

# **Session 7**

## **Differential privacy**

# Reminder

A function (mechanism)  $F$  satisfies differential privacy if for all neighboring  $x$ ,  $x'$ , and all possible outputs  $S$ ,

$$\frac{P\left(F(x) = S\right)}{P\left(F(x') = S\right)} \leq e^\epsilon$$

# Reminder: Laplace Mechanism

For a function  $f$  with sensitivity  $s$ , define the Laplace mechanism

$$F(x) = f(x) + \text{Laplace} \left( \frac{s}{\epsilon} \right)$$

# Reminder: Sensitivity

A function  $f : \mathcal{D} \rightarrow \mathbb{R}$  has global sensitivity

$$\text{GS } f = \max_{x, x'; d(x, x')=1} |f(x) - f(x')| ,$$

where if  $x'$  is constructed from  $x$  by adding or removing one row, then

$$d(x, x') = 1 .$$

# Reminder: Exponential Mechanism

We have

1. Set  $\mathcal{R}$  of possible outputs
2. Scoring function  $u : \mathcal{D} \times \mathcal{R} \rightarrow \mathbb{R}$  with sensitivity  $\Delta u$
3. Output  $r \in \mathcal{R}$  with probability

$$\propto \exp \left( \frac{\epsilon u(x, r)}{2\Delta u} \right)$$