# assignment2

### 2023-02-15

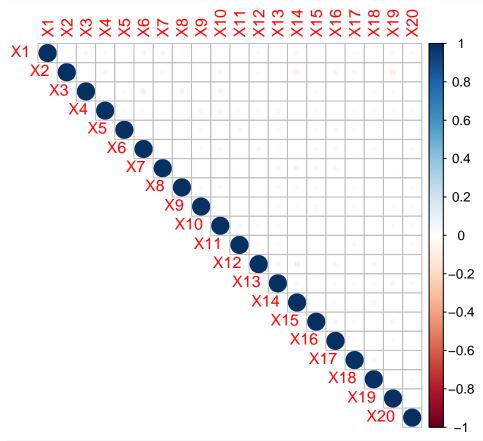
Running the file provided by Professor first and then starting with assignment 02

```
#HW02.R
#run a lasso and elastic net model
library(survival)
library(coxed)
## Loading required package: rms
## Loading required package: Hmisc
## Loading required package: lattice
## Loading required package: Formula
## Loading required package: ggplot2
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:base':
##
##
       format.pval, units
## Loading required package: SparseM
##
## Attaching package: 'SparseM'
## The following object is masked from 'package:base':
##
##
       backsolve
## Loading required package: mgcv
## Loading required package: nlme
## This is mgcv 1.8-40. For overview type 'help("mgcv-package")'.
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.1-4
library(corrplot)
## corrplot 0.92 loaded
#Simulate time-to-event data
set.seed(123)
n <- 1000
x1 = matrix(rbinom(n * 10, size = 1, prob = 0.3), n, 10)
```

```
x2 = matrix(rnorm(n * 10, mean=0, sd=.4), n, 10)
simdata <- sim.survdata(N=n,T=365, censor=0.15,</pre>
                      0.4, 0.4, 0.5, 0.5, 0.5, 0, 0, 0, 0, 0),
                      X = cbind(x1,x2)
data <- simdata$data
attach(data)
setwd("~/StatisticalModelingandComputing/")
#save graphics output in pdf - saves graph(s) in working directory
pdf(file="HW02_out.pdf")
cormat <- round(cor(data[,1:20]),2)</pre>
cormat #the correlation coefficients among the predictors are small
##
         Х1
               Х2
                    ХЗ
                          Х4
                                Х5
                                      Х6
                                           Х7
                                                 Х8
                                                       Х9
                                                           X10
                                                                 X11
                                                                       X12
## X1
       1.00 0.00 0.05 -0.03 -0.01 -0.06 0.05 -0.02 0.00 0.01 0.00 -0.04
## X2
       0.00 1.00 0.01 0.05 0.00 -0.01 0.03 -0.01 0.00 -0.04 -0.02 -0.03
## X3
       0.05 \quad 0.01 \quad 1.00 \quad -0.01 \quad -0.04 \quad 0.08 \quad 0.01 \quad -0.07 \quad 0.00 \quad 0.06 \quad -0.02 \quad 0.00
     -0.03 0.05 -0.01 1.00 -0.04 0.02 -0.01 0.00 0.05 0.05 0.02 -0.03
     -0.01 0.00 -0.04 -0.04 1.00 -0.01 -0.02 0.01 0.04 0.01 -0.05 -0.01
## X5
## X6 -0.06 -0.01 0.08 0.02 -0.01 1.00 0.00 0.01 0.02 -0.04 0.01 0.04
       0.05 0.03 0.01 -0.01 -0.02 0.00 1.00 0.02 0.00 -0.01 -0.03 0.02
## X7
## X8 -0.02 -0.01 -0.07 0.00 0.01 0.01 0.02 1.00 0.03 0.04 0.01 0.01
       0.00 \quad 0.00 \quad 0.00 \quad 0.05 \quad 0.04 \quad 0.02 \quad 0.00 \quad 0.03 \quad 1.00 \quad 0.01 \quad 0.01 \quad 0.01
## X9
## X10 0.01 -0.04 0.06 0.05 0.01 -0.04 -0.01 0.04 0.01 1.00 -0.04 0.02
## X11 0.00 -0.02 -0.02 0.02 -0.05 0.01 -0.03 0.01 0.01 -0.04 1.00 -0.02
## X12 -0.04 -0.03 0.00 -0.03 -0.01 0.04 0.02 0.01 0.01 0.02 -0.02
## X13 0.00 -0.02 0.00 -0.06 0.02 -0.02 -0.05 0.04 -0.02 0.02 -0.02 0.04
## X14 -0.06 -0.08 0.00 -0.01 -0.01 -0.02 0.07 0.03 0.03 -0.01 0.00 0.08
## X15 0.00 -0.01 -0.03 -0.04 0.02 0.03 0.03 0.02 -0.05 0.01 -0.01 0.00
## X16 0.01 0.04 0.00 -0.01 0.03 -0.04 -0.04 0.01 0.01 0.00 0.00 -0.04
0.02
## X18 -0.01 -0.01 -0.02 0.02 0.00 -0.03 0.01 -0.01 0.01 0.00 0.01
                                                                     0.05
## X19 -0.05 -0.09 -0.03 -0.03 -0.02 0.01 0.02 0.00 -0.03 0.03 -0.01
## X20
      0.02 0.00 -0.01 -0.03 0.00 0.03 0.02 0.02 -0.04 -0.04 -0.03 0.00
##
        X13
              X14
                   X15
                         X16
                               X17
                                    X18
                                         X19
                                                X20
## X1
       0.00 -0.06 0.00 0.01 0.02 -0.01 -0.05 0.02
     -0.02 -0.08 -0.01 0.04 0.04 -0.01 -0.09 0.00
       0.00 0.00 -0.03 0.00 0.00 -0.02 -0.03 -0.01
## X3
      -0.06 -0.01 -0.04 -0.01 -0.02 0.02 -0.03 -0.03
## X4
## X5
       0.02 -0.01 0.02 0.03 0.02 0.00 -0.02 0.00
## X6 -0.02 -0.02 0.03 -0.04 0.00 -0.03 0.01 0.03
## X7 -0.05 0.07 0.03 -0.04 0.00 0.01 0.02 0.02
       0.04 0.03 0.02 0.01 -0.02 -0.01 0.00 0.02
## X8
## X9 -0.02 0.03 -0.05 0.01 0.02 0.01 -0.03 -0.04
## X10 0.02 -0.01 0.01 0.00 0.00 0.00 0.03 -0.04
## X11 -0.02 0.00 -0.01 0.00 -0.05 0.01 -0.01 -0.03
## X12 0.04 0.08 0.00 -0.04 0.02 0.05 0.00 0.00
## X13 1.00 -0.04 0.01 0.02 -0.03 0.02 0.05 -0.04
## X14 -0.04 1.00 -0.01 0.02 0.01 0.05 -0.01 -0.01
```

```
## X15  0.01 -0.01  1.00  0.05  0.02 -0.01 -0.06 -0.01  ## X16  0.02  0.02  0.05  1.00 -0.02  0.00 -0.03  0.00  ## X17 -0.03  0.01  0.02 -0.02  1.00  0.03  0.00  0.01  ## X18  0.02  0.05 -0.01  0.00  0.03  1.00 -0.02  0.02  ## X19  0.05 -0.01 -0.06 -0.03  0.00 -0.02  1.00  0.00  ## X20 -0.04 -0.01 -0.01  0.00  0.01  0.02  0.00  1.00
```

corrplot(cormat, type="upper")



model <- coxph(Surv(y, failed) ~ ., data=data)
model\$coefficients ## model-estimated coefficients</pre>

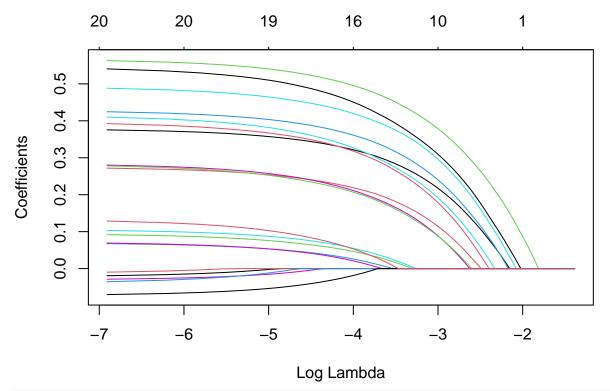
```
##
                        Х2
                                   ХЗ
                                                            Х5
                                                                        Х6
                                                   0.50063956 -0.03073943
##
  0.38553508 0.27916537 0.57810539
                                      0.43436549
           Х7
                       Х8
                                   Х9
                                               X10
                                                           X11
##
  -0.02313047 -0.01384174 0.09575907
                                      0.06933871
                                                   0.42155723
                                                               0.28890993
##
          X13
                       X14
                                  X15
                                              X16
                                                           X17
   0.55808911
               0.40491251 0.29214823 -0.04087630 0.10750969
##
                                                               0.07324933
          X19
                       X20
## -0.07680564 0.13702470
```

summary(model)

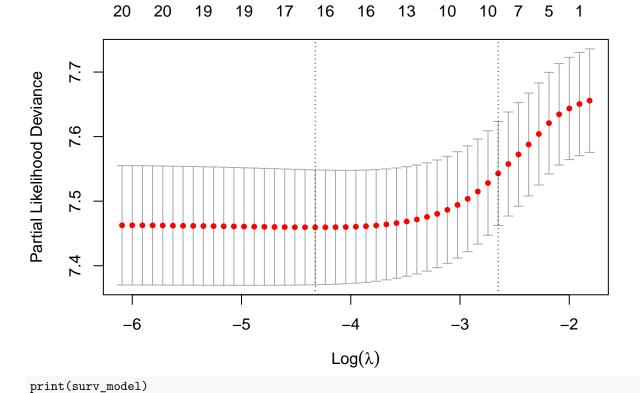
```
## Call:
## coxph(formula = Surv(y, failed) ~ ., data = data)
##
## n= 1000, number of events= 842
##
## coef exp(coef) se(coef) z Pr(>|z|)
```

```
## X1
       0.38554
                 1.47040 0.07768 4.963 6.94e-07 ***
## X2
       0.27917
                 1.32203 0.07687 3.632 0.000281 ***
                          0.07716 7.492 6.79e-14 ***
## X3
       0.57811
                 1.78266
## X4
       0.43437
                 1.54398
                          0.07754 5.602 2.12e-08 ***
## X5
       0.50064
                 1.64978
                          0.07956 6.293 3.12e-10 ***
## X6
                 -0.03074
      -0.02313
                          0.07762 -0.298 0.765693
## X7
                 0.97713
      -0.01384
## X8
                 0.98625
                          0.07679 -0.180 0.856960
## X9
       0.09576
                 1.10049
                          0.07838 1.222 0.221807
## X10 0.06934
                 1.07180
                          0.07638 0.908 0.363981
## X11 0.42156
                 1.52433
                          0.09187
                                   4.589 4.46e-06 ***
## X12 0.28891
                 1.33497
                          0.08811
                                   3.279 0.001042 **
## X13 0.55809
                 1.74733
                          0.09007
                                   6.196 5.80e-10 ***
## X14 0.40491
                 1.49917
                          0.08823 4.589 4.45e-06 ***
## X15 0.29215
                 1.33930
                          0.09136 3.198 0.001384 **
## X16 -0.04088
                 0.95995
                          0.08892 -0.460 0.645749
## X17 0.10751
                          0.08645 1.244 0.213623
                  1.11350
## X18 0.07325
                  1.07600
                          0.08728 0.839 0.401355
## X19 -0.07681
                          0.09030 -0.851 0.395021
                 0.92607
## X20 0.13702
                 1.14686
                          0.08709 1.573 0.115613
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
       exp(coef) exp(-coef) lower .95 upper .95
## X1
         1.4704
                    0.6801
                              1.2627
                                         1.712
## X2
         1.3220
                    0.7564
                              1.1371
                                          1.537
## X3
          1.7827
                    0.5610
                              1.5324
                                          2.074
## X4
         1.5440
                    0.6477
                              1.3263
                                         1.797
## X5
                    0.6061
         1.6498
                              1.4116
                                          1.928
## X6
         0.9697
                    1.0312
                              0.8342
                                         1.127
## X7
         0.9771
                    1.0234
                              0.8392
                                         1.138
## X8
         0.9863
                    1.0139
                              0.8484
                                         1.146
## X9
         1.1005
                    0.9087
                              0.9438
                                         1.283
## X10
                              0.9228
         1.0718
                    0.9330
                                          1.245
## X11
         1.5243
                    0.6560
                              1.2732
                                         1.825
## X12
         1.3350
                    0.7491
                              1.1232
                                         1.587
## X13
         1.7473
                    0.5723
                              1.4645
                                         2.085
## X14
         1.4992
                    0.6670
                              1.2611
                                          1.782
## X15
         1.3393
                    0.7467
                              1.1197
                                         1.602
## X16
         0.9599
                    1.0417
                              0.8064
                                         1.143
## X17
         1.1135
                    0.8981
                              0.9400
                                         1.319
## X18
         1.0760
                    0.9294
                              0.9068
                                          1.277
## X19
         0.9261
                    1.0798
                              0.7759
                                          1.105
## X20
         1.1469
                    0.8719
                              0.9669
                                          1.360
## Concordance= 0.644 (se = 0.011)
## Likelihood ratio test= 208.6 on 20 df,
                                            p=<2e-16
## Wald test
                       = 208.8 on 20 df,
                                            p = < 2e - 16
## Score (logrank) test = 211.3 on 20 df,
                                            p=<2e-16
# Perform survival analysis using qlmnet
# Perform survival analysis using glmnet
```

```
\# assuming the predictors are in the first p columns and the response is in the last two columns
p <- ncol(data) - 2
р
## [1] 20
xmatrix=as.matrix(data[,1:p])
show_fit=glmnet(xmatrix,Surv(y, failed),standardize=TRUE,lambda=seq(0,0.25,.001),alpha=1,family = "cox"
#print(show_fit)
plot(show_fit, label=TRUE)
## Warning in regularize.values(x, y, ties, missing(ties), na.rm = na.rm):
## collapsing to unique 'x' values
             0
                            8
                                          10
                                                         14
                                                                        17
      0.5
      0.4
Coefficients
      0.3
      0.2
      0.1
             0
                            1
                                           2
                                                          3
                                                                         4
                                            L1 Norm
```



#show the use of the CV metric "Partial Likelihood Deviance"
surv\_model <- cv.glmnet(xmatrix,Surv(y, failed), family = "cox", type.measure = "deviance",alpha=1,nfole
plot(surv\_model)</pre>



##

```
## Call: cv.glmnet(x = xmatrix, y = Surv(y, failed), type.measure = "deviance",
                                                                                   nfolds = 10, fami
##
## Measure: Partial Likelihood Deviance
##
        Lambda Index Measure
                                  SE Nonzero
## min 0.01323
                  28 7.460 0.08895
## 1se 0.07060
                  10
                      7.543 0.08055
# Extract the optimal lambda value at lambda.1se
lambda_opt <- surv_model$lambda.1se</pre>
# Fit the model using the optimal lambda value
fit <- glmnet(xmatrix,Surv(y, failed), family = "cox", type.measure = "deviance",alpha=1,lambda = lambd
coef(fit)
## 20 x 1 sparse Matrix of class "dgCMatrix"
##
## X1 0.145632493
## X2 0.040743048
## X3 0.303992347
## X4 0.158165765
## X5 0.209541491
## X6 .
## X7
## X8
## X9
## X10 .
## X11 0.105349378
## X12 0.007016571
## X13 0.224756848
## X14 0.086701559
## X15 0.012951787
## X16 .
## X17 .
## X18 .
## X19 .
## X20 .
# Make predictions
predictions <- predict(fit, newx = xmatrix[,1:p], type = "response")</pre>
# Evaluate the model performance using concordance index (c-index)
c_index <- Cindex(predictions,Surv(y, failed))</pre>
c_index
## [1] 0.6351173
#show the use of CV metric "C"
surv_model_C = cv.glmnet(xmatrix,Surv(y, failed), family = "cox", type.measure = "C", alpha=1,nfolds =
plot(surv_model_C)
```

# 20 20 19 19 17 16 16 13 10 10 7 5 1

```
print(surv_model_C)
##
##
## Measure: C-index
##
      Lambda Index Measure
##
                              SE Nonzero
               26 0.6378 0.008766
## min 0.01593
                                     16
## 1se 0.05861
               12 0.6304 0.007090
# Extract the optimal lambda value at lambda.1se
lambda_opt <- surv_model_C$lambda.1se</pre>
# Fit the model using the optimal lambda value
fit_C <- glmnet(xmatrix,Surv(y, failed), family = "cox", type.measure = "C",alpha=1,lambda = lambda_opt</pre>
coef(fit_C)
## 20 x 1 sparse Matrix of class "dgCMatrix"
##
## X1 0.18707001
## X2 0.08315443
## X3 0.34697746
## X4 0.20533298
## X5
     0.25941205
## X6
```

## X7 . ## X8 . ## X9 . ## X10 .

## X11 0.15478563

```
## X12 0.05398264
## X13 0.27324345
## X14 0.13936475
## X15 0.05567932
## X16 .
## X17 .
## X18 .
## X19 .
## X20 .
# Make predictions
predictions <- predict(fit_C, newx = xmatrix[,1:p], type = "response")
# Evaluate the model performance using concordance index (c-index)
c_index <- Cindex(predictions, Surv(y, failed))
c_index</pre>
```

### ## [1] 0.6399806

0.05 0.03

-0.02 -0.01 -0.07

## X7

## X8

## X9

### Assignment 2

a. Redo the simulation where you select 5 of the X coefficients among the binary X's to be 0 and 5 of the X coefficients among the normally distributed X's to be 0.

Note: just modify the line in the program: beta = c(0.4, 0.4, 0.5, 0.5, 0.5, 0.5, 0, 0, 0, 0, 0.4, 0.4, 0.5, 0.5, 0.5, 0.5, 0.0, 0, 0, 0, 0)

Generate the text output and the graphical output to answer parts b - f below.

0.01 -0.01 -0.02 0.00 1.00

0.00 0.01 0.01 0.02

0.00 0.00 0.00 0.05 0.04 0.02 0.00 0.03 1.00 0.01

## X10 0.01 -0.04 0.06 0.05 0.01 -0.04 -0.01 0.04 0.01 1.00 -0.04 0.02 ## X11 0.00 -0.02 -0.02 0.02 -0.05 0.01 -0.03 0.01 0.01 -0.04 1.00 -0.02

```
#Simulate time-to-event data
set.seed(123)
n <- 1000
x1 = matrix(rbinom(n * 10, size = 1, prob = 0.3), n, 10)
x2 = matrix(rnorm(n * 10, mean=0, sd=.4), n, 10)
simdata <- sim.survdata(N=n,T=365, censor=0.15,</pre>
                        beta = c(0, 0.4, 0.5, 0, 0.5, 0, 0.4, 0.4, 0, 0.5,
                                 0.5, 0, 0, 0, 0.4, 0, 0.5, 0.5, 0, 0),
                        X = cbind(x1,x2)
data <- simdata$data
cormat <- round(cor(data[,1:20]),2)</pre>
cormat #the correlation coefficients among the predictors are small
##
          X1
                Х2
                                                    X8
                                                          Х9
                                                               X10
                      ХЗ
                            Х4
                                  Х5
                                        Х6
                                              X7
                                                                      X11
## X1
        1.00
            0.00
                   0.05 -0.03 -0.01 -0.06 0.05 -0.02 0.00
                                                              0.01
                                                                    0.00 -0.04
## X2
        0.00
             1.00 0.01 0.05 0.00 -0.01
                                           0.03 -0.01
                                                        0.00 -0.04 -0.02 -0.03
        0.05 0.01 1.00 -0.01 -0.04 0.08 0.01 -0.07
                                                        0.00
                                                              0.06 -0.02 0.00
## X3
       -0.03 0.05 -0.01
                         1.00 -0.04
                                     0.02 -0.01
                                                  0.00
                                                        0.05
## X4
                                                              0.05
                                                                    0.02 - 0.03
## X5
      -0.01 0.00 -0.04 -0.04 1.00 -0.01 -0.02 0.01
                                                        0.04 0.01 -0.05 -0.01
                   0.08 0.02 -0.01 1.00 0.00
## X6
      -0.06 -0.01
                                                  0.01
                                                        0.02 - 0.04
                                                                    0.01
```

0.02

1.00

0.03

0.00 -0.01 -0.03

0.04

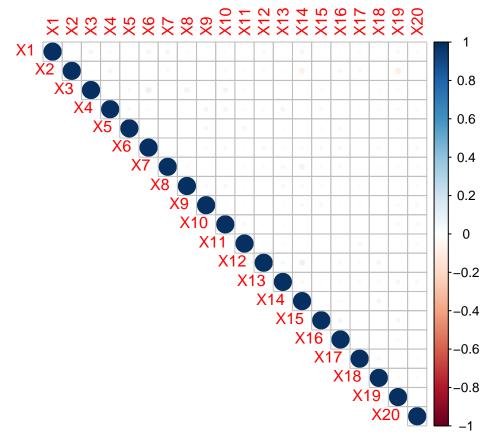
0.01

0.01

0.02

0.01

```
## X12 -0.04 -0.03 0.00 -0.03 -0.01 0.04 0.02 0.01 0.01 0.02 -0.02 1.00
## X13 0.00 -0.02 0.00 -0.06 0.02 -0.02 -0.05 0.04 -0.02 0.02 -0.02 0.04
## X14 -0.06 -0.08 0.00 -0.01 -0.01 -0.02 0.07 0.03 0.03 -0.01 0.00 0.08
## X15 0.00 -0.01 -0.03 -0.04 0.02 0.03 0.03 0.02 -0.05 0.01 -0.01 0.00
## X16 0.01 0.04 0.00 -0.01 0.03 -0.04 -0.04 0.01 0.01 0.00 0.00 -0.04
## X18 -0.01 -0.01 -0.02 0.02 0.00 -0.03 0.01 -0.01 0.01 0.00 0.01
## X19 -0.05 -0.09 -0.03 -0.03 -0.02 0.01 0.02 0.00 -0.03 0.03 -0.01
                                                                0.00
## X20 0.02 0.00 -0.01 -0.03 0.00 0.03 0.02 0.02 -0.04 -0.04 -0.03 0.00
##
                 X15
                       X16
                            X17
                                  X18
                                      X19
                                            X20
       X13
            X14
## X1
       0.00 -0.06 0.00 0.01 0.02 -0.01 -0.05 0.02
     -0.02 -0.08 -0.01 0.04 0.04 -0.01 -0.09 0.00
## X2
      0.00 0.00 -0.03 0.00 0.00 -0.02 -0.03 -0.01
## X3
## X4
     -0.06 -0.01 -0.04 -0.01 -0.02 0.02 -0.03 -0.03
## X5
      0.02 -0.01 0.02 0.03 0.02 0.00 -0.02 0.00
## X6
     -0.02 -0.02 0.03 -0.04 0.00 -0.03 0.01 0.03
## X7
     -0.05 0.07 0.03 -0.04 0.00 0.01 0.02 0.02
      0.04 0.03 0.02 0.01 -0.02 -0.01 0.00 0.02
## X8
## X9 -0.02 0.03 -0.05 0.01 0.02 0.01 -0.03 -0.04
## X10 0.02 -0.01 0.01 0.00 0.00 0.00 0.03 -0.04
## X11 -0.02 0.00 -0.01 0.00 -0.05 0.01 -0.01 -0.03
## X12 0.04 0.08 0.00 -0.04 0.02 0.05 0.00 0.00
## X13 1.00 -0.04 0.01 0.02 -0.03 0.02 0.05 -0.04
## X14 -0.04 1.00 -0.01 0.02 0.01 0.05 -0.01 -0.01
## X15 0.01 -0.01 1.00 0.05 0.02 -0.01 -0.06 -0.01
## X16 0.02 0.02 0.05 1.00 -0.02 0.00 -0.03 0.00
## X17 -0.03 0.01 0.02 -0.02 1.00 0.03 0.00 0.01
## X18 0.02 0.05 -0.01 0.00 0.03 1.00 -0.02 0.02
## X19 0.05 -0.01 -0.06 -0.03 0.00 -0.02 1.00 0.00
## X20 -0.04 -0.01 -0.01 0.00 0.01 0.02 0.00 1.00
corrplot(cormat, type="upper")
```



model <- coxph(Surv(y, failed) ~ ., data=data)
model\$coefficients ## model-estimated coefficients</pre>

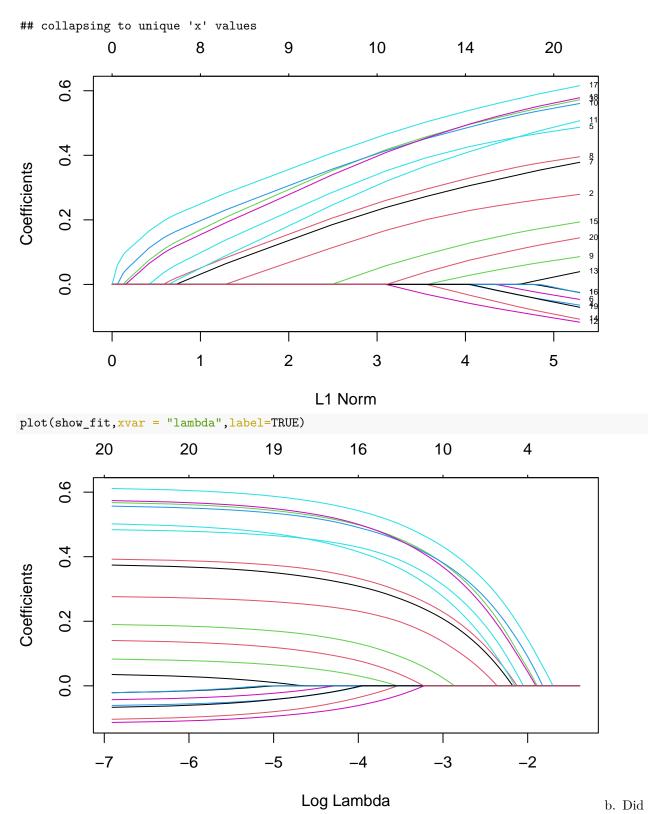
```
X1
                     Х2
                                ХЗ
                                           Х4
                                                      Х5
                                                                 Х6
## -0.02761794
             0.49590014 -0.04703972
##
          X7
                     Х8
                                Х9
                                           X10
                                                     X11
##
   0.38352880
              0.40301909
                         0.08843731
                                   0.56915107
                                               0.51425466 -0.12223634
         X13
                     X14
                               X15
                                          X16
                                                     X17
                                                                X18
   0.04293680 -0.10845914
                         0.19784765 -0.03132104
                                              0.62660513 0.58952345
##
##
         X19
                     X20
## -0.07229006
             0.14748694
```

summary(model)

```
## Call:
## coxph(formula = Surv(y, failed) ~ ., data = data)
##
    n= 1000, number of events= 842
##
##
##
         coef exp(coef) se(coef)
                                   z Pr(>|z|)
## X1
               0.97276  0.07672 -0.360  0.718849
     -0.02762
## X2
      0.28552
               1.33045 0.07694 3.711 0.000206 ***
               1.79077 0.07714 7.553 4.27e-14 ***
      0.58265
## X3
## X4
     1.64198 0.07956 6.233 4.58e-10 ***
## X5
      0.49590
## X6
     -0.04704
               0.95405 0.07709 -0.610 0.541741
               1.46745 0.07834 4.896 9.80e-07 ***
## X7
      0.38353
               1.49634 0.07767 5.189 2.11e-07 ***
## X8
      0.40302
```

```
## X9
        0.08844
                  1.09247 0.07836 1.129 0.259037
## X10 0.56915
                  1.76677 0.07801 7.296 2.97e-13 ***
## X11 0.51425
                  1.67239
                           0.09230 5.572 2.52e-08 ***
                           0.08817 -1.386 0.165635
## X12 -0.12224
                  0.88494
## X13 0.04294
                  1.04387
                           0.08778 0.489 0.624736
## X14 -0.10846
                  0.89722 0.08734 -1.242 0.214301
## X15 0.19785
                           0.09071 2.181 0.029178 *
                  1.21878
## X16 -0.03132
                  0.96916
                           0.08918 -0.351 0.725427
## X17
       0.62661
                  1.87125
                           0.08843
                                    7.086 1.38e-12 ***
## X18 0.58952
                  1.80313
                           0.08929 6.603 4.04e-11 ***
## X19 -0.07229
                  0.93026
                           0.09038 -0.800 0.423807
## X20
                  1.15892 0.08721 1.691 0.090807 .
      0.14749
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
       exp(coef) exp(-coef) lower .95 upper .95
## X1
          0.9728
                     1.0280
                               0.8370
                                          1.131
## X2
          1.3305
                     0.7516
                               1.1442
                                          1.547
## X3
          1.7908
                               1.5395
                                          2.083
                     0.5584
## X4
          0.9347
                     1.0699
                               0.8049
                                          1.085
## X5
          1.6420
                     0.6090
                               1.4049
                                          1.919
## X6
          0.9540
                               0.8203
                     1.0482
                                          1.110
## X7
          1.4675
                     0.6815
                               1.2586
                                          1.711
## X8
         1.4963
                     0.6683
                               1.2851
                                          1.742
## X9
         1.0925
                     0.9154
                               0.9369
                                          1.274
## X10
         1.7668
                     0.5660
                               1.5163
                                          2.059
## X11
                                          2.004
          1.6724
                     0.5979
                               1.3956
## X12
         0.8849
                     1.1300
                               0.7445
                                          1.052
## X13
         1.0439
                     0.9580
                               0.8789
                                          1.240
## X14
         0.8972
                               0.7561
                     1.1146
                                          1.065
## X15
          1.2188
                     0.8205
                               1.0203
                                          1.456
## X16
          0.9692
                     1.0318
                               0.8137
                                          1.154
## X17
          1.8712
                     0.5344
                               1.5735
                                          2.225
## X18
          1.8031
                     0.5546
                               1.5137
                                          2.148
## X19
          0.9303
                     1.0750
                               0.7792
                                          1.111
## X20
                               0.9768
          1.1589
                     0.8629
                                          1.375
##
## Concordance= 0.676 (se = 0.01)
## Likelihood ratio test= 281.2 on 20 df,
                                             p = < 2e - 16
## Wald test
                        = 284.6 on 20 df,
                                             p=<2e-16
## Score (logrank) test = 287.7 on 20 df,
                                             p=<2e-16
# Perform survival analysis using glmnet
# Perform survival analysis using glmnet
# assuming the predictors are in the first p columns and the response is in the last two columns
p <- ncol(data) - 2
xmatrix=as.matrix(data[,1:p])
show_fit=glmnet(xmatrix,Surv(data$y, data$failed),standardize=TRUE,lambda=seq(0,0.25,.001),alpha=1,fami
#print(show_fit)
plot(show_fit, label=TRUE)
```

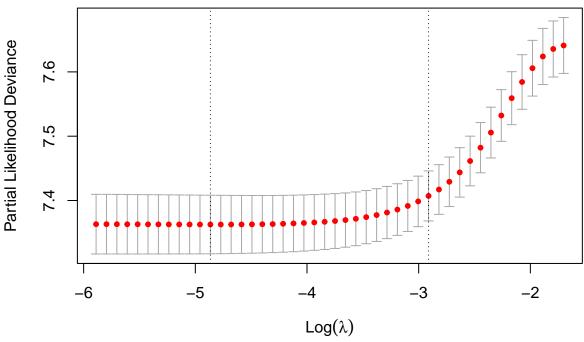
## Warning in regularize.values(x, y, ties, missing(ties), na.rm = na.rm):



the Lasso proportional hazards model correctly select the 10 significant predictors using the partial likelihood deviance metric? Comment.

# #show the use of the CV metric "Partial Likelihood Deviance" surv\_model <- cv.glmnet(xmatrix,Surv(data\$y, data\$failed), family = "cox", type.measure = "deviance",alplot(surv\_model)</pre>

# 20 20 20 19 18 17 16 14 14 12 10 9 9 8 4 0



```
print(surv_model)
##
## Call: cv.glmnet(x = xmatrix, y = Surv(data$y, data$failed), type.measure = "deviance",
                                                                                                   nfolds
## Measure: Partial Likelihood Deviance
##
##
        Lambda Index Measure
                                  SE Nonzero
## min 0.00771
                  35
                       7.363 0.0455
## 1se 0.05440
                  14
                       7.407 0.0389
                                          10
# Extract the optimal lambda value at lambda.1se
lambda_opt <- surv_model$lambda.1se</pre>
# Fit the model using the optimal lambda value
fit <- glmnet(xmatrix,Surv(data$y, data$failed), family = "cox", type.measure = "deviance",alpha=1,lamb</pre>
coef(fit)
## 20 x 1 sparse Matrix of class "dgCMatrix"
##
## X1
## X2
       0.121750947
```

0.362140703

0.294950075

## X7 0.192964532

## X3 ## X4 ## X5

## X6

All the 10 significant predictors were selected by using partial likelihood deviance without penalizing any coefficient to 0.

c. What is the C-index for the optimal lambda chosen to be Lambda.1se using the partial likelihood deviance metric?

```
# Make predictions
predictions <- predict(fit, newx = xmatrix[,1:p], type = "response")

# Evaluate the model performance using concordance index (c-index)
c_index <- Cindex(predictions,Surv(data$y, data$failed))
c_index</pre>
```

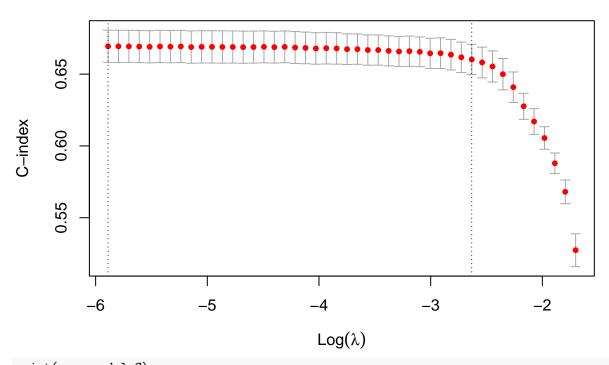
## ## [1] 0.6697602

The C-index using likelihood deviance metric is 0.6697602

d. Did the Lasso proportional hazards model correctly select the 10 significant predictors using Cross Validation with the C-index metric? Comment.

```
#show the use of CV metric "C"
surv_model_C = cv.glmnet(xmatrix,Surv(data$y, data$failed), family = "cox", type.measure = "C", alpha=1
plot(surv_model_C)
```

# 20 20 20 19 18 17 16 14 14 12 10 9 9 8 4 0



```
print(surv_model_C)
```

## X7

## X9

0.13685449

## X8 0.15623710

## X10 0.30678742 ## X11 0.18229053

```
##
## Call: cv.glmnet(x = xmatrix, y = Surv(data$y, data$failed), type.measure = "C",
                                                                                            nfolds = 10, f
##
## Measure: C-index
##
        Lambda Index Measure
##
                                   SE Nonzero
## min 0.00277
                  46 0.6694 0.01120
                                           20
## 1se 0.07191
                  11 0.6602 0.01054
# Extract the optimal lambda value at lambda.1se
lambda_opt <- surv_model_C$lambda.1se</pre>
# Fit the model using the optimal lambda value
fit_C <- glmnet(xmatrix,Surv(data$y, data$failed), family = "cox", type.measure = "C",alpha=1,lambda = "</pre>
coef(fit_C)
## 20 x 1 sparse Matrix of class "dgCMatrix"
##
               s0
## X1
## X2 0.06869792
## X3 0.29469540
## X4
## X5
       0.22618656
## X6
```

```
## X12 .
## X13 .
## X14 .
## X15 .
## X16 .
## X17 0.35684786
## X18 0.27916891
## X19 .
## X20 .
```

Using CV all 10 significant predictors were selected without penalizing any coefficient to 0.

e. What is the C-index for the optimal lambda chosen to be Lambda.1se using the C-index metric?

```
# Make predictions
predictions <- predict(fit_C, newx = xmatrix[,1:p], type = "response")
# Evaluate the model performance using concordance index (c-index)
c_index <- Cindex(predictions,Surv(data$y, data$failed))
c_index</pre>
```

### ## [1] 0.6673913

The C-index using C-index metric is 0.6673913

f. Comment using just 1 sentence on the size of the correlations between pairs of the predictors.

Correlation between the pairs of predictors is small as its smaller than 1 and not very different than 0.6

detach(data)
##-----##