
##                          Dependent variable:
##               -------------------------------------
##                                lnhrpay
## ---------------------------------------------------
## lnurate                      -0.102***
##                               (0.019)
##
## Constant                      2.493***
##                               (0.038)
##
## ---------------------------------------------------
## Observations                  39,934
## R2                             0.001
## Adjusted R2                    0.001
## F Statistic        30.049*** (df = 1; 39932)
## ===================================================
## Note:                   *p<0.1; **p<0.05; ***p<0.01
##               Robust standard errors in parenthesis
```

Now we plot the predicted values and compare them against the

```
# pdf("Lecture6plot_Pooled.pdf",width = 5.5, height = 4) # uncomment to save as pdf
ggplot(pdata_USoc, aes(x=lnurate,y=pred_POLS0)) +
  geom_point(aes(colour = "red")) +
  geom_line(aes(colour = "red")) +
  geom_point(aes(y = mean_lnhrpay,colour = "blue")) +
  ggtitle("Predicted values - Pooled OLS") +
  ylab("Log Hourly Wage") +
  xlab("Log Unemployment Rate") +
```

```r
  scale_colour_manual(name="Data/Model", values = c(red = "red", blue = "blue"),labels=c("Data", "POLS"
```




```r
# dev.off() # uncomment to save as pdf
```

Now we will include a dummy variable for `wave == 3`. The `wave` variable is a factor variable with two levels (1 and 3) for waves 1 and 3.

```r
POLS1 <- lm(lnhrpay~lnurate+wave, data = pdata_USoc)
stargazer_HC(POLS1)
```

```
##
## ==========================================================
##                             Dependent variable:
##                      -------------------------------------
##                                   lnhrpay
## ----------------------------------------------------------
## lnurate                          -0.097***
##                                   (0.019)
##
## wave3                            -0.019***
##                                   (0.006)
##
## Constant                          2.491***
##                                   (0.038)
##
## ----------------------------------------------------------
## Observations                       39,934
```

```
## R2                                     0.001
## Adjusted R2                            0.001
## Residual Std. Error          0.634 (df = 39931)
## F Statistic               19.596*** (df = 2; 39931)
## ============================================================
## Note:                            *p<0.1; **p<0.05; ***p<0.01
##                        Robust standard errors in parenthesis
```

The first wave is the base category of `wave` and hence is not included. So far we have used the standard `lm` function to estimate this model.

Alternatively this could be estimated using the `plm` package

```
POLS1a <- plm(lnhrpay~lnurate+wave, data = pdata_USoc, model = "pooling")
stargazer_HC(POLS1a)
```

```
##
## ===================================================
##                        Dependent variable:
##                 -----------------------------------
##                              lnhrpay
## ---------------------------------------------------
## lnurate                     -0.097***
##                              (0.019)
##
## wave3                       -0.019***
##                              (0.006)
##
## Constant                    2.491***
##                              (0.038)
##
## ---------------------------------------------------
## Observations                 39,934
## R2                            0.001
## Adjusted R2                   0.001
## F Statistic        19.596*** (df = 2; 39931)
## ===================================================
## Note:                   *p<0.1; **p<0.05; ***p<0.01
##                 Robust standard errors in parenthesis
```

This regression will have observations for individuals for which we only observe one wave (`n_wave == 1`). Let's restrict the analysis to only individuals for which we have two waves (`n_wave == 2`).

```
POLS2 <- lm(lnhrpay~lnurate+wave, data = pdata_USoc, subset = (n_wave ==2))
stargazer_HC(POLS2)
```

```
##
## ============================================================
##                                Dependent variable:
##                        -------------------------------------
##                                      lnhrpay
## ------------------------------------------------------------
## lnurate                             -0.096***
##                                      (0.022)
##
## wave3                                -0.005
##                                      (0.008)
```

```
##
## Constant                              2.544***
##                                        (0.046)
##
## ----------------------------------------------------------
## Observations                          26,156
## R2                                     0.001
## Adjusted R2                            0.001
## Residual Std. Error              0.611 (df = 26153)
## F Statistic                   10.027*** (df = 2; 26153)
## ==========================================================
## Note:                          *p<0.1; **p<0.05; ***p<0.01
##                        Robust standard errors in parenthesis
```

or using the `plm` function

```
POLS2a <- plm(lnhrpay~lnurate+wave, data = pdata_USoc, subset = (n_wave ==2), model = "pooling")
stargazer_HC(POLS2a)
```

```
##
## ===================================================
##                         Dependent variable:
##                 -----------------------------------
##                               lnhrpay
## ---------------------------------------------------
## lnurate                      -0.096***
##                               (0.022)
##
## wave3                         -0.005
##                               (0.008)
##
## Constant                      2.544***
##                               (0.046)
##
## ---------------------------------------------------
## Observations                  26,156
## R2                             0.001
## Adjusted R2                    0.001
## F Statistic        10.027*** (df = 2; 26153)
## ===================================================
## Note:                  *p<0.1; **p<0.05; ***p<0.01
##                 Robust standard errors in parenthesis
```

Now we estimate a first difference (FD) model. We will only do this using the `plm` function. If we were to use the `lm` function we had to first calculate differenced series (which we have done on this occasion, but only to illustrate the mechanics). Before we estimate the model let's look at the data for a few respondents.

```
pdata_USoc %>% filter(pidp %in% c("3915445","68001367","68004087","68195851")) %>%
              select(c("pidp","male","wave","lnhrpay","Dlnhrpay","lnurate", "Dlnurate")) %>%
              print()
```

```
## # A tibble: 6 x 9
## # Groups:   region, year [5]
##   region         year pidp     male   wave    lnhrpay  Dlnhrpay lnurate Dlnurate
##   <fct>         <dbl> <fct>    <fct>  <fct> <dbl+lbl> <dbl+lbl>   <dbl>    <dbl>
## 1 scotland       2011 3915445  female 3          1.88   NA          2.09   NA
```

```
## 2 north east     2009 68001367 male   1          2.45   NA          2.22  NA
## 3 north east     2009 68004087 male   1          1.83   NA          2.22  NA
## 4 north east     2011 68004087 male   3          1.90    0.0728     2.38   0.160
## 5 north west     2009 68195851 female 1          2.20   NA          2.13  NA
## 6 west midlands  2011 68195851 female 3          1.84   -0.360      2.08  -0.0488
```

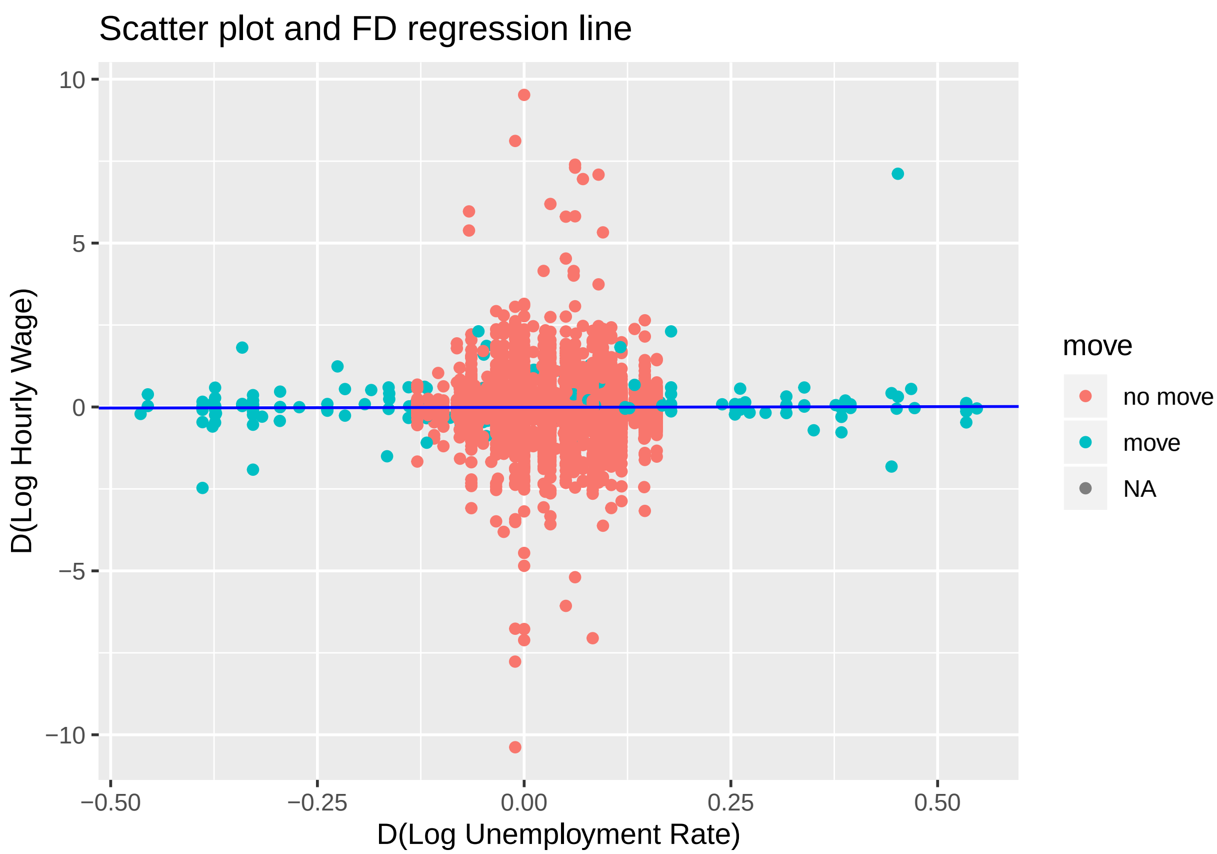
When estimating a FD model we are basically running a regression of `Dlnhrpay` on `Dlnurate`. Respondents for whom we do not have two waves will not be used in such a model. The calculation of the `Dlnhrpay` and `Dlnurate` series happens automatically inside the `plm` function when we specify `model = "fd"`.

```r
FD1a <- plm(lnhrpay~lnurate, data = pdata_USoc, subset = (n_wave ==2), model = "fd")
stargazer_HC(FD1a)
```

```
##
## ====================================================
##                          Dependent variable:
##               --------------------------------------
##                               lnhrpay
## ----------------------------------------------------
## lnurate                        0.042
##                               (0.071)
##
## Constant                     -0.011**
##                               (0.005)
##
## ----------------------------------------------------
## Observations                  13,078
## R2                            0.00003
## Adjusted R2                  -0.00005
## F Statistic           0.353 (df = 1; 13076)
## ====================================================
## Note:                  *p<0.1; **p<0.05; ***p<0.01
##               Robust standard errors in parenthesis
```

We can show a scatter plot of the available difference observations and the regression line estimated by `FD1a`.

```r
# pdf("Lecture6plot_FD_R.pdf",width = 5.5, height = 4) # uncomment to save as pdf
ggplot(pdata_USoc, aes(x=Dlnurate,y=Dlnhrpay,color=move)) +
  geom_point() +
  geom_abline(intercept = FD1a$coefficients[1], slope = FD1a$coefficients[2],colour = "blue") +
  ggtitle("Scatter plot and FD regression line") +
  ylab("D(Log Hourly Wage)") +
  xlab("D(Log Unemployment Rate)")
```




```
# dev.off() # uncomment to save as pdf
```

As you can see, there is no obvious relationship between the changes in hourly pay and the respective local unemployment rate.

Now we will show models, `POLS0a`, `POLS1a`, `POLS2a` and `FD1a` in one table. In previous tables you may have seen that the F-stat takes up a lot of space and hence we use the `omit_stat` option to indicate that we do not want to see the F-statistic.

```
stargazer_HC(POLS0a,POLS1a,POLS2a,FD1a,omit.stat = "f")
```

```
##
## ======================================================
##                            Dependent variable:
##              -----------------------------------------
##                                 lnhrpay
##                  (1)        (2)        (3)       (4)
## ------------------------------------------------------
## lnurate       -0.102***  -0.097*** -0.096***   0.042
##                (0.022)    (0.022)   (0.029)   (0.060)
##
## wave3                    -0.019***  -0.005
##                           (0.005)   (0.005)
##
## Constant       2.493***  2.491***  2.544***  -0.011***
##                (0.046)    (0.046)   (0.058)   (0.004)
##
## ------------------------------------------------------
```

```
## Observations   39,934    39,934    26,156    13,078
## R2             0.001      0.001     0.001    0.00003
## Adjusted R2    0.001      0.001     0.001   -0.00005
## =======================================================
## Note:                      *p<0.1; **p<0.05; ***p<0.01
##                  Robust standard errors in parenthesis
```