

Denvative

The denvictive of for point xo of domain is delived as the slope of the tangent of fat xo

 $f'(x_0) = \lim_{N\to0} \frac{f(x_0+h)-f(x_0)}{N}$ 

L> the derivative only exists if the limit exists and vis finee

Motations: ey', f'(x),  $\frac{d}{dx}$  f(x),  $D_x f$ ,  $f'(x_0) = \frac{d}{dx} f(x_0) |_{x=x_0}$ 

Differentiability

fis differentiable at xo -> f(xo) exists

Singular points

xo is a singular point - f (xo) does not exist

Left & Right Denvatives  $f'_{\pm}(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$ 

Power rule

Differentiation nules

- · Differentiable implies continuous
- for f and g differentiable at x (f+g)'(x) = f'(x) + g'(x) (kf)'(x) = kf'(x)
- Product rule (f(x)g(x))' = f(x)g(x) + g'(x)f(x)

$$\frac{\partial^{\times}}{\partial x} (x_{\mu}) = N \cdot x_{\mu-1}$$

$$= \frac{\partial}{\partial x} (x_{\mu}) \cdot x + x_{\mu} \frac{\partial}{\partial x} (x_{\mu})$$

we use = 
$$(n \cdot x)^{n-1} \cdot x + x^{n-1} \cdot x^{n-1}$$

whoin rule

 $f(x) = Jg(x)$ 
 $f(x) = g'(x)$ 

Chain rule

$$\frac{d}{dx} \left[ f(g(x)) \right] = f \left[ g(x) \right] \cdot g'(x)$$

$$g(x) = ee - \frac{d}{dx} f(u(x)) = \frac{df}{du} \cdot \frac{du}{dx}$$

Quotient rule: 
$$\int_{X} \left[ \frac{f(x)}{g(x)} \right] = \frac{f(x)g(x) - g'(x)f(x)}{[g(x)]^2}$$

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Exercises
(1) \quad \int (x) = \frac{1}{(x^2+1)}
Derivatives of trigonometric functions
 Introduction
                                   < lan(x)
     \times > (x) \times (x)
         <=> \ \frac{\sqrt{N(\chi)}}{\sqrt{}} \cdot \cdot \
                                  \leq \frac{ton(x)}{x}
    \frac{\text{lom}(x)}{x} = \frac{\text{sen}(x)}{\cos(x)} = \frac{\text{sen}(x)}{x}
                COZ(X) \subset \frac{X}{S(N(X))} \leq 1
                             SIN(x) 10 Included between
                            (cos(x) and 1, so the
                            Cinut lim Sivia
   UM SIMIKI
                            aince sin/x) is even
Derivatives
 \frac{dx}{dx}(S_{x}(X)) = CQS(X)
                        [PW : 21.N (x+1) 1.- 2(N(x)
 E'mpsom's
                        lim (2)005 (x + 2) $141
51N(a)-510(6)
= 2\cos\left(\frac{3+b}{2}\right)\sin\left(\frac{3-b}{2}\right) time \sin\left(\frac{b}{2}\right)
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$$\frac{1}{\sqrt{3}} (e^{x}) = e^{x}$$

$$\frac{1}{\sqrt{3}} (e^$$

Migher order derivatives.

second derivative:  $f''(x) = \frac{d^2f}{dx}$