#### **Lecture 3 Numerical Measures**

BIO210 Biostatistics

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### Summarise data using numbers

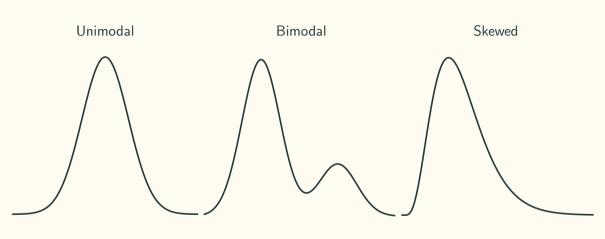
- Central tendency (mean, median, mode)
- Extremes (smallest, largest)
- Range
- Interquartile range (IQR)
- Dispersion (variance, standard deviation)

$$\bullet \ \ \text{Arithmetic mean:} \ \ \bar{x} = \frac{x_1 + x_2 + x_3 + \dots + x_{n-1} + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

• Median: the 50th percentile

• Mode: the most frequent values

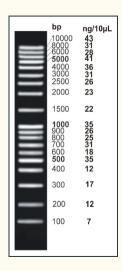
	Mean	Median	Mode
1, 2, 3, 4, 5, 6, 7, 8, 9	5	5	Χ
2, 3, 5, 7, 7, 7, 11, 13	6.89	7	7
2, 3, 5, 7, 7, 7, 11, 13, 100	16.2	7	7
2, 2, 2, 5, 6, 100, 100, 100, 103, 104	52.4	53	2, 100
2, 3, 4, 5, 6, 100, 101, 102, 103, 104	53	53	Х

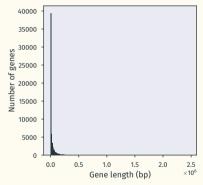


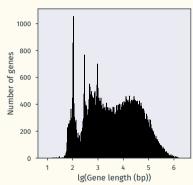
Geometric mean: 
$$GM = \sqrt[n]{x_1 x_2 x_3 \cdots x_{n-1} x_n} = \left(\prod_{i=1}^n x_i\right)^{\frac{1}{n}}$$

$$\bar{\log}x = \frac{1}{n} \sum_{i=1}^{n} \log x_i$$

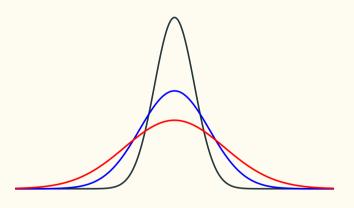
### Log scale in biology







# Dispersion



### Dispersion

• Variance: 
$$\mathbb{V}\mathrm{ar} = \frac{1}{n}\sum_{i=1}^n(x_i-\mu)^2 \text{ or } \frac{1}{n-1}\sum_{i=1}^n(x_i-\bar{x})^2$$

• Standard deviation:  $\sqrt{\mathbb{V}ar}$ 

#### **Grouped data**

Transcription factor binding motif length (bp):

Mean:

### **Grouped data**

Motif length (bp)   Absolute frequency		Relative frequency	
11	10	0.5	
13	7	0.35	
16	2	0.1	
17	1	0.05	
Total 20		1	
Iotal	20	1	

### Weighted average

Value	Absolute frequency	
$x_1$	$f_1$	
$x_2$	$f_2$	
$x_3$	$f_2$	
:	:	
÷	:	
$x_{n-1}$	$f_{n-1}$	
$x_{n-1}$ $x_n$	$f_n$	

$$\bar{x} = \frac{x_1 f_1 + x_2 f_2 + \dots + x_{n-1} f_{n-1} + x_n f_n}{f_1 + f_2 + \dots + f_{n-1} + f_n}$$

$$= \frac{x_1 f_1 + x_2 f_2 + \dots + x_{n-1} f_{n-1} + x_n f_n}{\sum_{i=1}^n f_i}$$

$$= \frac{f_1}{\sum_{i=1}^n f_i} x_1 + \frac{f_2}{\sum_{i=1}^n f_i} x_2 + \dots + \frac{f_n}{\sum_{i=1}^n f_i} x_n$$

$$= w_1 x_1 + w_2 x_2 + \dots + w_n x_n = \sum_{i=1}^n w_i x_i$$

### Weighted average

#### Grading system:

Attendance Assignments		Mid-term exam   Final exam	
10%	15%	30%	45%

#### Pixel luminance:

$$0.2126 \times R + 0.7152 \times G + 0.0722 \times B$$

$$0.299 \times R + 0.587 \times G + 0.114 \times B$$

### Weighted average

A badly manufactured dodecahedron die



Values		Relative frequency	
	1	8%	
	2	5%	
	3	5%	
	4	5%	
	5	5%	
	6	10%	
	7	10%	
	8	10%	
	9	10%	
	10	12%	
	11	10%	
	12	10%	

We roll the die repeadly for a large number of times. What will be the average number?

### Summary of descriptive statistics

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Tables (absolute/relative frequency table)

Graphs (Bar chart, pie chart, histogram, box plot, line graph, scatter plot)

Data presentation 

Central tendency (arithmetic/geometric mean, median, mode)

Dispersion (variance, standard deviation)

Others (range, IQR)
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New way of calculating mean: weighted average  $ar{x} = \sum_{i=1}^n w_i x_i$