## assignment9

## 2023-04-14

#HW09 #Use the R programs covered in the MultipleTesting module as a guide for HW09.

#Perform a multiple regression on all 100 predictors from the meatspec dataset in the #faraway package and extract the p-values for the coefficients of the 100 variables.

```
library(faraway)
data(meatspec,package="faraway") #the dataset meatspec is found in the faraway package
lmod=lm(fat ~ . , data=meatspec)
summary(lmod)
##
## Call:
   lm(formula = fat ~ ., data = meatspec)
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
## -2.9833 -0.4982 0.0135
                            0.4864
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                    7.302
                                1.876
                                        3.892 0.000168 ***
##
  (Intercept)
                10898.047
                             3003.614
## V1
                                        3.628 0.000428 ***
## V2
               -12174.864
                             5520.233
                                       -2.205 0.029426
## V3
                             8868.517
                -5953.285
                                       -0.671 0.503398
## V4
                23229.862
                            15426.530
                                        1.506 0.134875
## V5
               -28386.219
                            19758.501
                                       -1.437 0.153554
## V6
                12748.270
                            17381.421
                                        0.733 0.464794
## V7
               -11422.335
                            11454.169
                                       -0.997 0.320769
## V8
                 7102.332
                             7123.935
                                        0.997 0.320892
## V9
                  783.655
                             5228.808
                                        0.150 0.881130
## V10
                 3512.239
                             6787.803
                                        0.517 0.605856
## V11
               -10547.574
                            10580.407
                                       -0.997 0.320926
                34638.288
## V12
                            18344.772
                                        1.888 0.061543 .
## V13
               -38705.447
                            23098.395
                                       -1.676 0.096542
## V14
                            19952.355
                                        1.448 0.150293
                28895.947
## V15
               -13726.347
                            13312.307
                                       -1.031 0.304676
## V16
                -7062.769
                             8172.878
                                       -0.864 0.389308
## V17
                 2571.597
                             6279.661
                                        0.410 0.682932
                 5263.427
                                        0.851 0.396432
## V18
                             6183.397
## V19
                 8860.827
                             8925.154
                                        0.993 0.322914
## V20
               -12149.937
                            15184.189
                                       -0.800 0.425276
## V21
               -19284.872
                            20536.132
                                       -0.939 0.349680
```

36626.953

22847.592

## V22

1.603 0.111680

```
## V23
                -11165.390
                            19302.712
                                        -0.578 0.564111
## V24
                -15008.939
                            13616.072
                                        -1.102 0.272655
                 16698.992
                             8582.462
## V25
                                         1.946 0.054151
## V26
                 -4891.852
                             5901.456
                                        -0.829 0.408880
## V27
                 -6334.752
                             6072.685
                                        -1.043 0.299084
## V28
                 24043.786
                             8144.906
                                         2.952 0.003834 **
## V29
                -39940.900
                            12335.575
                                        -3.238 0.001578 **
## V30
                 33309.092
                            17674.622
                                         1.885 0.062034
## V31
                -23174.509
                            20974.708
                                        -1.105 0.271539
## V32
                 18764.305
                            18959.821
                                         0.990 0.324423
## V33
                 -3747.892
                            13458.994
                                        -0.278 0.781158
## V34
                 -6671.747
                             9353.448
                                        -0.713 0.477122
## V35
                 -5318.549
                             7534.861
                                        -0.706 0.481716
## V36
                 10488.898
                             5773.159
                                         1.817 0.071869 .
## V37
                                        -1.427 0.156202
                 -8410.539
                             5892.265
## V38
                  -408.228
                             7970.269
                                        -0.051 0.959241
## V39
                            11338.219
                                         1.748 0.083206 .
                 19815.971
## V40
                -23690.179
                            15971.026
                                        -1.483 0.140748
## V41
                 29398.659
                            19340.032
                                         1.520 0.131256
## V42
                -32055.252
                            20639.448
                                        -1.553 0.123170
## V43
                11826.000
                            17491.895
                                         0.676 0.500356
## V44
                                        -0.874 0.383969
                 -9994.257
                            11435.392
## V45
                 23017.798
                             8927.175
                                         2.578 0.011200 *
## V46
                 -9041.633
                             6218.630
                                        -1.454 0.148705
## V47
                 -4846.799
                             3520.124
                                        -1.377 0.171246
## V48
                  1536.042
                             4401.789
                                         0.349 0.727764
## V49
                  2188.418
                             7363.225
                                         0.297 0.766848
## V50
                -13170.870
                             9829.843
                                        -1.340 0.182947
## V51
                 26420.737
                            13371.372
                                         1.976 0.050580 .
## V52
                -23565.834
                            16339.395
                                        -1.442 0.151968
## V53
                 -2005.210
                            16742.496
                                        -0.120 0.904878
## V54
                 30327.413
                            14023.378
                                         2.163 0.032658 *
## V55
                -31802.344
                            10650.780
                                        -2.986 0.003461 **
## V56
                 12428.271
                             6395.916
                                         1.943 0.054463
## V57
                  -102.107
                             4676.993
                                        -0.022 0.982620
## V58
                   210.251
                             4388.133
                                         0.048 0.961869
## V59
                 -7679.011
                             4511.526
                                        -1.702 0.091465 .
## V60
                 11590.949
                             3967.244
                                         2.922 0.004199 **
                 -6559.639
                                        -1.746 0.083485
## V61
                             3756.703
## V62
                  2533.819
                             3939.248
                                         0.643 0.521370
## V63
                 11950.924
                             5296.267
                                         2.256 0.025947 *
## V64
                -18515.851
                             7070.171
                                        -2.619 0.010021 *
## V65
                  4051.697
                             8539.248
                                         0.474 0.636066
## V66
                             9691.472
                                         0.023 0.981694
                   222.861
## V67
                 10439.030
                            10111.231
                                         1.032 0.304061
## V68
                -22570.742
                             9493.417
                                        -2.378 0.019094 *
## V69
                 17285.149
                             8168.742
                                         2.116 0.036520 *
## V70
                   -45.036
                             7357.838
                                        -0.006 0.995127
## V71
                 -8134.714
                             6796.093
                                        -1.197 0.233802
## V72
                 -1768.780
                             6344.295
                                        -0.279 0.780905
## V73
                 15744.948
                             5531.706
                                         2.846 0.005246 **
## V74
                -11219.545
                             5666.910
                                        -1.980 0.050132 .
## V75
                  5289.427
                             5067.718
                                         1.044 0.298810
## V76
                 -2454.612
                             4760.274
                                       -0.516 0.607101
```

```
## V77
                  740.608
                             4922.688
                                        0.150 0.880677
                -5730.806
                             5518.607
                                       -1.038 0.301257
## V78
## V79
                12166.493
                             6026.835
                                        2.019 0.045863 *
## V80
               -22688.979
                             7023.823
                                       -3.230 0.001616 **
## V81
                14991.763
                             8595.338
                                        1.744 0.083824
## V82
                             9984.910
                                        0.334 0.739264
                 3331.367
## V83
                -6651.082
                            11358.746
                                       -0.586 0.559337
## V84
                -6752.949
                            12405.922
                                       -0.544 0.587276
## V85
                16271.066
                            12434.546
                                        1.309 0.193323
## V86
                 5512.031
                            13689.180
                                        0.403 0.687955
## V87
               -21092.220
                            15770.171
                                       -1.337 0.183730
## V88
                 9657.690
                            15143.593
                                        0.638 0.524921
## V89
                  273.586
                            13103.448
                                        0.021 0.983379
                                       -0.394 0.694180
## V90
                -5489.915
                            13927.199
## V91
                 2891.941
                            15479.740
                                        0.187 0.852133
## V92
                10160.850
                            14407.777
                                        0.705 0.482103
## V93
                -3183.235
                            11882.686
                                       -0.268 0.789269
## V94
                -7330.650
                            10959.287
                                       -0.669 0.504913
## V95
                 5551.521
                             9450.485
                                        0.587 0.558075
## V96
                -3320.415
                             8349.562
                                       -0.398 0.691613
## V97
                -2512.787
                             7974.922
                                       -0.315 0.753272
## V98
                -5979.563
                             7355.289
                                       -0.813 0.417935
                                        1.047 0.297336
## V99
                 8283.253
                             7911.765
                 -101.926
                             3591.166
## V100
                                       -0.028 0.977407
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.22 on 114 degrees of freedom
## Multiple R-squared: 0.9951, Adjusted R-squared: 0.9908
## F-statistic:
                  232 on 100 and 114 DF, p-value: < 2.2e-16
```

## # Extract p-values for coefficients and exluding the intercept p\_values <- summary(lmod)\$coefficients[-1, 4]</pre>

## p\_values

```
V4
                                                                                     V6
              V1
                            V2
                                          ٧3
                                                                       V5
## 0.0004283297 0.0294256650 0.5033981889 0.1348745281 0.1535538037 0.4647943207
              V7
                            ٧8
                                          V9
                                                       V10
                                                                      V11
                                                                                    V12
  0.3207693528 0.3208916975 0.8811299832 0.6058559085 0.3209258938 0.0615433570
##
##
             V13
                           V14
                                         V15
                                                       V16
                                                                      V17
                                                                                    V18
  0.0965422164 0.1502926730 0.3046755629 0.3893083081 0.6829323019 0.3964319860
             V19
                           V20
                                         V21
                                                       V22
                                                                      V23
                                                                                    V24
##
## 0.3229136323 0.4252764439 0.3496800608 0.1116799533 0.5641105785 0.2726547758
             V25
                           V26
                                         V27
                                                       V28
                                                                      V29
                                                                                    V30
  0.0541511081 0.4088802236 0.2990835887 0.0038340431 0.0015775341 0.0620343696
                           V32
##
             V31
                                         V33
                                                       V34
                                                                      V35
                                                                                    V36
   0.2715386246 \ 0.3244226674 \ 0.7811579873 \ 0.4771222175 \ 0.4817158475 \ 0.0718690219
##
             V37
                           V38
                                         V39
                                                       V40
                                                                      V41
                                                                                    V42
  0.1562020058 0.9592407305 0.0832059828 0.1407482329 0.1312561915 0.1231696311
##
             V43
                           V44
                                         V45
                                                       V46
                                                                      V47
                                                                                    V48
  0.5003562519 \ \ 0.3839687639 \ \ 0.0111996624 \ \ 0.1487052405 \ \ 0.1712463541 \ \ 0.7277641070
##
             V49
                           V50
                                         V51
                                                       V52
                                                                      V53
                                                                                    V54
```

```
## 0.7668477428 0.1829470928 0.0505798445 0.1519677289 0.9048779908 0.0326584621
##
            V55
                         V56
                                       V57
                                                     V58
                                                                  V59
                                                                               V60
## 0.0034611034 0.0544625942 0.9826203770 0.9618689776 0.0914645627 0.0041986807
                         V62
                                       V63
                                                    V64
                                                                  V65
## 0.0834846286 0.5213704458 0.0259469095 0.0100214548 0.6360656884 0.9816939643
                         V68
                                       V69
                                                    V70
##
            V67
                                                                  V71
## 0.3040610504 0.0190942824 0.0365201162 0.9951269670 0.2338017348 0.7809045001
##
            V73
                         V74
                                       V75
                                                     V76
                                                                  V77
## 0.0052463432 0.0501317942 0.2988096151 0.6071008125 0.8806771054 0.3012574109
##
            V79
                         V80
                                       V81
                                                     V82
                                                                  V83
                                                                                V84
## 0.0458632490 0.0016162837 0.0838241617 0.7392639838 0.5593371748 0.5872756605
            V85
                         V86
                                                     V88
                                                                  V89
                                                                               V90
                                       V87
## 0.1933231459 0.6879553379 0.1837297663 0.5249211429 0.9833787242 0.6941796989
            V91
                         V92
                                       V93
                                                    V94
                                                                  V95
                                                                               V96
## 0.8521330321 0.4821032694 0.7892692561 0.5049125530 0.5580750742 0.6916131495
##
            V97
                         V98
                                       V99
                                                   V100
## 0.7532723377 0.4179350446 0.2973355717 0.9774068543
#Use the p-values vector to list the variables with coefficients that are significantly
#different from O with
#a) using no FWER adjustment (alpha=.05 for each test of hypothesis).
alpha <- 0.05
print(p_values[p_values < alpha])</pre>
                                       V28
                                                     V29
                                                                  V45
                                                                               V54
##
             V1
                           ۷2
## 0.0004283297 0.0294256650 0.0038340431 0.0015775341 0.0111996624 0.0326584621
            V55
                         V60
                                       V63
                                                    V64
                                                                  V68
## 0.0034611034 0.0041986807 0.0259469095 0.0100214548 0.0190942824 0.0365201162
##
            V73
                         V79
                                       VRO
## 0.0052463432 0.0458632490 0.0016162837
names(p_values[p_values < alpha])</pre>
## [1] "V1" "V2" "V28" "V29" "V45" "V54" "V55" "V60" "V63" "V64" "V68" "V69"
## [13] "V73" "V79" "V80"
# We reject these 15 features based on the p values
#b) using the Bonferroni procedure to control the FWER alpha at 0.05.
#Get adjusted p value
p_values_bonfadjust <- p.adjust(p_values, method = "bonferroni")</pre>
# Identify variables with significant coefficients
adj_bonferroni <- p_values_bonfadjust[p_values_bonfadjust < alpha]</pre>
adj_bonferroni
           V1
```

## 0.04283297

```
names(adj_bonferroni)

## [1] "V1"

# We reject only V1 based on the Bonferroni procedure

#c) using the Holm procedure to control the FWER alpha at 0.05.

# Get the adjusted p-val
p_values_holmadjust <- p.adjust(p_values, method = "holm")

# Identify variables with significant coefficients
adj_holm <- p_values_holmadjust[p_values_holmadjust < alpha]
adj_holm

## V1
## 0.04283297

names(adj_holm)

## [1] "V1"

#We again reject only V1 based on Holm procedure as well</pre>
```