

Dynamic Programming Assignment

1. On a positive integer, you can perform any one of the following 3 steps. 1.) Subtract 1 from it. ($n=n-1$), 2.) If its divisible by 2, divide by 2. (if $n\%2==0$, then $n=n/2$), 3.) If its divisible by 3, divide by 3. (if $n\%3 == 0$, then $n = n / 3$). Now the question is, given a positive integer n , find the minimum number of steps that takes n to 1 eg:
 - a. For $n = 1$, output: 0
 - b. For $n=4$, output: 2 ($4/2=2/2=1$)
 - c. For $n=7$, output: 3 ($7-1=6/3=2/2=1$)
2. Given a string find the longest substring which is a palindrome.
3. Coin Change: Given a list of N coins, their values (V_1, V_2, \dots, V_N), and the total sum S . Find the minimum number of coins the sum of which is S (we can use as many coins of one type as we want), or report that it's not possible to select coins in such a way that they sum up to S .
4. Given weights and values of n items, put these items in a knapsack of capacity W to get the maximum total value in the knapsack. In other words, given two integer arrays $val[0..n-1]$ and $wt[0..n-1]$ which represent values and weights associated with n items respectively. Also given an integer W which represents knapsack capacity, find out the maximum value subset of $val[]$ such that sum of the weights of this subset is smaller than or equal to W . You cannot break an item, either pick the complete item, or don't pick it (0-1 property).
5. Given a 2D array with 0 & 1. Find largest square with all zeroes.
6. Find the longest subsequence in a string which is a palindrome.
7. Given a string, find the smallest number n such that string can be partitioned it into n palindromic substrings.
8. Check if an array can be partitioned in two parts such that their sum is equal.
9. You have n boxes all with height 1. You have two arrays of size n containing lengths & widths of boxes. One box can be placed above another one only if its width and height is less than the other box. Find max height you can obtain by stacking these boxes over one another.