



 DEVITO

AUTOMATIC GENERATION OF PRODUCTION-GRADE HYBRID MPI-OPENMP PARALLEL WAVE PROPAGATORS USING DEVITO

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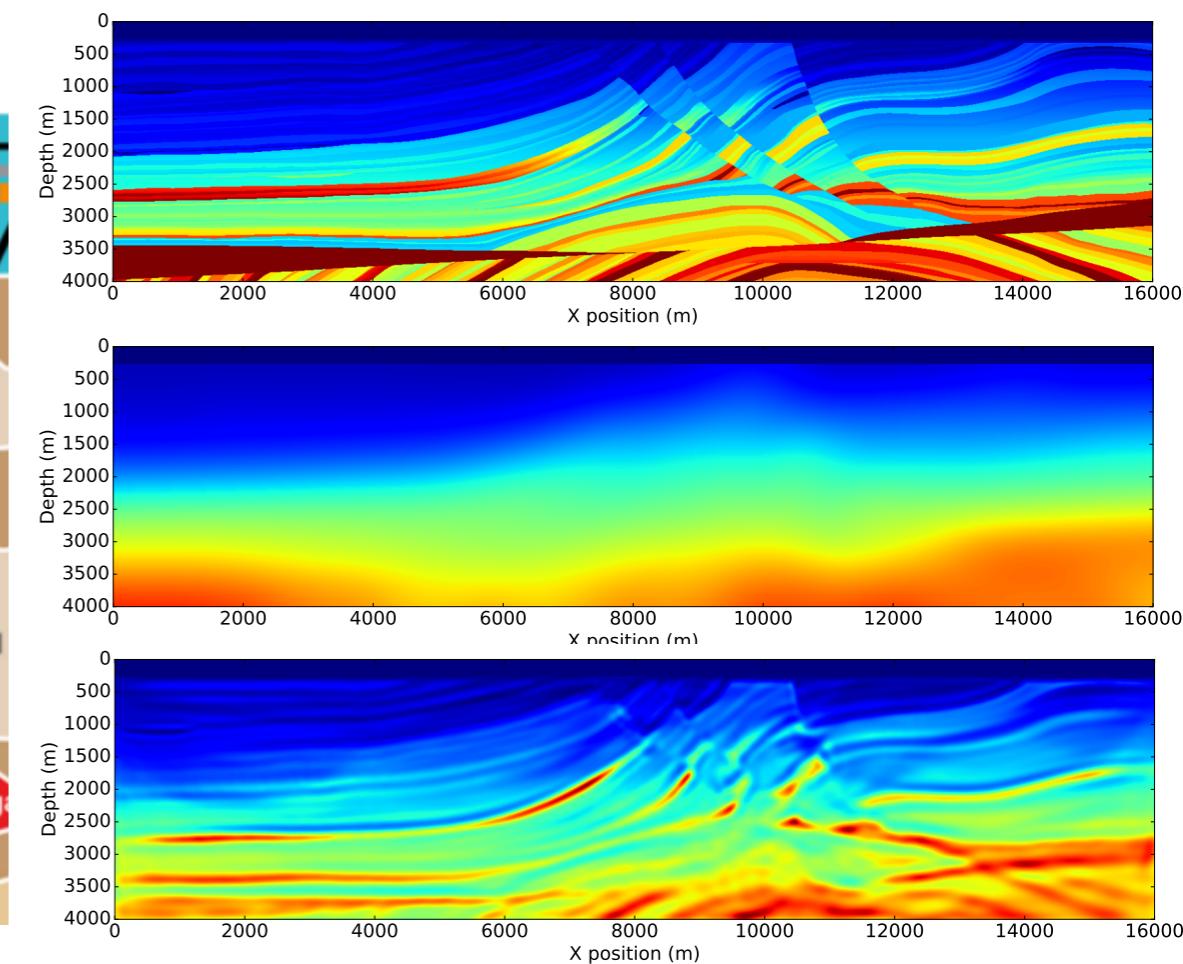
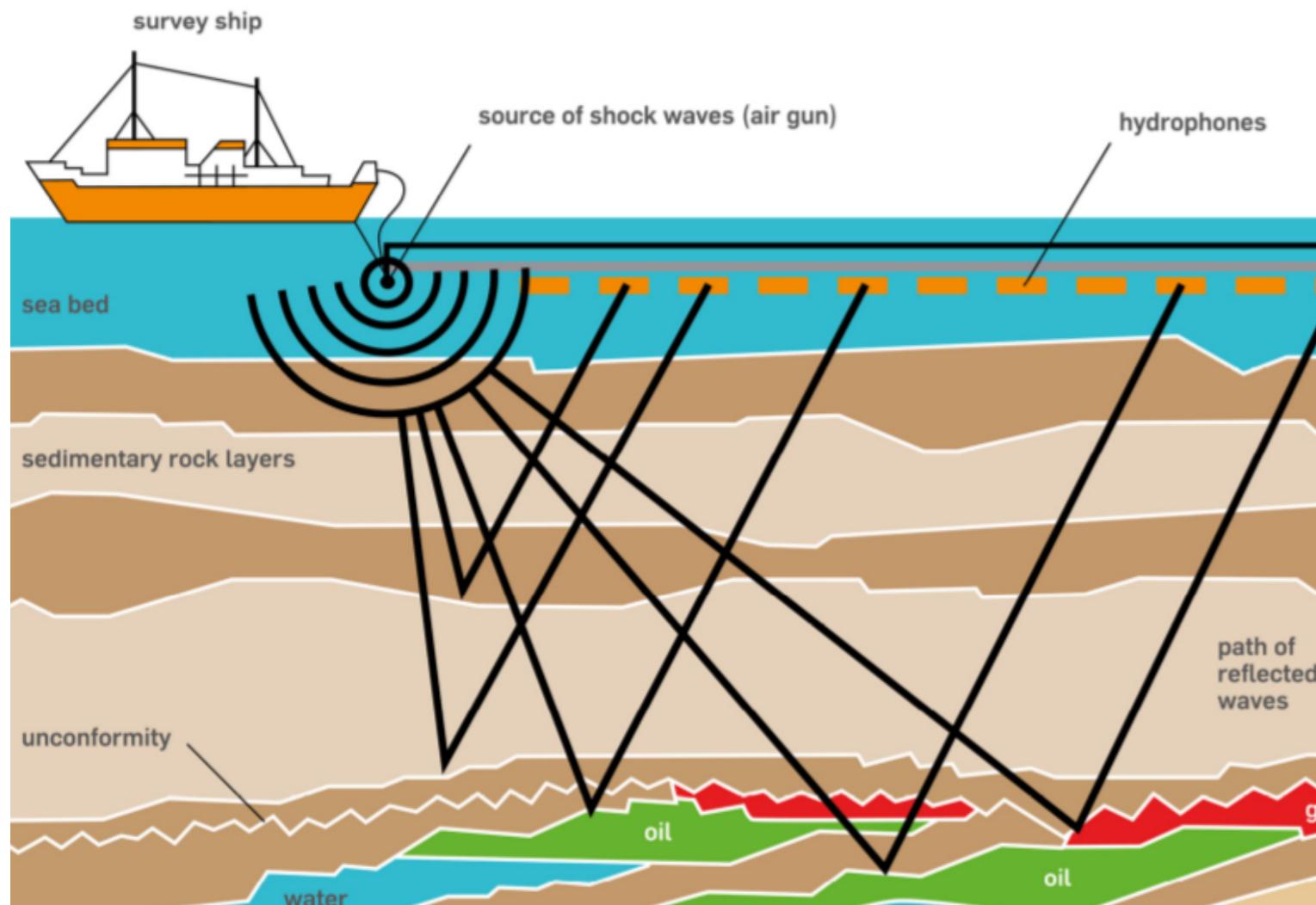
⁴DUG - DownUnder Geosolutions

⁵Shell

Devito: a DSL and compiler for explicit finite differences

- Embedded in Python – easy to learn.
- Devito is a compiler:
 - Generates optimized parallel C code: SIMD, OpenMP, MPI.
 - Support for multiple architectures.
 - Xeon and Xeon Phi (KNL) – fully supported.
 - ARM64 – experimental.
 - GPU's – in development.
- Straightforward to integrate with existing codes in other languages.
- Open source platform – MIT license.
- **Used commercially – easy to play with, but not a toy...**
- Testing (continuous integration), code reviewing, examples, ...

Overarching target application: inversion for seismic imaging



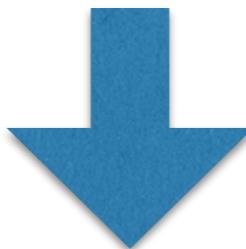
<http://www.open.edu/openlearn/science--maths--technology/science/environmental--science/earths--physical--resources--petroleum/content--section--3.2.1>

Real-life

**Full-waveform
inversion**

Raising the level of abstraction

$$m \frac{\partial^2 u}{\partial t^2} + \eta \frac{\partial u}{\partial t} - \Delta u = 0$$



```
void kernel(...) {  
    ...  
    <impenetrable code with aggressive  
     performance optimizations>  
    ...  
}
```

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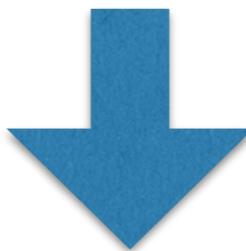
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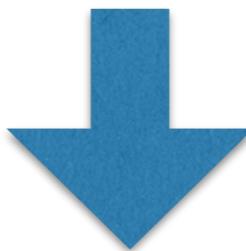
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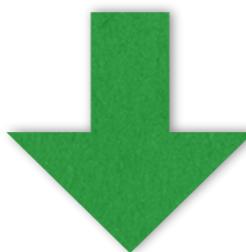
```
eqn = m * u.dt2 + eta * u.dt - u.laplace
```

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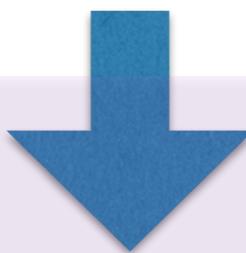
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```
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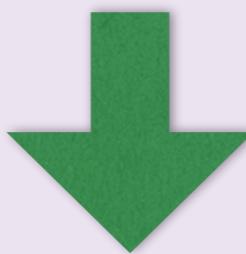
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Devito

```
eqn = m * u.dt2 + eta * u.dt - u.laplace
```



```
void kernel(...) { ... }
```

The code really needs to fly

Realistic full-waveform inversion (FWI) scenario

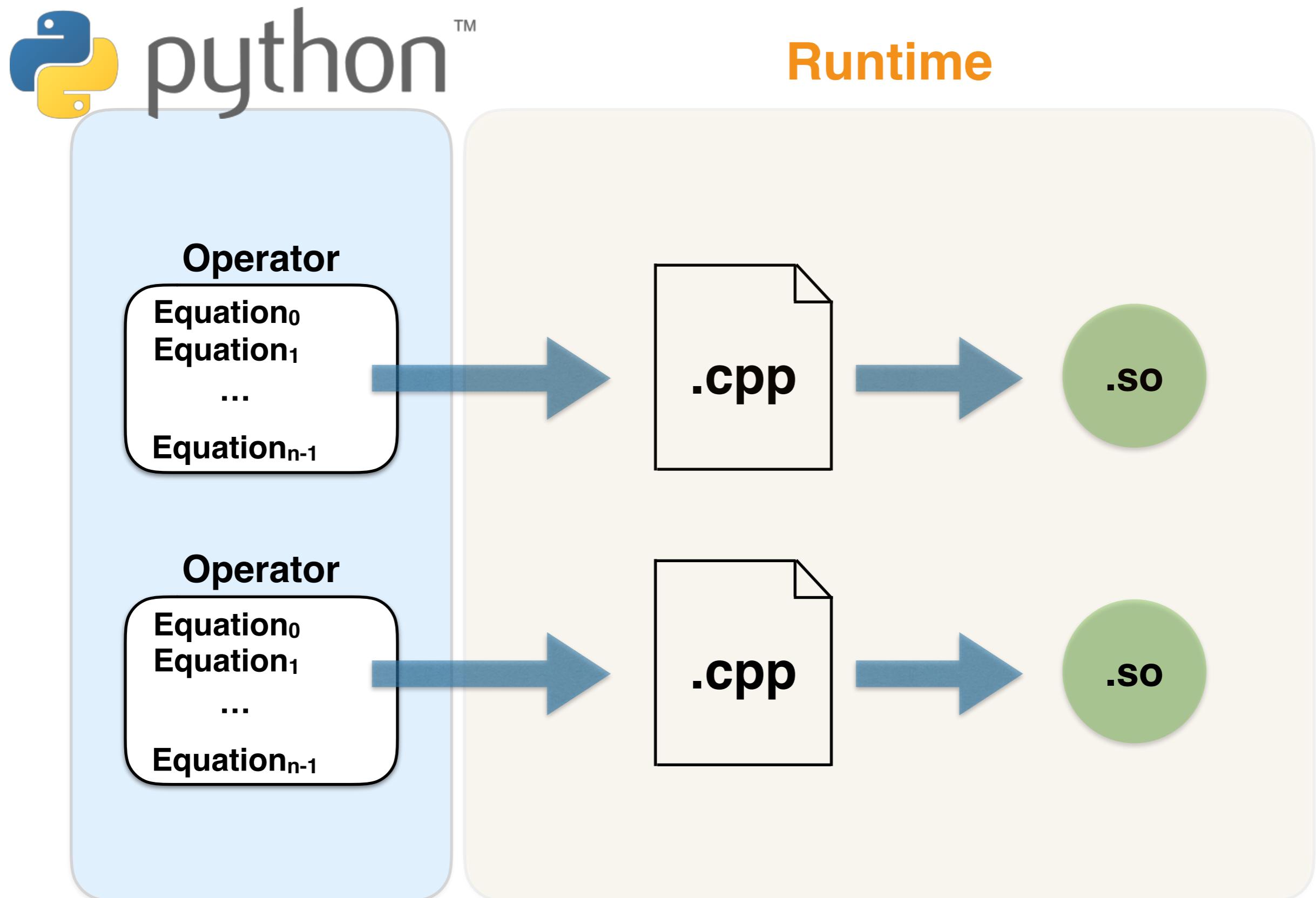
- **$\mathcal{O}(10^3)$** FLOPs per loop iteration or high memory pressure
 - 3D grids with **$>10^9$** grid points
 - Often more than **3000** time steps
 - Two operators: forward + adjoint, to be executed **~ 15** times
 - Usually **30000** shots
- $\approx \mathcal{O}(\text{billions}) \text{ TFLOPs}$

Which means days, or weeks, or months on supercomputers!

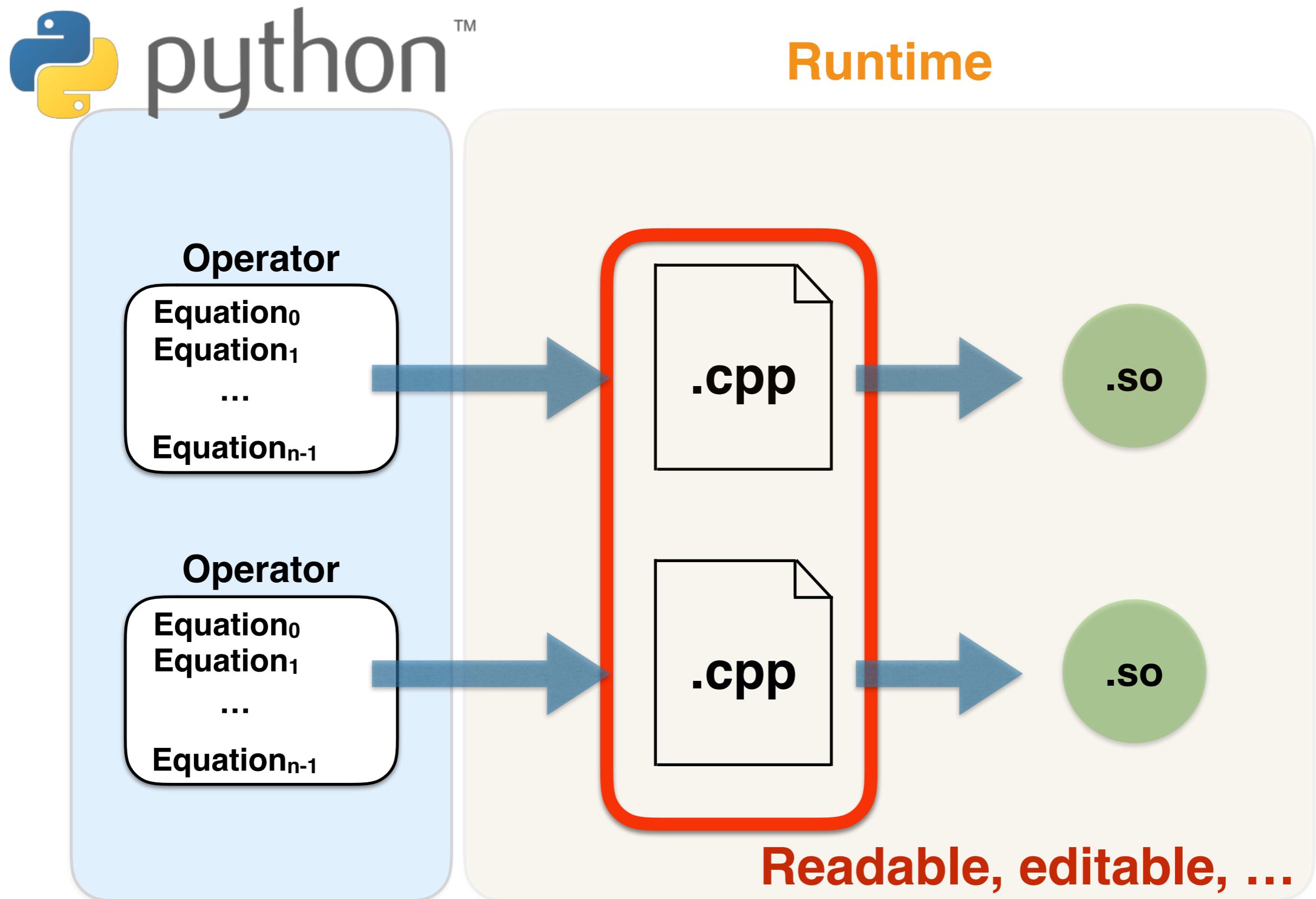
Lots of variations in physics, mathematics, platforms, ...

- Many formulations of wave equations (R&D still super active)
- Many space and time discretizations
- Many types of boundary conditions in finite differences (too many)
- Unstructured computation (e.g., interpolation for sparse data)
- Proliferation of computer architectures (functional and performance portability)
- ...

So, what does it look like?



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Production-Grade Hybrid MPI-OpenMP Parallel Wave Propagators using Devito — the key steps

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Create a grid

```
>>> grid = Grid(shape=..., extent=...) )
```

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Define the functions present in the PDE

```
>>> m = Function(name="m", grid=grid, space_order=12)
>>> u = TimeFunction(name="wavefield", grid=grid, ...)
```

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Write out the PDE

```
>>> pde = m*u.dt2 - u.laplace
>>> eqn = Eq(u.forward, solve(pde, u.forward))
```

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Write out the boundary conditions (or use Absorbing layers, or...)

```
>>> ... # "Just" other Eqs or Functions
```

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Define the source/receivers to inject/record seismic waves

```
>>> src = SparseTimeFunction(name="source", grid=grid, ...)  
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Create an Operator

```
>>> op = Operator(eqn, bcs, src.inject(...), rec.interpolate(...))
```

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This will generate OpenMP + MPI code !

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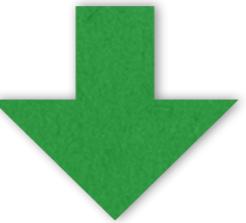
If you want (...), run the Operator

```
>>> op.apply(...)
```

Flexibility in space/time discretization

Define the functions used in the PDE

```
>>> m = Function(name="m", grid=grid, space_order=so)
>>> u = TimeFunction(name="wavefield", grid=grid, space_order=so)
```



so=4

```
for (int time = time_m, t0 = (time)%(3), t1 = (time + 1)%(3), t2 = (time + 2)%(3);
time <= time_M; time += 1, t0 = (time)%(3), t1 = (time + 1)%(3), t2 = (time + 2)%(3))
    for (int x = x_m; x <= x_M; x += 1)
        for (int y = y_m; y <= y_M; y += 1)
            for (int z = z_m; z <= z_M; z += 1)
                u[t1][x + 4][y + 4][z + 4] = 2*pow(dt, 3)*(-2.083333333333e-4F*u[t0][x + 2]
[y + 4][z + 4] + 3.333333333333e-3F*u[t0][x + 3][y + 4][z + 4] -
2.083333333333e-4F*u[t0][x + 4][y + 2][z + 4] + 3.333333333333e-3F*u[t0][x + 4][y +
3][z + 4] - 2.083333333333e-4F*u[t0][x + 4][y + 4][z + 2] + 3.333333333333e-3F*u[t0]
[x + 4][y + 4][z + 3] - 1.875e-2F*u[t0][x + 4][y + 4][z + 4] +
3.333333333333e-3F*u[t0][x + 4][y + 4][z + 5] - 2.083333333333e-4F*u[t0][x + 4][y +
4][z + 6] + 3.333333333333e-3F*u[t0][x + 4][y + 5][z + 4] - 2.083333333333e-4F*u[t0]
[x + 4][y + 6][z + 4] + 3.333333333333e-3F*u[t0][x + 5][y + 4][z + 4] -
2.083333333333e-4F*u[t0][x + 6][y + 4][z + 4])/pow(dt, 2)*damp[x + 1][y + 1][z + 1] +
2*dt*m[x + 4][y + 4][z + 4]) + pow(dt, 2)*damp[x + 1][y + 1][z + 1]*u[t2][x + 4][y + 4]
[z + 4]/(pow(dt, 2)*damp[x + 1][y + 1][z + 1] + 2*dt*m[x + 4][y + 4][z + 4]) + 4*dt*m[x
+ 4][y + 4][z + 4]*u[t0][x + 4][y + 4][z + 4]/(pow(dt, 2)*damp[x + 1][y + 1][z + 1] +
2*dt*m[x + 4][y + 4][z + 4]) - 2*dt*m[x + 4][y + 4][z + 4]*u[t2][x + 4][y + 4][z + 4]/
(pow(dt, 2)*damp[x + 1][y + 1][z + 1] + 2*dt*m[x + 4][y + 4][z + 4]);
```

so=12

```
for (int time = time_m, t0 = (time)%(3), t1 = (time + 1)%(3), t2 = (time + 2)%(3);
time <= time_M; time += 1, t0 = (time)%(3), t1 = (time + 1)%(3), t2 = (time + 2)%(3))
    for (int x = x_m; x <= x_M; x += 1)
        for (int y = y_m; y <= y_M; y += 1)
            for (int z = z_m; z <= z_M; z += 1)
                u[t1][x + 12][y + 12][z + 12] = 2*pow(dt, 3)*(-1.5031265031265e-7F*u[t0][x +
6][y + 12][z + 12] + 2.5974025974026e-6F*u[t0][x + 7][y + 12][z + 12] -
2.23214285714286e-5F*u[t0][x + 8][y + 12][z + 12] + 1.32275132275132e-4F*u[t0][x + 9][y
+ 12][z + 12] - 6.69642857142857e-4F*u[t0][x + 10][y + 12][z + 12] +
4.28571428571429e-3F*u[t0][x + 11][y + 12][z + 12] - 1.5031265031265e-7F*u[t0][x + 12]
[y + 6][z + 12] + 2.5974025974026e-6F*u[t0][x + 12][y + 7][z + 12] -
2.23214285714286e-5F*u[t0][x + 12][y + 8][z + 12] + 1.32275132275132e-4F*u[t0][x + 12]
[y + 9][z + 12] - 6.69642857142857e-4F*u[t0][x + 12][y + 10][z + 12] +
4.28571428571429e-3F*u[t0][x + 12][y + 11][z + 12] - 1.5031265031265e-7F*u[t0][x + 12]
[y + 12][z + 6] + 2.5974025974026e-6F*u[t0][x + 12][y + 12][z + 7] -
2.23214285714286e-5F*u[t0][x + 12][y + 12][z + 8] + 1.32275132275132e-4F*u[t0][x + 12]
[y + 12][z + 9] - 6.69642857142857e-4F*u[t0][x + 12][y + 12][z + 10] +
4.28571428571429e-3F*u[t0][x + 12][y + 12][z + 11] - 2.2370833333333e-2F*u[t0][x + 12]
[y + 12][z + 12] + 4.28571428571429e-3F*u[t0][x + 12][y + 12][z + 13] -
6.69642857142857e-4F*u[t0][x + 12][y + 12][z + 14] + 1.32275132275132e-4F*u[t0][x + 12]
[y + 12][z + 15] - 2.23214285714286e-5F*u[t0][x + 12][y + 12][z + 16] +
2.5974025974026e-6F*u[t0][x + 12][y + 12][z + 17] - 1.5031265031265e-7F*u[t0][x + 12][y
+ 12][z + 18] + 4.28571428571429e-3F*u[t0][x + 12][y + 13][z + 12] -
6.69642857142857e-4F*u[t0][x + 12][y + 14][z + 12] + 1.32275132275132e-4F*u[t0][x + 12]
[y + 15][z + 12] - 2.23214285714286e-5F*u[t0][x + 12][y + 16][z + 12] +
2.5974025974026e-6F*u[t0][x + 12][y + 17][z + 12] - 1.5031265031265e-7F*u[t0][x + 12][y
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+ 12][z + 12])/pow(dt, 2)*damp[x + 1][y + 1][z + 1] + 2*dt*m[x + 12][y + 12][z + 12]) +
pow(dt, 2)*damp[x + 1][y + 1][z + 1]*u[t2][x + 12][y + 12][z + 12] + 4*dt*m[x + 12][y + 12][z
+ 12]*u[t0][x + 12][y + 12][z + 12]/(pow(dt, 2)*damp[x + 1][y + 1][z + 1] + 2*dt*m[x + 12][y
+ 12][z + 12]) - 2*dt*m[x + 12][y + 12][z + 12]*u[t2][x + 12][y + 12][z + 12]/(pow(dt, 2)*damp[x
+ 1][y + 1][z + 1] + 2*dt*m[x + 12][y + 12][z + 12]);
```

Data dependence analysis

- Represents data (array) accesses as (labelled) vectors in \mathbb{Z}^n

$$u[t+2, x-3] \rightarrow \begin{bmatrix} t+2 \\ x-3 \end{bmatrix}$$

- Currently uses a simple in-house framework based on Lamport theory
- The Devito compiler relies on data dependence analysis for many tasks
 - Inferring the iteration direction (`i++` or `i--`?)
 - Loop scheduling (convert list of equations into a tree of loops)
 - Loop optimizations (e.g., discovery of parallel loops)
 - MPI optimizations (e.g., reshuffling/merging communications)
- Might one day move to an external tool (ISL?) if all of our use cases are supported

Example: inferring the propagation direction

```
>>> pde = ...
>>> eqn = Eq(u.forward, solve(pde, u.forward))
```

$$u[t+1, \dots] = f(u[t, \dots], u[t-1, \dots], \dots)$$

versus

```
>>> pde = ...
>>> eqn = Eq(u.backward, solve(pde, u.backward))
```

$$u[t-1, \dots] = f(u[t, \dots], u[t+1, \dots], \dots)$$

In the first case, the t loop iterates forward ($t++$),
in the latter case it iterates backwards ($t--$)

Code generation for Higdon BCs is based on this exact framework

Example: topological sorting for maximal “loop fusion”

$u[t+1, x] = F0(u[t, x], u[t-1, x], v[t, x], \dots)$

$u[t+1, s] = F1(u[t+1, u_coords[s]], \dots)$

$v[t+1, x] = F2(v[t, x], v[t-1, x], u[t, x], \dots)$

$v[t+1, s] = F3(u[t+1, v_coords[s]], \dots)$

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$v[t+1, s] = F3(u[t+1, v_coords[s]], \dots)$

**Only flow-dependences in
the time (t) dimension!**

Example: topological sorting for maximal “loop fusion”

$$u[t+1, x] = F_0(u[t, x], u[t-1, x], v[t, x], \dots)$$

$$u[t+1, s] = F_1(u[t+1, u_{\text{coords}}[s]], \dots)$$



$$v[t+1, x] = F_2(v[t, x], v[t-1, x], u[t, x], \dots)$$

$$v[t+1, s] = F_3(u[t+1, v_{\text{coords}}[s]], \dots)$$

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Example: topological sorting for maximal “loop fusion”

$u[t+1, x] = F0(u[t, x], u[t-1, x], v[t, x], \dots)$

$v[t+1, x] = F2(v[t, x], v[t-1, x], u[t, x], \dots)$

$u[t+1, s] = F1(u[t+1, u_coords[s]], \dots)$

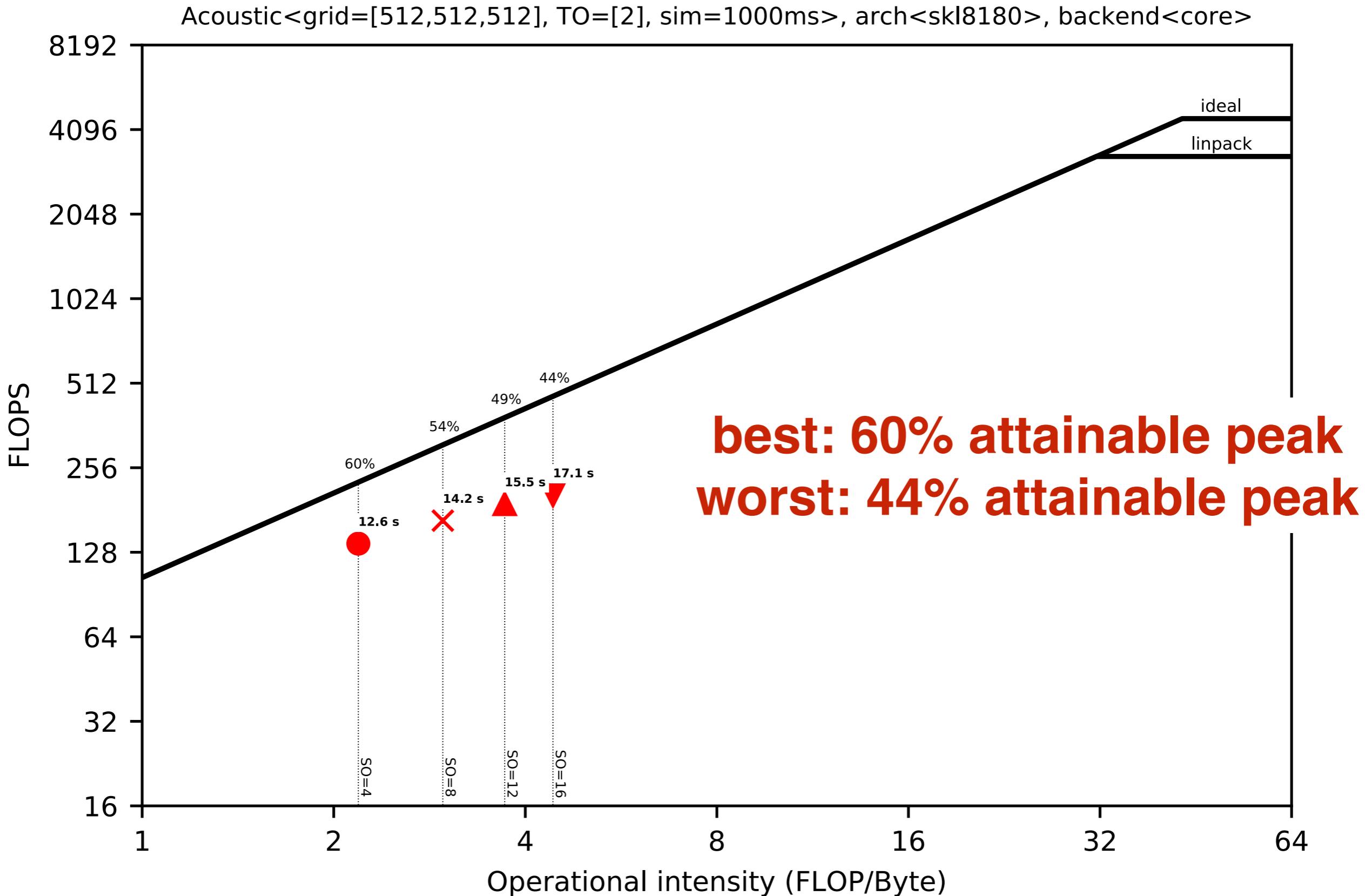
$v[t+1, s] = F3(u[t+1, v_coords[s]], \dots)$

Example: topological sorting for maximal “loop fusion”

```
for t = t_m to t_M, t++  
  for x = x_m to x_M, x++  
    u[t+1,x] = F0(u[t,x], u[t-1,x], v[t,x], ...)  
    v[t+1,x] = F2(v[t,x], v[t-1,x], u[t,x], ...)
```

```
for s = s_m to s_M, s++  
  u[t+1,s] = F1(u[t+1,u_coords[s]], ...)  
  v[t+1,s] = F3(u[t+1,v_coords[s]], ...)
```

Single-socket — Isotropic acoustic on Skylake 8180



Software and workloads used in performance tests may have been optimized for performance only on Intel microprocessors. Performance tests, such as SYSmark and MobileMark, are measured using specific computer systems, components, software, operations and functions. Any change to any of those factors may cause the results to vary. You should consult other information and performance tests to assist you in fully evaluating your contemplated purchases, including the performance of that product when combined with other products. For more complete information visit www.intel.com/benchmarks. Intel internal measurements as of Dec 2017 on Intel® Xeon Phi™ processor 7250 with 16 GiB MCDRAM, 96 GiB DDR4 and/or Intel® Xeon® processor 8108 with 128 GiB DDR. Benchmark results were obtained prior to implementation of recent software patches and firmware updates intended to address exploits referred to as "Spectre" and "Meltdown". Implementation of these updates may make these results inapplicable to your device or system.

Generalized Common Sub-expressions Elimination

```
a = sin(phi[i,j]) + sin(phi[i-1,j-1]) + sin(phi[i+2,j+2])
```

Observations:

Same operators (`sin`) , same operands (`phi`) , same indices (`i, j`)

Linearly dependent index vectors (`[i, j], [i-1, j-1], [i+2, j+2]`)

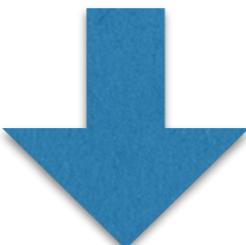
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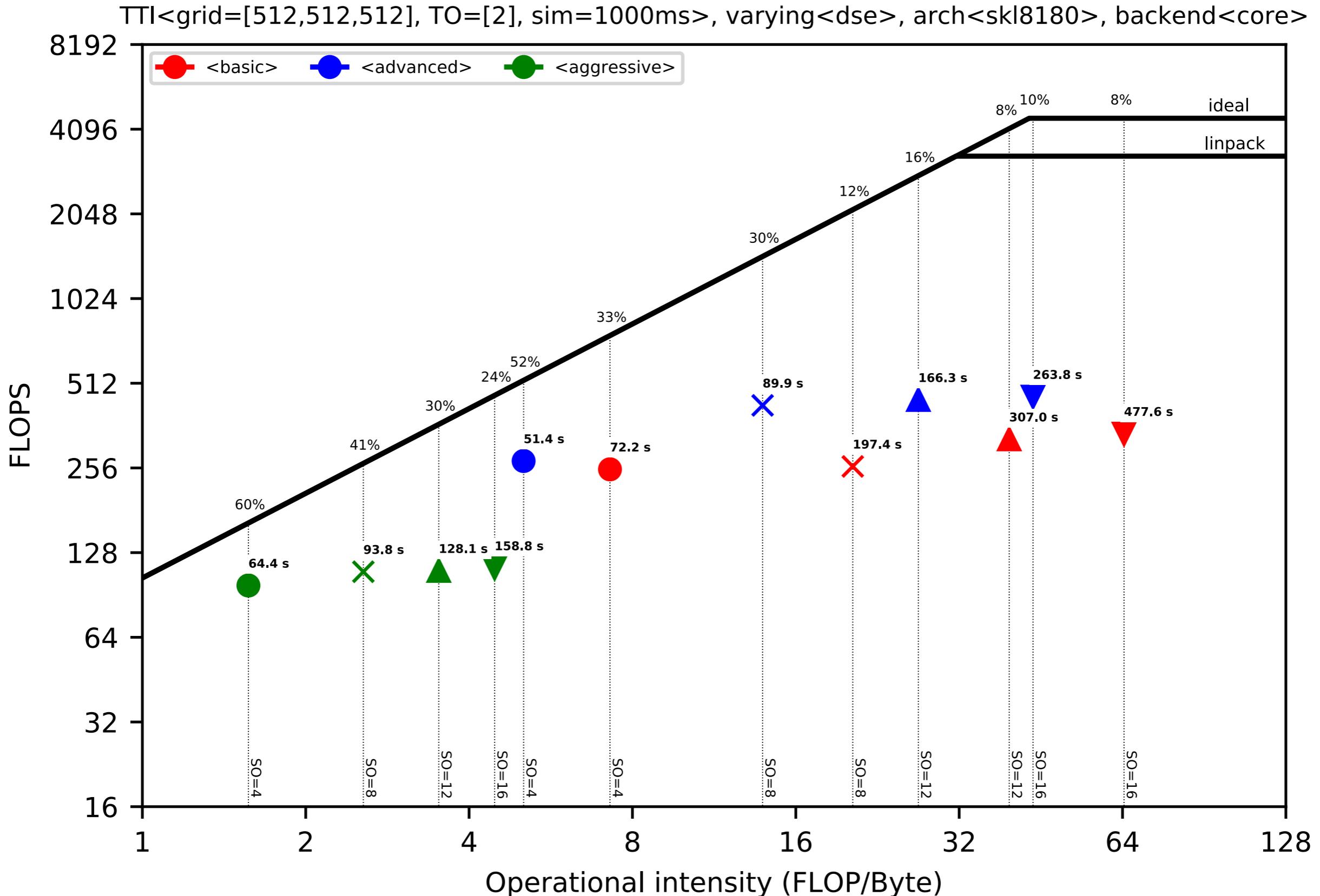


```
B[i,j] = sin(phi[i,j])
```

```
a = B[i,j] + B[i-1,j-1] + B[i+2,j+2]
```

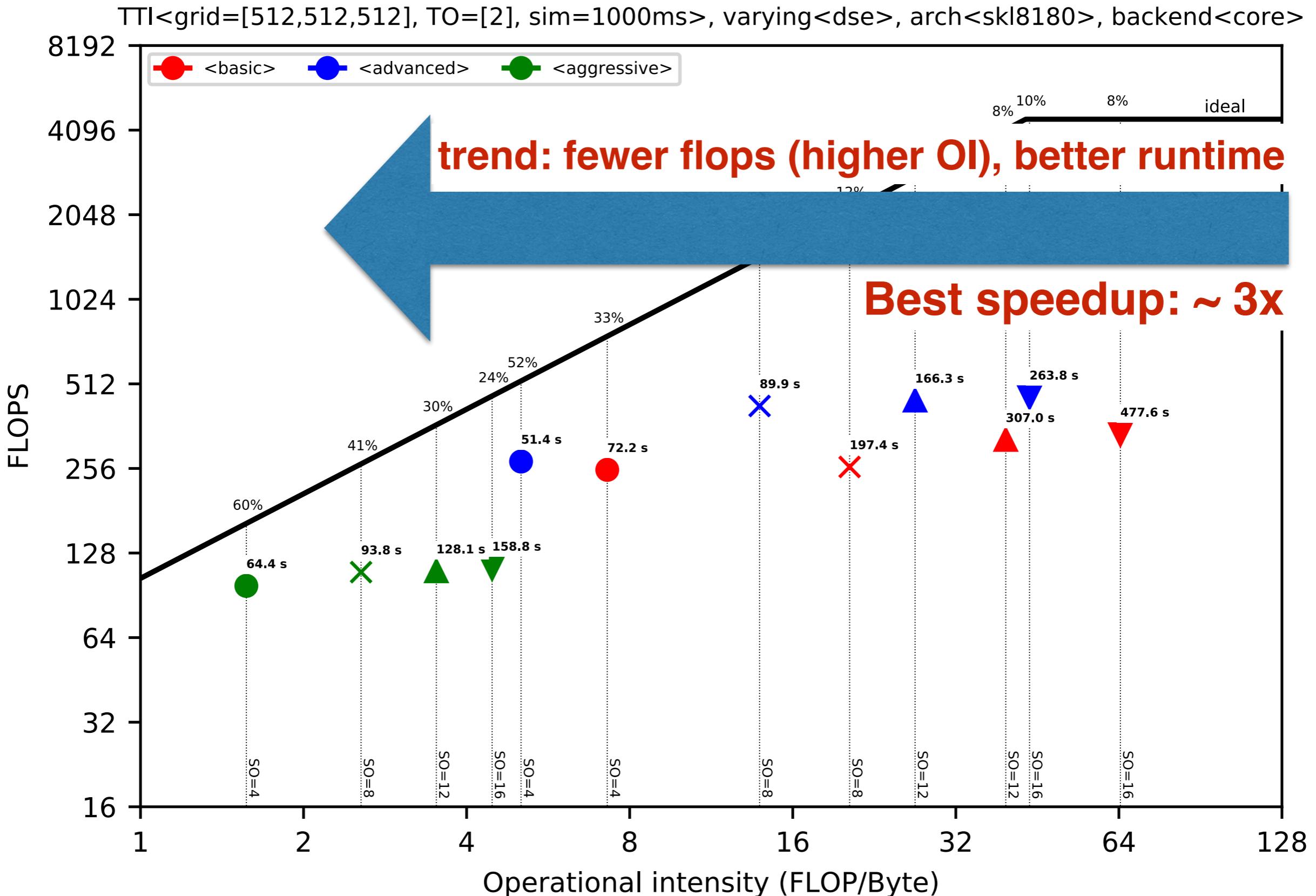
Trade-off FLOPs/storage

Single-socket — TTI on Skylake 8180



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Single-socket — TTI on Skylake 8180



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MPI support — for free

mpirun <mpi args> python app.py

And that's it.

MPI support — for free

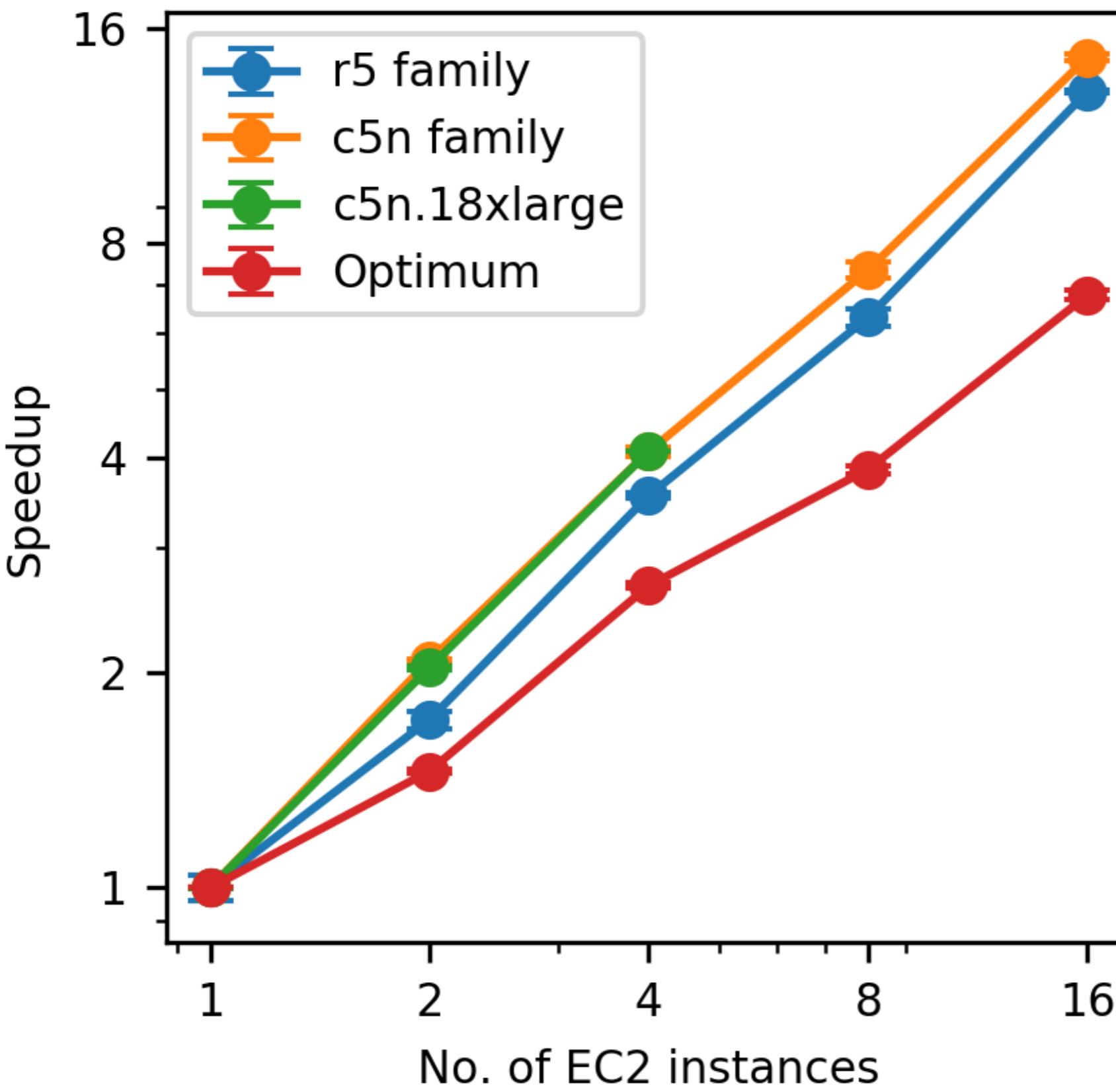
Python-level features:

- Domain decomposition based on MPI Cartesian grid abstraction.
- New package *numpy4mpi*: NumPy arrays automatically split and distributed according to domain decomposition.
 - Parallel data slicing dealt with efficiently under the hood
- Sources/receivers (i.e. “sparse data”) distributed automatically.

C-level features:

- Generated code contains the MPI halo exchanges. Required halo exchanges identified through data dependence analysis.
- Optimizations (e.g., reshuffling halo updates, computation/communication overlap) also exploit data dependence analysis.
- Data packing/unpacking is threaded for performance.

Cluster/cloud — TTI strong scaling on AWS and Optimum



These are best-case scenario experiments: one process/thread per **node** (i.e., the whole bandwidth at full disposal)

Conclusions

- Devito is an open-source high-productivity and high-performance Python framework for finite-differences.
- Driven by real-world seismic imaging, inspired by projects such as FEniCS/Firedrake.
- Based on actual compiler technology.
- Interdisciplinary, interinstitutional, international research effort.
- Growing community and user base
 - Academic: e.g. used by SLIM team to develop JUDI, [...]
 - Commercial: Production code by DUG, [...]
 - Many other R&D teams [...]

Useful links and resources

Website: <http://www.devitoproject.org>

GitHub: <https://github.com/opesci/devito>

Slack: <https://opesci-slackin.now.sh>

Appendix

Experimentation details

- Architectures
 - Intel® Xeon® Platinum 8180 Processor (“Skylake”, 28 cores)
 - Intel® XeonPhi® 7250 (68 cores)
 - Quadrant mode (still no support for NUMA)
 - Tried 1, 2, 4 threads per core. Shown best.
- Compiler
 - ICC 18 -xHost -O3
 - -xMIC-AVX512 on Xeon Phi
 - -qopt-zmm-usage=high on Skylake
- Runs
 - Single socket
 - Pinning via Numactl
 - On the XeonPhi®, data fits in MCDRAM
- Roofline calculations:
 - Memory bandwidth: STREAM
 - CPU peak: pen & paper
 - Operational intensity: source-level analysis (automated through Devito)

Experimentation details

- Experiments on AWS and Optimum

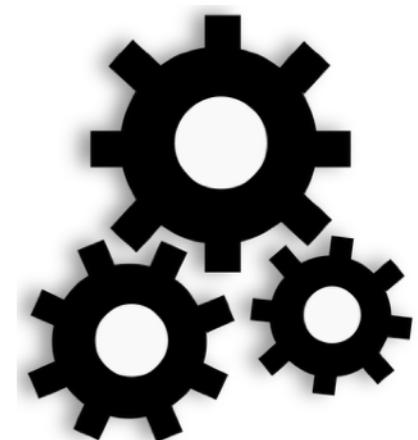
Instance	Architecture	(v)CPUs	Cores/s
m4.4xlarge	Intel Xeon E5-2686 v4 @ 2.30GHz	16	8
r5.12xlarge	Intel Xeon Platinum 8175M @ 2.50 GHz	48	24
r5.24xlarge	Intel Xeon Platinum 8175M @ 2.50 GHz	96	24
c5n.9xlarge	Intel Xeon Platinum 8124M @ 3.00 GHz	36	18
c5n.12xlarge	Intel Xeon Platinum 8142M @ 3.00 GHz	72	18
r5.metal	Intel Xeon Platinum 8175M @ 2.50 GHz	96	24
Optimum	Intel Xeon E5-2680 v2 @ 2.80GHz	20	10

What Devito does **NOT** (and probably will never) do

- Parallel I/O
- (Obviously) the overarching application (though we provide examples)
- Implicit solvers
- Many other things

Many optimizations BEFORE creating a tree of loops...

- “Loop fusion” => Equation clustering
- “Loop-invariant code motion” => Cluster lifting
- Common sub-expressions elimination (both cross- and intra-iteration), factorization, ... they all happen at the cluster level



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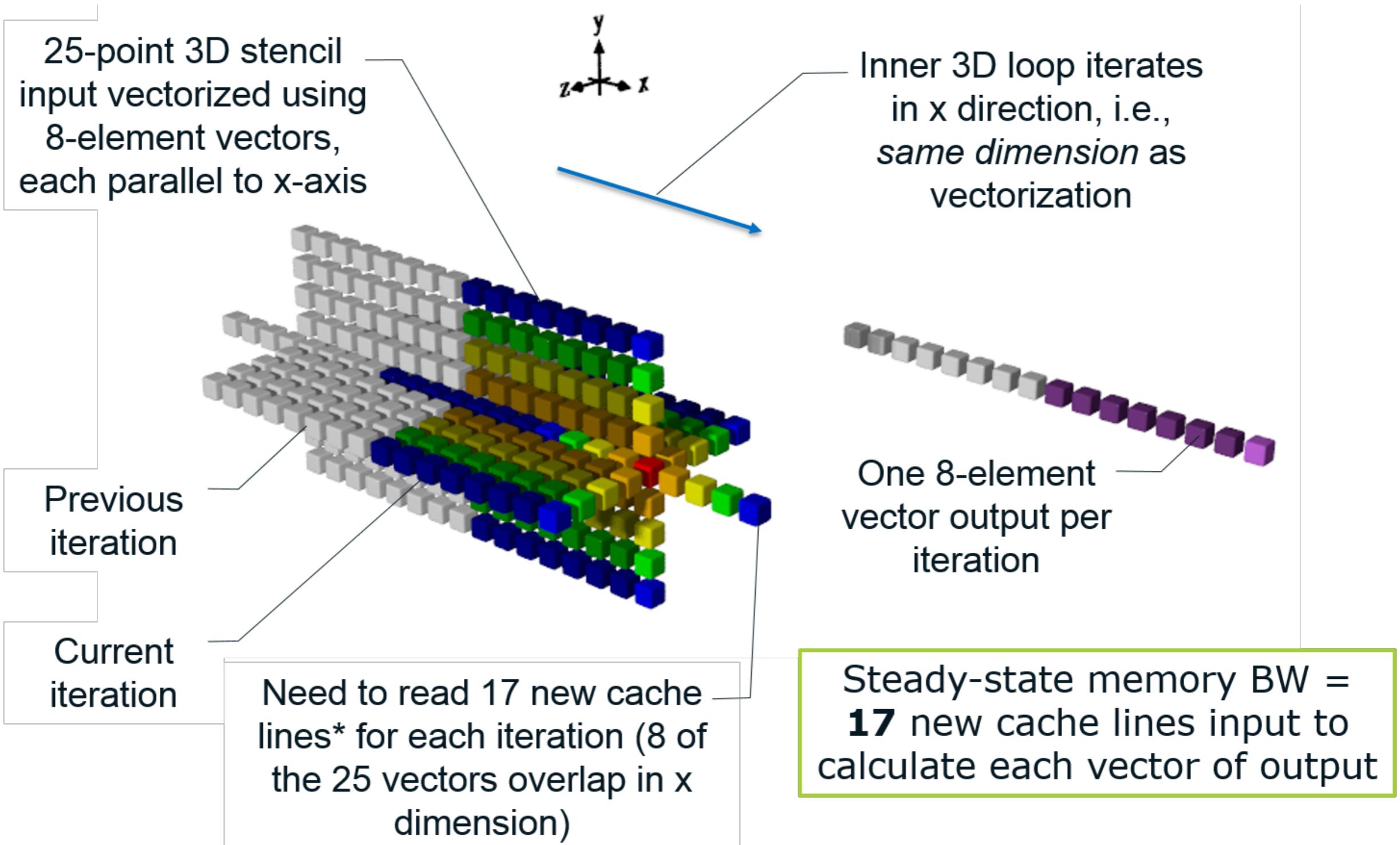
While others are applied on the tree

- OpenMP (with nested parallelism)
- SIMD-ization
- Loop blocking
- ...



Beyond 1D vectorization ...

Traditional “1D” vectorization requires lots of bandwidth

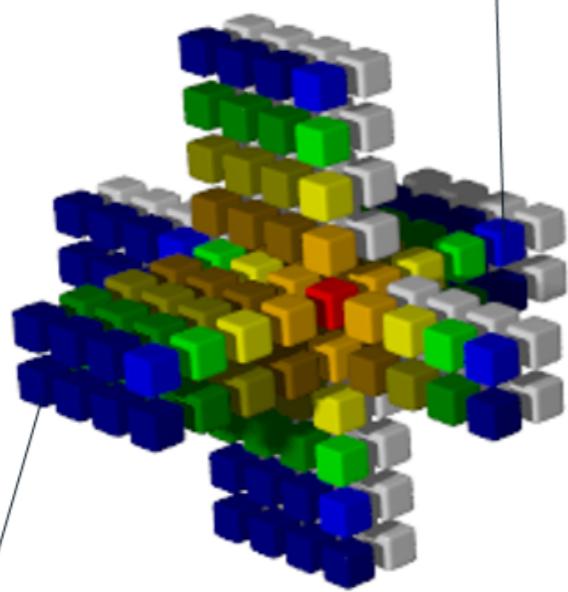


*Assuming cache line size = vector size.

Vector folding via YASK (a Devito backend)

Data layout transformation + cross-loop vectorization to optimize bandwidth usage

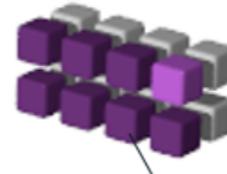
25-point 3D stencil
input vectorized using
8-element vectors,
*each containing a 4x2
grid in the x-y plane*



Need to read only 7 new cache lines for each iteration
(vectors overlap in x-y dimensions within an iteration and in z dimension between iterations)



Inner 3D loop iterates in z direction, i.e., *perpendicular* to 2D vector



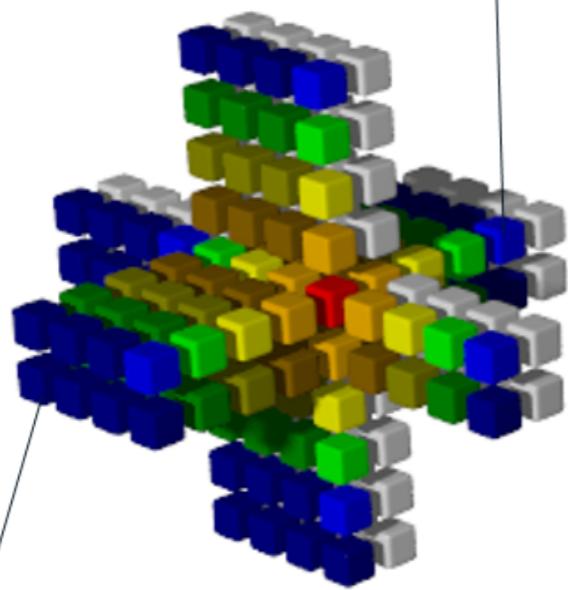
One 8-element (4x2) vector output per iteration

Steady-state memory BW = **7** new cache lines input to calculate each vector of output:
2.4x lower than in-line

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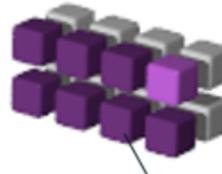
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One 8-element (4x2) vector output per iteration

**There's actually much more:
multi-level tiling
software prefetching
temporal waveform blocking**

Dual-socket — TTI on Skylake 8175

grid = 512 x 512 x 1024

single-socket, OMP only: **783** s (\pm 12 s)

dual-socket, OMP only: **626** s (\pm 45 s)

dual-socket, OMP+MPI: **319** s (\pm 8 s)

Loop scheduling

The problem: **convert a list of equations into a tree of loops**

```
>>> op = Operator(eqn, bcs, src.inject(...), rec.interpolate(...))
```

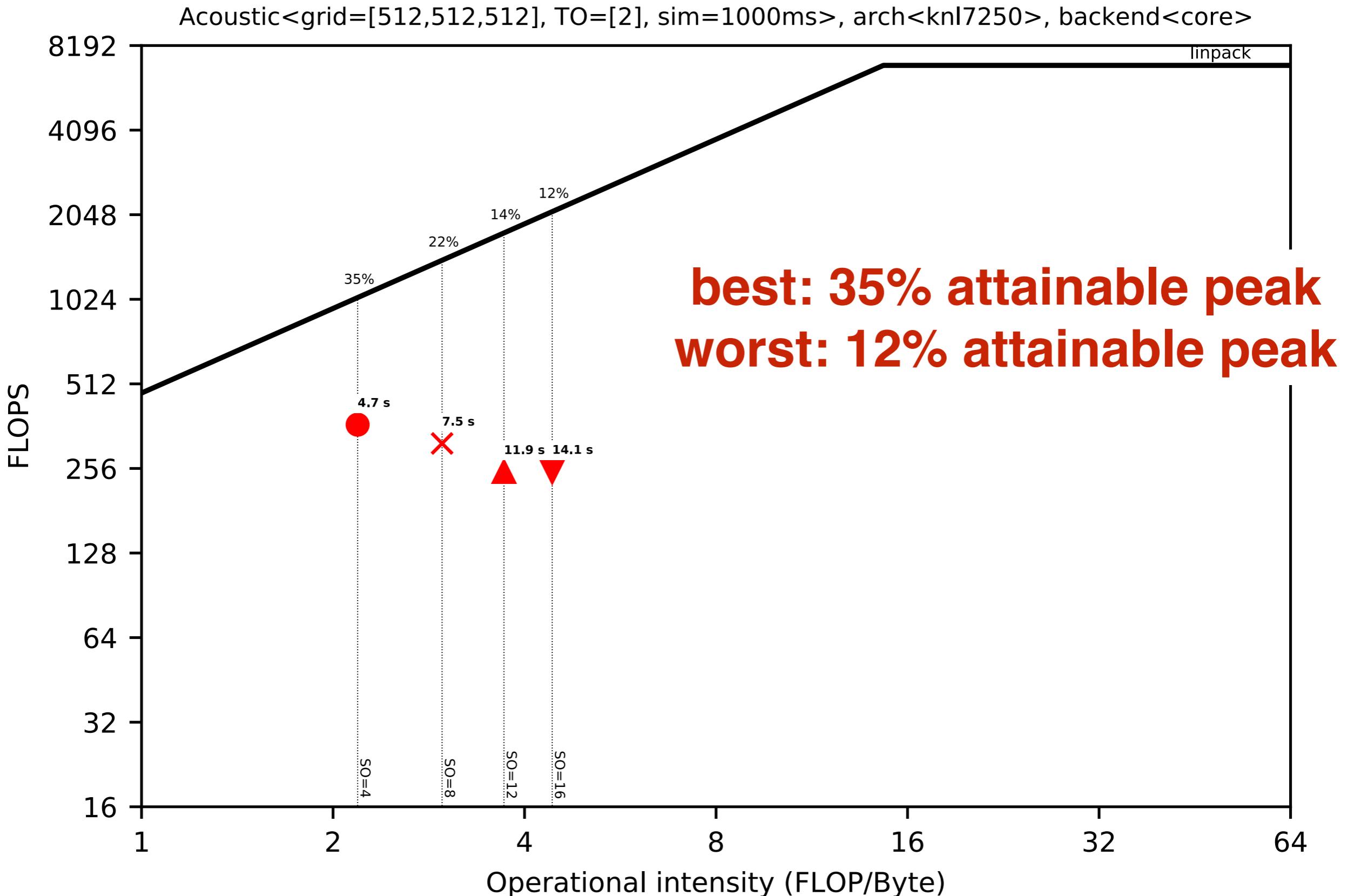
Need to support:

- Control flow (e.g., for data sub-sampling)
- Optimizations (e.g., fusion, code motion, ...)
- Human-readable (e.g., generate routines to avoid repetitions)

The key ingredients:

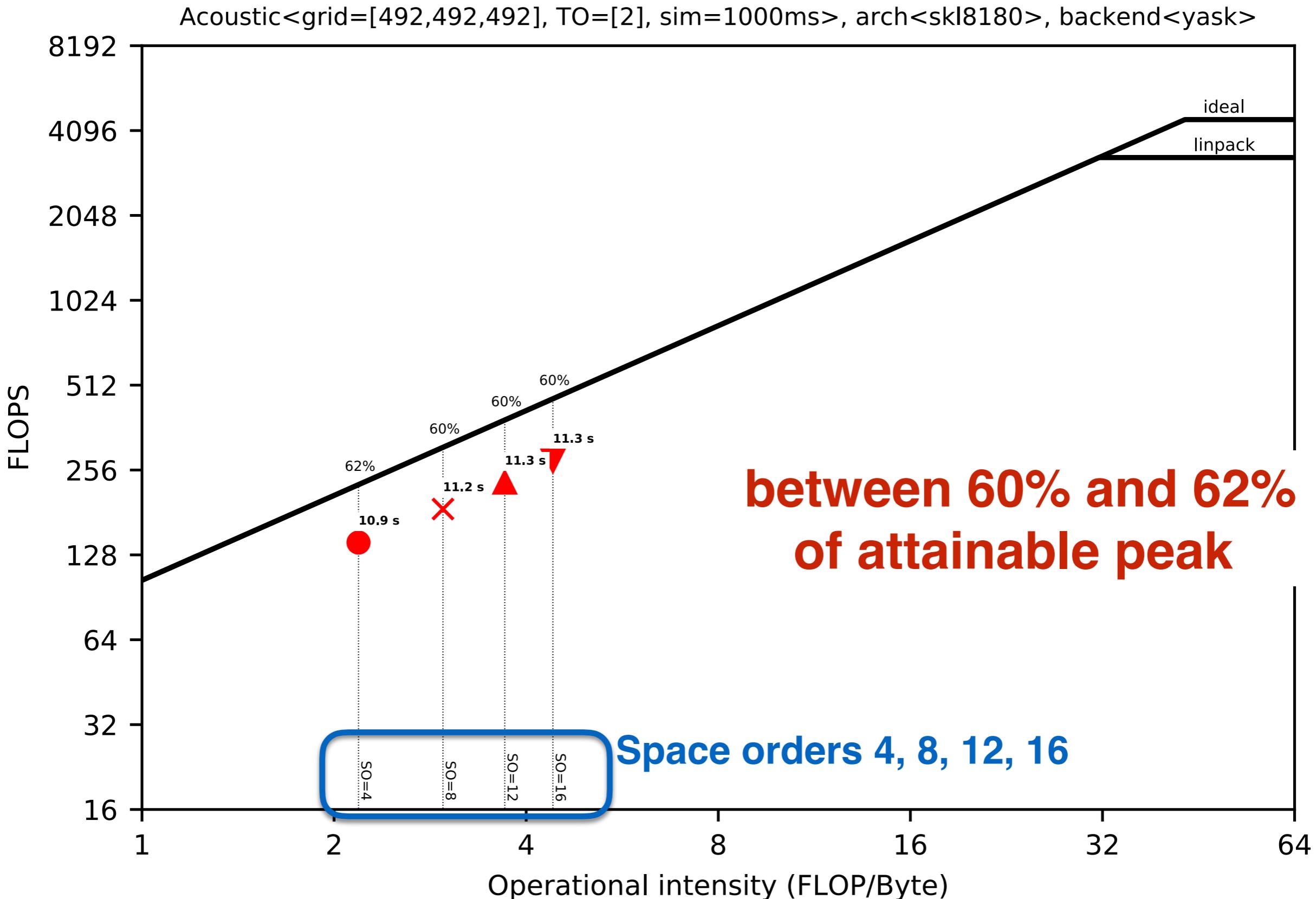
- Data dependence analysis
- Topological sorting

Single-socket — Isotropic acoustic on Xeon Phi 7250



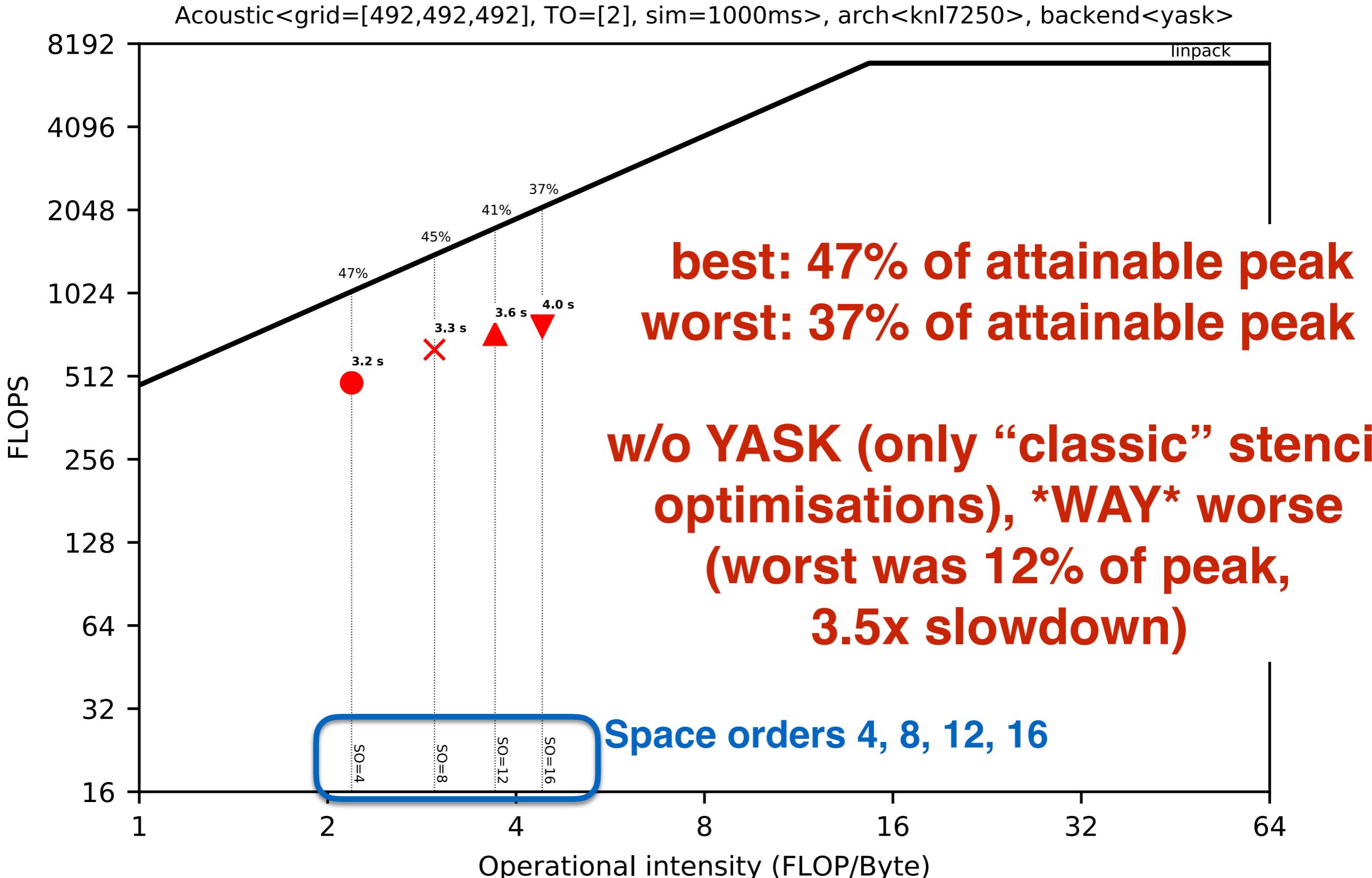
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Acoustic on Skylake 8180 with YASK



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Acoustic on Xeon Phi 7250 with YASK



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