Tutorial Sheet

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1 Subjective Questions:

- 1. Define the following terms:
 - a) Automaton
 - b) Alphabet
 - c) String
 - d) Language
- 2. Given an alphabet $\Sigma = \{a, b\}$, list some valid strings over Σ .
- 3. Explain why we need a simpler way of discussing computing machines.
- 4. Describe the concept of an automaton and its role as a mathematical model of a computing device.
- 5. What are the reasons for building models in computing? Explain the significance of finite automata as abstractions of computers.

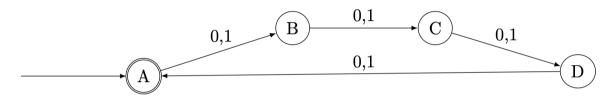
- 6. Define an alphabet and a string over an alphabet Σ . Provide examples.
- 7. Given an alphabet $\Sigma = \{a, b, c\}$, list some valid strings in the language of palindromes over Σ .

2 Objective Questions:

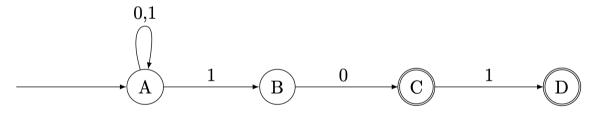
- 1. Define an NFA and explain how it differs from a DFA in terms of determinism.
- 2. Define the formal structure of a DFA and NFA (hint: look at the 5 tuple structure I disussed in the lecture).

3 Design DFA

Q1. What language is accepted by the following DFA?



Q2. What language is accepted by the following NFA?



- Q3. Construct a DFA that accepts binary strings of any length, except 3.
- Q4. Let $\Sigma = \{a, b\}$ and let $L = \{baa\}$. Design a DFA for L.
- Q5. Let $\Sigma = \{a, b\}$ and let $L = \{w \mid \Sigma^* \mid w = \text{ and the first and last character of } w \text{ are the same } \}$. Design a DFA for L.
- Q6. Let $\Sigma = \{a, b\}$ and let $L = \{w \mid \Sigma^* \mid w \text{ is a nonempty string whose characters alternate between a's and b's \}. Design a DFA whose language is L.$

4 Design NFA

- Q7. Let $\Sigma = \{a, b, c\}$ and let $L = \{w \mid \Sigma^* \mid w \text{ ends in cab }\}$. Design an NFA for L.
- Q8. Let $\Sigma = \{a, b, c\}$ and let $L = \{w \mid \Sigma^* \mid \text{ some character in } \Sigma \text{ appears at most twice in } w$ }. Design an NFA for L.

Q9. Let $\Sigma = \{a, b\}$ and let $L = \{w \mid \Sigma^* \mid \text{the third-from-last character of } w \text{ is a } \}$. Design an NFA for L. Your NFA should use at most four states.

5 More Practice Questions

Q10. Give NFAs with the specified number of states recognizing each of the following languages. In all cases, the alphabet is $\Sigma = \{0, 1\}$.

- Q10.1. The language { w Σ * | w ends with 00 } with three states.
- Q10.2. The language { w Σ * | w contains the substring 0101, i.e., w = x0101y for some x, y $\Sigma *$ } with five states.
- Q10.3. The language { w Σ * | w contains at least two 0s, or exactly two 1s } with six states.
- Q10.4. The language { } with one state.

5.1 More simple/fun Questions



Warning

Important: I will give you solutions to these questions but they may be slightly wrong, you need to figure out what is wrong and fix that ¹.

- 1. **Heat Wave in The Netherlands**: Design a DFA to determine if a heat wave has occurred in The Netherlands (the definition of a heatwave is that the temperature should be greater than 25°C for 5 days straight).
- $L = \{ w \text{ in } \{ \langle =25, \rangle 25 \}^* \mid w \{ \text{ contains at least five consecutive } \} > 25 \}$
 - 2. Password Strength: Design a DFA that accepts passwords that are at least 3 characters long, contain at least one uppercase letter, one lowercase letter, and one digit.

¹Trust me this is better than having no solutions!

L = { w in {a-z, A-Z, 0-9}* | w { contains at least one upper case, one lowercase, one digit, and has length } >= 3 }

- 3. **Elevator Button Presses**: Design an NFA where the elevator goes to the 5th floor only if the 2nd and 4th-floor buttons are pressed consecutively.
- $L = \{ w \text{ in } \{1,2,3,4,5\}^* \mid w \{ \text{ contains 2 followed by 4} \} \}$
 - 4. **Traffic Light Sequence**: Design a DFA that represents the sequence of traffic lights (Red -> Green -> Yellow -> Red).
- $L = \{ w \text{ in } \{R, G, Y\}^* \mid w \{ \text{ follows the pattern } \} RGY \}$
 - 5. **Coffee Machine**: Design a DFA that accepts sequences where a user selects a coffee type, adds sugar (optional), and then presses the start button.
- $L = \{ w \text{ in } \{ \text{coffee, sugar, start} \}^* \mid w \{ \text{ starts with coffee and ends with start} \} \}$
 - 6. **Library Book Return**: Design an NFA that accepts if a book is returned either on or before its due date or within two days after its due date.
- $L = \{ w \text{ in } \{on\text{-time, late}\}^* \mid w \{ \text{ is either on-time or late up to two days} \} \}$
 - 7. **ATM Transactions**: Design a DFA that accepts sequences where a user inserts a card, enters a PIN, selects an account, chooses a transaction type, and then takes the cash or completes the transaction.
- $L = \{ w \text{ in } \{ card, PIN, account, transaction, cash} \}^* \mid w \{ starts with card and ends with cash or transaction} \}$
 - 8. **Music Playlist Shuffle**: Design a DFA that shuffles songs without repeating the same song until all songs in the playlist have been played.
- $L = \{ w \text{ in } \{ song_1, song_2, \dots song_n \}^* \mid w \{ does \text{ not repeat any song until all songs have been played} \}$