



So, solve det (A-II) = 0 for à degree n. (characteristic equation) polynomial. Example: Find the eigenvalues of A= [2]  $A-\lambda T = \begin{bmatrix} 2 & 1 & 7 & -1 & 1 & 0 \\ 1 & 2 & 3 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 2-\lambda & 1 & 1 \\ 1 & 2-\lambda & 1 \end{bmatrix}$  $det(A-1) = (2-1)^2 - 1 = 1^2 - 41 + 3$  $det (A-1) = 0 \implies 1^2 - 41 + 3 = 0 \iff (\lambda-1)(\lambda-3) = 0$   $\iff \lambda_1 = 1, \lambda_2 = 3$ And find the corresponding eigenvectors.  $A_1 = 1 : A - \lambda_1 T = \begin{cases} 1 & 1 : 0 \\ 1 & 1 : 0 \end{cases} \quad \begin{cases} 1 & 0 \\ 0 &$  $\lambda_2 = 3$  :  $A - 1_2 = [-1 \ 1 \ 0] \sim [1 \ -1 \ 0] = [-1 \ 0] with x_2 + 0$ Example: A= [5 5]  $V = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$   $AV = \begin{bmatrix} 5 \\ 5 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 10 \\ 10 \end{bmatrix} = \begin{bmatrix} 10 \\ 1 \end{bmatrix}$   $A_1 = \begin{bmatrix} 10 \\ 10 \end{bmatrix}$  $u = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$   $Au = \begin{bmatrix} 5 \\ 5 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} = 0 \cdot \begin{bmatrix} 1 \\ 1 \end{bmatrix}$  b = 0.  $\begin{bmatrix} 1 & 2 & 5 & 7 & (1) & -1 & 0 & -1 & 0 \\ y & 2 & 2 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 1 & 0 & 0 \end{bmatrix} = 0 \cdot \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}$ Example:  $A = \begin{bmatrix} 5 & 1 & 0 \\ 0 & -3 & 1 \\ 0 & 0 & -3 \end{bmatrix}$ 





