



## CHANGE POINT DETECTION IN END-TO-END MEASUREMENTS TIME SERIES

Diego Ximenes Mendes

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Orientador: Edmundo Albuquerque de Souza  
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Diego Ximenes Mendes

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Diego Ximenes Mendes

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Advisor: Edmundo Albuquerque de Souza e Silva

Department: Systems Engineering and Computer Science

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# Chapter 1

## Introduction

### 1.1 Contributions

### 1.2 Dissertation Outline

# Chapter 2

## Change Point Detection

A change point detection algorithm is concerned to identify points in time where the statistical properties of a time series have changed. This problem have a broad application in different knowledge fields, and in general, the algorithms performance are closely related with the input characteristics. Also, if the latent information of the procedures that generated a time series is missing, the target statistical properties can be considered subjective, bringing difficulties not only in the detection phase but also in the problem formalization.

In this context this chapter specifies the problem and briefly discusses several change point detection algorithms. The literature of this area is extensive, and it is common to find methods that presents a poor performance due to a variety of reasons, such as they are too specific or because the mechanisms were only analyzed through theoretical aspects. Therefore, it was chosen a set of methods that can provide a good practical and theoretical perspective, and also flexibility to insert adaptations that can better handle some input peculiarities. Furthermore, through this chapter is exposed several obstacles when dealing with real data, and some adopted solutions which are not described in literature.

### 2.1 Problem Definition

The problem can be categorized in offline or online. In the offline version, to decide if a specific point at time  $t$  is a change point the solver has available the whole time series, including past and future information on  $t$ . In the other hand, in the online version the information is available up to time  $t$ . The choice between these options is defined by the application domain, in some cases data are processed in real time and the change points should be detected as soon as possible, but in others the changes are identified by historical purposes and offline algorithms can be used.

It is intuitive that the offline case is more robust, since there are more information to make a classification. In practice, to increase the statistical confidence of a

decision the online definition is relaxed, and to decide if a point at time  $t$  is a change point it is possible to use data up to a small window in the future of  $t$ , which in real time processing means that the application should wait until more data are available. This trick plays a trade-off between minimizing the time to detect a change and correctly classify a point. Therefore, in some cases, the online version can be transformed in the offline case by only modifying the input availability.

In this work it is considered the following input and change points characteristics, which were defined considering the final application scenario:

- Univariate time series. However, it is possible to extend several methods presented here to deal with multivariate data.
- Unevenly time series, that is, data is not regularly sampled in time.
- Time series with different lengths.
- Unknown number of change points.
- Different number of points between change points.
- Focus on changes in the underlying mean and distribution, disregarding other kinds of changes such as in periodicity.
- Outliers are not considered statistical changes.
- There is no latent information of the time series.
- It is considered the online and offline options.

## 2.2 Notation

An univariate time series composed of  $n$  points is defined by two vectors,  $\mathbf{x} = (x_1, \dots, x_n)$  and  $\mathbf{y} = (y_1, \dots, y_n)$ . The value  $y_i$  indicates the  $i$ -th sampled value and  $x_i$  indicates the associated sample time. It is assumed that the points are sorted by time, that is,  $x_{i-1} < x_i$  for  $i = 2, \dots, n$ . Since unevenly time series is considered,  $x_i - x_{i-1}$  can be different for different  $i$  values. For  $s \geq t$  the following convention is adopted:  $\mathbf{y}_{s:t} = (y_s, \dots, y_t)$ .

The presence of  $k$  change points implies that data is split into  $k + 1$  segments, also called windows. Let  $\tau_i$  indicates the  $i$ -th change point for  $i = 1, \dots, k$ . Also let  $\tau_0 = 0$ ,  $\tau_{k+1} = n$  and  $\boldsymbol{\tau} = (\tau_0, \dots, \tau_{k+1})$ . Then, the  $i$ -th segment is defined by  $\mathbf{y}_{\tau_{i-1}+1:\tau_i}$ , assuming that  $\tau_{i-1} < \tau_i$  for  $i = 1, \dots, k + 1$ .

Through the previous definitions, change point detection algorithms mainly aim to find both  $k$  and  $\boldsymbol{\tau}$ .

## 2.3 Sliding Windows

Sliding windows techniques use two sliding windows over the time series, and reduce the problem of detecting change points to the problem of testing whether data from the segments were generated by different distributions. One approach is to consider a distance metric between two empirical distributions as the base to infer the change points. Letting  $d(\mathbf{a}, \mathbf{b})$  be the distance between two empirical distributions defined by the windows  $\mathbf{a}$  and  $\mathbf{b}$ , and considering windows of length  $m$ , the Algorithm 1 presents a simple sliding windows method.

---

**Algorithm 1** Sliding Windows

---

```

1:  $i \leftarrow 1$ 
2: while  $i + 2m - 1 \leq n$  do
3:   if  $d(\mathbf{y}_{i:i+m-1}, \mathbf{y}_{i+m:i+2m-1}) > \alpha$  then
4:     Report  $i + m - 1$  as a change point
5:      $i \leftarrow i + m$ 
6:   else
7:      $i \leftarrow i + 1$ 
8:   end if
9: end while

```

---

In this method, when the distance between the distributions is above some threshold  $\alpha$  a change point is reported. This is a common approach for an online application, however, it is possible to increase the classification accuracy in offline cases. As an example, the top plot of figure 2.1 presents a simulated time series, the segment  $\mathbf{y}_{1:1000}$  was generated sampling a  $N(1, 0.2)$  distribution, and  $\mathbf{y}_{1001:2000}$  was sampled through  $N(5, 0.2)$ . The distribution of a window was constructed binning the data with bins of size 0.02. The bottom plot of the same figure presents the associated Hellinger distance [1] between two sliding windows, where the point  $(i, H_i)$  represents the distance between the windows  $\mathbf{y}_{i-100:i-1}$  and  $\mathbf{y}_{i:i+99}$ .

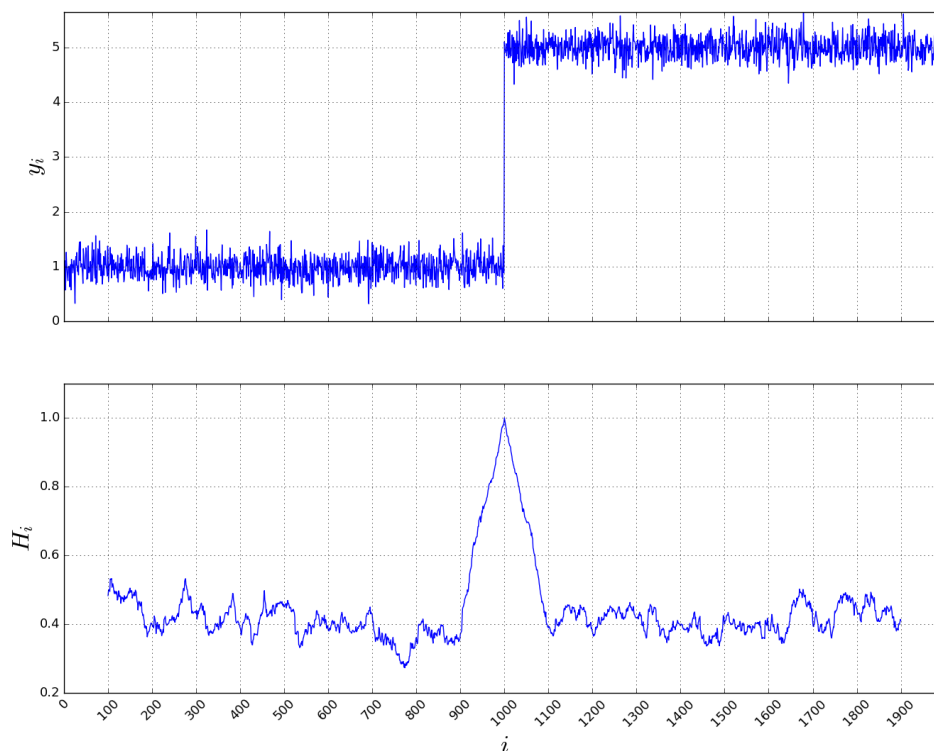


Figure 2.1: Toy example of a sliding windows method.

It can be observed that there is a peak on the distance in the exact location where the distribution changed. However, using only the threshold method it is possible to prematurely infer the position of the change point, therefore, an alternative is to also use a peak detection algorithm. Besides, the distance function choice has a direct impact on the classification accuracy.

As stated in [2], a performance improvement can be achieved concurrently executing the same sliding windows algorithm, however, with different windows lengths, which facilitates the detection of segments with distinct number of points.

## 2.4 Optimization Model

Given a fixed value of  $k$ , one approach is to define a cost function that measures the homogeneity of a window, and therefore, choose the change points that globally optimize this homogeneity. Let the cost of the  $i$ -th segment be defined as  $C(\mathbf{y}_{\tau_{i-1}+1:\tau_i})$ , then the cost of a segmentation is the sum of all segments costs.

A common choice for the function  $C$  is the MSE (Mean Squared Error), which can capture changes in the mean. Another usual approach is to consider distribution changes through negative maximum log-likelihood functions, considering that data within a window is iid.

Therefore, given a fixed  $k$ , the optimal segmentation is obtained through the following optimization problem, which is called the constrained case [3]:

$$\min_{\tau_{1:k}} \sum_{i=1}^{k+1} C(\mathbf{y}_{\tau_{i-1}+1:\tau_i}) \quad (2.1)$$

This problem can be solved using dynamic programming with  $O(kn^2f(n))$  time complexity, where  $f(n)$  is related with  $C$  evaluation. Several segment cost functions can be evaluated in  $O(1)$  after a  $O(n)$  preprocessing phase, implying in an overall  $O(kn^2)$  complexity. It is possible to proof that MSE, negative maximum log-likelihood functions of normal, exponential, poisson and binomial distributions have this characteristic. Also, the formulation can consider a minimum value of a window length.

Modeling segments with continuous distributions can lead to practical difficulties. One of them is the fact that segments can form degenerate distributions, that is, the data of a window can have zero variance, which is always the case of unitary length segments. In these scenarios the negative maximum log-likelihood is undefined. Two approaches can be used to overcome this situation. The first one tries to avoid degenerate segments adding a white noise with small variance to the time series. The second one considers that the cost of any degenerate distribution is equal to a constant.

When the number of change points is unknown an usual way is to introduce a non decreasing penalty function  $g(k)$ . Then, the new optimization problem, called penalized case [3], is:

$$\min_{k, \tau_{1:k}} \sum_{i=1}^{k+1} C(\mathbf{y}_{\tau_{i-1}+1:\tau_i}) + g(k) \quad (2.2)$$

This problem can be solved in  $O(Kn^2f(n))$ . However, if the penalty function is linear in  $k$ , the problem can be formulated more efficiently and solved in  $O(n^2f(n))$ .

Also, there are several pruning algorithms to speedup the computation [3–5], in general trying to reduce the  $\tau$  search space but maintaining optimality.

## 2.5 HMM (Hidden Markov Model)

The idea that each segment is associated with a specific latent configuration has a direct interpretation to a HMM model [6–8]. In this context, each window is related to a hidden state of a HMM, and the observation distribution of this state represents the distribution of that segment. Therefore, the mechanism models the time series using a HMM, and through the hidden state path assesses the times

when a transition between different hidden states occur.

There are several approaches in the detection and training phases. For example, given a trained HMM, is possible to analyze the most probable hidden state path that a time series can follow through the viterbi algorithm. Also, it is possible to evaluate the probability of a transition between different hidden states at time  $t$ , and then apply a threshold and peak detection methods, as well as in sliding windows techniques. For the training step, it is possible to use several time series to train a single HMM, and then use this model to detect change points in all time series. Another way is to, for each time series, train a single model using only the target time series.

It is important to note that the structure of the hidden state graph has a large impact on the performance. Using a fully connected graph, the number of states defines the maximum number of distribution configurations. Employing a left to right structure, the number of hidden states will induce the maximum number of segments.

In [8] is stated that when using a fully connected structure, the time interval that a time series stays in the same hidden state is low, which can not reflect real data. To overcome this problem, [8] suggests to increase the time that a time series stands in the same hidden state, using a dirichlet prior regularization.

## 2.6 Bayesian Inference

There are several Bayesian methods with the objective to assess the probability that a point is a change point. Following an offline fashion, the work of [9] recursively calculates, for each  $i$ , the probability of  $\mathbf{y}_{i:n}$  given a change point at  $i$ . With these probabilities is possible to simulate the time of the first change point, and then, compute the conditional distribution of the time of the second change given the first, and so on. To achieve this, the mechanism assumes that observations are independents, and that each segment is modeled by conjugate priors. Also, the procedure considers priors to model the number of changes and the time between two consecutive change points. The overall complexity of this method is  $O(n^2)$ , considering that the likelihood of a segment can be evaluated in  $O(1)$ .

In [10] it is also considered that parameters of different segments are independents, and that data within a window is iid. However, through an online mode, the procedure is concerned with the estimation of the distribution of the length of the current time since the last change point, called run length, given the data so far observed. To achieve this, the method assumes the probability of current run length given the last run length as a prior. Assuming exponential-family likelihoods to model a segment, the time complexity to process a point is linear in the number

of points already observed.



# Chapter 3

## Dataset

This chapter describes the used datasets, presenting their construction methodology and a brief descriptive analysis.

### 3.1 End-to-End Packet Loss Fraction Time Series Dataset

#### 3.1.1 Methodology

The results presented in this work are collected from cable-television infrastructure running DOCSIS with asymmetric download and upload bandwidths. The measurement infrastructure consists of regular home routers connected to the cable modem that run a software (from TGR, developed in partnership with UFRJ) to measure link throughput, round trip latency, loss rates, among others. Each home router communicates with one or more measurement servers devoted to execute the different measurement protocols and to store data. Measurement values from each home router are consolidated twice per hour and, by the end of every day, they are transferred to a database for analysis. The servers are strategically located by the ISP and, since the same home router can connect to more than one server, metrics from the same client to different servers can be contrasted. The resulted time series are unevenly due to a variate of reasons. One of them is that measurements are initiated only if the residential link is not under use by the ISP customer, another one is that the home router can be without Internet access or even electrical energy.

The focus of this work is to analyze the loss fraction, however, [11] presents a further analysis on other metrics. Round trip packet loss fraction between the home router and the associated server is obtained by sending a train of short UDP packets by the home router and bounced back by the server. The interval between two packets in a train is configurable as well as the length of the train. The data

presented in this work considers a train of 100 UDP packets of 32 bytes in which packets are 1 milliseconds apart.

### 3.1.2 Descriptive Analysis

The TGR software run in a subset of the ISP customers in several brazilian states. In the analysis of this section, was analysed the period from 01 may 2016 to 20 may 2016. Were selected every home router that measured at least one time and that all measures occurred to same server which necessarily belonged to the same ufs. This filter resulted in 1870 clients time series and 1537272 measures.

In figure 3.1 is presented the packet loss CDF of all time series. It is possible to note that 93.2% of the measures have zero losses.

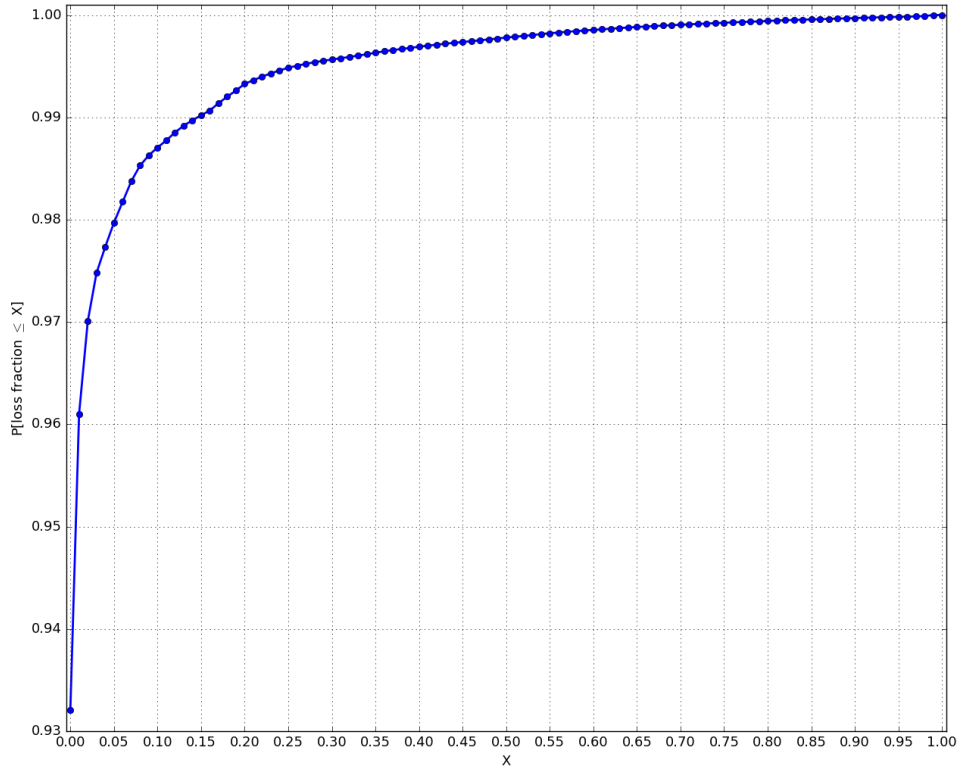
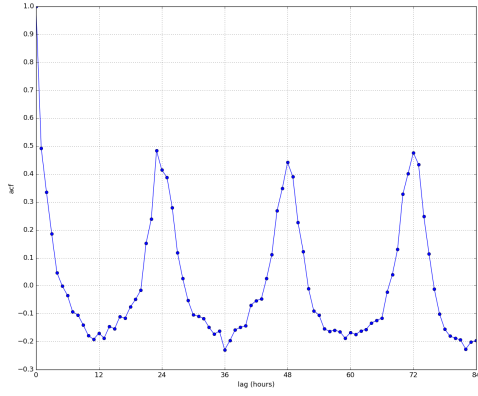
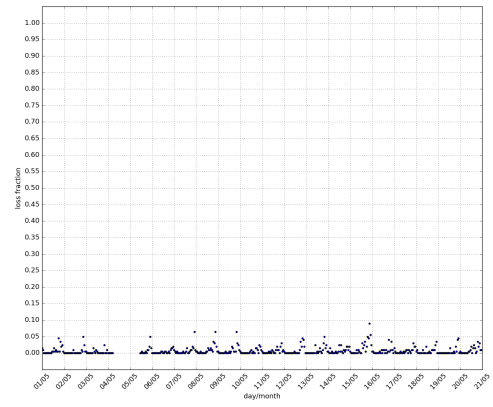


Figure 3.1: Packet loss fraction CDF.

Figures 3.2, 3.3, 3.4 show three examples with common autocorrelation patterns in this dataset together with the time series. Since the time series are unevenly, to compute the autocorrelation function, the raw time series is transformed, and it is only considered the date and hour of a measure, ignoring the minutes and seconds. Therefore, if more than one measure occurs in the same hour, it is considered the mean.

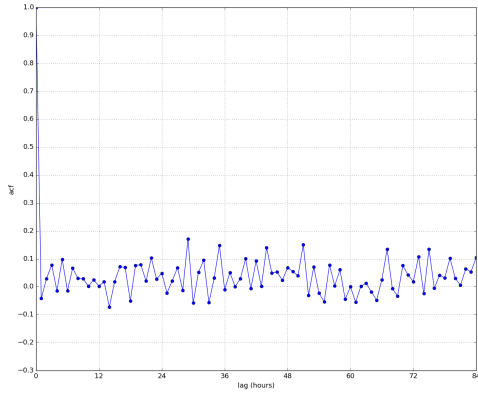


(a) Autocorrelation

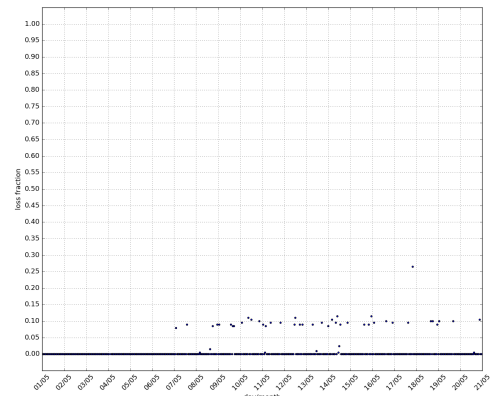


(b) Time Series

Figure 3.2: Client 1

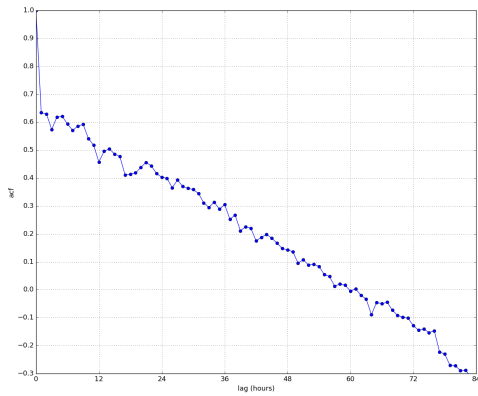


(a) Autocorrelation

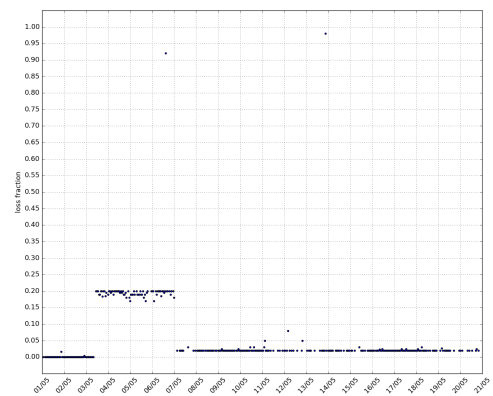


(b) Time Series

Figure 3.3: Client 2



(a) Autocorrelation



(b) Time Series

Figure 3.4: Client 3

The autocorrelation of figure 3.2 have a periodic pattern, with peaks in multiple of 24 hours. In this client, it is possible to observe that losses are more frequent in the end of the day. However, in figure 3.3 the autocorrelation quickly decreases and fluctuates around zero. The correspondent time series have a common characteristics, until day 06 of May there are no measures with losses, however, from then on frequently measures with losses alternated with zero losses measures. Figure 3.4 shows an linear decreasing autocorrelation, and the associated time series, which presents abrupt change in the mean.

Also, through a visual analysis, as in the previous figures, is possible to observe diverse time series patterns and change point patterns.

As in figure 3.2 same clients have a daily pattern in which losses occur more frequently at night, in which the Internet usage is known to be bigger. Figure ?? corroborates that observation, which presents the mean and variance of the measures that occurred in a specific hour during the 20 days period. This can be an indication of congestion during peak of usage hours.

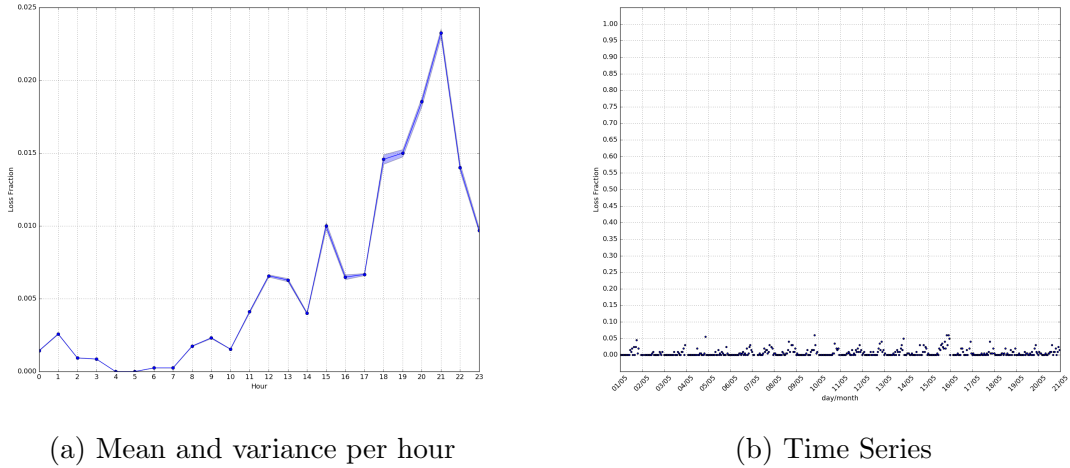


Figure 3.5: Client 1

## 3.2 Change Points Dataset

There are several approaches to construct a change points dataset to test a change point detection method. Some works in the literature simply create a simulated time series through generative models, however different segments are generated by the same model but with different parameters. In general, this type of time series is more easily handled in change point detection algorithms, since some methods assume the same models that generated the data or because real data can have more complex characteristics. Another way is to create a time series appending different segments provenient from different real time series data. In this case it is easy to sim-

plify the dataset since some characteristics as the segments lengths are defined by the dataset creator and another ones are fakely introduced. Another works assumes that the latent information of the time series are available, and with specific knowledge of the application field, it is possible to assume what kinds of configuration changes could induce a change in the time series. In the case of the application field of the present work this would be difficult, since the latent information would be connected with the network situation such as network topology, characteristics of routers congestions, physical equipments problems, which is a too complex, or even impossible information to collect and also to assume which variables could impact the time series. Other apprach also uses the latent information but instead creates a controlled environment in which is possible to change the configuration over time, but as in the previous case, this would be too complex. The approach followed by this work was to use a visual annotation of the time series. It were conducted, with an application domain specialist, visuallyu indicating the relevant changes. It is known that human visual inspection methods can bring erroneous conclusions, but with the data and application scenarion it was the best fit, as network engineers visually identify, after simple automatic filters, the change points.

This work is interested in work directly with real data and satisfy a real application problem.

As in other tasks, it is difficult to translate a human visual perception in a sistematically method.

In general, when the exact types of target changes are previously know the problem is easier.

### **3.3 Methodology**

### **3.4 Descriptive Analysis**

- explain possible ways to get the ground truth
- description of the volunteer
- user instructions
- snapshots of system
- how time series were selected to be in the survey

### **3.5 Description of Change Points Dataset**

- number of time series, number of change points: it is a high dimensional problem
- distribution number of changes per time series
- distribution time between change points
- distribution time for the first change point
- distribution time from last change point to time series end
- distribution of classification time?
- measure the difference between consecutive segments?

### **3.6 Performance Evaluation**

- how the performance is asserted in literature
- ROC curve
- confusion matrix and accuracy metrics

## Chapter 4

## Conclusions

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