

1. **Theorem:** Given a number N , let d be a divisor of N . Then the number of pairs $\{a, N\}$, where $1 \leq a \leq N$ and $\gcd(a, N) = d$, is $\phi(N/d)$.
2. Approximate number of primes under $n = (n/\ln(n))$
3. Approximate upper limit of number of divisor $= 2\sqrt[3]{N}$
4. Diphonite eqn gulai negative number niye hisab korte hbe (see hyperbolic eqn in khata)
5. Once we find a pair (x, y) using `ext_gcd`, we can generate infinite pairs of Bezout coefficients using the formula:

$$(x + (k*b)/\gcd(a, b), y - (k*a)/\gcd(a, b))$$

6. **Goldbach's Conjecture:**

For any integer n ($n \geq 4$) there exist two prime numbers p_1 and p_2 such that $p_1 + p_2 = n$.

7. For a given positive integer n ($0 < n < 231$) we need to find the number of such m that $1 \leq m \leq n$, $\gcd(m, n) \neq 1$ and $\gcd(m, n) \neq m$
 $n - \phi(n) - (a_1 + 1) * (a_2 + 1) * \dots * (a_k + 1) + 1$

8. Summation of any series with equal interval like:

$2+4+5+6$ or $3+6+9+12$ is equal

$\text{Sum} = n * (\text{first number} + \text{last number}) / 2$

9. Upper limit for $n*(n+1)/2$ is 1414213563

10. **Right Angle Triangle :**

If the given side is an even number, then find $(N^2)/4$. The integer before and after this value will make a right angled triangle. Example, if 8 is the given side, then $(8^2)/4 = 16$. So the other two sides of the right angled triangle will be 15 and (edit)17.

Now if the given side is an odd number, then find $(N^2)/2$. Here also, the integers before and after the found out value will make the right angled triangle. For example, if 3 is the number. Then $(3^2)/2 = 4.5$ So the other two sides will be 4 and 5.

11. $(a^{(b^c)}) \% \text{mod} = (a^{(b^c \% \phi(m))}) \% m$ (**provided a and m coprime**)

12. $a^x \% m = ((a \% m) ^ (x \% \phi(m))) \% m$ (**provided a and m coprime**)