

Machine Learning Final Exam

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1 In a galaxy far, far away

1.1

The variance of the red-shifts in the spectroscopic training data was calculated to be:

$$0.0106$$

(where from now on, unless specified, values are shown to 3 significant places).

The MSE on the test SDSS predictions was calculated to be:

$$0.000812$$

This shows that the predictions were quite accurate.

1.2

The linear regression was done in Python, using the `sklearn` linear regression package. This performs an ordinary least squares linear regression. The error function is a Mean Squared Error.

The parameters of the model were (taken from the announcement):

$$\begin{aligned} &[0.0185134, 0.0479647, -0.0210943, -0.0274002, \\ &-0.0226798, 0.0064449, 0.0151842, 0.0120738, \\ &0.0103486, 0.00599684, -0.0294513, 0.069059, \\ &0.00630583, -0.00472042, -0.00873932, 0.00311043, \\ &0.0017252, 0.00435176] \end{aligned}$$

*** CHECK AND MAYBE PLUG THESE INTO THE MODEL ***

with bias term:

$$-0.801881$$

The error on the training data was calculated to be 0.00187, and on the test data was 0.00187 also. The errors normalised by the variance, σ_{red}^2 were equal to 0.176 for both the test and the training data.

This normalised error falling below one signifies that...

1.3

For the non-linear regression, I chose to apply the K-nearest neighbours (KNN) algorithm. I chose this method for its simplicity (following Occam's razor), and therefore its intuitive understanding. The simplicity of the algorithm is also reflected in the single hyperparameter, k (if you consider a fixed distance metric), which means that there is less computation in tuning the hyperparameter.

I utilised the `neighbours` library from the `sklearn` package.

The KNN algorithm uses a distance metric to calculate the distance between a (set of) training point(s) and the other points. I used the Euclidian distance, given by $\|\mathbf{x} - \mathbf{x}'\|$, or $\sqrt{\mathbf{x}^T \mathbf{x}'}$. The algorithm works by calculating the distances from a test point to the other points, and then finding the nearest K points to that point. In a regression task, the test point is assigned the value of the mean of the nearest K neighbours.

My method involved using model selection methods such as cross-validation and grid search. Since this is model selection, cross validation was needed as we only use the training data during model selection. This gave us a better way to prevent overfitting of the training data. I used the `GridSearchCV` package from `sklearn`. The range of possible k values was given as the odd numbers between 1 and 29. This performed a 5-fold cross validation on each of the possible values of k , averaging out the resulting error (i.e. splitting the data into 5 equal chunks, using 4 as the training set, and 1 as the validation set, and then cycling through all possible 5 validation sets). The error function used in the algorithm was the mean squared error.

This method resulted in the optimum hyperparameter as $k = 7$, with a MSE of 0.00118 on the test data, and a MSE of 0.000870.

Clearly, the KNN Regressor worked better on the training data, which is to be expected due to the model's simplicity in using the k training points' average to return the regression results - therefore the training points are bound to have a low MSE. In comparison, the training data in the linear regressor performed the same as the test data. The difference in this would be due to the nature of a linear regressor, which would 'average out' the regression line over the points, thus leading to a small MSE on both the training and test data. On the test data, the KNN Regressor did perform a bit better than the linear regressor - perhaps due to the non-linear nature of KNN capturing the underlying nature of the data slightly more accurately. Overall, I believe the

KNN method worked well as we had a relatively low variance on the data - KNN can be skewed by big outliers in the data. The cross-validation helped to prevent overfitting on the data, which may have also caused the error on the test data to drop in comparison to the linear regressor.

2 Weed

2.1

The logistic regression was done in python, using the `LogisticRegression` package from `sklearn`. This implementation uses the logistic function. We are trying to classify testing points according to binary labels (0 - weeds, 1 - crops). The algorithm tries to minimise the following function:

$$\min_{w,c} \frac{1}{2} w^T w + C \sum_{i=1}^n \log e^{(-y_i(X_i^T w + c)) + 1)}$$

It also uses a coordinate descent algorithm, which is a derivative-free optimization algorithm that performs a line search in one coordinate direction for the current point in each iteration. (Wikipedia, The Free Encyclopedia, 2016)

The parameters produced by the model were:

$$\begin{aligned} &[-0.0391283, 0.01549887, 0.00295803, 0.00033714, \\ &-0.00039954, 0.00348062, -0.00715483, 0.00473467, \\ &-0.02685346, -0.05592747, -0.04317431, 0.00579407, \\ &-0.00998736] \end{aligned}$$

with bias term:

$$-1.47771341e - 05$$

The zero-one loss on the training data was: 0.0200, and on the test data: 0.0348.