

$\forall x \in \mathbb{R} : [(x^2 \text{ is divisible by } 3) \Rightarrow (x \text{ is divisible by } 3)]$

Contrapositive

$\forall x \in \mathbb{Z} : (x \text{ not div. } 3) \Rightarrow (x^2 \text{ not div } 3)$

Let  $x \in \mathbb{Z}$  and assume  $x = 3K + 1$

$$x^2 = x \cdot x$$

$$= (3K + 1)(3K + 1)$$

Since neither term is divisible by 3,

neither  $x^2$  is divisible by 3

This is correct, but I also need to consider  $3K + 2$  and prove it with that as well.