Deduce	YV Y	from yy	-
1. Yy	, ψ	(given)	
2.	ΙΨ	(ass unphion)	
3	ΨνΨ	$I_{\checkmark}(2)$	X
4.	Y	(ass impha)	-
5.	YVY	I, (4)	X
6. V	V	F, (1, 2, 3, 4	,5)

Prove
$$(p \wedge Q) \rightarrow (p \vee Q)$$

1. $p \wedge Q$ (assume)

2. $p \vee Q$
 $p \vee Q$

Forgother rule:

Tuesday, November 7,2023 12:15 PM Give proofs using natural deduction:

(1) deduce $(R \rightarrow P) \rightarrow (R \rightarrow Q)$ from $P \rightarrow Q$ (2) $((P \lor Q) \land R) \rightarrow ((P \lor R) \land (Q \lor R))$ (3) $P \lor \neg P$ (Hand.)(9) $((P \rightarrow R) \land (S \rightarrow R)) \rightarrow ((P \lor S) \rightarrow R)$

 $(((\land \land) \land () \rightarrow ()) \rightarrow (())$ $(() \land () \land () \rightarrow ()) \rightarrow (())$

1.
$$P$$
 (assumption)

2. P (assumption)

3. $P \in A(1)$

4. $P \in A(1)$

5. $Q \in A(1)$

5. $Q \in A(1)$

6. $P \rightarrow Q \in A(1)$

7. $Q \in A(1)$

7. $Q \in A(1)$

7. $Q \in A(1)$

8. $Q \in A(1)$

9. $Q \in A(1)$

1. $Q \in A(1)$

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3. $Q \in A(1)$

4. $Q \in A(1)$

5. $Q \in A(1)$

6. $Q \in A(1)$

7. $Q \in A(1)$

ruesuay, November 7, 2025	12.55 FW			
1.	(PVQ) AR	(as		
2	PVQ	£ / (')	€ hine 2	not need
3	R	En(1)		
- /) QUR			
4	PVR			
5			In(4,5)	
6.		n (QVR)		
$\overline{(I_{D}, \kappa)}$	$(108) \rightarrow ($	$(P_{V}R)$, f	(AVR)	(16)
7, KY V U		// // ()	× 1 + 7	()

