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# Rainbows and Uniform Spaces

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## I. INTRODUCTION

Scientific progress depends on the proper evaluation of evidence from data. The evaluation process usually starts by visualizing data produced from an experiment or procedure. For example, a radiologist determines the type and severity of a bone fracture by looking at an image representation of x-ray data. Visual variables are characteristics of a data visualization graphic, such as the height of a bar on a bar chart [1]–[3]. Color is one of the more complicated visual variables. A common way to represent data with color is by using a colormap.

A colormap is a function that assigns data points to an ordering of colors known as a color scheme. Some call colormaps an interface between the data and your brain [4]. A scientist interested in visualizing a data set must choose a colormap that reflects the nature of the data. At their best, colormaps reveal hidden structure that would go unnoticed otherwise. At their worst, they distort the perception of the data and cause viewers to misinterpret the data. This can have serious consequences. Doctors must interpret medical data correctly to give a proper diagnosis and treatment. Politicians use data to design public policies. Business executives make decisions with financial consequences using data, often presented through a visualization. Plenty of research on colormaps and their applications, there are serious debates in the data visualization community about the use of spectral, or rainbow color schemes.

Despite visually distorting the data, many scientists prefer a rainbow color scheme for its aesthetic appeal and historical use in scientific publications. This literature review explores the advantages and disadvantages of rainbow colormaps, why they are preferred by some scientists and discouraged by others, and how spectral color schemes are used in applied data analysis. First, this review gives a basic summary of the color theoretic properties of rainbow colormaps. Then, it will address color perception issues of spectral color schemes, including color vision impairment. Finally, rainbow colormap

applications are discussed in medical imaging, cartography, and business analytics.

## II. COLOR THEORY AND COLORMAPS

Colormaps have a variety of properties that make them unique and potentially useful. However, there is controversy among scientists and visualization experts over certain properties of the rainbow colormap. First, the rainbow gradient is not a perceptually consistent ordering of colors. Similarly, it is not perceptually uniform as the variation in lightness is inconsistent. Finally, the rainbow colormap traverses through many highly saturated colors in color space.

## A. A Brief History of Color Theory Development

The first issue with color is that there is no natural ordering of the colors from least to greatest. Some might argue that there is a natural ordering—the brain's interpretation of the electromagnetic spectrum. Based on light wave frequency, this color ordering is rainbow-like with respect to the color hues [5]. It starts with red and on to orange, yellow, green, blue, and so forth. This is the foundation for the rainbow colormap. It was especially popular among physicists and soon grew to become the default in many scientific software applications [6], [7]. However, this colormap was not created for data representation. It was designed based on accurately representing light waves, not data.

A scientist interested in visualizing a data set must choose a colormap that reflects the nature of the data, if she is to produce a truthful representation of the data. There are several color schemes and combinations of color schemes [3]. However, there are three main types of color schemes that define a colormap. Sequential color schemes vary in lightness but do not vary in hue. If two sequential color schemes have different hues and are connected at their lightest ends, it is called a diverging color scheme. Qualitative color schemes vary in hues with little variation in lightness and saturation [5]. After the scientist has determined the right color scheme for her data, she can use a colormap to plot the data set in color. The images in Fig. 2 are examples of image data plotted using sequential, diverging, and rainbow colormaps.



Fig. 1. An image of a calf. This and corresponding images were created by the author.







Fig. 2. The calf image plotted with a sequential, diverging, and rainbow colormap.

One advantage of the rainbow colormap is that it is easy to implement because it is based on an older, simpler color model. Scientists use color models to understand and work with color. These models are abstract mathematical representations that describe a color as a collection of numbers that describe physical or perceptual characteristics. These models have evolved to describe color specification systems, color distance, and color appearance in different viewing conditions [8]. When a color model is used to produce color on a specific medium, the resulting set of colors is called a color space. For example, the RGB model describes color as the combination of red, green, and blue light. A computer screen renders color using the RGB model, thus the color produced by digital screens with the RGB model is a color space. Another example is the CMYK model, which describes color as combinations of cyan, magenta, yellow, and black. Printers produce colors using this model. [?], [5]. The combination of cyan, magenta, yellow, and black ink on a printer constitutes a color space. The selection and modification of color models and spaces happens before colormaps or data visualizations can be created.

Most color spaces produce a similar set of colors. However, there are some colors that do not translate well between color spaces. For example, consider the image shown below. If you are reading this as a digital document, the colors will look different than the colors on a printed copy of the same document. This represents a transformation from an RGB color space to a CMYK color space [9]. Color is lost in translation. This is the motivation for developing perceptually uniform color models, as in the CIECAM02-UCS color model. Good models of color distance may not preserve absolute color, but perceived color difference tends to remain the same across all media [8]. Perceptually uniform colormaps can be produced using these models [4]. In general, rainbow colormaps are not perceptually uniform because the lightness is not consistent.

This has not stopped some from attempting to modify—and therefore preserve—the rainbow colormap. The adjustments refer to the Munsell color specification system, which describes color with hue, saturation, and lightness. This system divides up the colors humans are capable of perceiving into equal perceptual divisions of color lightness and color saturation for each color hue. [5] Hue refers to the attribute generally associated with the color name (i.e. red, orange, yellow, green, blue). On a color wheel, hue is the position of the color on the color wheel. Saturation is the intensity of the hue. In physical terms, it is the purity of the light wave frequency. Lightness is the amount of light emitted by a color. Low lightness results in a darker color; high lightness results in a lighter color. [3]. Sisneros et al created a colormap

modification framework that smooths the variation in luminance (or lightness) and chromaticity, which is a combination of saturation and hue. Their method can be applied to any perceptually non-uniform colormap. However, their focus was on improving the rainbow colormap, since it is still widely used in science. Their improved rainbow colormap contains subdued colors that better represented image data [10].

Colors rendered in a color space are light waves—the physical representation of color. These light waves are interpreted by our brain when the light hits our eyes [4]. These light waves enter the human eye where they hit the retina. The retina has two kinds of light receptors, called rods and cones. Cones are more concentrated near the fovea centralis, the main focus point of our eyes [?]. The cones capture red, green, or blue light depending on the characteristics of each cone. Rods do not interpret color [5].

What are the criteria for evaluating a colormap? Several authors have created methods to evaluate color choice. In one paper, color schemes are evaluated by three variables of the CIELUV color model. The first is color distance. The CIELUV model is designed to measure distance between colors. If the distances are equally spaced, thats a good thing. Linear separation is the second variable. It refers to the ability to separate targets from non-targets in the colour model being used. For example, suppose a doctor wants to identify a tumor and uses a colormap to display the data. If the colors are not linearly sepparable in the color model, it will be more difficult to identify the tumor even if the colors are mathematically different. The third variable is color category. This refers to color regions in which there are both target and nontarget elements [2]. These characteristics do not account for multidimensional data projected into two-dimensional space. CheckViz attempts to account for this problem by using a perceptually uniform color coding so that distortions such as those described above are accounted for when scientists want to visualize multidimensional data [11]. The specific criteria of the color model and color space must reflect the attributes of the colormap.

Sometimes, when color encodings are converted to grayscale, it can alter the perception of the data. There are many algorithms to cast a color encoding to grayscale.

# B. Rainbow Colormaps

There are multiple advantages to using rainbow colormaps. For one, it is clear that users tend to prefer it over other colormaps for its aesthetic appeal [12]–[14]. The varietyin hue also can accentuate relationships in the data than a sequential, single-hue colormap. History is an advantage.

However, the advantages can also be disadvantages. When accentuating relationships, a human interpreter might see signal where there is none. This seems to be what happens when the data lie in certain regions (as in between blue green and yellow) [2].

Readers of scientific literature will recognize the rainbow colormap. It appears often in scientific publications and has broad appeal in the scientific community [?], [6], [12], [14]. Historically, rainbow colormaps like MATLABs jet have been the default colormaps used in data-handling software [7]. Despite its prevalence, many scientists oppose rainbow-gradient representations of data [4], [6], [14], [15]. In one study, medical students were asked to identify risk factors for heart disease in visualizations of artery data. On average, the participants using rainbow-colored visualizations took more time and made more errors than participants using divergence-colored visualizations. Furthermore, the participants thought they did well using the rainbow color map even when in reality they did not perform as well as the participants who used the diverging color map [15]. This compelling evidence suggests that the rainbow colormap is clearly inferior to other colormaps.

Others disagree. They claim that users have learned to read data with the rainbow colormap and prefer its aesthetic appeal [12], [13]. One experiment tested data interpretation accuracy under diverging, sequential, and spectral (rainbow) color schemes. Of 63 subjects who evaluated spectral and sequential schemes, 56 percent selected spectral as the best...We had expected the spectral scheme to interfere with map-reading accuracy and with understanding map patterns, but this did not occur, Brewer writes. Our subjects preferred the spectral scheme and performed well with it [12]. While the rainbow colormap did not outperform other colormaps, it appears to do no harm. Users can accurately interpret rainbow-colored data visualizations.

## III. COLOR PERCEPTION AND COLOR VISION IMPAIRMENT

One of the advantages of using perceptually uniform colormaps is that they show the data accurately even if the colors do not appear the same. Color perception can change for a number of reasons. When colors are placed near each other, it changes the way our eyes see that color. The brain adjusts the amount of light that enters the eyes based on external conditions. For example, colors appear more bright under diffused light. Competing bright colors also diminishes the overall perception of their brightness.

Mark Rothko and Josef Albers are notable artists who explored the human relationship with color perception. Some colors blend together while others almost appear to be in conflict with each other, causing a perceived vibration in the colors.

Another example of color perception under different conditions is the color-of-the-dress meme that became popular in 2015. The picture was sent on social media sites asking whether the dress was black and blue or white and gold. This effect happens because our eyes perform a kind of normalization under different light conditions. This adjustment alters the perception of what the colors look like. Other examples from psychology place the same color in two images with different colors surrounding the color being studied. Even though the colors are the same, they appear to be different because of the context that they are in. This means that sometimes we see color differences even when there are none.

Other times, color differences can't be detected easily or at all. This is especially common among people who have some form of color vision impairment, as in colorblindness. The

estimated colorblind population is somewhere around 5-8% and affects mostly males of European descent.

Colorblindness results in colors falling on confusion lines—lines in which it is difficult or impossible to distinguish between two colors. People with full color vision also have confusion lines and so in some sense are colorblind because we can't see the entire spectrum of light as colors. However, color deficient viewers are special in that they do not see the normal range of colors as their peers. There are multiple kinds of colorblindness. Full color deficiency results in black and white vision and is very rare. The most common form of color deficiency results in confusing shades of red and green. An example of a map colored with bright orange and green and what a deutoronome would see is given in Figure 3.

For these genetic color deficiencies, it seems reasonable to design data visualizations with colorblindness in mind. Unfortunately for the rainbow colormap, the colors that a colorblind user sees are not the same as those seen by a person with full color vision. Especially for high values, which are displayed in reds, the variation in green is not easy to interpret for colorblind viewers. In fact, though they are aesthetically pleasing, people are slower at interpreting data with large variations in color and make more errors. Yet, colorblind people still seem to get by fine.

Color deficient viewers use clues to distinguish between colors that easily confuse them. Brewer has conducted extensive research into how color deficient viewers interpret color-encoded information. She has suggested several ways in which maps and information visualizations can be designed to help color deficient viewers. A common theme in her research, as well as others, is that colormaps are greatly improved when the dark-to-light variation is controlled and used to show progression. This is the idea behind perceptually uniform colormaps. Even when converted to black and white, the visuals still preserve the nature of the data and are easy to interpret.

# IV. APPLICATIONS

Use of color in data visualization extends to multiple industries and disciplines including engineering, med-icine, statistics, computer science, graphic design, and psychology [3]. [arteryvis] [standardizemedimg] [visvars] [mapchoropleth]

# V. CONCLUSION

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