Contact Information Northern Arizona University

Department of Mathematics & Statistics

801 South Osborne Drive, PO Box 5717

Flagstaff, AZ 86011

Education

University of Colorado, Boulder, CO

PhD, Mathematics, Advisor: Dr. R.M. Green

Dissertation: A diagrammatic representation of an affine C Temperley-Lieb algebra

Northern Arizona University, Flagstaff, AZ

May 2000

928.523.6852

Aug 2008

dana.ernst@nau.edu

http://danaernst.com

MS, Mathematics, Advisor: Dr. M. Falk

Thesis: Cell complexes for arrangements with group actions

George Mason University, Fairfax, VA

May 1997

BS, Mathematics

Academic **Positions**

The Academy of Inquiry Based Learning, Toronto, ON

Co-director Fall 2019-Present

Northern Arizona University, Flagstaff, AZ

Department Chair, Department of Mathematics & Statistics July 2025–Present Full Professor, Department of Mathematics & Statistics July 2025–Present Associate Professor, Department of Mathematics & Statistics Aug 2017–July 2025 Assistant Professor, Department of Mathematics & Statistics Aug 2012–July 2017

Plymouth State University, Plymouth, NH

Assistant Professor, Mathematics Department Aug 2008–May 2012

University of Colorado, Boulder, CO

Graduate Teaching Instructor, Department of Mathematics Aug 2003–May 2008 Lead Graduate Teacher, Graduate Teacher Program Aug 2006-May 2007

Front Range Community College, Boulder, CO

Full-time Faculty, Department of Mathematics Aug 2001-May 2003

Northern Arizona University, Flagstaff, AZ

Instructor, Mathematics & Statistics Department Jun 2000-May 2001 Graduate Assistant, North Learning Assistance Center Jan 2000-May 2000 Graduate Teaching Instructor, Mathematics & Statistics Department Jan 1998-Dec 1999

Graduate Assistant, South Learning Assistance Center

Aug 1997–Dec 1997

Research Interests

General

Interplay between combinatorics and algebraic structures; scholarship of teaching and learning (SoTL) and undergraduate mathematics education.

Specific

Combinatorics of Coxeter groups, generalized Temperley-Lieb algebras, diagram algebras; combinatorial game theory; enumerative combinatorics, combinatorics of genome rearrangements, pattern avoidance; inquiry-based learning (IBL).

Publications In Preparation

- P3. A. Claesson, G. Cerbai, **D.C. Ernst**, and H. Golab*. Pattern avoidance in Cayley permutations, Part 2 (tentative title).
- P2. B.J. Benesh, **D.C. Ernst**, M. Meyer, S.K. Salmon*, and N. Sieben. Impartial geodetic destroying games on graphs.
- P1. F. Awik*, F. Burkhart*, H. Denoncourt, **D.C. Ernst**, T. Rosenberg*, and A. Stewart*. Enumerating signed permutations by reversal distance.

Submitted/Preprints

- S2. J. Barnes*, J. Breland*, **D.C. Ernst**, and R. Perry*. Braid graphs in simply-laced triangle-free Coxeter systems are median. [arXiv:2408.16839]
- S1. A. Claesson, G. Cerbai, **D.C. Ernst**, and H. Golab*. Pattern-avoiding Cayley permutations via combinatorial species. [arXiv:2407.19583]

Books

- B4. **D.C. Ernst** and J. Hagood. *Introduction to Discrete Mathematics*. Free undergraduate discrete mathematics textbook, 2024. [PDF]
- B3. **D.C. Ernst**. *Introduction to Real Analysis*. Free undergraduate real analysis textbook, 2023. [PDF]
- B2. **D.C. Ernst**. An Inquiry-Based Approach to Abstract Algebra. Open-source textbook for undergraduate abstract algebra, 2022. [GitHub] [PDF]
- B1. **D.C. Ernst**. An Introduction to Proof via Inquiry-Based Learning. MAA Press, 2022. Textbook for an introduction to proof course. [Project Webpage]

Journal Articles

- J23. B. Bašić, P. Ellis, **D.C. Ernst**, D. Popović*, N. Sieben. Categories of impartial rulegraphs and gamegraphs. Accepted to *Int. J. Game Theory*. [arXiv:2312.00650]
- J22. B.J. Benesh, **D.C. Ernst**, M. Meyer, S.K. Salmon*, and N. Sieben. Impartial geodetic building games on graphs. Accepted to *Int. J. Game Theory* (pending minor revisions), [arXiv:2307.07095]
- J21. **D.C. Ernst**, J. Slye. Using the $\mathrm{Spin}_{3\times3}$ virtual manipulative to introduce group theory. PRIMUS~34(6),~2024. [ePrint]
- J20. F. Awik*, J. Breland*, Q. Cadman*, and D.C. Ernst. Braid graphs in simply-laced triangle-free Coxeter systems are partial cubes. European Journal of Combinatorics 118, 2024. [arXiv:2104.12318] [ePrint]
- J19. B.J. Benesh, **D.C. Ernst**, and N. Sieben. The spectrum of nim-values for achievement games for generating finite groups. *INTEGERS* 23, 2023. [arXiv:2004.08980] [ePrint]
- J18. B.J. Benesh, **D.C. Ernst**, and N. Sieben. Impartial achievement games for generating nilpotent groups. *J. Group Theory* 22(3), 515–527, 2019. [arXiv:1805.01409] [ePrint]

- J17. **D.C. Ernst**. Diagram calculus for a type affine C Temperley–Lieb algebra, II. J. Pure Appl. Alg. 222(12), 3795–3830, 2018. [arXiv:1101.4215] [ePrint]
- J16. **D.C. Ernst** and N. Sieben. Impartial achievement and avoidance games for generating finite groups. *Int. J. Game Theory* 47(2), 509–542, 2017. [arXiv:1407.0784] [ePrint]
- J15. **D.C. Ernst**, T.J. Hitchman, and A. Hodge. Bringing Inquiry to the First Two Years of College Mathematics. *PRIMUS* 27(7), 641–645, 2017. [ePrint]
- J14. **D.C. Ernst**, A. Hodge, and S. Yoshinobu. Doceamus: What Is Inquiry-Based Learning? *Notices of the AMS* 64(6), 2017. [ePrint]
- J13. B. Benesh, **D.C. Ernst**, and N. Sieben. Impartial achievement and avoidance games for generating generalized dihedral groups. *Australas. J. Combin.* 68(3), 371-384, 2017. [arXiv:1608.00259] [ePrint]
- J12. **D.C. Ernst**, M. Hastings*, and S.K. Salmon*. Factorization of Temperley-Lieb diagrams. *Involve* 10(1), 89–109, 2017. [arXiv:1509.01241] [ePrint]
- J11. B.J. Benesh, **D.C. Ernst**, and N. Sieben. Impartial avoidance and achievement games for generating symmetric and alternating groups. *Int. Electron. J. Algebra* 20, 70–85, 2016. [arXiv:1508.03419] [ePrint]
- J10. N. Diefenderfer, D.C. Ernst, M. Hastings*, L.N. Heath*, H. Prawzinsky*, B. Preston*, J. Rushall, E. White*, A. Whittemore*. Prime Vertex Labelings of Several Families of Graphs. *Involve* 9(4), 667-688, 2016. [arXiv:1503.08386] [ePrint]
- J9. B.J. Benesh, **D.C. Ernst**, and N. Sieben. Impartial avoidance games for generating finite groups. *North-W. Eur. J. of Math.* 2, 83–101, 2016. [arXiv:1506.07105] [ePrint]
- J8. H. Denoncourt, **D.C. Ernst**, and D. Story*. On the number of commutation classes of the longest element of the symmetric group. *Open Problems in Mathematics* Vol 4, 2016. [arXiv:1602.08328] [ePrint]
- J7. E. Kennedy, B. Beaudrie, **D.C. Ernst**, and R. St. Laurent. Inverted Pedagogy in Second Semester Calculus. *PRIMUS* 25(9–10), 892–906, 2015. [ePrint]
- J6. B. Love, A. Hodge, C. Corritore, and **D.C. Ernst**. Inquiry-Based Learning and the Flipped Classroom Model. *PRIMUS* 25(8), 745–762, 2015. [ePrint]
- J5. **D.C. Ernst**, M. Leingang, and R. Taylor. To friend or not to friend? Facebook for professional educators. *MAA FOCUS* June/July 2015. [ePrint]
- J4. **D.C. Ernst**, A. Hodge, and A. Schultz. Enhancing Proof Writing via Cross-Institutional Peer Review. *PRIMUS* 25(2), 121–130, 2015. [ePrint]
- J3. **D.C. Ernst**. Diagram calculus for a type affine C Temperley–Lieb algebra, I. J. Pure Appl. Alg. 216(11), 2012. [arXiv:0910.0925] [ePrint]
- J2. T. Boothby*, J. Burkert*, M. Eichwald*, **D.C. Ernst**, R.M. Green, and M. Macauley. On the cyclically fully commutative elements of Coxeter groups. *J. Algebraic Combin.* 36(1), 2012. [arXiv:1202.6657] [ePrint]
- J1. **D.C. Ernst**. Non-cancellable elements in type affine C Coxeter groups. Int. Electron. J. Algebra 8, 2010. [arXiv:0910.0923] [ePrint]

Book Chapters

- BC2. **D.C. Ernst** and A. Hodge. Within ϵ of Independence: An Attempt to Produce Independent Proof-Writers via IBL. In *Beyond Lecture: Resources and Pedagogical Techniques for Enhancing the Teaching of Proof-Writing Across the Curriculum*, R. Schwell, A. Steurer, & J.F. Vasquez (Eds.), MAA Notes, 2016.
- BC1. **D.C. Ernst**, A. Hodge, M. Jones, and S. Yoshinobu. The many faces of IBL. In *STEM Education: An Overview of Contemporary Research, Trends, and Perspectives*, E. Ostler (Ed.), 2015.

Conference Proceedings (Peer-Reviewed)

- C2. B. Beaudrie, D.C. Ernst, and B. Boschmans. Redesigning an Algebra for Precalculus Course. In Proceedings of World Conference on E-Learning in Corporate, Government, Healthcare, and Higher Education, T. Bastiaens & G. Marks (Eds.), 2013.
- C1. B. Beaudrie, **D.C. Ernst**, and B. Boschmans. First Semester Experiences in Implementing a Mathematics Emporium Model. In *Proceedings of Society for Information Technology & Teacher Education International Conference*, R. McBride & M. Searson (Eds.), 2013.

Miscellaneous

- M6. D.C. Ernst. Instructor Guide: An Introduction to Proof via Inquiry-Based Learning. [PDF]
- M5. M. Annabel, **D.C. Ernst**, C. Howard, and W. Spalding. A Date with the Pines: Takes From the 2023 Pinyons and Pines. Bikepacking.com. May 2023.
- M4. D. Daly et al. AIBL Handbook for Online Professional Development: Lessons Learned from PRODUCT Workshops. Ethnography & Evaluation Research, & the Academy of Inquiry Based Learning. Boulder, CO, and San Luis Obispo, CA: University of Colorado Boulder, Ethnography & Evaluation Research; and Academy of Inquiry Based Learning. [ePrint]
- M3. D.C. Ernst. 2019 Pinyons and Pines: Event Recap. Bikepacking.com. Aug 2019.
- M2. D.C. Ernst. Dana's AZT, Part 2. Bedrock Bags Blog. Jul 2018.
- M1. D.C. Ernst. Dana's AZT, Part 1. Bedrock Bags Blog. Jun 2018.

Online Columns & Blog Posts

- O18. **D.C. Ernst**. The Role of Failure and Struggle in the Mathematics Classroom. *Teaching Tidbits*. Nov 2017. [Teaching Tidbits]
- O17. **D.C. Ernst**. Want to Give Your Teaching Style a Makeover This Summer? Here's How. *Teaching Tidbits*. Apr 2017.
- O16. D.C. Ernst. Who generates the examples? Teaching Tidbits. Nov 2016.
- O15. **D.C. Ernst**. Teaching Calculus 1 with a Focus on Student Presentations. *Discovering the Art of Mathematics Blog.* Oct 2015. [artofmathematics.org]
- O14. D.C. Ernst. Setting the Stage. Math Ed Matters. Jan 2015. [Math Ed Matters]

- O13. D.C. Ernst. The Twin Pillars of IBL. Math Ed Matters. Jan 2015.
- O12. **D.C. Ernst**. Fear is the mind-killer. *Math Ed Matters*. Jun 2014.
- O11. D.C. Ernst. Encouraging Students to Tinker. Math Ed Matters. Aug 2014.
- O10. **D.C. Ernst**, A. Hodge, and T.J. Hitchman. Engaging in Inquiry-Based Learning. *Math Ed Matters*. Feb 2014.
- O9. D.C. Ernst and A. Hodge. Math Ed Mania at the JMM. Math Ed Matters. Jan 2014.
- O8. **D.C. Ernst** and A. Hodge. The JMM: What's Mathematics Education Got to Do with It? *Math Ed Matters*. Dec 2013.
- O7. D.C. Ernst. Give the Students the Colored Pen. Math Ed Matters. Aug 2013.
- O6. **D.C. Ernst** and R. Talbert. 4+1 interview with Dana Ernst. Casting Out Nines, The Chronicle Blog Network. Aug 2013. [chronicle.com/blognetwork/castingoutnines]
- O5. D.C. Ernst. Personality Matters? Math Ed Matters. Jul 2013.
- O4. D.C. Ernst. Grade School Utopia? Math Ed Matters. Jul 2013.
- O3. D.C. Ernst and A. Hodge. Try, Fail, Understand, Win. Math Ed Matters. Jun 2013.
- O2. **D.C. Ernst**. What the Heck Is IBL? *Math Ed Matters*. May 2013.
- O1. **D.C. Ernst** and S. Yoshinobu. IBL Instructor Perspectives: Professor Dana Ernst. *The IBL Blog.* Feb 2012. [TheIBLBlog.com]

Grant Activity

- G25. Impartial Geodetic Destroying Games on Graphs

 Co-PI, AIM SQuaREs. SQuaREs (Structured Quartet Research Ensembles) allow a dedicated group of four to six mathematicians to spend a week at American Institute of Mathematics (AIM) in San Jose, California. AIM provides both the research facilities and the financial support for each SQuaRE group. Joint with B.J. Benesh, M. Meyer, S. Salmon, N. Sieben. (Unfunded)
- G24. Conversion of OER textbook to PreTeXt Summer 2023 **PI**, Elevating Excellence award for Affordable Learning Materials. Support the conversion of OER textbook from LaTeX to PreTeXt. (Funded: \$1,000)
- G23. MAA OPEN Math

 2022–2025

 Senior Personnel, NSF-DUE. Participate in the development of facilitators for a variety of online pedagogy workshops, assist in the delivery of workshops. (Funded: \$1,685,867)
- G22. Enumeration of signed permutations under the action of reversals

 Co-PI, Hooper Undergraduate Research Award (HURA). Awarded funds to support John
 (Frank) Burkhart and Alex Stewart to work on undergraduate research project during 2021–2022 academic year. (Funded: \$3,350)

- G21. Impartial achievement & avoidance games for generating finite groups Summer 2022 Co-PI, Collaborate@ICERM. Program offers teams of 3–6 researchers the opportunity to spend five days at The Institute for Computational and Experimental Research in Mathematics (ICERM) during the summer or in the month of January. ICERM provides both the research facilities and the financial support for each research group. Joint with B.J. Benesh, M. Meyer, S. Salmon, N. Sieben. (Funded: \$9,000)
- G20. Impartial achievement & avoidance games for generating finite groups Fall 2019

 Co-PI, AIM SQuaREs. SQuaREs (Structured Quartet Research Ensembles) allow a dedicated group of four to six mathematicians to spend a week at American Institute of Mathematics (AIM) in San Jose, California. AIM provides both the research facilities and the financial support for each SQuaRE group. Joint with B.J. Benesh, M. Meyer, S. Salmon, N. Sieben. (Unfunded)
- G19. Impartial achievement & avoidance games for generating finite groups Fall 2018

 Co-PI, AIM SQuaREs. SQuaREs (Structured Quartet Research Ensembles) allow a dedicated group of four to six mathematicians to spend a week at American Institute of Mathematics (AIM) in San Jose, California. AIM provides both the research facilities and the financial support for each SQuaRE group. Joint with B.J. Benesh, M. Meyer, S. Salmon, N. Sieben. (Unfunded)
- G18. Active Learning in Calculus Fall 2017

 Co-PI, SEMINAL. Requested funds to support an increase in the amount of active learning instruction in Calculus I and II. Joint with A. Hodge and E. Kennedy. (Unfunded)
- G17. A Pragmatic Design for Informal STEM Learning about Scientific Reasoning: Drawing on Diagrams, Models and Citizen Science

 Fall 2017

 Senior Personnel, NSF-STEM-AISL. Project aims to develop an integrated set of learning tools and collaborative research activities that will engage the public in the exploration and use of diagrams in scientific reasoning as citizen-scientists. (Unfunded)
- G16. Computing maximal sorting length of signed permutations 2017–2018 Co-PI, Hooper Undergraduate Research Award (HURA) and NASA Space Grant. Awarded funds to support Tanner Rosenberg to work 10 hours per week on undergraduate research project during 2017–2018 academic year. (Funded: \$3,350)
- G15. PRODUCT 2015–2020 Senior Personnel, NSF-IUSE. Participate in the development of facilitators for Inquiry-Based Learning workshops and assist in the delivery of workshops. (Funded: \$2,800,000)
- G14. SPIGOT

 Senior Personnel, NSF-TUES II. The IBL Workshop provides an intensive four-day program for math instructors interested in learning to implement IBL in college-level mathe-
- G13. ROPE: Resource of Open Problems for Education Fall 2014 & Spring 2014 Co-PI, NSF-IUSE. Requested funds to develop an online, electronic library that provides a large number of innovative, well-tested, and documented problems that instructors and students may use in a wide range of courses and for a wide range of assignment types. Joint with G. LaRose (University of Michigan) and S. Hamblen (McDaniel College). (Unfunded)

matics courses. (Funded: \$540,000)

G12. Applets for Calculus

Fall 2013

PI, Interns to Scholars (I2S) Program at NAU. Awarded funds to support one undergraduate intern during the Spring 2014 and Fall 2014 semesters to work 6 hours per week for 10 weeks on creating applets for first semester calculus. (Funded: \$1,296)

G11. Prime labelings of graphs

Fall 2013

- **Co-PI**, Center for Undergraduate Research in Mathematics (CURM). Awarded funds to support seven undergraduate students to conduct research for 2014–2015 academic year. Joint with J. Rushall (NAU). (Funded: \$33,100)
- G10. Toward's a Cyclic Version of Matsumoto's Theorem

 Fall 2013

 PI, Faculty Grants Program at NAU. Requested one month of summer salary to support my research program in the combinatorics of Coxeter groups. (Unfunded)
 - G9. Undergraduate Research Program in Mathematics

 Senior Personnel, NSF-DMS: Workforce Division. Requested support for REU program at NAU for summers of 2014–2016. (Unfunded)
- G8. An open problem library for mathematics

 PI, Faculty Grants Program at NAU. Awarded summer salary to support development of an online open problem library for undergraduate mathematics courses. (Funded: \$7,500)
- G7. Toward a factorization of Temperley–Lieb diagrams

 PI, NAU NASA Space Grant Program. Requested support for two undergraduate research students for the 2013–2014 academic year. (Unfunded)
- G6. Combinatorics of the CFC elements of Coxeter groups Fall 2012

 PI, Center for Undergraduate Research in Mathematics (CURM). Requested funds to support three undergraduate students to conduct research for academic year. (Unfunded)
- G5. An Open Problem Library for Mathematics

 Co-PI, NSF-TUES. Proposal seeks to develop an online, electronic library that will provide a large number of innovative, well-tested, and documented problems that instructors and students may use in a wide range of courses and for a wide range of assignment types. Joint with G. LaRose (University of Michigan) and S. Hamblen (McDaniel College). (Unfunded)
- G4. *IBL course materials for group theory*PI, Academy of Inquiry-Based Learning. Awarded Category 2 Small Grant to fund development of course materials for an IBL abstract algebra course that emphasizes visualization and incorporates technology. (Funded: \$2,500)
- G3. Conjugacy and reducibility in Coxeter groups

 Co-PI, NSF-DMS: Number Theory, Algebra, and Combinatorics. Requested funds to support summer research and travel for PIs and full-year support for undergraduate research assistants. Joint with R.M. Green (CU Boulder) and M. Macauley (Clemson). (Unfunded)
- G2. Combinatorics of the CFC-finite Coxeter groups

 PI, Center for Undergraduate Research in Mathematics (CURM). Requested funds to support two undergraduate students to conduct research for academic year. (Unfunded)

G1. The conjugacy problem for Coxeter groups

Fall 2009

Co-PI, NSF-DMS: Number Theory, Algebra, and Combinatorics. Requested funds to support summer research and travel for PIs and full-year support for undergraduate research assistants. Joint with R.M. Green (CU Boulder) and M. Macauley (Clemson). (Unfunded)

Teaching Experience

Summary

Over 25 years of teaching experience; recipient of several teaching awards (most recent: 2024 Educator of Influence, 2021 NAU President's Distinguished Teaching Fellow, 2016 MAA Southwest Section Teaching Award).

Courses Taught

Combinatorial Game Theory (graduate), Enumerative Combinatorics (graduate), Reflection Groups and Coxeter Groups (graduate), Combinatorics of Genome Rearrangements (graduate), Topology, Real Analysis, Abstract Algebra (graduate and undergraduate), Number Theory, Linear Algebra, Introduction to Proof, Discrete Mathematics, Problem Solving, Calculus I–III, Precalculus, Trigonometry, College Algebra, Survey of Algebra, Finite Mathematics, Quantitative Reasoning, College Math with Applications, Mathematics for Elementary School Teachers I.

Advising & Mentoring

Masters Theses

Braid Graphs in Coxeter systems of type Λ are median Fall 2023–Spring 2024 Ruth Perry (NAU).

Pattern avoidance in Cayley permutations Fall 2023–Spring 2024 Hannah Golab (NAU).

Structural properties of braid graphs in simply-laced Coxeter systems Fall 2021–Spring 2022 Jillian Barnes (NAU).

Structure of braid graphs in simply-laced Coxeter systems Fall 2020–Summer 2021 Quentin Cadman (NAU).

The reversal poset of signed permutations Fall 2020–Spring 2021 Fadi Awik (NAU).

On the maximum cardinality of braid classes Fall 2016—Summer 2017 Zach Parker (NAU).

A Study of T-Avoiding Elements of Coxeter Groups Fall 2015—Spring 2016 Taryn Laird (NAU).

Exploration of the type \widetilde{C} Temperley–Lieb algebra Fall 2015–Spring 2016 Kevin Salmon (NAU).

Conjugacy classes of CFC elements in Coxeter groups of type A Fall2013–Spring 2014 Brooke Fox (NAU).

A cellular quotient of the Temperley–Lieb algebra of type D Fall 2013–Spring 2014 Kirsten Davis (NAU).

Undergrad Research Projects

Enumeration of signed permutations under the action of reversals Fall 2021–Spring 2022

John (Frank) Burkhart, Alex Stewart (NAU). Funded by Hooper Undergraduate Research Award (HURA). 2 presentations, paper in progress.

Structure of braid graphs for reduced words in Coxeter systems Fall 2019–Spring 2020 Jens Niemi, Jack Sullivan, Jordan Wright (NAU).

Architecture of braid classes in simply-laced Coxeter systems Fall 2018–Spring 2019 Fadi Awik, Jadyn Breland, Quentin Cadman (NAU). 3 presentations, 1 article.

Switch: An impartial game for generating graphs Fall 2018–Spring 2019 Ryan Davis, Adeline Moll (NAU). 4 presentations.

On signed permutations of maximal reversal length Fall 2017–Fall 2018 Rebecca Fix, Tanner Rosenberg (NAU). Rosenberg funded by Hooper Undergraduate Research Award (HURA) and NASA Space Grant during 2017–2018 academic year. 3 presentations.

Braid graphs for reduced words in Coxeter groups of types A and B Fall 2017–Spring 2018 Emalina Bidari, Brandon Samz (NAU). 3 presentations.

Exploration of combinatorial games on closure systems

Fall 2017

Peter Brosten, Brandon Samz (NAU). Joint with N. Sieben. 1 presentation.

Star reduction graphs for elements of Coxeter groups of type B Spring 2017 Emalina Bidari (NAU). 2 presentations.

Star reduction graphs for elements of Coxeter groups of type A Fall 2016 Brittany Carr (NAU). 3 presentations.

Cominuscule elements of Coxeter groups of type affine C Spring 2016 Joni Hazelman, Parker Montfort, Robert Voinescu, Ryan Wood (NAU). 2 presentations.

A simplified version of Conway's Sylver Coinage Fall 2015–Spring 2016 Joni Hazelman, Parker Montfort, Robert Voinescu, Ryan Wood (NAU). 4 presentations.

Commutation classes of the longest element in the symmetric group Fall 2015–Spring 2016 Dustin Story (NAU). 2 presentations, 1 publication.

Prime vertex labelings of graphs Fall 2014—Spring 2015 Nathan Diefenderfer, Michael Hastings, Levi Heath, Hannah Prawzinsky, Briahna Preston, Emily White, and Alyssa Whittemore (NAU). 5 presentations, 2 articles. Joint with J. Rushall (NAU). Funded by a mini-grant from the Center for Undergraduate Research in

Diagrammatic representation of the canonical basis for a TL-algebra Molly Green (NAU). 2 presentations.

Mathematics (CURM).

Spring 2014

Factorization of Temperley–Lieb diagrams Fall 2013–Spring 2014 Michael Hastings and Sarah Salmon (NAU). 5 presentations, 1 publication.

Exploration of T-avoiding elements in Coxeter groups of type F Spring 2013 Selina Gilbertson (NAU). 2 presentations.

Mathematics of Spinpossible Spring 2013–Spring 2014
Dane Jacobson and Michael Woodward. 4 presentations.

Exploration of T-avoiding elements in Coxeter groups of type F Fall 2011–Spring 2012 Ryan Cross, Katie Hills-Kimball, and Christie Quaranta (PSU). 2 presentations.

T-avoiding permutations in Coxeter groups of types A and B Fall 2010–Spring 2011 Joseph Cormier, Zachariah Goldenberg, Jessica Kelly, and Christopher Malbon (PSU). 3 presentations.

Counting generators in Temperley-Lieb algebras of types A and B Sarah Otis and Leal Rivanis (PSII) 1 presentation

Spring 2010

Sarah Otis and Leal Rivanis (PSU). 1 presentation.

Honors & Awards

NAU President's Distinguished Teaching Fellow

Fall 2021–Present

Awarded annually to outstanding teaching scholars who have made a significant impact on undergraduate learning at NAU.

Educator of Influence

Fall 2015, Spring 2018, Spring 2019, Spring 2024

Named by Gold Axe recipients as most influential educator.

MAA Southwest Section Teaching Award

Spring 2016

Recipient of 2016 MAA Southwest Section Award for Distinguished College or University Teaching of Mathematics.

University College Faculty Fellow

Fall 2012–Spring 2016

Chosen as a Faculty Fellow of the NAU University College via a selection process. Includes annual stipend.

Chair's Award for Research

and/or creative activities.

Spring 2015

Awarded by chair of Department of Mathematics and Statistics at NAU.

Provost's Award for Excellence in Undergraduate Inquiry & Creativity Spring 2014 Award honors a faculty mentor at NAU who has demonstrated initiative, productivity, and dedication in contributing to the university community in the areas of research, scholarly,

Finalist for NH Excellence in Education Award

Spring 2012

PSU's sole nominee for this statewide teaching award.

Distinguished Professor of Mathematics

May 2009 & 2011

Teaching award determined by mathematics majors at PSU.

Project NExT Fellow

Fall 2008–Spring 2009

Mathematical Association of America professional development and mentoring program for new PhDs in mathematics.

 $Graduate\ Part\text{-}Time\ Instructor\ Teaching\ Excellence\ Award$

Spring 2008

University-wide award given to outstanding graduate teaching instructors at CU.

Burton W. Jones Teaching Excellence Award

Mav 2007

Recognizes outstanding accomplishments in teaching by CU grad students in mathematics.

Thron Fellowship

Summer 2007

Financial award to support summer research, given to most outstanding graduate student in mathematics at CU.

Best Should Teach Award

Fall 2006

Awarded to outstanding Lead Graduate Teachers at CU.

Honorable Mention for Burton W. Jones Teaching Excellence Award

May 2006

Recognizes outstanding accomplishments in teaching by CU grad students in mathematics.

CU Mathematics Department Summer Fellowship

Summer 2006

Financial award to support summer research.

Residence Life Academic Teaching Award

Dec 2003

Awarded to instructors at CU based on nominations from students.

Finalist for Master Teacher Award

May 2002 & 2003

Awarded to instructors at FRCC based on nominations from students.

Mary K. Cabell Award

May 1997

Awarded to the most outstanding graduating mathematics major at GMU.

Presentations Invited

Pattern-avoiding Cayley permutations via combinatorial species

Nov 2024

University of Arizona Mathematical Physics & Probability Seminar, UofA, Tucson, AZ.

Braid graphs in simply-laced triangle-free Coxeter systems are median

Mar 2024

CU Lie Theory Seminar. CU Boulder, Boulder, CO.

Adopting, Adapting and Creating Open Education Resources (panel discussion)

NAU Teaching and Learning Center, NAU.

Jun 2023

Oct 2023

Enumerating signed permutations by reversal distance University of Iceland Mathematics Seminar, Reykjavik, Iceland.

Morphisms of impartial combinatorial games

Apr 2023

Virtual Combinatorial Game Theory Seminar.

Some enumeration results for sorting signed permutations by reversals

Mar 2022

ASU Discrete Mathematics Seminar, ASU, Tempe, AZ.

Rights of the Learner (plenary address)

Apr 2020 (Cancelled)

ArizMATYC/MAA-Southwest Section, Grand Canyon University, Phoenix, AZ

Architecture of braid classes in Coxeter systems

Jan 2020

AMS Special Session on Interactions between Combinatorics, Representation Theory, and Coding Theory, 2020 Joint Mathematics Meetings, Denver, CO.

Pennies and Paperclips

Sep 2019

Flagstaff Festival of Science Math Circles, Coconino High School, Flagstaff, AZ.

What is mathematical inquiry? (plenary address)

Jun 2019

2019 IBL Workshop, Portland, OR.

 $Enhancing\ Student\ Engagement\ and\ Understanding\ via\ Inquiry-Based\ Learning$

The Good Teaching Round Table, Boise State University, Boise, ID.

What is mathematical inquiry? (plenary address)

Jun 2018

Feb 2019

2018 IBL Workshop, DePaul University, Chicago, IL.

Experiencing IBL (plenary address)

Jun 2018

2018 IBL Workshop, DePaul University, Chicago, IL.

Enhancing Student Engagement & Understanding via Inquiry-Based Learning — Jan 2018 Creating Meaningful Classroom Activities to Deepen Student Learning, Project NExT Panel Discussion, 2018 Joint Mathematics Meetings, San Diego, CA.

The Futurama Theorem

Sep 2017

DePaul Math Club, DePaul University, Chicago, IL.

Impartial achievement and avoidance games for generating finite groups

Sep 2017

DePaul Mathematical Sciences Colloquium, DePaul University, Chicago, IL.

What is mathematical inquiry? (plenary address)

Jun 2017

2017 IBL Workshop, Cal Poly, San Luis Obispo, CA.

 $Transitioning\ students\ from\ consumers\ to\ producers\ ({\it opening\ address})$

Apr 2016

ArizMATYC/MAA-Southwest Section, Coconino Community College, Flagstaff, AZ.

Student presentations in calculus

Jan 2016

Increasing Student Engagement & Understanding through Active Learning Strategies in Calculus I minicourse, 2016 Joint Mathematics Meetings, Seattle, WA.

Open problems with monetary rewards

Oct 2014

2014 NAU High School Math Day, NAU.

Soup to Nuts: My Approach to IBL (plenary address)

Aug 2014

2014 IBL Workshop, Portland, OR.

Inquiry-Based Education in Mathematics: Models, Methods, & Effectiveness Jul 2014 Workshop on Innovations in Higher Education Mathematics Teaching, Cardiff University, Cardiff, Wales.

Tried & True Practices for IBL & Active Learning

Jan 2014

Project NExT Panel Discussion, 2014 Joint Mathematics Meetings, Baltimore, MD.

Teaching Strategies for Improving Student Learning

May 2013

Michigan Project NExT Panel Discussion, 2013 Spring MAA Michigan Section Meeting, Lake Superior State University, Sault Ste. Marie, MI.

Games on Groups

Apr 2013

Omaha Area Math Teachers Circle, University of Nebraska at Omaha, Omaha, NE.

Impartial games for generating groups

Apr 2013

Cool Math Talks, University of Nebraska at Omaha, Omaha, NE.

Using IBL as an assessment strategy

Jan 2013

Project NExT Alternative Assessment Panel Discussion, 2013 Joint Mathematics Meetings, San Diego, CA.

Inquiry-Based Learning Panel Discussion

Oct 2012

Indiana MAA Section Meeting, Butler University, Indianapolis, IN.

Inquiry-Based Learning: What, Why, and How?

Oct 2012

UA Mathematics Instructional Colloquium, University of Arizona, Tucson, AZ.

Permutation Puzzles Feb 2012

Math Teachers' Circle at University of Nebraska at Omaha, Omaha, NE.

The Futurama Theorem Feb 2012

UNO Mathematics Colloquium, University of Nebraska at Omaha, Omaha, NE.

The prisoner of Benda and the Futurama Theorem Nov 2011

Mathematics Forum, Gordon College, Wenham, MA.

Technology Sampler Aug 2010

Issues for Early Career Mathematicians in Academia, 2010 MathFest, Pittsburgh, PA.

On an open problem of the symmetric group Feb 2009

Mathematics Seminar, Keene State College, Keene, NH.

Other

Structure of braid graphs for reduced words in Coxeter groups

Jun 2025

15th Nordic Combinatorial Conference, Reykjavik University, Iceland.

Topics in combinatorics Nov 2023

Mathematics and Statistics Putnam Exam Preparation, NAU.

 $Impartial\ geodetic\ convexity\ achievement\ \mathcal{E}\ avoidance\ games\ on\ graphs \\$

Combinatorial Game Theory Colloquium IV, S. Miguel, Azores.

12 presentations (see webpage for details) Spring 2000, 2008, Fall 2012–Present Mathematics & Statistics Colloquium, NAU

3 presentations (see webpage for details) Fall 2012–Present Mathematics Seminar, NAU.

35 presentations (see webpage for details) Fall 2012–Present Algebra, Combinatorics, Geometry, & Topology (ACGT) Seminar, NAU.

18 presentations (see webpage for details) Fall 2012–Present Friday Afternoon Mathematics Undergrad Seminar (FAMUS), NAU.

4 presentations (see webpage for details) Fall 2013–Present NAU Mathematics and Statistics Teaching Seminar, NAU.

Open-source course materials for an inquiry-based approach to an introduction to proof course and abstract algebra

Jan 2018

Advancement of Open Educational Resources, 2018 Joint Math Meetings, San Diego, CA.

A quide-on-the-side approach to calculus

Jan 201:

First-Year Calculus: Fresh Approaches for Jaded Students, 2015 Joint Mathematics Meetings, San Antonio, TX.

Transitioning students from consumers to producers

Teaching Inquiry, 2015 Joint Mathematics Meetings, San Antonio, TX.

Mathematics as a Creative Endeavor: Is Mathematics Communication? Sep 2014 Liberal Studies Town Hall, NAU. Joint with T. Blows (NAU).

Creating Independent Learners

Aug 2014
Fall 2014 Tutor Training, NAU. Joint with E. Kennedy (NAU).

A Pentagon of Assessments

Apr 2014

12th Annual Assessment Fair, NAU. Joint with B. Beaudrie and B. Boschmans (NAU).

Lumberjack Mathematics Center Poster

Sep 2013

Showcase at the President and Provost Speaker Series, NAU. Joint with B. Beaudrie and B. Boschmans (NAU).

Implementing IBL in an Introduction to Proof Course

Jun 2013

Legacy of R.L. Moore Conference, Austin, TX.

Designing Inquiry-Based Learning Experiences

Oct 2012

Faculty Development Workshop, NAU.

Inquiry-Based Learning: What, Why, and How?

Oct 2012

ArizMATYC Conference, Yavapai College, Prescott, AZ.

Effective and efficient grading for an IBL course

Jun 2012

Legacy of R.L. Moore Conference, Austin, TX.

Collaborative peer review between two IBL number theory courses

Jan 2012

Scholarship of Teaching and Learning in Collegiate Mathematics, 2012 Joint Mathematics Meetings, Boston, MA.

3 presentations (see webpage for details)

Spring 2010-Fall 2011

Mathematics Seminar, PSU.

Diagram algebras as combinatorial tools for exploring Kazhdan–Lusztig theory Oct 2011 Dartmouth Combinatorics Seminar, Dartmouth College, Hanover, NH.

Mendeley: Reference manager meets social networking

Aug 2011

Faculty Workshop Days, PSU.

Within ϵ of independence: An attempt to produce independent proof-writers via an IBL approach in a real analysis course Jan 2011

Getting Students Involved in Writing Proofs, 2011 Joint Mathematics Meetings, New Orleans, LA.

 $A\ diagrammatic\ representation\ of\ the\ Temperley-Lieb\ algebra$

Apr 2010

Hudson River Undergraduate Mathematics Conference, Keene State College, Keene, NH.

Using wikis to enhance collaboration

Apr 2010

2010 Spotlight on Faculty Using Technology, PSU.

On the cyclically fully commutative elements of Coxeter groups

Jan 2010

AMS Session on Discrete Mathematics, 2010 Joint Math Meetings, San Francisco, CA.

 $A\ diagrammatic\ representation\ of\ an\ affine\ C\ Temperley-Lieb\ algebra$

Jan 2009

MAA Project NExT-YMN Poster Session, 2009 Joint Math Meetings, Washington, DC.

Diagram calculus for the Temperley-Lieb algebra

Nov 2008

MAA Northeastern Section Meeting, Bentley University, Waltham, MA.

Weak star reducibility in Coxeter groups

Nov 2007

Algebraic Lie Theory Seminar, CU Boulder.

3 presentations (see webpage for details)

Fall 2006-Fall 2007

Slow Pitch Colloquium, CU Boulder.

Diagram calculus for the Temperley-Lieb algebra

Apr 2007

Graduate Student Combinatorics Conference, University of Washington, Seattle, WA.

10 Things I Wish I Would Have Known Before I Started Teaching Graduate Teacher Program, CU Boulder.

Nov 2006

Introduction to finite reflection groups Coxeter Groups Seminar, CU Boulder. Oct 2006

A cell complex for configuration space

Apr 2000

MAA Southwest Section Meeting, Arizona State University, Tempe, AZ.

Synergistic Activities

Facilitator for OPEN Math Pre-Workshops Planning

Fall 2021-Present

The OPEN Math project serves the national interest to advance implementation and understanding of effective practices in delivering online professional development focused on teaching and learning to undergraduate mathematics instructors. My role was to train the facilitators that would be running the various summer workshops. Funded by NSF.

Co-director of Academy of Inquiry-Based Learning

Fall 2019-Present

The Academy of Inquiry Based Learning (AIBL) is an association of professors, instructors, teachers, and non-teaching supporters (such as retired professors or teachers having IBL experience, administrators, foundation personnel). AIBL is focused on supporting the math community through building community to address the ongoing challenge of equitable and inclusive teaching via IBL and alternative grading methods.

Member of NAU Teaching Academy

Fall 2021-Present

The Academy's members have been recognized by their colleges as instructional leaders and are appointed for three-year terms.

Facilitator for IBL Workshops

Summers 2013–2020

The IBL Workshop provides an intensive four-day program for math instructors interested in learning to implement IBL in college-level mathematics courses. A comprehensive follow-up program is also provided after the workshop that includes mentoring, course materials, and continued interaction at upcoming conferences. Funded by NSF.

Special Projects Coordinator for Academy of Inquiry-Based Learning Fall 2012–Spring 2021 Help organize, promote, and run IBL-related events including workshops, special sessions, and conferences.

IBL Mentor for Academy of Inquiry-Based Learning

Fall 2011–Present

Mentor for small cohort of mathematics instructors that are new to IBL.

Faculty Mentor for Project NExT Fellows

Fall 2019-Present

Project NExT (New Experiences in Teaching) is a professional development program for new or recent Ph.D.s in the mathematical sciences. I am currently a mentor for two fellows.

Co-editor for MathBlogging.org

Summer 2013–Spring 2022

Mathblogging.org is devoted to aggregating math-related blogs and news sources across the Internet. My job as editor is to select blog posts to be included in the Editors' Picks list.

Co-organizer & Facilitator for Problem Solving via Inquiry-Based Learning Summer 2018 Ran eight-day workshop on problem solving for middle and high school teachers in the Western Regional Noyce Alliance. Joint with E. Kennedy.

Co-organizer & Facilitator for SSU IBL Workshop

Spring 2018

Ran two-day workshop at the Savannah State University on nuts and bolts of how to effectively implement an inquiry-based learning approach in mathematics and other STEM fields. Joint with G. Karakok.

Co-author/Editor for Teaching Tidbits

Summer 2016–Spring 2018

Teaching Tidbits is an online column sponsored by the Mathematical Association of America. Column explores topics and current events related to undergraduate mathematics education.

Guest Editor for PRIMUS

Spring 2015–Fall 2017

One of three guest editors for *PRIMUS* Special Issue on Inquiry-Based Learning in First and Second Year Courses. Joint with A. Hodge and T.J. Hitchman.

Co-author/Editor for Math Ed Matters

Spring 2013–Spring 2016

Math Ed Matters is an online column sponsored by the Mathematical Association of America. Column explores topics and current events related to undergraduate mathematics education. Joint with A. Hodge.

Co-organizer for session on IBL in 1st and 2nd Year Courses Fall 2014—Spring 2015 2015 Joint Mathematics Meetings, San Antonio, TX. Associated with a special issue of PRIMUS.

Co-organizer for session on IBL Best Practices

Summers 2012–2014

2014 MathFest, Portland, OR.

2013 MathFest, Hartford, CT.

2012 MathFest, University of Wisconsin, Madison, WI.

Co-organizer & Facilitator for UNO IBL Workshop

Summer 2012

Ran three-day workshop at the University of Nebraska at Omaha on nuts and bolts of how to effectively implement an inquiry-based learning approach in mathematics and other STEM fields. Joint with S. Yoshinobu and A. Hodge. Funded by Kelly Foundation, Educational Advancement Foundation, and Haddix Initiatives.

Co-organizer of AMS Special Session on Combinatorics of Coxeter groups Spring 2011 AMS Spring Eastern Sectional Meeting, College of the Holy Cross, Worcester, MA.

Service Professional

Web Master, MAA Southwest Section Summer 2023–Present Member, Mathematics Teacher Education Partnership (MTEP) Fall 2023-Present Member, Editorial Board for Math Horizons Spring 2014–Spring 2021 Spring 2016–Summer 2016 Member, MAA Social Media Taskforce Member, ArizMATYC/MAA-Southwest Section Organizing Committee Spring 2016 Volunteer, Navajo Math Festival at Diné College Spring 2015 Member, Planning Committee of Legacy of R.L. Moore Conference Summer 2013 Judge, JMM Undergraduate Student Poster Session Jan 2012

Community

Member, Board of Directors for Arizona Trail Association Fall 2021–Present Regional Advisor, Bikepacking Roots Fall 2019–Summer 2023

Northern Arizona University, Flagstaff, AZ	
Mentor, Faculty Mentor Program	Spring 2024–Present
Chair, Department Curriculum Committee Fall 2021–Spri	ing 2022, Fall 2023–Present
Member, NAU's team for AAC&U Institute on OER	Summer 2023–Present
Member, Department Webpage Committee	Fall 2015–Present
Co-organizer, ACGT/Mathematics Seminar	Fall 2014–Present
Observer, 12 distinct classroom observations	Fall 2013–Present
Member, CEFNS College Promotion & Tenure Committee	Fall 2022–Spring 2024
	2001, Fall 2018–Spring 2024
Member, Department Curriculum Committee	Fall 2022
Co-chair, Tenure Track Assistant Professor Hiring Committee	Fall 2021–Spring 2022
Coordinator, MAT 136	Fall 2018–Spring 2022
Member, Steering Committee for NASA Space Grant	Fall 2015–Spring 2022
Member, Teaching Annual Review Subcommittee	Falls 2017, 2021
Co-chair, Calculus Textbook Committee	Fall 2019–Spring 2020
Chair, Tenure Track Assistant Professor Hiring Committee	Fall 2019–Spring 2020
	014, 2015, 2018, 2019, 2020
Member, Faculty Status Committee	Fall 2017–Spring 2019
Member, Instructor Screening Committee	Springs 2013, 2015, 2019
,	2016, Fall 2017–Spring 2018
Member, Tenure Track Assistant Professor Hiring Committee	Fall 2016–Spring 2017
Coordinator, FAMUS	Fall 2015–Spring 2016
Coordinator, NAU Mathematics Undergraduate Research	Fall 2015–Spring 2016
Faculty Advisor, NAU Math Club	Fall 2015–Spring 2016
Member, Calculus Textbook Committee	Fall 2015–Spring 2016
Faculty Fellow, University College	Fall 2012–Spring 2016
Co-coordinator, MAT 136/137	Fall 2014–Spring 2015
Member, Department Scholarships Committee	Fall 2014–Spring 2015
Member, Interns 2 Scholars (I2S) Ranking Committee	Fall 2014
Member, LMC Assessment Committee	Fall 2012–Summer 2014
Member, Department Graduate Operations Committee	Fall 2013–Spring 2014
Member, Department Assessment Committee	Fall 2012–Spring 2013
Co-organizer, Yavapai County Math Contest	Spring 2001
Member, Lecturer Hiring Committee	Spring 2001 Spring 2001
Member, GTA Training Committee	Fall 2000–Spring 2001
Co-organizer, High School Math Day	Falls 2000, 1999
Co-organizer, High School Math Day	rans 2000, 1999
Plymouth State University, Plymouth, NH	
Organizer, PSU Mathematics Seminars	Spring 2009–Spring 2012
Member, Academic Technology Committee	Fall 2011–Spring 2012
Chair, Online/Blended Learning in Mathematics Policy Commit	
Member, Learning Technology Online Education Director Hiring	Committee Fall 2011
Member, Academic Technology Advisory Group	Fall 2010–Spring 2011
Member, Contract Faculty Hiring Committee	Summer 2010
Advisor, PSU Cycling Club	Spring 2010–Spring 2012
Co-organizer, 2010 Plymouth Bike/Walk to Work Day	Spring 2010
Coauthor, PSU Carbon Action Plan	Spring 2010
Member, Wellness Works Committee	Fall 2009–Spring 2012

 $\begin{array}{lll} \textit{Co-organizer}, \ \text{New Faculty Orientation} & \text{Summer 2009} \\ \textit{Member}, \ \text{President's Commission on Environmental Sustainability} & \text{Spring 2009-Fall 2011} \\ \textit{Member}, \ \text{Mathematics Curriculum Committee} & \text{Spring 2009} \end{array}$

University of Colorado, Boulder, CO

Co-organizer, Workshop on Inquiry-Driven Learning

Co-organizer, Graduate Student Orientation

Summers 2006–2007

Front Range Community College, Boulder, CO

 $Advisor, \, \text{STEM Club} \\ \textit{Co-organizer}, \, \pi \, \, \text{Day} \\ \textit{Co-organizer}, \, \text{FRCC Fun Run}$

Fall 2002–Spring 2003 Spring 2002